

Bias Estimation of Biological Reference Points Under Two-Parameter SRRs

Nick Grunloh

In collaboration with:

Dr. E.J. Dick

Dr. H. K.H. Lee



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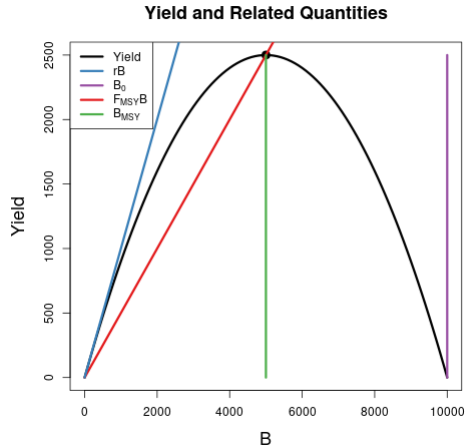


General Surplus-Production Structure

$$I_t = qB_t e^{\epsilon} \quad \epsilon \sim N(0, \sigma^2)$$

$$\frac{dB(t)}{dt} = P(B(t); \theta) - Z(t)B(t)$$

$$RP : MSY, \frac{F_{MSY}}{M}, \frac{B_{MSY}}{B_0}$$



Conceptually:

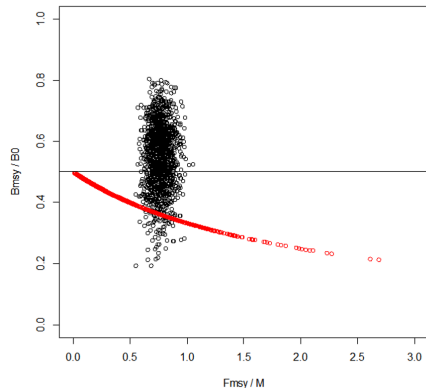
$$\frac{F_{MSY}}{M} \in \mathbb{R}^+ \quad \frac{B_{MSY}}{B_0} \in (0, 1)$$

Mangel et al. 2013, CJFAS:

- BH Model:

$$\frac{F_{MSY}}{M} \in \mathbb{R}^+ \quad \frac{B_{MSY}}{B(0)} = \frac{1}{F_{MSY}/M + 2}$$

- Similar Constraints for other Two-Parameter Curves

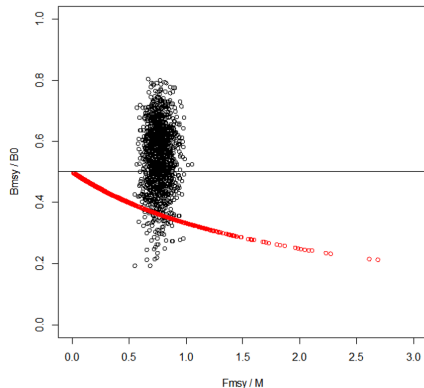


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Mangel et al. 2013, CJFAS:

- BH Model:
 $F_{MSY} \in \mathbb{R}^+ \quad \frac{B_{MSY}}{B(0)} = \frac{1}{F_{MSY}/M+2}$
- Similar Constraints for other Two-Parameter Curves
- Three-Parameter Relationships Allow Independent RP Estimation



- Isolalting RP Bias is Hard:
 - Chaos in the Dynamical System
 - Time Integrator Inaccuracy
 - Model Identifiability
 - Global Optimization
 - etc...
- Production Models are simplified places to build intuition
- See my analysis of the mechanisms of bias in the Schaefer Model \Rightarrow

Schaefer RP Analysis



<https://ggle.io/5EnI>

Schnute 1985, CJFAS

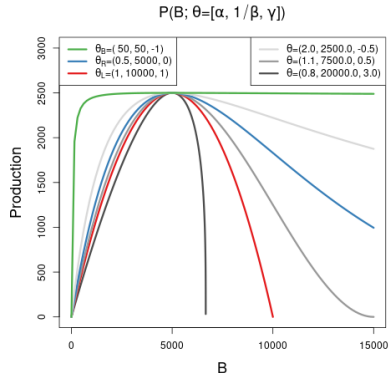
$$\frac{dB}{dt} = P(B; \theta) - (M + F)B$$

$$P(B; [\alpha, \beta, \gamma]) = \alpha B(1 - \beta\gamma B)^{\frac{1}{\gamma}}$$

$\gamma = -1 \Rightarrow$ Beverton-Holt

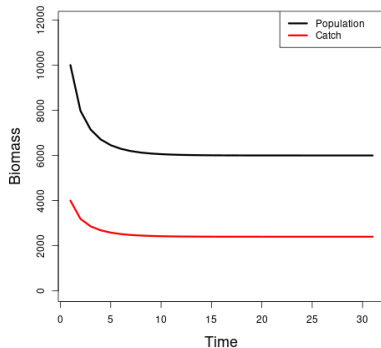
$\gamma \rightarrow 0 \Rightarrow$ Ricker

$\gamma = 1 \Rightarrow$ Logistic

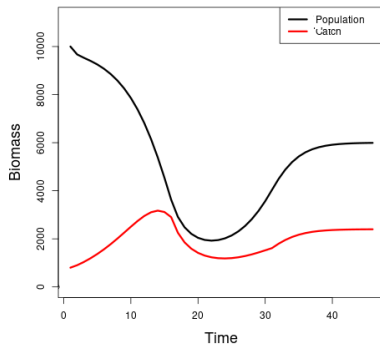


Catch

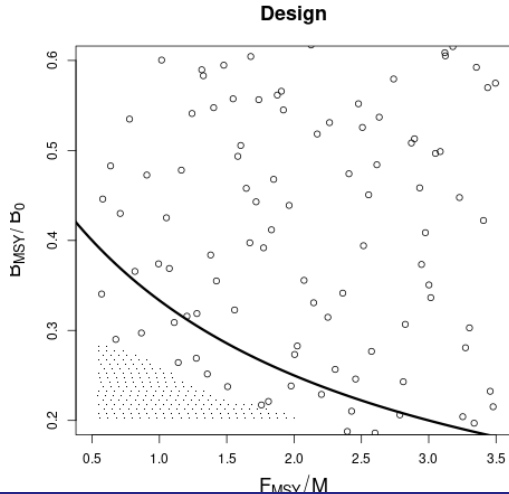
Low Contrast Fishery



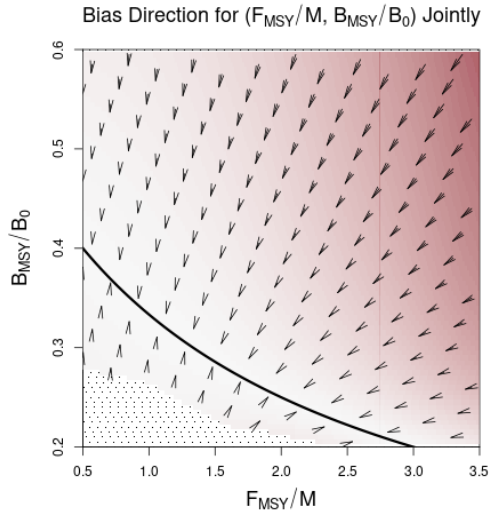
High Contrast Fishery



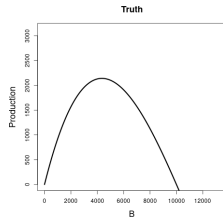
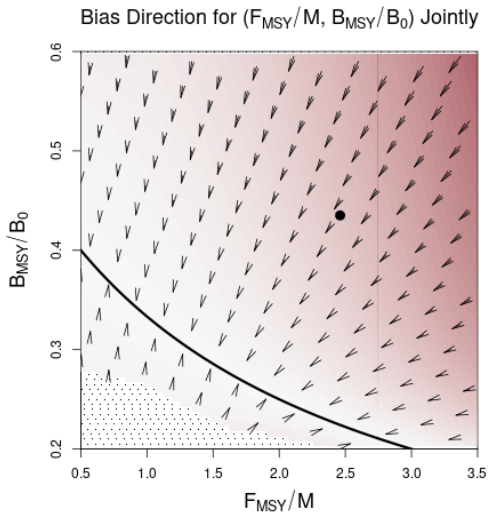
Simulation Design



High Contrast

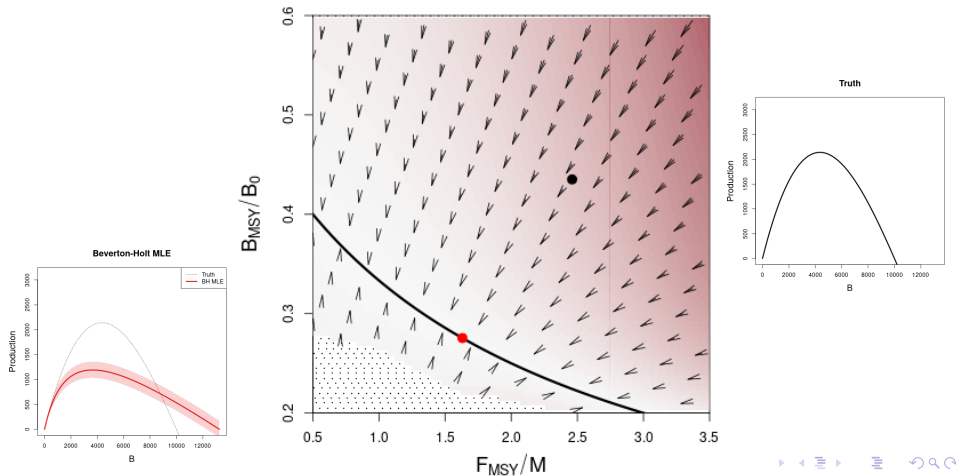


High Contrast



High Contrast

Bias Direction for $(F_{MSY}/M, B_{MSY}/B_0)$ Jointly

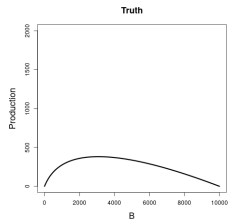
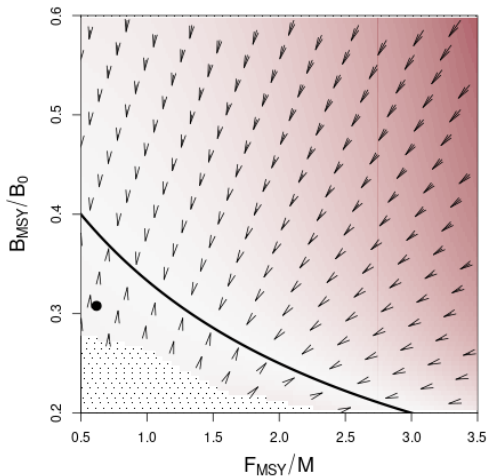


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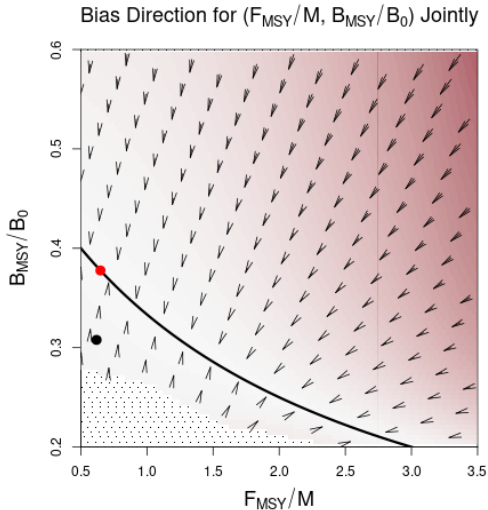
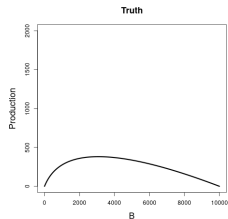
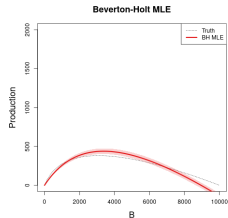
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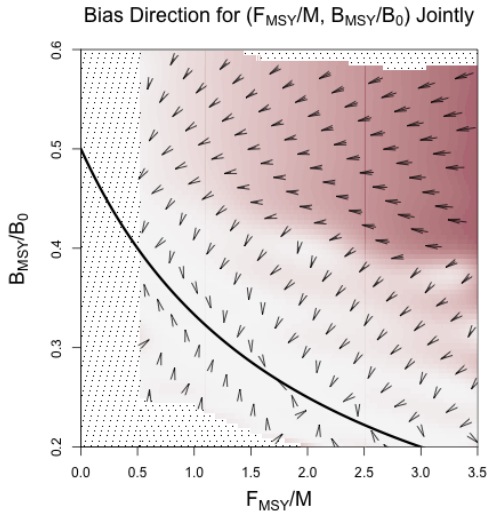
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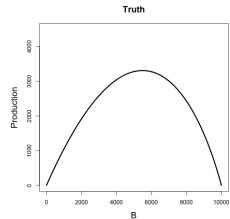
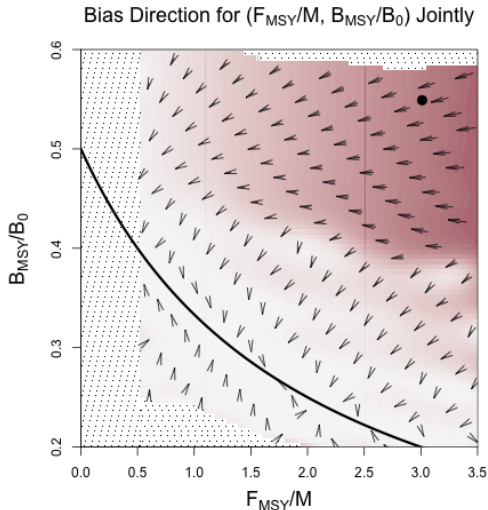
High Contrast



Low Contrast

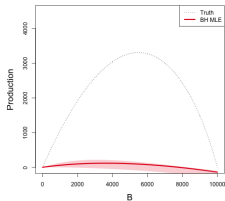
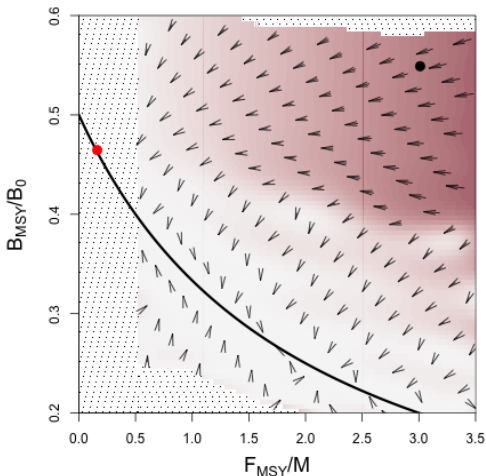


Low Contrast

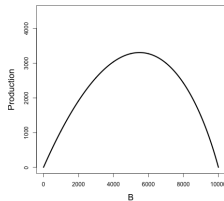


Low Contrast

Beverton-Holt MLE

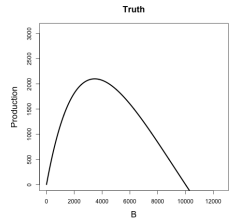
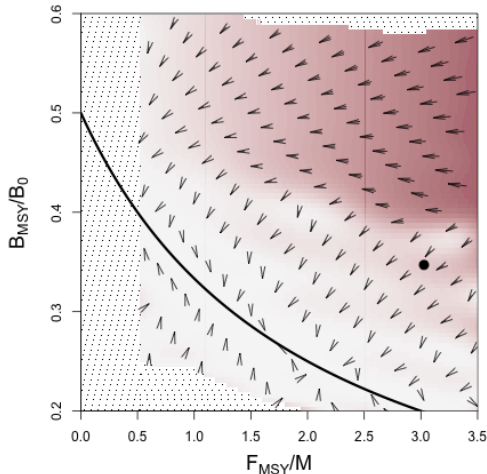
Bias Direction for $(F_{MSY}/M, B_{MSY}/B_0)$ Jointly

Truth



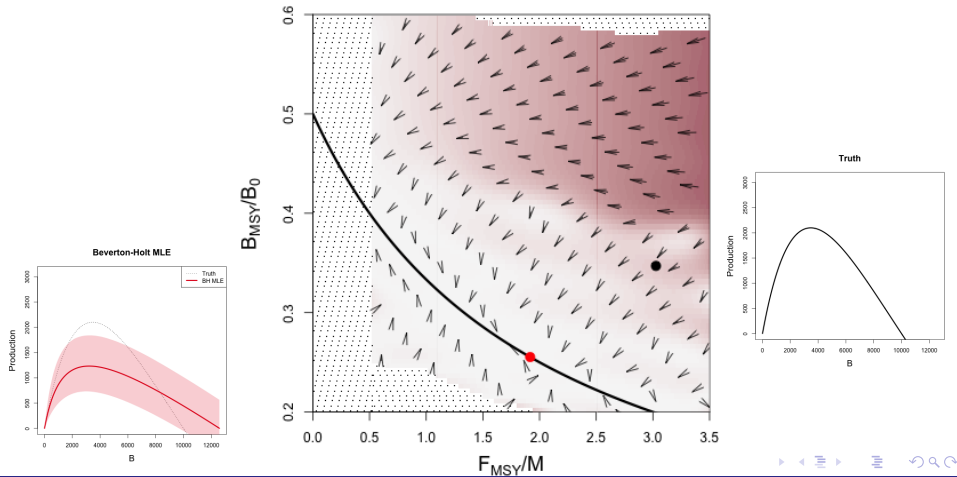
Low Contrast

Bias Direction for $(F_{MSY}/M, B_{MSY}/B_0)$ Jointly



Low Contrast

Bias Direction for $(F_{MSY}/M, B_{MSY}/B_0)$ Jointly



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Conclusions

- Contrast story
- Importance of getting the computational details correct for moving to analysis of Delay Difference and age structure

Many Thanks:

- UCSC Advisors
- SWFSC Groundfish
- NMFS Sea Grant



Metamodel Details

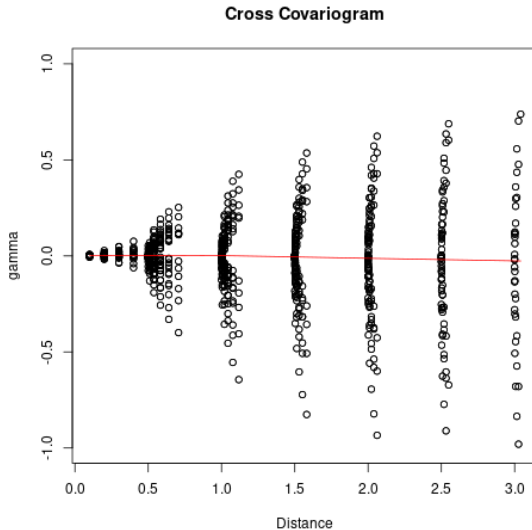
$$\mathbf{x} = \left(F_{MSY}, \frac{B_{MSY}}{\bar{B}(0)} \right)$$

$$\hat{\mu} = \beta_0 + \beta' \mathbf{x} + f(\mathbf{x}) + \epsilon$$

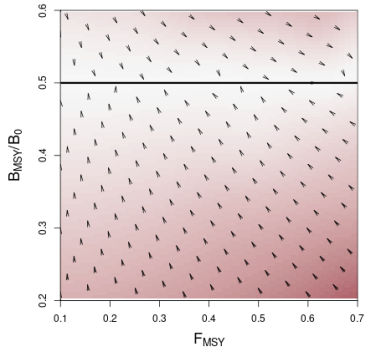
$$f(\mathbf{x}) \sim \text{GP}(0, \tau^2 R(\mathbf{x}, \mathbf{x}'))$$

$$\epsilon_i \sim \text{N}(0, \hat{\omega}_i).$$

$$R(\mathbf{x}, \mathbf{x}') = \exp \left(\sum_{j=1}^2 \frac{-(x_j - x'_j)^2}{2\ell_j^2} \right)$$

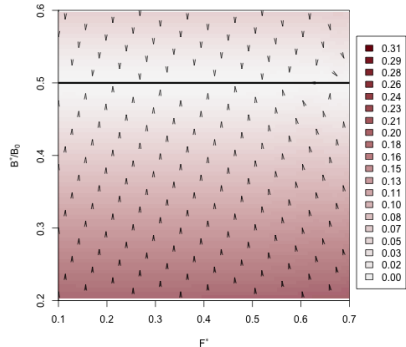


Low Contrast

Bias Direction for $(F_{\text{MSY}}, B_{\text{MSY}}/B_0)$ Jointly

High Contrast

Directional Bias



Schnute RP-Parameter System of Equations

$$\frac{B_{MSY}}{B_0} = \frac{1 - \left(\frac{M + F_{MSY}}{\alpha} \right)^\gamma}{1 - \left(\frac{M}{\alpha} \right)^\gamma}$$
$$\alpha = (M + F_{MSY}) \left(1 + \frac{\gamma F_{MSY}}{M + F_{MSY}} \right)^{1/\gamma}$$
$$\beta = \frac{1}{\gamma B_0} \left(1 - \left(\frac{M}{\alpha} \right)^\gamma \right)$$

Common Discretization

$$\frac{dB}{dt} = P_{\theta}(B(t)) - C(t)$$

$$B(\tau + 1) \approx B(\tau) + P_{\theta}(B(\tau)) - c(\tau)$$

