Casimir Effect in COM Framework

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Energy Pattern Density

The energy pattern density between two surfaces is:

$$\rho_{E}(x,d) = \rho_{0} \sum_{n=1}^{\infty} \sin^{2} \left(\frac{n \pi x}{d} \right) LZ^{-n}$$

where:

- ρ_E is the energy density
- ρ_0 is the base energy density
- *d* is the separation between surfaces
- *x* is the position between surfaces

Octave-Based Mode Restriction

The allowed energy modes between surfaces follow:

$$\omega_n = \frac{n \pi c}{d} \left\{ 1 + \frac{\operatorname{Oct}(n)}{2LZ} \right\}$$

where:

- ω_n is the frequency of the *n*th mode
- *c* is the speed of light
- Oct(n) is the octave position of n

COM-Casimir Force

The Casimir force in the COM framework is:

$$F_{\text{COM}} = -\frac{\partial}{\partial d} \left[\int_{0}^{d} (\rho_{\text{butside}} - \rho_{\text{E}}(x, d)) dx \right]$$

Which evaluates to:

$$F_{\text{COM}} = -\frac{\pi^2 \hbar cA}{240 d^4} \cdot \frac{\text{LZ}^4}{(1 - \text{HQS})^2}$$

where:

- *A* is the area of the surfaces
- The factor $\frac{LZ^4}{(1-HQS)^2}$ is the COM correction to the traditional Casimir force

LZ-Based Distance Scaling

The force scaling with distance follows:

$$\frac{F_{\text{COM}}(d_1)}{F_{\text{COM}}(d_2)} = \left(\frac{d_2}{d_1}\right)^4 \cdot LZ^{\text{Oct}(d_2/d_1)}$$

HQS Threshold Effect

At distances approaching the HQS scale, the force is modified:

$$F_{\text{COM}}(d) = F_{\text{classical}}(d) \left[1 + \tanh \left(\frac{\text{HQS LZ}}{d} \right) \right]$$

Modified Casimir Force with Octave-Structured Vacuum

$$F_{\text{modified}}(d, r_0) = F_{\text{classical}}(d) \left\{ 1 + \eta \cdot \sin \left(\frac{2 \pi \cdot \log (d/r_0)}{\log (\lambda)} \right) \right\} \cdot \frac{\lambda^4}{(1-\eta)^2}$$

where:

- $\eta = 0.235 \text{ (HQS)}$
- $\lambda = 1.23498 \text{ (LZ)}$
- r_0 is a fundamental length scale

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$$F_{\text{classical}}(d) = -\frac{\pi^2 \hbar c A}{240 d^4}$$

Unified Mathematical Framework

Energy-Phase Tensor

Both EDM and Casimir effect can be described using the energy-phase tensor:

$$T_{ij} = \int_{V} \Psi_{i}(x, t) \cdot \nabla_{\varphi_{j}}(x, t) dV$$

Scale Bridging Equation

The relationship between EDM and Casimir scales:

$$\frac{E_{\rm EDM}}{e \cdot \lambda_{\rm r}} \approx \frac{F_{\rm COM} d^4}{\hbar c A} LZ^{-2}$$

where:

- *e* is the elementary charge
- λ_c is the Compton wavelength

Experimental Prediction Equation

The COM framework predicts deviations from classical behavior:

$$\Delta_{\text{COM}} = 1 - \frac{\text{Measured}}{\text{Classical}} \approx \text{Oct} \left(\frac{d}{\lambda} \right) \text{HQS}$$

where Δ_{COM} is the fractional deviation from classical predictions.