

CS-204 THEORY OF COMPUTATION

Time: 3:00 Hours

Max. Marks: 50

Note: Attempt any five questions. Assume suitable missing data, if any

Q.No. 1

- A. Construct DFA that accepts string over  $\{0, 1\}$  if and only if the value of the strings interpreted as a binary representation of an integer is  $0 \pmod 5$ . For example 0101, 1111 representing integer '5' and '15' respectively are to be accepted.

[5] CO1 BTL-3

- B. What is pumping lemma for regular expression? Show that the language  $L = \{0^n \mid n \text{ is a Perfect Square}\}$  is not regular.

[5] CO1 BTL-1,3

Q.No. 2

- A. Design Moore and Mealy machine for binary input sequence if it ends in 1010, output is 'HELLO' if it ends in '1011' output is 'DELHI', otherwise 'DTU'.

[5] CO3 BTL-3,4

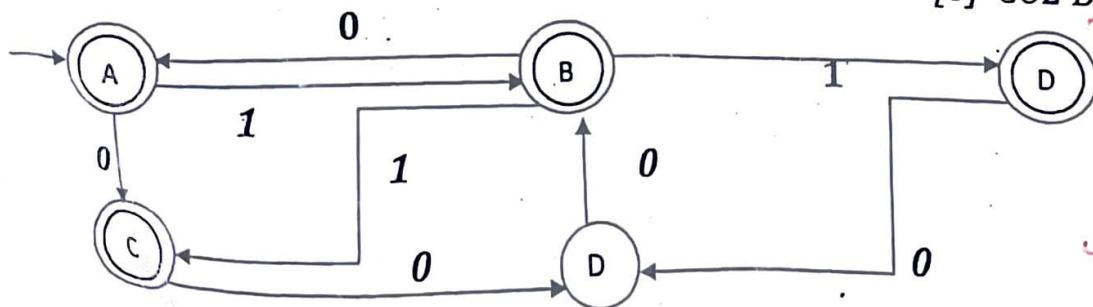
- B. Construct a Context Free Grammar (CFG) for the alphabet  $\{0,1\}$  with number of 0's not equal to number of 1's and also explain chomsky's classification for the grammar.

[5] CO2 BTL-2,3

Q.No. 3

- A. What is Arden's theorem? Find a regular expression (RE) corresponding to the following FA using Arden's theorem.

[5] CO2 BTL-2,4



B. Is it possible for every context-free grammar to be converted to both CNF and GNF? [5] CO2 BTL-1,2

i. Convert the following grammar to CNF.

$S \rightarrow bA \mid aB$  ,  $A \rightarrow bAA \mid aS \mid a$  ,  $B \rightarrow aBB \mid bS \mid b$  ] 2

ii. Convert following CFG to GNF

$S \rightarrow AB$ ,  $A \rightarrow BS \mid b$ ,  $B \rightarrow SA \mid a$  ] 2

Q.No. 4

A. Explain equivalence of two finite Automata (FA) and Construct a DFA to recognize the regular expression  $(a+b(b+ab)^*aa)^*$ . [5] CO1 BTL-2,3

B. Construct a push down automata for the following Language ] 5  
 $L = \{ a^n b^{n+2} \mid n=1, 2, 3, \dots \}$ . [5] CO4 BTL-5

Q.No. 5

A. What is pumping lemma for context free language? Prove that the language  $L = \{ a^n b^n c^n \mid n \geq 0 \}$  is not CFL using pumping lemma for context free language (CFL). 2 [5] CO3 BTL-3

B. Why the Universal Turing Machine (UTM) concept is important in the theory of computation? Design a Turing Machine (TM) that accepts all palindromes over the input alphabet  $\{0,1\}$ . 4 [5] CO5 BTL-4,5

Q.No. 6

A. Construct the CFG generating the language accepted by the following PDA:  $M = (\{ q_0, q_1 \}, \{0,1\}, \{Z_0, X\}, \delta, q_0, Z_0, \phi)$  where  $\delta$  is given below: [5] CO4 BTL-5

$\delta(q_0, 1, Z_0) = \{(q_0, XZ_0)\}$

$\delta(q_0, 1, X) = \{(q_0, XX)\}$

$\delta(q_0, 0, X) = \{(q_1, X)\}$

$\delta(q_0, \epsilon, Z_0) = \{(q_0, \epsilon)\}$

$\delta(q_1, 1, X) = \{(q_1, \epsilon)\}$

$\delta(q_1, 0, Z_0) = \{(q_0, Z_0)\}$  ] 5

B. Explain following with suitable example

i. Halting problem and Church's thesis. [2.5] CO5 BTL-1,2

ii. Post Correspondence Problem (PCP) and Myhill-Nerode Theorem. [2.5] CO4 BTL-1,2