1 Prepared for Submission to JHEP

₂ Spin Number in WL

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⁷ Abstract: Notes on Spin Number

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12 1 Derivation in 2208.10522

We are investigating the spin number of two products, say v_x and v_x' . They can be defined as

$$v_x = v \exp(im(\theta_0 - \theta))$$

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$$v_x' = v' \exp\bigl(im'(\theta_0' - \theta)\bigr)$$

We know to get the component of a complex number, we have Re $z=(z+z^*)/2$ and Im $z=(z-z^*)/2i$.

Then 2208.10522 then computes $v_x^*v_x'$ and v_xv_x' :

$$v_x^* v_x' = v'v \exp\left(-i(m'-m)\theta + m'\theta_0 - m\theta_0\right)$$
(1.1)

 $v_x v_x' = v'v \exp(-i(m'+m)\theta + m'\theta_0 + m\theta_0)), \tag{1.2}$

and argues you can compute the "**products between the components**" of v_x and v_x' with these two quantities. This is not true, unless taking the real and imaginary part is also considered a linear operation (it is not, by definition of linearity however). Moreover, the components of a field does **have a definition of spin**, because it has no phase (just real number). I think the authors actually meant that they want the **components of the product**, but in that case, what we need is actually v_xv_x' and $(v_x'v_x)^*$, according to the relationship in the previous section. They are, quite naively,

$$v_x^* v_x'^* = v' v \exp(i(m' + m)\theta + m'\theta_0 + m\theta_0)$$
 (1.3)

 $v_x v_x' = v'v \exp(-i(m'+m)\theta + m'\theta_0 + m\theta_0)), \tag{1.4}$

This essentially says that, the product between a spin-m and a spin-m' product should just be spin-m + m'.

2 Other Reasons

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I also think there are other evidence for my argument. First, I think the statement in 22 0208.10522:

Define $\partial = \frac{\partial}{\partial z} = \frac{\partial}{\partial x} + i \frac{\partial}{\partial y}$.

we may also calculate the following:

$$\kappa = \frac{1}{2} \partial^* \partial \psi, \tag{2.1}$$

$$\gamma = \frac{1}{2}\partial\partial\psi = |\gamma|e^{2i\phi}, \qquad (2.2)$$

If we are saying a spin-m quantity times a spin-m' quantity gives a spin-m+m' and a spin-m-m' component, then it looks like γ , which is product of a spin-0 quantity and two spin 1 quantity, it should have both spin-2 and spin-0 component. However, it only has a spin-2 component.

We then see κ is a spin-0 quantity. If we say $z'=e^{-i\theta}z$, we have $\partial=\frac{\partial}{\partial e^{-i\theta}z}=e^{i\theta}\partial$ and $\partial^*=\frac{\partial}{\partial e^{i\theta}z^*}=e^{-i\theta}\partial^*$. Because ψ never changes phase with rotation (being a real potential).

Taking a further complex gradient, we may define two more complex fields:

$$F = \frac{1}{2}\partial^*\partial\partial\psi = |F|e^{i\phi}, \quad (10)$$

$$G = \frac{1}{2}\partial\partial\partial\psi = |G|e^{3i\phi}, \quad (11)$$
 (2.4)

These are the ways to derive spin quantities more comfortable to me. Note that derivative and the coordinates, while having the same spin number, transform differently.

So the correct way to see the spin number of product of two γ

$$\gamma\gamma = |\gamma|^2 e^{4i\phi}$$

47 Acknowledgments

- This is the most common positions for acknowledgments. A macro is available to maintain the same layout and spelling of the heading.
- $_{50}$ **Note added.** This is also a good position for notes added after the paper has been $_{51}$ written.

52 References

- [1] Author, Title, J. Abbrev. vol (year) pg.
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