

# Advice for applying machine learning

# Deciding what to try next

#### **Debugging a learning algorithm:**

Suppose you have implemented regularized linear regression to predict housing prices.

$$J(\theta) = \frac{1}{2m} \left[ \sum_{i=1}^{m} (h_{\theta}(x^{(i)}) - y^{(i)})^2 + \lambda \sum_{j=1}^{m} \theta_j^2 \right]$$

However, when you test your hypothesis on a new set of houses, you find that it makes unacceptably large errors in its predictions. What should you try next?

X1, X2, X3, ..., X100

- -> Get more training examples
  - Try smaller sets of features
- -> Try getting additional features
  - Try adding polynomial features  $(x_1^2, x_2^2, x_1x_2, \text{etc.})$
  - Try decreasing  $\lambda$
  - Try increasing  $\lambda$

# **Machine learning diagnostic:**

Diagnostic: A test that you can run to gain insight what is/isn't working with a learning algorithm, and gain guidance as to how best to improve its performance.

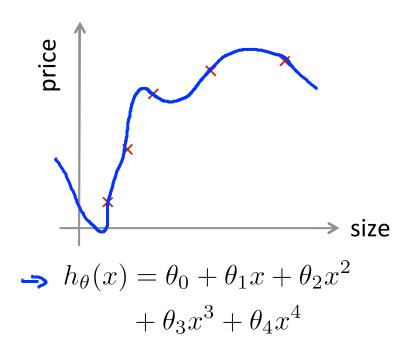
Diagnostics can take time to implement, but doing so can be a very good use of your time.



# Advice for applying machine learning

# Evaluating a hypothesis

# **Evaluating your hypothesis**

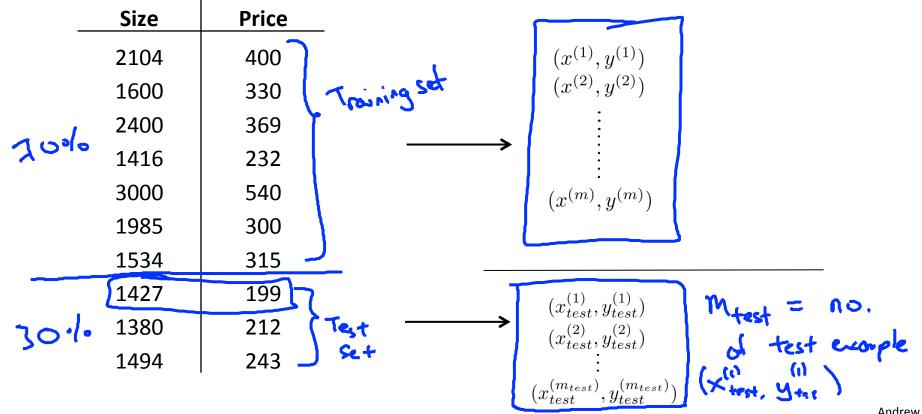


Fails to generalize to new examples not in training set.

```
x_1= size of house x_2= no. of bedrooms x_3= no. of floors x_4= age of house x_5= average income in neighborhood x_6= kitchen size .
```

# **Evaluating your hypothesis**

Dataset:



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# Training/testing procedure for linear regression

 $\rightarrow$  - Learn parameter  $\theta$  from training data (minimizing training error  $J(\theta)$ )

- Compute test set error:

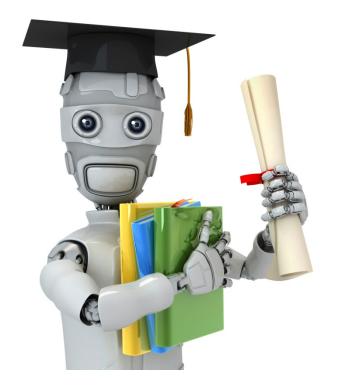
$$\frac{1}{1+est}(6) = \frac{1}{2m_{test}} \left(\frac{h_0(x_{test}) - y_{test}}{1+est}\right)^2$$

# Training/testing procedure for logistic regression

- Learn parameter heta from training data
- Compute test set error:

$$J_{test}(\theta) = -\frac{1}{m_{test}} \sum_{i=1}^{m_{test}} y_{test}^{(i)} \log h_{\theta}(x_{test}^{(i)}) + (1 - y_{test}^{(i)}) \log h_{\theta}(x_{test}^{(i)})$$

- Misclassification error (0/1 misclassification error):

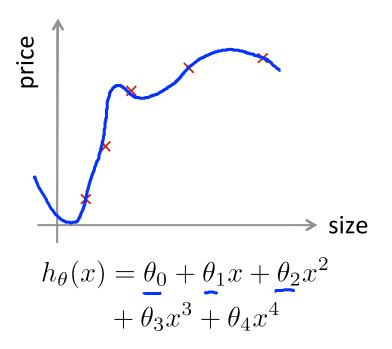


Machine Learning

# Advice for applying machine learning

Model selection and training/validation/test sets

### **Overfitting example**



Once parameters  $\theta_0, \theta_1, \ldots, \theta_4$ were fit to some set of data (training set), the error of the parameters as measured on that data (the training error  $J(\theta)$  ) is likely to be lower than the actual generalization error.

### **Model selection**

de degree of polynomial

Choose 
$$\theta_0 + \dots \theta_5 x^5$$

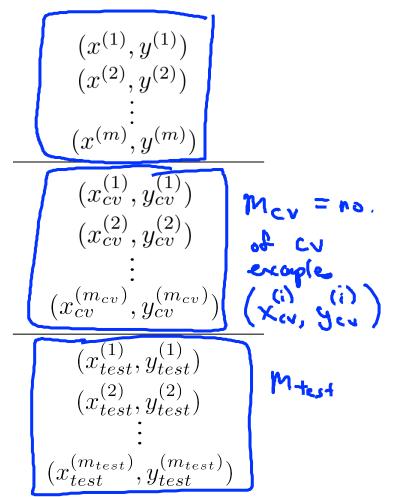
How well does the model generalize? Report test set error  $J_{test}(\theta^{(5)})$ .

Problem:  $J_{test}(\theta^{(5)})$  is likely to be an optimistic estimate of generalization error. I.e. our extra parameter  $\underline{d} = \text{degree}$  of polynomial) is fit to test set.

# **Evaluating your hypothesis**

#### Dataset:

	Size	Price	7
	2104	400	
60%	1600	330	
	2400	369 Town	
	1416	232	
	3000	540	7
	1985	300	
20%	1534	315 7 Cross ve	kidutiun
204	1427	199	۲۷)
70.1	1380	212 } test set	<b></b>
200.	1494	243	



# Train/validation/test error

### Training error:

$$\rightarrow J_{train}(\theta) = \frac{1}{2m} \sum_{i=1} (h_{\theta}(x^{(i)}) - y^{(i)})^2$$

#### **Cross Validation error:**

$$J_{cv}(\theta) = \frac{1}{2m_{cv}} \sum_{i=1}^{\infty} (h_{\theta}(x_{cv}^{(i)}) - y_{cv}^{(i)})^2$$

#### Test error:

$$J_{test}(\theta) = \frac{1}{2m_{test}} \sum_{i=1}^{n} (h_{\theta}(x_{test}^{(i)}) - y_{test}^{(i)})^2$$

#### **Model selection**

Pick 
$$\theta_0 + \theta_1 x_1 + \cdots + \theta_4 x^4 \leftarrow$$

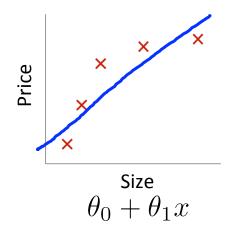
Estimate generalization error for test set  $J_{test}(\theta^{(4)})$ 



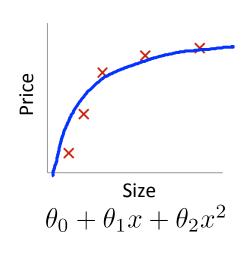
# Advice for applying machine learning

Diagnosing bias vs. variance

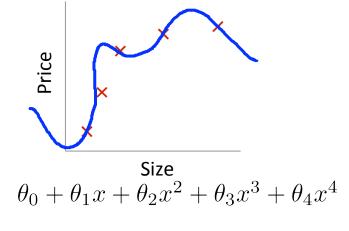
## Bias/variance



High bias (underfit) 2=1



"Just right"

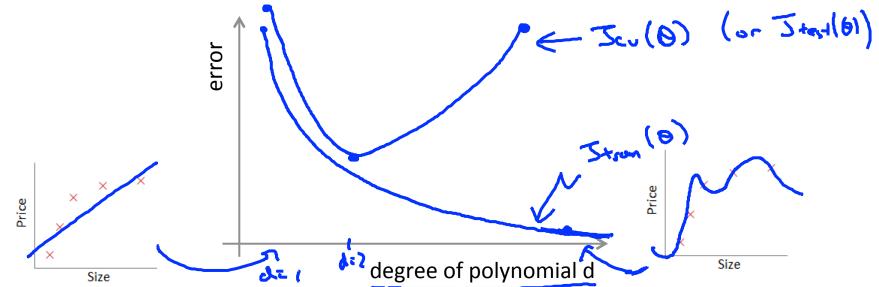


High variance (overfit)

### Bias/variance

Training error: 
$$J_{train}(\theta) = \frac{1}{2m} \sum_{i=1}^{n} (h_{\theta}(x^{(i)}) - y^{(i)})^2$$

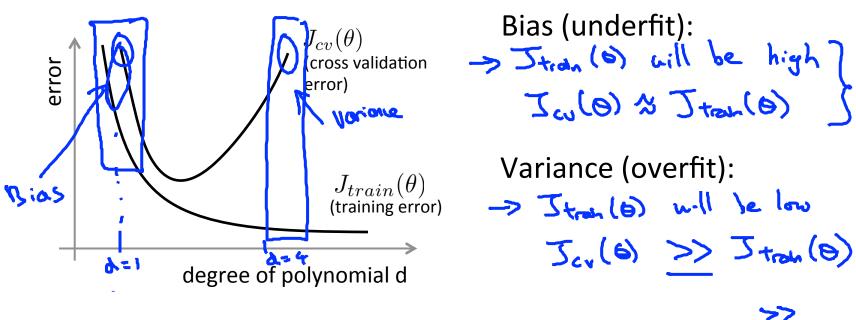
Cross validation error: 
$$J_{cv}(\theta) = \frac{1}{2m_{cv}} \sum_{i=1}^{m_{cv}} (h_{\theta}(x_{cv}^{(i)}) - y_{cv}^{(i)})^2$$

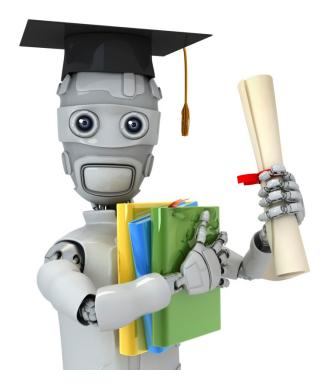


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### Diagnosing bias vs. variance

Suppose your learning algorithm is performing less well than you were hoping. ( $J_{cv}(\theta)$  or  $J_{test}(\theta)$  is high.) Is it a bias problem or a variance problem?



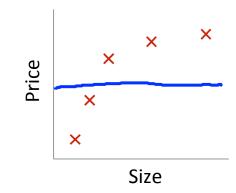


# Advice for applying machine learning

Regularization and bias/variance

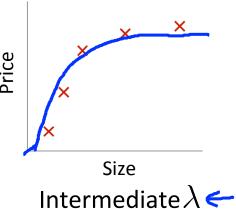
# Linear regression with regularization

$$\text{Model: } h_{\theta}(x) = \theta_0 + \underbrace{\theta_1 x + \theta_2 x^2 + \theta_3 x^3 + \theta_4 x^4}_{m} \leftarrow J(\theta) = \frac{1}{2m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)})^2 + \underbrace{\frac{\lambda}{2m} \sum_{j=1}^m \theta_j^2}_{j=1} \leftarrow J(\theta)$$

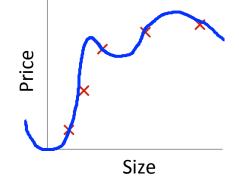


Large  $\lambda$  ← → High bias (underfit)

 $\lambda = 10000. \ \theta_1 \approx 0, \theta_2 \approx 0, \dots$ 



"Just right"



 $\rightarrow$  Small  $\lambda$  High variance (overfit)

$$\rightarrow \lambda = 0$$

# Choosing the regularization parameter $\lambda$

$$h_{\theta}(x) = \theta_{0} + \theta_{1}x + \theta_{2}x^{2} + \theta_{3}x^{3} + \theta_{4}x^{4}$$

$$J(\theta) = \frac{1}{2m} \sum_{i=1}^{m} (h_{\theta}(x^{(i)}) - y^{(i)})^{2} + \frac{\lambda}{2m} \sum_{j=1}^{m} \theta_{j}^{2}$$

$$J_{train}(\theta) = \frac{1}{2m} \sum_{i=1}^{m} (h_{\theta}(x^{(i)}) - y^{(i)})^{2}$$

$$J_{cv}(\theta) = \frac{1}{2m_{cv}} \sum_{i=1}^{m_{cv}} (h_{\theta}(x^{(i)}_{cv}) - y^{(i)}_{cv})^{2}$$

$$J_{test}(\theta) = \frac{1}{2m_{test}} \sum_{i=1}^{m_{test}} (h_{\theta}(x^{(i)}_{test}) - y^{(i)}_{test})^{2}$$

$$J_{test}(\theta) = \frac{1}{2m_{test}} \sum_{i=1}^{m_{test}} (h_{\theta}(x^{(i)}_{test}) - y^{(i)}_{test})^{2}$$

# Choosing the regularization parameter $\lambda$

Model: 
$$h_{\theta}(x) = \theta_0 + \theta_1 x + \theta_2 x^2 + \theta_3 x^3 + \theta_4 x^4$$
  

$$J(\theta) = \frac{1}{2m} \sum_{i=1}^{m} (h_{\theta}(x^{(i)}) - y^{(i)})^2 + \frac{\lambda}{2m} \sum_{j=1}^{m} \theta_j^2$$

$$Try \lambda = 0 \leftarrow \gamma \longrightarrow \min J(\Theta) \longrightarrow \Theta'' \longrightarrow J_{co}(\Theta'')$$

1. Try 
$$\lambda = 0 \leftarrow 1$$
  $\longrightarrow$  min  $J(\Theta) \rightarrow \Theta'' \rightarrow J_{CU}(\Theta''')$ 

2. Try  $\lambda = 0.01$   $\longrightarrow$   $J_{CU}(\Theta'')$ 

3. Try  $\lambda = 0.02$   $\longrightarrow$   $J_{CU}(\Theta'')$ 

4. Try  $\lambda = 0.04$   $\longrightarrow$   $J_{CU}(\Theta'')$ 

5. Try  $\lambda = 0.08$ 

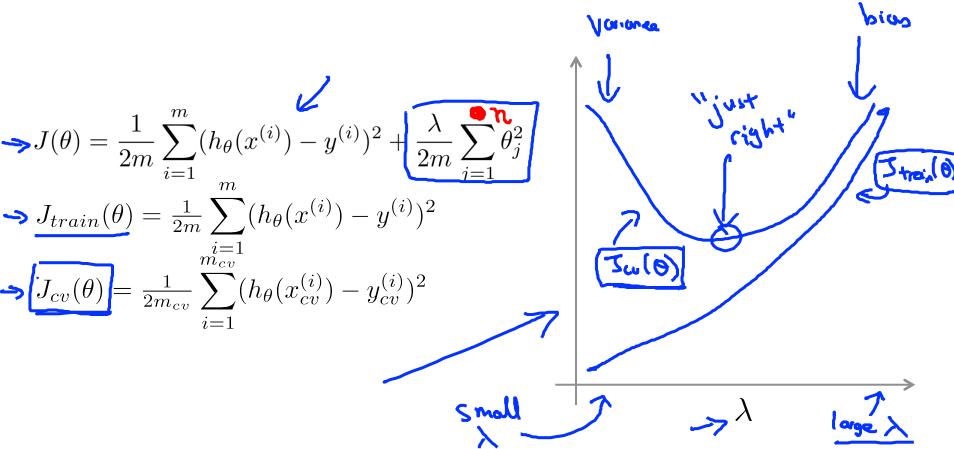
3. Try 
$$\lambda = 0.02$$
  $\longrightarrow$   $\searrow$   $\searrow$   $\searrow$   $\searrow$   $\swarrow$ 

4. Try 
$$\lambda = 0.04$$

Fry 
$$\lambda = 10$$
 Pick (say)  $\theta^{(5)}$ . Test error:  $\sum_{k \in \mathcal{L}} \left( \delta^{(5)} \right)$ 

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Bias/variance as a function of the regularization parameter  $\,\lambda\,$ 



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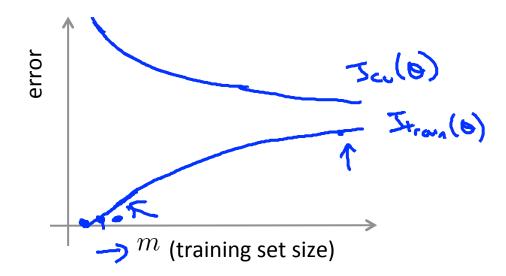
# Advice for applying machine learning

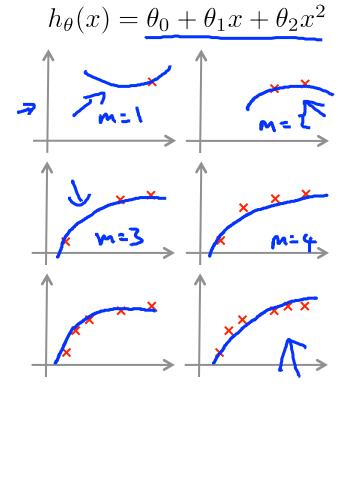
Learning curves

### **Learning curves**

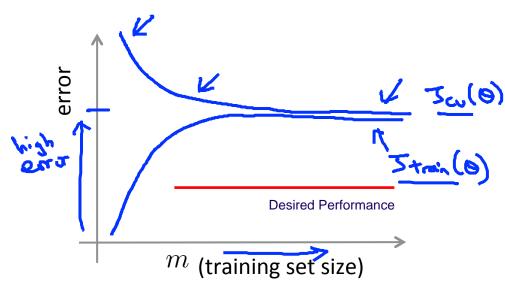
$$J_{train}(\theta) = \frac{1}{2m} \sum_{i=1}^{m} (h_{\theta}(x^{(i)}) - y^{(i)})^2 \leftarrow$$

$$J_{cv}(\theta) = \frac{1}{2m_{cv}} \sum_{i=1}^{m_{cv}} (h_{\theta}(x_{cv}^{(i)}) - y_{cv}^{(i)})^2$$

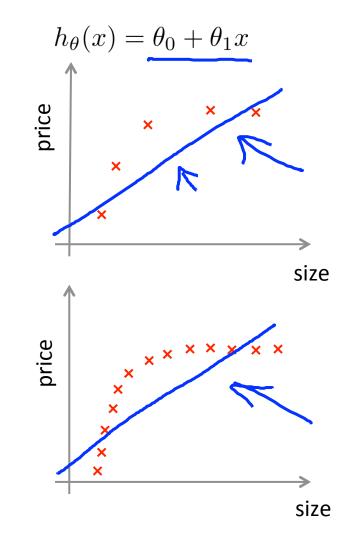




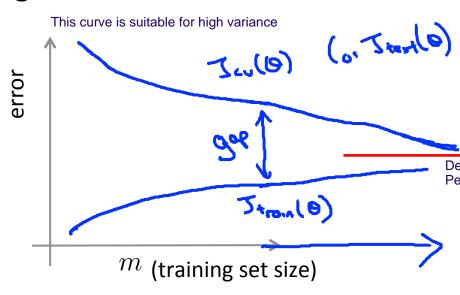
# **High bias**



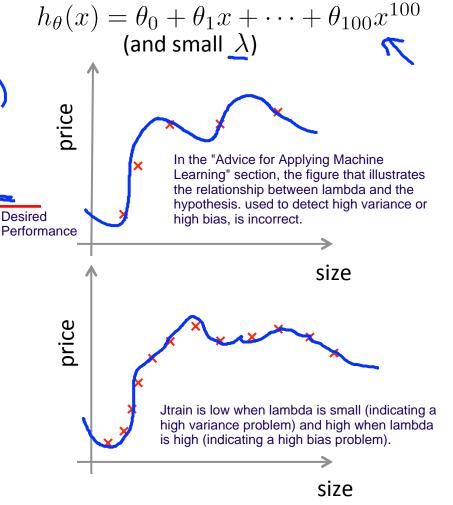
If a learning algorithm is suffering from high bias, getting more training data will not (by itself) help much.



## **High variance**



If a learning algorithm is suffering from high variance, getting more training data is likely to help.  $\leftarrow$ 





# Advice for applying machine learning

Deciding what to try next (revisited)

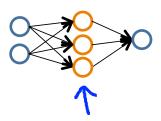
#### **Debugging a learning algorithm:**

Suppose you have implemented regularized linear regression to predict housing prices. However, when you test your hypothesis in a new set of houses, you find that it makes unacceptably large errors in its prediction. What should you try next?

- Get more training examples -> fixe high vorione
- Try smaller sets of features -> Fixe high voice
- Try getting additional features -> free high bias
- Try adding polynomial features  $(x_1^2, x_2^2, x_1x_2, \text{etc}) \rightarrow \{$
- Try decreasing  $\lambda$  fixes high high
- Try increasing  $\lambda$  -> fixes high variance

### **Neural networks and overfitting**

"Small" neural network (fewer parameters; more prone to underfitting)



Computationally cheaper

"Large" neural network (more parameters; more prone to overfitting) Computationally more expensive.

Use regularization ( $\lambda$ ) to address overfitting.

