

Shepherd

$Z = M + F$

Pelka - Tomlinson

$$\frac{dP}{dt} = \frac{\alpha P}{1 + \beta P^\gamma} - ZP$$

set  $\frac{dP}{dt} = 0$

$$Z\bar{P} = \frac{\alpha \bar{P}}{1 + \beta \bar{P}^\gamma}$$

$$1 + \beta \bar{P}^\gamma = \frac{\alpha}{Z}$$

$$\bar{P}^{\frac{1}{\gamma}} = \frac{\frac{\alpha}{Z} - 1}{\beta}$$

$$\bar{P} = \frac{1}{\beta^\gamma} \left[ \frac{\alpha}{Z} - 1 \right]^\gamma$$

BH

$$\bar{P} = \frac{1}{\beta} \left[ \frac{\alpha}{Z} - 1 \right]$$

Ricker

$$\bar{P} = \frac{1}{\beta} \log\left(\frac{\alpha}{Z}\right)$$

$$\frac{dP}{dt} = \alpha P \left( 1 + \beta \left( 1 - \left( \frac{P}{P_0} \right)^\gamma \right) \right) - ZP$$

set  $\frac{dP}{dt} = 0$

$$Z\bar{P} = \alpha \bar{P} \left( 1 + \beta \left( 1 - \left( \frac{\bar{P}}{P_0} \right)^\gamma \right) \right)$$

$$\frac{Z}{\alpha} - 1 = \beta \left( 1 - \left( \frac{\bar{P}}{P_0} \right)^\gamma \right)$$

$$\left( \frac{\bar{P}}{P_0} \right)^\gamma = 1 - \frac{1}{\beta} \left[ \frac{Z}{\alpha} - 1 \right]$$

$$\bar{P} = P_0 \left( 1 - \frac{1}{\beta} \left[ \frac{Z}{\alpha} - 1 \right] \right)^{\frac{1}{\gamma}}$$
$$= P_0 \left( 1 + \frac{1}{\beta} \left[ 1 - \frac{Z}{\alpha} \right] \right)^{\frac{1}{\gamma}}$$

Ricker-Power

$$\frac{dP}{dt} = \alpha P e^{-\beta \left( 1 - \frac{P}{P_0} \right)^\gamma} - ZP$$

set  $\frac{dP}{dt} = 0$

$$Z\bar{P} = \alpha \bar{P} e^{-\beta \left( 1 - \frac{\bar{P}}{P_0} \right)^\gamma}$$

$$\log\left(\frac{Z}{\alpha}\right) = -\beta \left( 1 - \frac{\bar{P}}{P_0} \right)^\gamma$$

$$\left[ \frac{1}{\beta} \log\left(\frac{Z}{\alpha}\right) \right]^{\frac{1}{\gamma}} = \left( \frac{\bar{P}}{P_0} - 1 \right)$$

$$\bar{P} = P_0 \left( 1 + \frac{1}{\beta^\gamma} \log\left(\frac{Z}{\alpha}\right) \right)^{\frac{1}{\gamma}}$$

Peris0

$$\frac{dP}{dt} = \frac{\alpha P}{(1 + \beta P)^\gamma} - ZP$$

set  $\frac{dP}{dt} = 0$

$$Z\bar{P} = \frac{\alpha \bar{P}}{(1 + \beta \bar{P})^\gamma}$$
$$\bar{P} = \frac{1}{\beta} \left[ \left( \frac{\alpha}{Z} \right)^{\frac{1}{\gamma}} - 1 \right]$$

$$1 + \beta \bar{P} = \left( \frac{\alpha}{Z} \right)^{\frac{1}{\gamma}}$$