

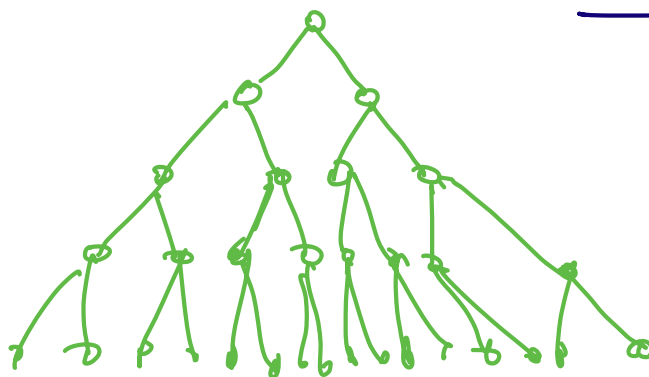
effort  
log n

3

2

1

0



$$\rightarrow 1 \quad \rightarrow \frac{n}{n} = \frac{n}{2^{\log_2 n}}$$

$$\frac{8}{3} = \frac{3}{2^2}$$

$$\frac{4}{1} = \frac{n}{2^1}$$

$$\frac{2}{3}$$

$$S = \frac{n}{2} \times 0 + \frac{n}{2^2} \times 1 + \frac{n}{2^3} \times 2 + \dots + \frac{n}{2^{\log_2 n - 1}} (\log_2 n - 2) + \frac{n}{2^{\log_2 n}} (\log_2 n - 1)$$

$$2S = n \times 0 + \frac{n}{2} \times 1 + \frac{n}{2^2} \times 2 + \frac{n}{2^3} \times 3 + \dots + \frac{n}{2^{\log_2 n - 1}} (\log_2 n - 1)$$

$$2S - S = \frac{n}{2} + \frac{n}{2^2} + \frac{n}{2^3} + \dots + \frac{n}{2^{\log_2 n - 1}} - \frac{n}{2^{\log_2 n}} (\log_2 n - 1)$$

$$n \left( \frac{1}{2} + \frac{1}{2^2} + \frac{1}{2^3} + \dots + \frac{1}{2^{\log_2 n - 1}} \right)$$

$$\frac{1}{2} \left( 1 - \left( \frac{1}{2} \right)^{\log_2 n - 1} \right) = 1 - \left( \frac{1}{2} \right)^{\log_2 n - 1}$$

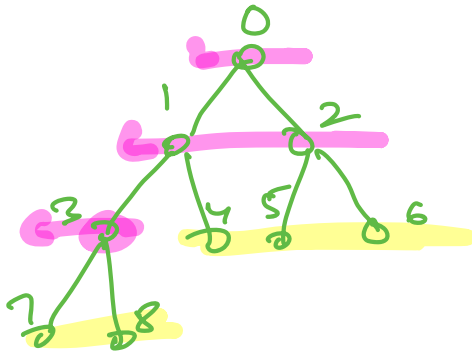
$$= 1 - \frac{\left( \frac{1}{2} \right)^{\log_2 n}}{\left( \frac{1}{2} \right)}$$

$$= 1 - \frac{2^{-\log_2 n}}{\left( \frac{1}{2} \right)} = 1 - \frac{\left( \frac{1}{n} \right)}{\left( \frac{1}{2} \right)}$$

$$= 1 - \frac{2}{n} \approx \frac{n-2}{n} \approx O(1)$$

$$n(i) = \frac{n}{2^{\log_2 i}} (\log_2 n - 1)$$

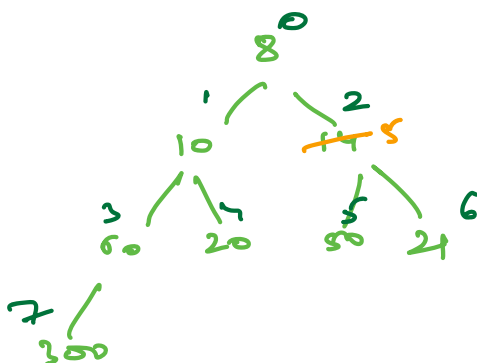
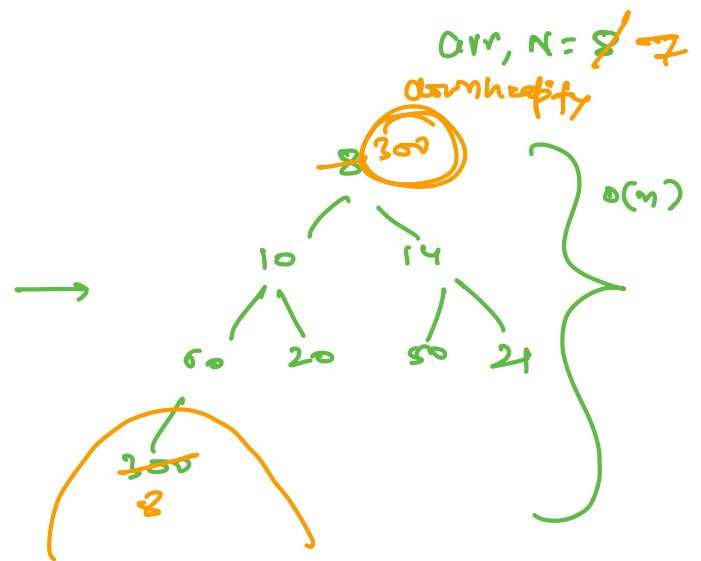
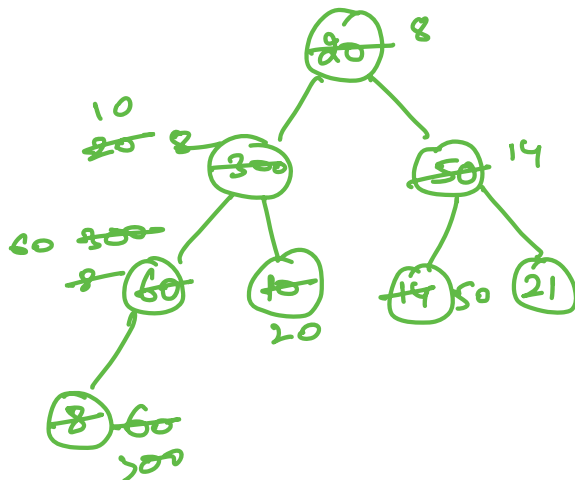
$$n - \log_2 n + 1 = O(n)$$



$$N=9$$

$$\frac{N}{2} \rightarrow N-1 \quad \left. \vphantom{\frac{N}{2}} \right\} \text{leaf}$$

$$\frac{N}{2} = 4 \rightarrow 8 \quad \left. \vphantom{\frac{N}{2}} \right\} \text{leaf}$$



$$2 \rightarrow 5 \quad \checkmark$$

$$\text{arr}(2) = 5 \quad \times$$

$$\text{upheapify}(2)$$

# Heap Sort

elements → heap create

dec

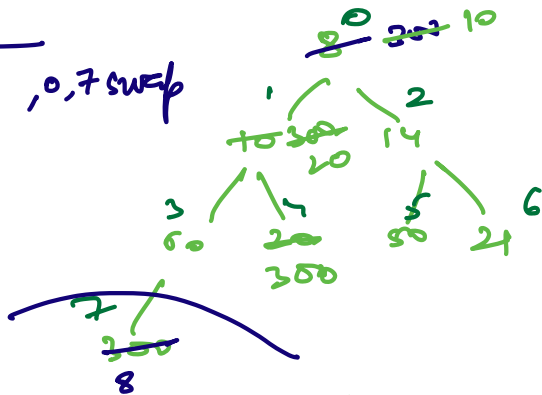
bug, let

swap

N=8

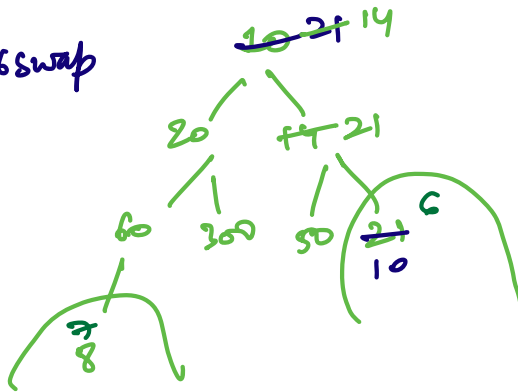
i=7, 0,7 swap

down(0,7)



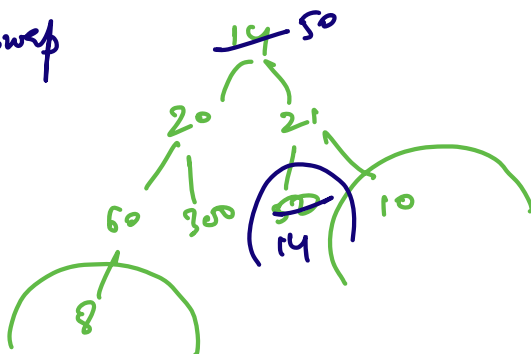
i=6, 0,6 swap

down(0,6)



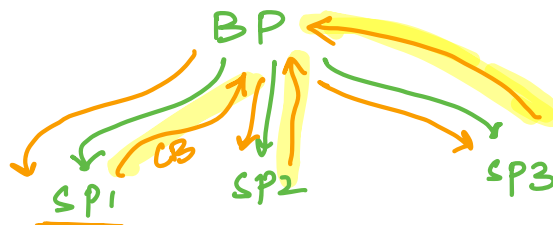
i=5, 0,5 swap

down(0,5)

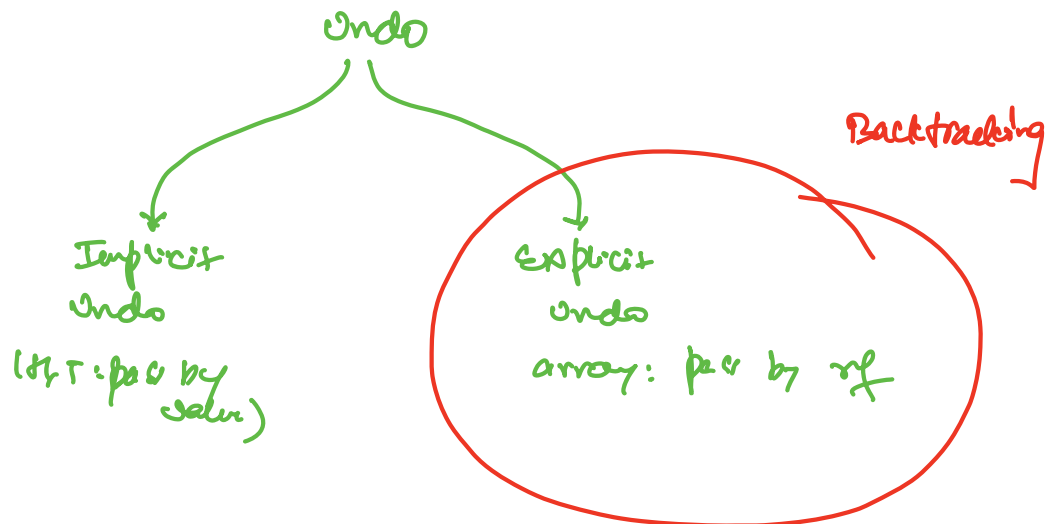
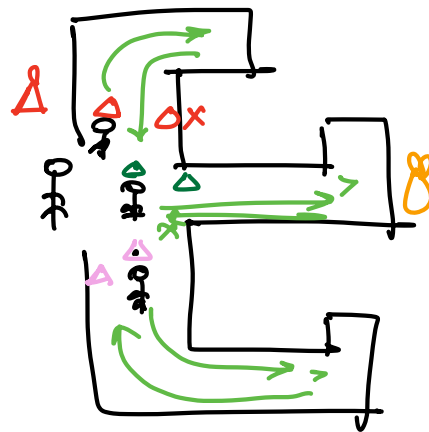
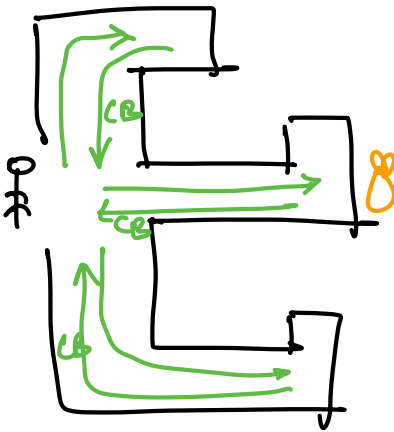
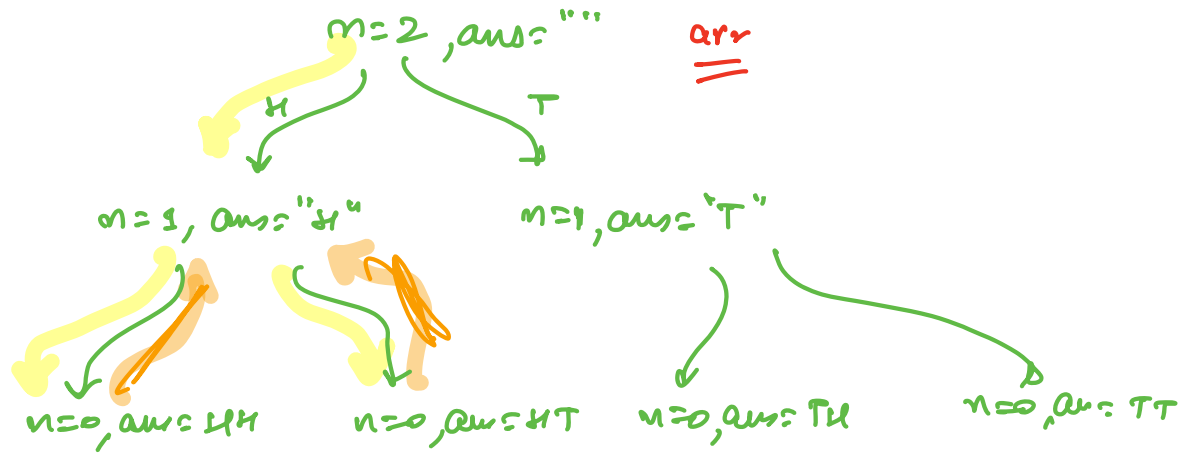


## Backtracking

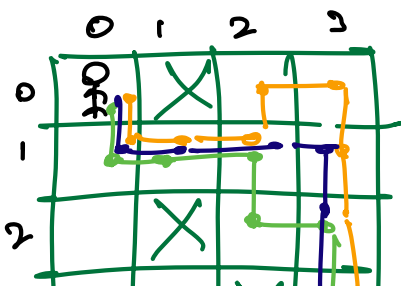
DP?



Pass by Value



Blocked Maze



(0,0) → (3,3)

DRRDRD  
DRRURDDD  
DRRRDD

