

**CSIS734-01** Data Mining & Predictive Analytics  
Garth Mortensen, [mort0052@stthomas.edu](mailto:mort0052@stthomas.edu)

**Graduate Program in Software**  
**CSIS 734-01: Data Mining & Predictive Analytics**  
Assignment #7 (100 points)  
Due Date: April 28<sup>th</sup>, 2018

Following table has the training data for our classification task.

ID	A	B	C	D	class
1	0	0	1	1	Y
2	0	0	1	1	Y
3	1	1	0	0	Y
4	1	1	0	0	Y
5	1	0	1	0	X
6	1	1	0	1	X
7	0	1	0	0	Y
8	0	1	0	0	Y
9	0	1	1	0	X
10	0	1	0	1	X
R1	1	0	1	1	?
R2	0	1	1	1	?

We want to predict the classes of the following two records:

R1 = {A = 1, B = 0, C = 1, D = 1}, and

R2 = {A = 0, B = 1, C = 1, D = 1}.

Use Naïve Bayes Theorem to determine the classes of the two records. Please include your calculations.

ID	A	B	C	D	Class
1	0	1	0	1	N
2	0	1	1	0	N
3	1	0	1	0	N
4	1	1	0	1	N
5	0	0	1	1	Y
6	0	0	1	1	Y
7	0	1	0	0	Y
8	0	1	0	0	Y
9	1	1	0	0	Y
10	1	1	0	0	Y
R1	1	0	1	1	?
R2	0	1	1	1	?

10 Total observations

Count 1	4	7	4	4	6 total Ys
Count 0	6	3	6	6	4 total Ns

Given  $d = (S, C, H, W)$  as a new instance.

Probability that the new instance  $d$  belong to class Yes.

$$P(Y | d) = (P(d | \text{Yes}) \times P(Y)) / (P(d))$$

$P(Y | d)$  = Posterior probability  $d$  belongs to class Yes, if  $d$  has attributes (sunny, cool, high humidity, windy)?

$(P(d | \text{Yes})$  Likelihood our trainings have attributes like  $d$  (sunny, cool, high humidity, windy) & belong to class Yes?

$P(Y)$  = Prior probability of trainings belong to class Yes in our training set.

$P(d)$  = Predictor prior probability

r1	a	b	c	d
	1	0	1	1

### Step 1 - Solve numerators

$$\begin{aligned} \text{r1 Yes } P(\text{Yes} | ((2/6) * (2/6) * (2/6) * (2/6) * 6/10) / P(r1) \\ = 0.007 / P(r1) \end{aligned}$$

$$\begin{aligned} \text{r1 No } P(\text{No} | ((2/4) * (1/4) * (2/4) * (2/4) * 4/10) / P(r1) \\ = 0.013 / P(r1) \end{aligned}$$

### Step 2 - Sum numerators

$$\text{Sum } 0.007 + 0.013 = 0.020$$

### Step 3 - Normalization

$$\begin{aligned} P(\text{Yes} | d) &= 0.007 / P(r1) * 1/\text{sum} = 0.372 \\ P(\text{No} | d) &= 0.013 / P(r1) * 1/\text{sum} = 0.628 \text{ greater} \end{aligned}$$

63%	probability No.				Class
R1	1	0	1	1	N

Assumption: Observations are independent and attributes are uncorrelated.

r2	a	b	c	d
	0	1	1	1

### Step 1 - Solve numerators

$$\begin{aligned} \text{r2 Yes } P(\text{Yes} | ((4/6) * (4/6) * (2/6) * (2/6) * (6/10)) / P(r2) \\ = 0.03 / P(r2) \end{aligned}$$

$$\begin{aligned} \text{r2 No } P(\text{No} | ((2/4) * (3/4) * (2/4) * (2/4) * (4/10) / P(r2) \\ = 0.038 / P(r2) \end{aligned}$$

### Step 2 - Sum numerators

$$\text{Sum } 0.03 + 0.038 = 0.067$$

### Step 3 - Normalization

$$\begin{aligned} P(\text{Yes} | d) &= 0.030 / P(r1) * 1/\text{sum} = 0.441 \\ P(\text{No} | d) &= 0.038 / P(r1) * 1/\text{sum} = 0.559 \text{ greater} \end{aligned}$$

56%	probability No.				Class
R2	0	1	1	1	N

Assumption: Observations are independent and attributes are uncorrelated.