

**%Facts**

```
bd(X11,X12,X13,X21,X22,X23,X31,X32,X33) .
```

**%Possible Moves**

```
move(
    _',
    bd(b,X12,X13,X21,X22,X23,X31,X32,X33) ,
    bd(X12,b,X13,X21,X22,X23,X31,X32,X33)
) .
move(
    _',
    bd(b,X12,X13,X21,X22,X23,X31,X32,X33) ,
    bd(X21,X12,X13,b,X22,X23,X31,X32,X33)
) .
move(
    _',
    bd(X11,X12,X13,b,X22,X23,X31,X32,X33) ,
    bd(b,X12,X13,X11,X22,X23,X31,X32,X33)
) .
move(
    _',
    bd(X11,X12,X13,b,X22,X23,X31,X32,X33) ,
    bd(X11,X12,X13,X31,X22,X23,b,X32,X33)
) .
move(
    _',
    bd(X11,X12,X13,b,X22,X23,X31,X32,X33) ,
    bd(X11,X12,X13,X22,b,X23,X31,X32,X33)
) .
move(
    _',
    bd(X11,X12,X13,X21,b,X23,X31,X32,X33) ,
    bd(X11,X12,X13,b,X21,X23,X31,X32,X33)
) .
move(
    N,
    bd(X11,X12,X13,X21,X22,X23,X31,X32,X33) ,
    bd(Y31,Y21,Y11,Y32,Y22,Y12,Y33,Y23,Y13)
) :-
    N<4,
    N1 is N + 1,
    move(
        N1,
        bd(X13,X23,X33,X12,X22,X32,X11,X21,X31) ,
        bd(Y11,Y12,Y13,Y21,Y22,Y23,Y31,Y32,Y33)
    ) .
```

**%Helpers**

```
printBoards([]) .
printBoards([B|Bs]) :- printBoard(B) , printBoards(Bs) .

printBoard(bd(X11,X12,X13,X21,X22,X23,X31,X32,X33)) :-
    format(
        "~n|~t~a~t~4| |~t~a~t~4+|~t~a~t~4+|~n",
        [X11,X12,X13]
    ) ,
    format(
        "|~t~a~t~4| |~t~a~t~4+|~t~a~t~4+|~n",
        [X21,X22,X23]
    ) ,
    format(
        "|~t~a~t~4| |~t~a~t~4+|~t~a~t~4+|~n",
        [X31,X32,X33]
    ) .

quicksort([],[]) .
quicksort([X|Xs],Ys) :-
    partition(Xs,X,Left,Right) ,
    quicksort(Left,Ls) ,
    quicksort(Right,Rs) ,
    append(Ls,[X|Rs],Ys) .
```

```

partition([], _, [], []).
partition([[K,Ks,H1]|L], [X,Xs,H2], M, [[K,Ks,H1]|N]) :-
    X > K, !,
    partition(L, [X,Xs,H2], M, N).
partition([K|L], X, [K|M], N) :-
    partition(L, X, M, N).

append([], Ys, Ys).
append([X|Xs], Ys, [X|Zs]) :- append(Xs, Ys, Zs).

%GameSolver
createValuedBoardList([], Y, Y).
createValuedBoardList([X|XS], Y, R) :-
    evaluate(X, V),
    createValuedBoardList(XS, [[V,X]|Y], R).

evaluate(
    bd(X11,X12,X13,X21,X22,X23,X31,X32,X33),
    R) :-
    eHelper([X11,X12,X13,X21,X22,X23,X31,X32,X33], 0, 1, R).

eHelper(_, V, 10, V).
eHelper([F|Fs], V, N, R) :-
    F=N,
    V1 is V+1,
    N1 is N+1,
    eHelper(Fs, V1, N1, R).
eHelper([F|Fs], V, N, R) :-
    N1 is N+1,
    eHelper(Fs, V, N1, R).

solveGame(BG) :-
    createValuedBoardList([BG], [], ValuedStart),
    addPath(ValuedStart, [], [], R),
    solver(R, [BG]).

addPath([], _, Y, Y).
addPath([V, BD]|Xs, H, Y, R) :- addPath(Xs, H, [[V, BD, H]|Y], R).

solver([[8, bd(1,2,3,4,5,6,7,8,b), Path]|VBDs], _) :-
    append(Path, [bd(1,2,3,4,5,6,7,8,b)], FinalPath),
    printBoards(FinalPath).
solver([[Value, BD, Path]|VBDs], KnownBD) :-
    findall(Y, (move(1, BD, Y), not(member(Y, KnownBD))), Moves),
    append(Moves, KnownBD, KnownBDNew),
    createValuedBoardList(Moves, [], ValuedMoves),
    append(Path, [BD], NewPath),
    addPath(ValuedMoves, NewPath, [], ValuedMovesPath),
    append(VBDs, ValuedMovesPath, VBDsNew),
    quicksort(VBDsNew, SortedValuedMoves),
    solver(SortedValuedMoves, KnownBDNew).

```