

Selected Solutions 11.1

10 decreasing in $\{(b,d), (f,g)\}$

12 $f'(x) > 0$ in $\{(a,b), (d,f), (g,h)\}$

16 local minimum at $x=d, x=g$

39 $f(x) = x^3 - 3x + 5$

$$f'(x) = 3x^2 - 3 = 3(x^2 - 1) \quad f'(x) = 0 \text{ at } x = -1, x = 1$$

$$f'(-2) = 9 > 0$$

$$f'(0) = -3 < 0 \quad + + + (-1) - - - (1) + + +$$

$$f'(2) = 9 > 0$$

local maximum at $x = -1$

local minimum at $x = 1$

55 $f(x) = x^4 - 18x^2$

$$f'(x) = 4x^3 - 36x = 4x(x^2 - 9) = 4x(x-3)(x+3)$$

$x =$ -4 -1 1 4 $f'(x) = 0$ at $x = 0, x = -3, x = 3$

$4x$ - - + +

$x-3$ - - - +

$x+3$ - + + +

$f'(x)$ - + - +

- - - (-3) + + + (0) - - - (3) + + +

min Max min

$$f(-3) = -81$$

$$f(0) = 0$$

$$f(3) = -81$$

