

Standard Physics Equations and Laws

This document compiles fundamental physics equations and laws that will be redefined under the COM (Continuous Oscillatory Model) framework.

Classical Mechanics

Newton's Laws of Motion

- First Law (Inertia): An object at rest stays at rest, and an object in motion stays in motion with the same speed and direction unless acted upon by an unbalanced force.
- Second Law (Force): $F = ma$ (Force equals mass times acceleration)
- Third Law (Action-Reaction): For every action, there is an equal and opposite reaction.

Kinematics

- Position: $x = x_0 + v_0 t + (1/2)at^2$
- Velocity: $v = v_0 + at$
- Acceleration: $a = dv/dt = d^2x/dt^2$
- Average velocity: $\bar{v} = \Delta x / \Delta t$
- Relative velocity: $v_{AB} = v_A - v_B$

Dynamics

- Momentum: $p = mv$
- Conservation of momentum: $p_0 + p_1 = p_0' + p_1'$ (in isolated systems)
- Impulse: $J = F \cdot \Delta t = \Delta p$
- Work: $W = F \cdot d = F \cdot d \cdot \cos(\theta)$
- Kinetic energy: $KE = (1/2)mv^2$
- Potential energy (gravitational): $PE = mgh$
- Conservation of energy: $E_0 = E_1$ (in isolated systems)
- Power: $P = dW/dt = F \cdot v$

Rotational Mechanics

- Angular position: θ
- Angular velocity: $\omega = d\theta/dt$
- Angular acceleration: $\alpha = d\omega/dt$
- Torque: $\tau = r \times F = r \cdot F \cdot \sin(\theta)$
- Moment of inertia: $I = \sum m r^2$
- Angular momentum: $L = I\omega$
- Rotational kinetic energy: $KE_{rot} = (1/2)I\omega^2$

Gravitation

- Newton's law of universal gravitation: $F = G(m_1 m_2)/r^2$

- Gravitational field: $g = GM/r^2$
- Gravitational potential energy: $U = -G(m_1 m_2)/r$
- Kepler's laws:
 - Planets move in elliptical orbits with the Sun at one focus
 - A line joining a planet and the Sun sweeps out equal areas in equal times
 - The square of the orbital period is proportional to the cube of the semi-major axis: $T^2 \propto a^3$

Thermodynamics

Laws of Thermodynamics

- Zeroth Law: If two systems are in thermal equilibrium with a third system, they are in thermal equilibrium with each other.
- First Law (Energy Conservation): $\Delta U = Q - W$
- Second Law (Entropy): $\Delta S \geq 0$ for isolated systems
- Third Law: As temperature approaches absolute zero, entropy approaches a constant minimum.

Thermodynamic Quantities

- Ideal gas law: $PV = nRT$
- Internal energy: $U = (3/2)nRT$ (for monatomic ideal gas)
- Heat capacity: $C = \Delta Q / \Delta T$
- Entropy: $S = k \cdot \ln(\Omega)$ (Boltzmann's entropy formula)
- Gibbs free energy: $G = H - TS$
- Enthalpy: $H = U + PV$

Statistical Mechanics

- Maxwell-Boltzmann distribution: $f(v) = \left(\frac{m}{2\pi kT}\right)^{3/2} \cdot 4\pi v^2 \cdot e^{-mv^2/2kT}$
- Partition function: $Z = \sum e^{-E_i/kT}$
- Boltzmann factor: $P_i = e^{-E_i/kT} / Z$

Electromagnetism

Electrostatics

- Coulomb's law: $F = k(q_1 q_2)/r^2$
- Electric field: $E = F/q = k(Q)/r^2$
- Electric potential: $V = k(Q)/r$
- Gauss's law: $\oint \mathbf{E} \cdot d\mathbf{A} = Q/\epsilon_0$

Magnetism

- Magnetic field due to current: $\mathbf{B} = \frac{\mu_0}{4\pi} \oint \mathbf{I} \cdot d\mathbf{l} \times \hat{\mathbf{r}}/r^2$

- Lorentz force: $\mathbf{F} = q(\mathbf{E} + \mathbf{v} \times \mathbf{B})$
- Biot-Savart law: $d\mathbf{B} = (\mu_0/4\pi)(I \cdot d\mathbf{l} \times \hat{\mathbf{r}}/r^2)$
- Ampere's law: $\mathbf{B} \cdot d\mathbf{l} = \mu_0 I$

Electromagnetic Induction

- Faraday's law: $\mathcal{E} = -d\Phi/dt$
- Lenz's law: Induced current flows to oppose the change that produced it
- Self-inductance: $\mathcal{E} = -L(dI/dt)$

Maxwell's Equations

- Gauss's law for electricity: $\nabla \cdot \mathbf{E} = \rho/\epsilon_0$
- Gauss's law for magnetism: $\nabla \cdot \mathbf{B} = 0$
- Faraday's law: $\nabla \times \mathbf{E} = -\partial \mathbf{B}/\partial t$
- Ampere-Maxwell law: $\nabla \times \mathbf{B} = \mu_0 \mathbf{J} + \mu_0 \epsilon_0 \partial \mathbf{E}/\partial t$

Electromagnetic Waves

- Wave equation: $\nabla^2 \mathbf{E} = (1/c^2)(\partial^2 \mathbf{E}/\partial t^2)$
- Speed of light: $c = 1/\sqrt{\epsilon_0 \mu_0}$
- Energy density: $u = (1/2)\epsilon_0 E^2 + (1/2)\mu_0 B^2$
- Poynting vector: $\mathbf{S} = (1/\mu_0)(\mathbf{E} \times \mathbf{B})$

Relativity

Special Relativity

- Time dilation: $\Delta t = \Delta t' / \sqrt{1-v^2/c^2}$
- Length contraction: $L = L' \sqrt{1-v^2/c^2}$
- Relativistic momentum: $\mathbf{p} = m\mathbf{v}/\sqrt{1-v^2/c^2}$
- Mass-energy equivalence: $E = mc^2$
- Relativistic energy: $E = mc^2/\sqrt{1-v^2/c^2}$
- Lorentz transformation:
 - $t' = \gamma(t - vx/c^2)$
 - $x' = \gamma(x - vt)$
 - $y' = y$
 - $z' = z$
 - where $\gamma = 1/\sqrt{1-v^2/c^2}$

General Relativity

- Einstein field equations: $G_{\mu\nu} = (8\pi G/c^4)T_{\mu\nu}$
- Geodesic equation: $d^2x^\mu/ds^2 + \Gamma^\mu_{\alpha\beta}(dx^\alpha/ds)(dx^\beta/ds) = 0$
- Schwarzschild metric: $ds^2 = (1-2GM/rc^2)c^2dt^2 - (1-2GM/rc^2)^{-1}dr^2 - r^2d\Omega^2$
- Gravitational time dilation: $\Delta t = \Delta t' / \sqrt{1-2GM/rc^2}$

Quantum Mechanics

Wave-Particle Duality

- De Broglie wavelength: $\lambda = h/p$
- Heisenberg uncertainty principle: $\Delta x \Delta p \geq \hbar/2$

Quantum State

- Schrödinger equation: $i\hbar(\partial\Psi/\partial t) = \hat{H}\Psi$
- Time-independent Schrödinger equation: $\hat{H}\Psi = E\Psi$
- Probability density: $|\Psi|^2$
- Normalization: $\int |\Psi|^2 dx = 1$
- Expectation value: $\langle A \rangle = \int \Psi^* \hat{A} \Psi dx$

Quantum Operators

- Position operator: $\hat{x} = x$
- Momentum operator: $\hat{p} = -i\hbar(\partial/\partial x)$
- Energy operator (Hamiltonian): $\hat{H} = -\hbar^2/(2m)(\partial^2/\partial x^2) + V(x)$
- Angular momentum operator: $\hat{L} = r \times \hat{p}$

Quantum Systems

- Particle in a box: $E = (n^2 \pi^2 \hbar^2)/(2mL^2)$
- Quantum harmonic oscillator: $E = \hbar(\omega + 1/2)$
- Hydrogen atom energy levels: $E = -13.6 \text{ eV}/n^2$

Quantum Field Theory

Quantum Electrodynamics

- Dirac equation: $(i\gamma^\mu \partial_\mu - m)\psi = 0$
- Feynman propagator: $D_F(x-y) = \int \frac{d^4k}{(2\pi)^4} (e^{i(-ik \cdot (x-y))})/(k^2 - m^2 + i\epsilon)$

Standard Model

- Lagrangian density of quantum field theory
- Higgs mechanism: $v = \sqrt{(-\mu^2/\lambda)}$
- Weak interaction: W and Z bosons
- Strong interaction: Quantum Chromodynamics (QCD)

Statistical and Thermal Physics

Statistical Distributions

- Fermi-Dirac distribution: $f(E) = 1/(e^{(E-\mu)/kT} + 1)$
- Bose-Einstein distribution: $f(E) = 1/(e^{(E-\mu)/kT} - 1)$

Phase Transitions

- Clausius-Clapeyron equation: $dP/dT = L/(T(V - V_c))$
- Critical exponents: various power laws near critical points

Wave Mechanics

Wave Properties

- Wave equation: $\partial^2 y / \partial t^2 = v^2 (\partial^2 y / \partial x^2)$
- Wave speed: $v = \lambda f$
- Superposition principle: $y = y_1 + y_2$
- Standing waves: $y(x,t) = 2A \cdot \sin(kx) \cdot \cos(\omega t)$
- Doppler effect: $f' = f((v \pm v_{\text{observer}})/(v \mp v_{\text{source}}))$

Acoustics

- Sound intensity: $I = P/A$
- Sound intensity level: $\beta = 10 \cdot \log(I/I_0)$ dB
- Speed of sound: $v = \sqrt{B/\rho}$ (in fluids)

Fluid Dynamics

Fluid Statics

- Pressure: $P = F/A$
- Pascal's principle: Pressure applied to an enclosed fluid is transmitted undiminished to all parts of the fluid
- Archimedes' principle: Buoyant force equals weight of displaced fluid

Fluid Dynamics

- Continuity equation: $A_1 v_1 = A_2 v_2$
- Bernoulli's equation: $P_1 + (1/2) \rho v_1^2 + \rho g h_1 = P_2 + (1/2) \rho v_2^2 + \rho g h_2$
- Viscous flow: Poiseuille's law: $Q = (\pi r^4 \Delta P)/(8 \eta L)$

Optics

Geometric Optics

- Snell's law: $n_1 \sin(\theta_1) = n_2 \sin(\theta_2)$
- Lens equation: $1/f = 1/s_o + 1/s_i$
- Magnification: $M = -s_i/s_o$

Wave Optics

- Interference: $I = I_1 + I_2 + 2\sqrt{I_1 I_2} \cos(\delta)$
- Diffraction: $\sin(\theta) = m \lambda / d$ (for diffraction grating)
- Polarization: Malus's law: $I = I_0 \cos^2(\theta)$