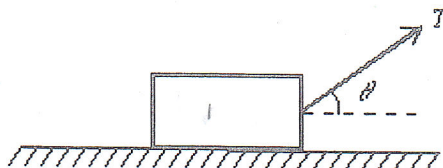


23. A block of mass  $m$  is pulled at constant velocity along a rough horizontal floor by an applied force  $\vec{T}$  as shown. The magnitude of frictional force is:

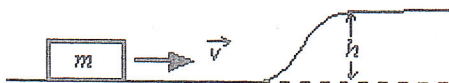


- A)  $T \cos \theta$   
 B)  $T \sin \theta$   
 C) zero  
 D)  $mg$   
 E)  $mg \cos \theta$

$$T \cos \theta + F_f = 0$$

$$F_f = -T \cos \theta$$

24. For a block of mass  $m$  to slide without friction up the rise of height  $h$  shown, it must have a minimum initial speed of:



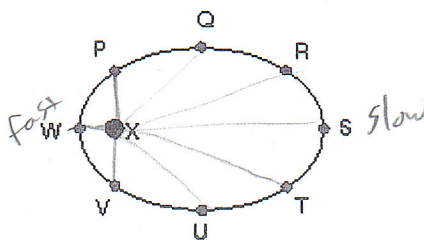
- A)  $1/2 \sqrt{gh}$   
 B)  $\sqrt{gh/2}$   
 C)  $\sqrt{2gh}$   
 D)  $2\sqrt{2gh}$   
 E)  $2\sqrt{gh}$

$$KE \rightarrow PE$$

$$\frac{1}{2} m v^2 = mgh$$

$$v = \sqrt{2gh}$$

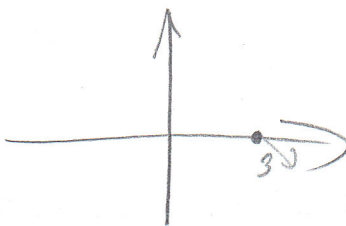
25. A planet travels in an elliptical orbit about a star X as shown. The magnitude of the acceleration of the planet is:



- A) greatest at point Q  
 B) greatest at point S  
 C) greatest at point U  
 D) greatest at point W  
 E) the same at all points

29. A 2.0-kg block starts from rest on the positive  $x$  axis 3.0 m from the origin and thereafter has an acceleration given by  $\vec{a} = 4.0\hat{i} - 3.0\hat{j}$  in  $\text{m/s}^2$ . The torque, relative to the origin, acting on it at the end of 2.0 s is:

- A) 0  
 B)  $(-18 \text{ N} \cdot \text{m})\hat{k}$   
 C)  $(+24 \text{ N} \cdot \text{m})\hat{k}$   
 D)  $(-144 \text{ N} \cdot \text{m})\hat{k}$   
 E)  $(+144 \text{ N} \cdot \text{m})\hat{k}$

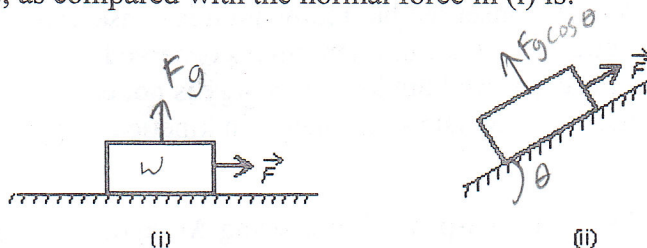


$$\begin{aligned}\tau &= \vec{r} \times \vec{F} \\ &= m(\vec{a} \times \vec{r}) \\ &= 2 \cdot -9 = (-18 \text{ N} \cdot \text{m})\hat{k}\end{aligned}$$

30. For a planet in orbit around a star the perihelion distance is  $r_p$  and its speed at perihelion is  $v_p$ . The aphelion distance is  $r_a$  and its speed at aphelion is  $v_a$ . Which of the following is true?

- A)  $v_a = v_p$   
 B)  $v_a/r_a = v_p/r_p$   
 C)  $v_a r_a = v_p r_p$   
 D)  $v_a/r_a^2 = v_p/r_p^2$   
 E)  $v_a r_a^2 = v_p/r_p^2$

31. A heavy wooden block is dragged by a force  $\vec{F}$  along a rough steel plate, as shown below for two cases. The magnitude of the applied force  $\vec{F}$  is the same for both cases. The normal force in (ii), as compared with the normal force in (i) is:



- A) the same  
 B) greater  
 C) less  
 D) less for some angles of the incline and greater for others  
 E) less or greater, depending on the magnitude of the applied force  $\vec{F}$ .

32. A 2.0-kg block starts from rest on the positive  $x$  axis 3.0 m from the origin and thereafter has an acceleration given by  $\vec{a} = 4.0\hat{i} - 3.0\hat{j}$  in  $\text{m/s}^2$ . At the end of 2.0 s its angular momentum about the origin is:

- A) 0  
 B)  $(-36 \text{ kg} \cdot \text{m}^2/\text{s})\hat{k}$   
 C)  $(+48 \text{ kg} \cdot \text{m}^2/\text{s})\hat{k}$   
 D)  $(-96 \text{ kg} \cdot \text{m}^2/\text{s})\hat{k}$   
 E)  $(+96 \text{ kg} \cdot \text{m}^2/\text{s})\hat{k}$

$$\begin{aligned}a &= \langle 4, -3 \rangle \\ v &= \langle 4t, -3t \rangle \rightarrow \langle 8, -6 \rangle \text{ at } t=2 \\ d &= \langle 3 + 2t^2, -\frac{3}{2}t^2 \rangle \rightarrow \langle 11, -6 \rangle\end{aligned}$$

$$\begin{aligned}L &= \vec{r} \cdot \vec{p} = MRV \\ &= 2 \cdot \langle 8, -6 \rangle \times \langle 11, -6 \rangle \\ &= -36\hat{k}\end{aligned}$$

37. Suitable units for the gravitational constant  $G$  are:

- A)  $\text{kg}\cdot\text{m}/\text{s}^2$
- B)  $\text{m}/\text{s}^2$
- C)  $\text{N}\cdot\text{s}/\text{m}$
- D)  $\text{kg}\cdot\text{m}/\text{s}$
- ☒ E)  $\text{m}^3/(\text{kg}\cdot\text{s}^2)$

$$G \rightarrow \text{N} \frac{\text{m}^2}{\text{kg}^2} \rightarrow \text{kg} \cdot \frac{\text{m}}{\text{s}^2} \cdot \frac{\text{m}^2}{\text{kg}^2} = \frac{\text{m}^3}{\text{s}^2 \cdot \text{kg}}$$

38. When the brakes of an automobile are applied, the road exerts the greatest retarding force:

- A) while the wheels are sliding
- ☒ B) just before the wheels start to slide
- C) when the automobile is going fastest
- D) when the acceleration is least
- E) at the instant when the speed begins to change

39. A sledge (including load) weighs 5000 N. It is pulled on level snow by a dog team exerting a horizontal force on it. The coefficient of kinetic friction between sledge and snow is 0.05. How much work is done by the dog team pulling the sledge 1000 m at constant speed?

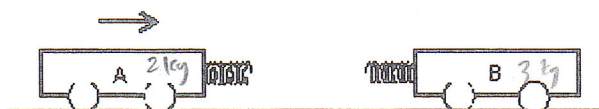
- A)  $2.5 \times 10^4 \text{ J}$
- ☒ B)  $2.5 \times 10^5 \text{ J}$
- C)  $5.0 \times 10^5 \text{ J}$
- D)  $2.5 \times 10^6 \text{ J}$
- E)  $5.0 \times 10^6 \text{ J}$

$$W = F \cdot d$$

$$= F_f \cdot \mu_k \cdot d$$

$$= 2.5 \times 10^5$$

☒ 40. Two carts (A and B), having spring bumpers, collide as shown. Cart A has a mass of 2 kg and is initially moving to the right. Cart B has a mass of 3 kg and is initially stationary. When the separation between the carts is a minimum:



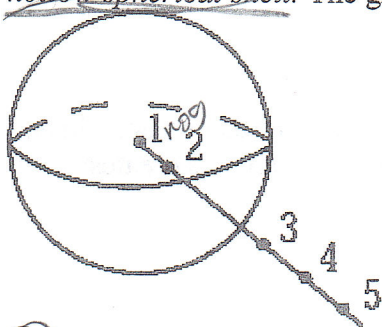
- A) cart B is still at rest
- ☒ B) cart A has come to rest
- C) the carts have the same momentum
- D) the carts have the same kinetic energy
- E) the kinetic energy of the system is at a minimum

Name: \_\_\_\_\_

Qiu, Ze Qin

Date: \_\_\_\_\_

- 4 1. Test masses are used to measure the gravitational field at various positions in and near a hollow spherical shell. The gravitational field will have its greatest value at point(s)



- (A) 3  
 B) 4  
 C) 5  
 D) 1, 2, and 5  
 E) 1 and 2

- 4 2. The mass density of a planet varies with distance from the center as  $\rho = \rho_0 (1 - C \frac{r}{R_p})$

where  $C$  is a dimensionless constant, and  $R_p$  is the radius of the planet. The gravitational field of the planet for  $r < R_p$  is

A)  $\vec{g} = -\rho_0 G (\frac{r}{2} - \frac{Cr^2}{3R_p}) \hat{r}$

\*  $4\pi$ 

B)  $\vec{g} = -\rho_0 G (\frac{r}{3} - \frac{Cr^2}{4R_p}) \hat{r}$

\*  $4\pi$ 

(C)  $\vec{g} = -\rho_0 G (r - \frac{Cr^2}{R_p}) \hat{r}$

\*  $4\pi$ 

D)  $\vec{g} = -\rho_0 G C \frac{r^2}{R_p} \hat{r}$

\*  $4\pi$ 

E)  $\vec{g} = -\rho_0 G \frac{r}{3} \hat{r}$

\*  $4\pi$ 

$$m_{enc} = \int_0^r \rho dr$$

$$= \int_0^r \rho_0 (1 - C \frac{r}{R_p}) dr$$

$$= \rho_0 \int_0^r (1 - C \frac{r}{R_p}) dr$$

$$= \rho_0 \left( r - C \frac{r^2}{2R_p} \right) \Big|_0^r$$

$$M_{enc} = \rho_0 \left( r - C \frac{r^2}{2R_p} \right)$$

$$g \cdot 4\pi r^2 = \frac{\rho_0 \left( r - C \frac{r^2}{2R_p} \right)}{r^2} \cdot 4\pi r^2$$

$$g = \rho_0 \left( \frac{1}{r} - \frac{C}{2R_p} \right)$$