

Quantum Computers.

How to Program Them?

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<https://github.com/gate42qc>

Topics

Part 1 (~40 min):

What is a quantum computer?

How are quantum computers different than conventional computers?

Universal Quantum Algorithms

Quantum Software

Part 2 (~1 hour):

Linear Algebra

Programming in Qiskit,

Teleportation Demo on IBM hardware and Simulator using Qiskit

What is a quantum computer?

QC \neq smaller, faster CC

Fundamentally new paradigm for processing information

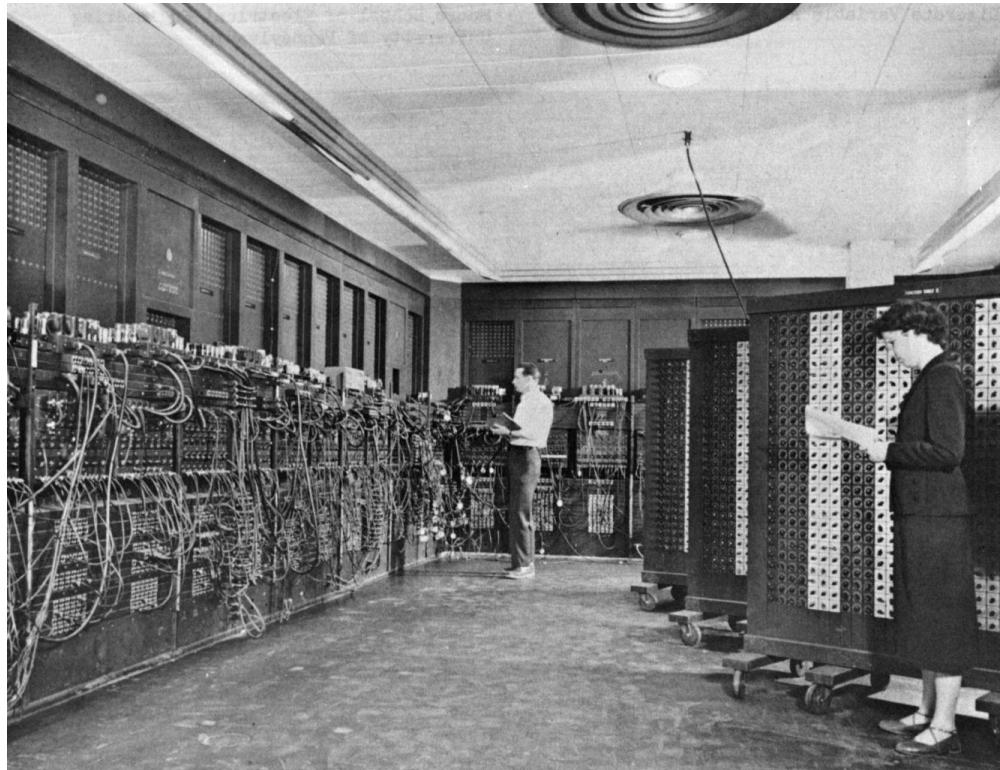
Violate strong Church-Turing thesis

Potential to exceed the performance of CC for problems such as:

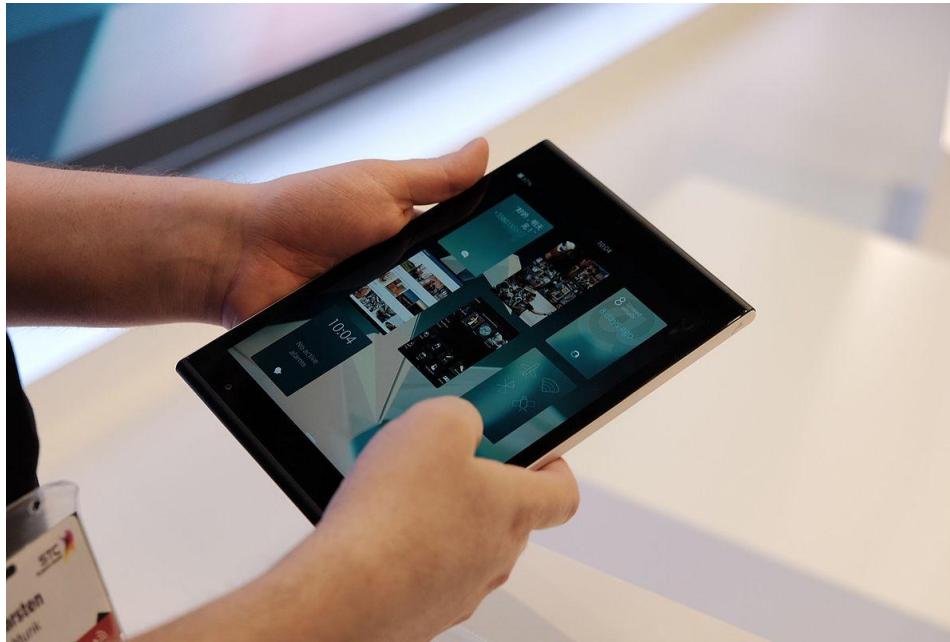
1. Cybersecurity
2. Materials science
3. Chemistry
4. Pharmaceuticals
5. Machine learning
6. Optimization

Over past 80 years CC's have changed dramatically

from the room-filling vacuum-tube-based computers like ENIAC...



....to the tablets and phones people use today.



What does a QC look like?

Currently, QCs look like an ENIAC than like a laptop or tablet



How Is a Quantum Computer Different?

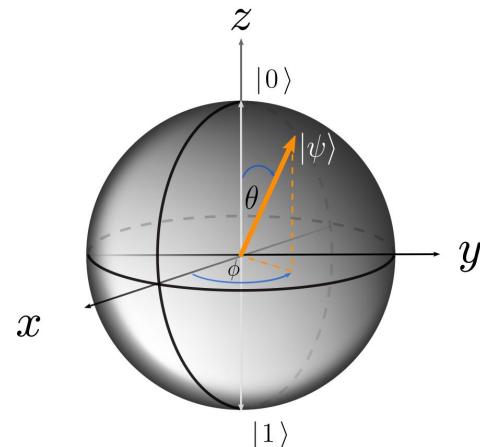
- For N bits, there are 2^N possible classical states.
- CC can represent only one of these N-bit states at a time.
- Qubits in a quantum computer can be set into a single superposition state that may simultaneously carry aspects of all 2^N components

$$|\psi\rangle = \cos(\theta/2)|0\rangle + e^{i\phi} \sin(\theta/2)|1\rangle$$

$$|0\rangle = \begin{bmatrix} 1 \\ 0 \end{bmatrix}$$

$$|1\rangle = \begin{bmatrix} 0 \\ 1 \end{bmatrix}$$

$$|\psi\rangle = \begin{bmatrix} \cos(\theta/2) \\ e^{i\phi} \sin(\theta/2) \end{bmatrix}$$



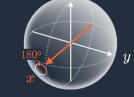
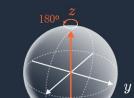
	Bits	Probabilistic Bits	Qubits
State (Single Unit)	Bit $\in \{0, 1\}$	\vec{s} Real Vector $\vec{s} = a\vec{0} + b\vec{1}$ $a, b \in R_+$ $a + b = 1$	Complex Vector $ \psi\rangle = \alpha 0\rangle + \beta 1\rangle$ $\alpha, \beta \in C$ $ \alpha ^2 + \beta ^2 = 1$
State (Multi Unit)	Bitstring $\in \{0, 1\}^n$	Prob. Distribution (Stochastic Vector) $\vec{s} = \{p_x\}_{x \in \{0,1\}^n}$	Wavefunction (Complex Vector) $ \psi\rangle = \{\alpha_x\}_{x \in \{0,1\}^n}$
Operations	Boolean Logic	Stochastic Matrices $\sum_{j=1}^S P_{i,j} = 1$	Unitary Matrices $U^\dagger U = 1$
Component Ops	Boolean Gates	Tensor Product of Matrices	Tensor Product of Matrices

$$|\psi\rangle = \alpha_0|00\cdots 0\rangle + \alpha_1|00\cdots 01\rangle + \cdots + \alpha_{2^n-1}|11\cdots 1\rangle$$

$$|\phi\rangle = a|00\rangle - b|11\rangle \leftarrow \textbf{Entangled State}$$

Classical and Quantum Gates

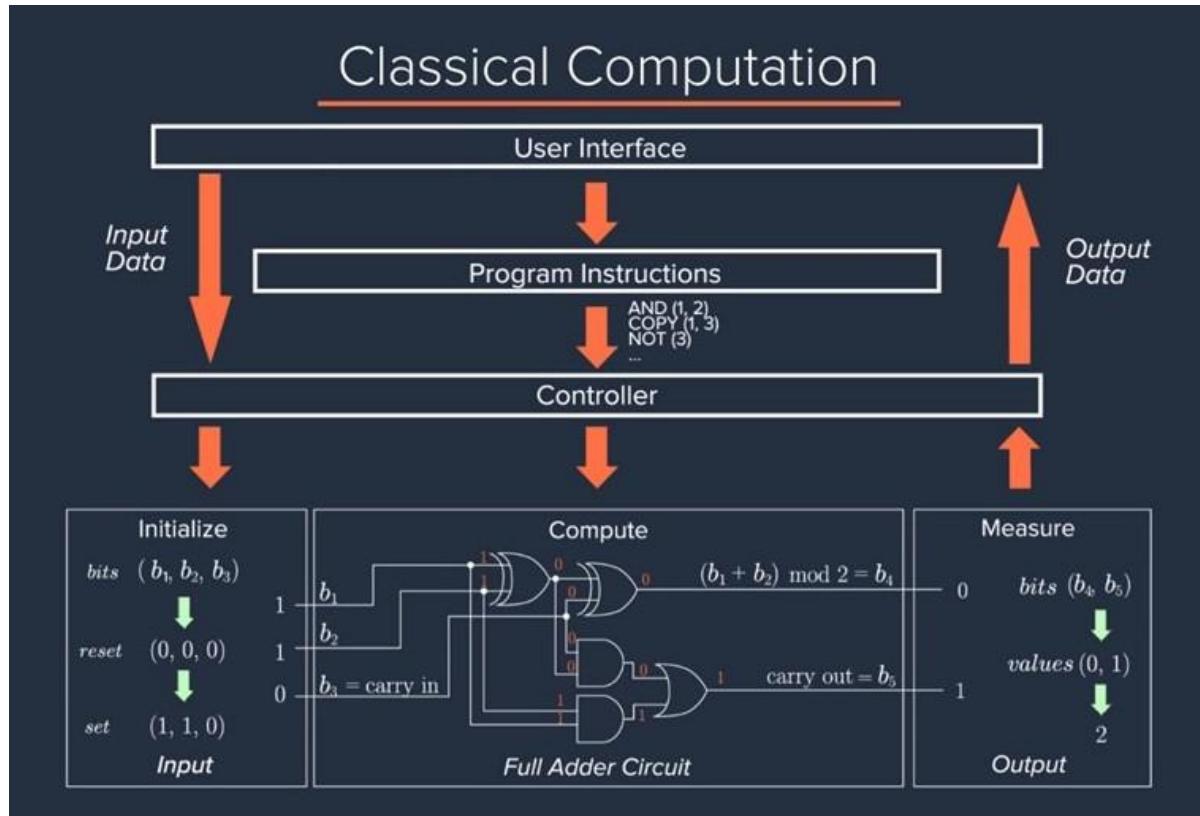
GATE	CIRCUIT REPRESENTATION	TRUTH TABLE										
NOT	The output is 1 when the input is 0 and 0 when the input is 1.											
		<table border="1"> <thead> <tr> <th>Input</th> <th>Output</th> </tr> </thead> <tbody> <tr> <td>0</td> <td>1</td> </tr> <tr> <td>1</td> <td>0</td> </tr> </tbody> </table>	Input	Output	0	1	1	0				
Input	Output											
0	1											
1	0											
AND	The output is 1 only when both inputs are 1, otherwise the output is 0.											
		<table border="1"> <thead> <tr> <th>Input</th> <th>Output</th> </tr> </thead> <tbody> <tr> <td>0 0</td> <td>0</td> </tr> <tr> <td>0 1</td> <td>0</td> </tr> <tr> <td>1 0</td> <td>0</td> </tr> <tr> <td>1 1</td> <td>1</td> </tr> </tbody> </table>	Input	Output	0 0	0	0 1	0	1 0	0	1 1	1
Input	Output											
0 0	0											
0 1	0											
1 0	0											
1 1	1											
OR	The output is 0 only when both inputs are 0, otherwise the output is 1.											
		<table border="1"> <thead> <tr> <th>Input</th> <th>Output</th> </tr> </thead> <tbody> <tr> <td>0 0</td> <td>0</td> </tr> <tr> <td>0 1</td> <td>1</td> </tr> <tr> <td>1 0</td> <td>1</td> </tr> <tr> <td>1 1</td> <td>1</td> </tr> </tbody> </table>	Input	Output	0 0	0	0 1	1	1 0	1	1 1	1
Input	Output											
0 0	0											
0 1	1											
1 0	1											
1 1	1											
NAND	The output is 0 only when both inputs are 1, otherwise the output is 1.											
		<table border="1"> <thead> <tr> <th>Input</th> <th>Output</th> </tr> </thead> <tbody> <tr> <td>0 0</td> <td>1</td> </tr> <tr> <td>0 1</td> <td>1</td> </tr> <tr> <td>1 0</td> <td>1</td> </tr> <tr> <td>1 1</td> <td>0</td> </tr> </tbody> </table>	Input	Output	0 0	1	0 1	1	1 0	1	1 1	0
Input	Output											
0 0	1											
0 1	1											
1 0	1											
1 1	0											
NOR	The output is 1 only when both inputs are 0, otherwise the output is 0.											
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Input	Output											
0 0	1											
0 1	0											
1 0	0											
1 1	0											
XOR	The output is 1 only when the two inputs have different value, otherwise the output is 0.											
		<table border="1"> <thead> <tr> <th>Input</th> <th>Output</th> </tr> </thead> <tbody> <tr> <td>0 0</td> <td>0</td> </tr> <tr> <td>0 1</td> <td>1</td> </tr> <tr> <td>1 0</td> <td>1</td> </tr> <tr> <td>1 1</td> <td>0</td> </tr> </tbody> </table>	Input	Output	0 0	0	0 1	1	1 0	1	1 1	0
Input	Output											
0 0	0											
0 1	1											
1 0	1											
1 1	0											
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0 0	1											
0 1	0											
1 0	0											
1 1	1											

GATE	CIRCUIT REPRESENTATION	MATRIX REPRESENTATION	TRUTH TABLE	BLOCH SPHERE						
I	Identity-gate: no rotation is performed.		$I = \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$	<table border="1"> <thead> <tr> <th>Input</th> <th>Output</th> </tr> </thead> <tbody> <tr> <td> 0></td> <td> 0></td> </tr> <tr> <td> 1></td> <td> 1></td> </tr> </tbody> </table> 	Input	Output	0>	0>	1>	1>
Input	Output									
0>	0>									
1>	1>									
X	X gate: rotates the qubit state by π radians (180°) about the x-axis.		$X = \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$	<table border="1"> <thead> <tr> <th>Input</th> <th>Output</th> </tr> </thead> <tbody> <tr> <td> 0></td> <td> 1></td> </tr> <tr> <td> 1></td> <td> 0></td> </tr> </tbody> </table> 	Input	Output	0>	1>	1>	0>
Input	Output									
0>	1>									
1>	0>									
Y	Y gate: rotates the qubit state by π radians (180°) about the y-axis.		$Y = \begin{pmatrix} 0 & -i \\ i & 0 \end{pmatrix}$	<table border="1"> <thead> <tr> <th>Input</th> <th>Output</th> </tr> </thead> <tbody> <tr> <td> 0></td> <td>$i 1\rangle$</td> </tr> <tr> <td> 1></td> <td>$-i 0\rangle$</td> </tr> </tbody> </table> 	Input	Output	0>	$i 1\rangle$	1>	$-i 0\rangle$
Input	Output									
0>	$i 1\rangle$									
1>	$-i 0\rangle$									
Z	Z gate: rotates the qubit state by π radians (180°) about the z-axis.		$Z = \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$	<table border="1"> <thead> <tr> <th>Input</th> <th>Output</th> </tr> </thead> <tbody> <tr> <td> 0></td> <td> 0></td> </tr> <tr> <td> 1></td> <td>$- 1\rangle$</td> </tr> </tbody> </table> 	Input	Output	0>	0>	1>	$- 1\rangle$
Input	Output									
0>	0>									
1>	$- 1\rangle$									
S	S gate: rotates the qubit state by $\frac{\pi}{2}$ radians (90°) about the z-axis.		$S = \begin{pmatrix} 1 & 0 \\ 0 & e^{i\frac{\pi}{2}} \end{pmatrix}$	<table border="1"> <thead> <tr> <th>Input</th> <th>Output</th> </tr> </thead> <tbody> <tr> <td> 0></td> <td> 0></td> </tr> <tr> <td> 1></td> <td>$e^{i\frac{\pi}{2}} 1\rangle$</td> </tr> </tbody> </table> 	Input	Output	0>	0>	1>	$e^{i\frac{\pi}{2}} 1\rangle$
Input	Output									
0>	0>									
1>	$e^{i\frac{\pi}{2}} 1\rangle$									
T	T gate: rotates the qubit state by $\frac{\pi}{4}$ radians (45°) about the z-axis.		$T = \begin{pmatrix} 1 & 0 \\ 0 & e^{i\frac{\pi}{4}} \end{pmatrix}$	<table border="1"> <thead> <tr> <th>Input</th> <th>Output</th> </tr> </thead> <tbody> <tr> <td> 0></td> <td> 0></td> </tr> <tr> <td> 1></td> <td>$e^{i\frac{\pi}{4}} 1\rangle$</td> </tr> </tbody> </table> 	Input	Output	0>	0>	1>	$e^{i\frac{\pi}{4}} 1\rangle$
Input	Output									
0>	0>									
1>	$e^{i\frac{\pi}{4}} 1\rangle$									
H	H gate: rotates the qubit state by π radians (180°) about an axis diagonal in the x-z plane. This is equivalent to an X-gate followed by a $\frac{\pi}{2}$ rotation about the y-axis.		$H = \frac{1}{\sqrt{2}} \begin{pmatrix} 1 & 1 \\ 1 & -1 \end{pmatrix}$	<table border="1"> <thead> <tr> <th>Input</th> <th>Output</th> </tr> </thead> <tbody> <tr> <td> 0></td> <td>$\frac{ 0> + 1>}{\sqrt{2}}$</td> </tr> <tr> <td> 1></td> <td>$\frac{ 0> - 1>}{\sqrt{2}}$</td> </tr> </tbody> </table> 	Input	Output	0>	$\frac{ 0> + 1>}{\sqrt{2}}$	1>	$\frac{ 0> - 1>}{\sqrt{2}}$
Input	Output									
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1>	$\frac{ 0> - 1>}{\sqrt{2}}$									

GATE	CIRCUIT REPRESENTATION	MATRIX REPRESENTATION	TRUTH TABLE										
Controlled-NOT gate: apply an X-gate to the target qubit if the control qubit is in state $ 1\rangle$		$CNOT = \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{pmatrix}$	<table border="1"> <thead> <tr> <th>Input</th><th>Output</th></tr> </thead> <tbody> <tr> <td>$00\rangle$</td><td>$00\rangle$</td></tr> <tr> <td>$01\rangle$</td><td>$01\rangle$</td></tr> <tr> <td>$10\rangle$</td><td>$11\rangle$</td></tr> <tr> <td>$11\rangle$</td><td>$10\rangle$</td></tr> </tbody> </table>	Input	Output	$ 00\rangle$	$ 00\rangle$	$ 01\rangle$	$ 01\rangle$	$ 10\rangle$	$ 11\rangle$	$ 11\rangle$	$ 10\rangle$
Input	Output												
$ 00\rangle$	$ 00\rangle$												
$ 01\rangle$	$ 01\rangle$												
$ 10\rangle$	$ 11\rangle$												
$ 11\rangle$	$ 10\rangle$												
Controlled-phase gate: apply a Z-gate to the target qubit if the control qubit is in state $ 1\rangle$		$cZ = \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & -1 \end{pmatrix}$	<table border="1"> <thead> <tr> <th>Input</th><th>Output</th></tr> </thead> <tbody> <tr> <td>$00\rangle$</td><td>$00\rangle$</td></tr> <tr> <td>$01\rangle$</td><td>$01\rangle$</td></tr> <tr> <td>$10\rangle$</td><td>$10\rangle$</td></tr> <tr> <td>$11\rangle$</td><td>$- 11\rangle$</td></tr> </tbody> </table>	Input	Output	$ 00\rangle$	$ 00\rangle$	$ 01\rangle$	$ 01\rangle$	$ 10\rangle$	$ 10\rangle$	$ 11\rangle$	$- 11\rangle$
Input	Output												
$ 00\rangle$	$ 00\rangle$												
$ 01\rangle$	$ 01\rangle$												
$ 10\rangle$	$ 10\rangle$												
$ 11\rangle$	$- 11\rangle$												
Control qubit "A" Target qubit "B"		$U_{AB}^c = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & u_{11} & u_{12} \\ 0 & 0 & u_{21} & u_{22} \end{bmatrix}$ $U_{A,B}^c = 0\rangle\langle 0 _A \otimes I_B + 1\rangle\langle 1 _A \otimes U_B$											

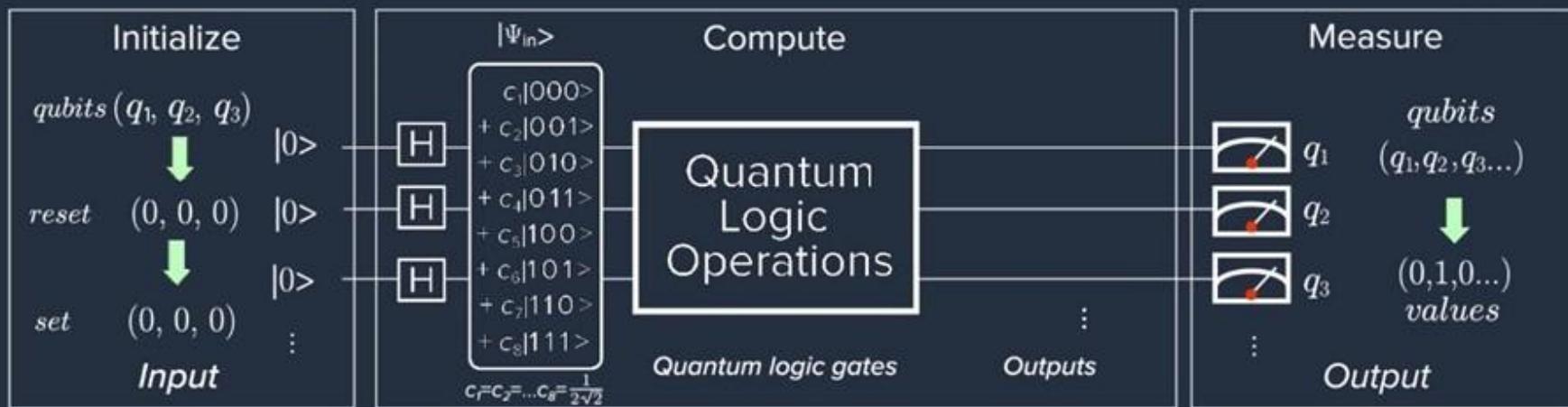
Universal Quantum Algorithms

How a Universal Algorithm Works: Classical

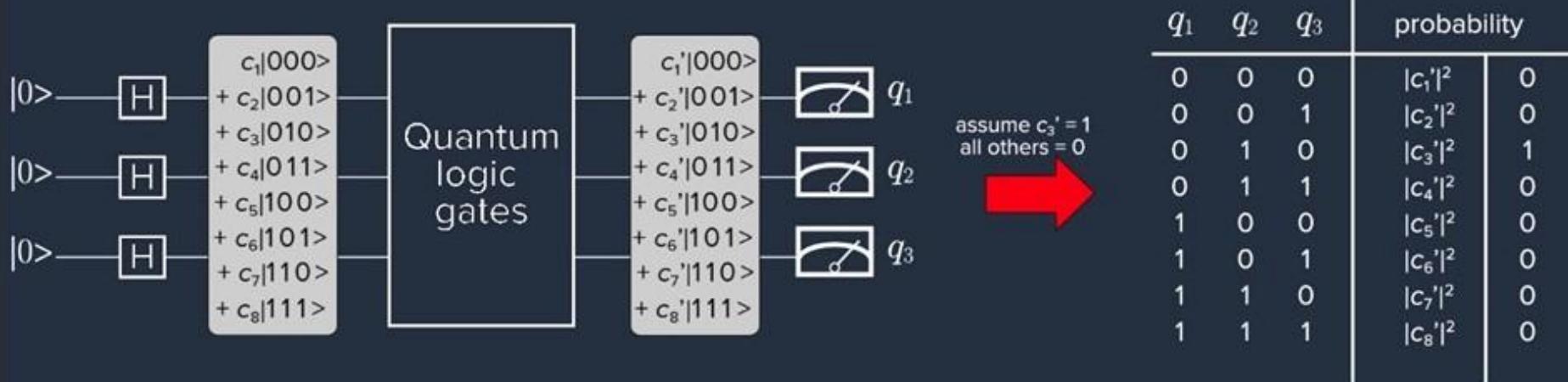


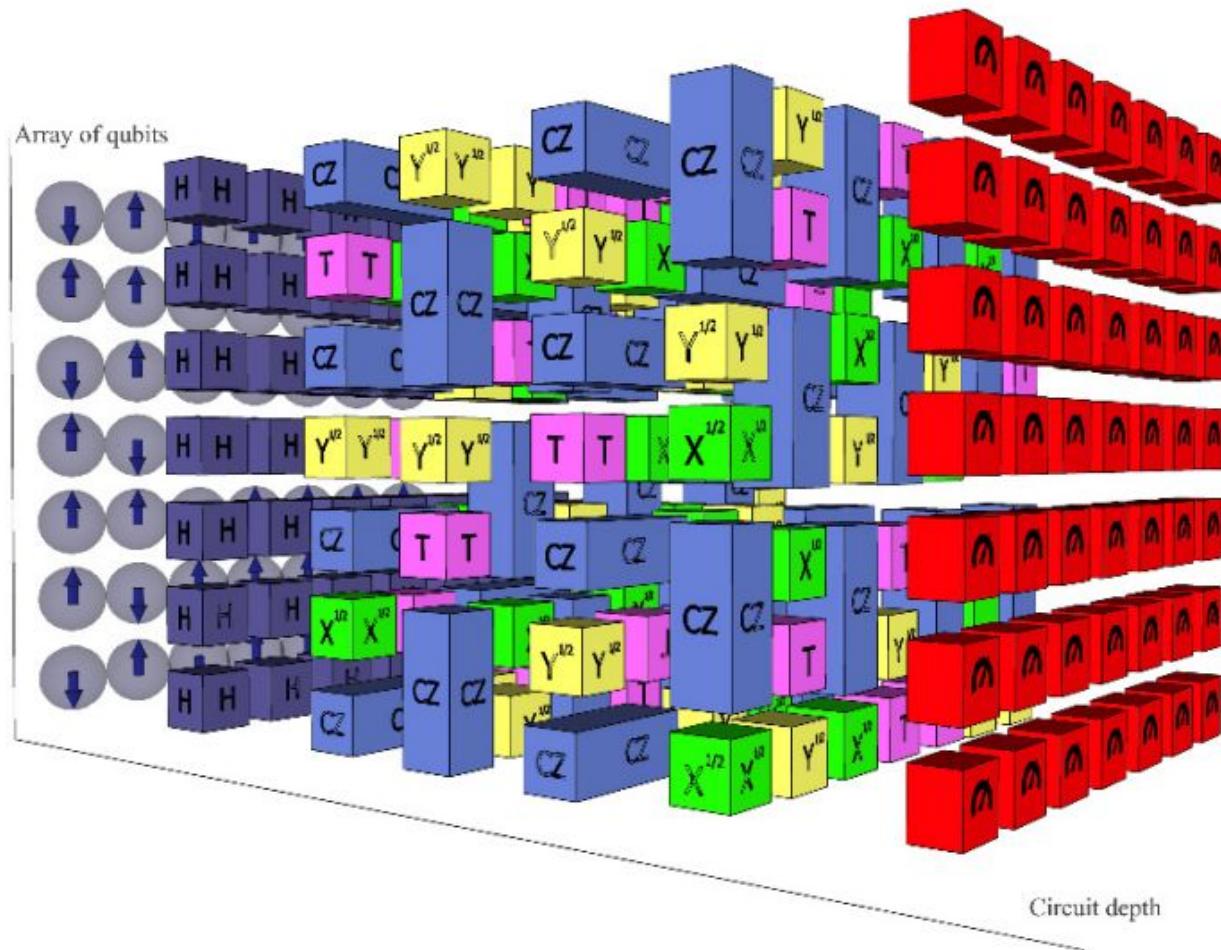
How a Universal Algorithm Works: Quantum

Quantum Computation



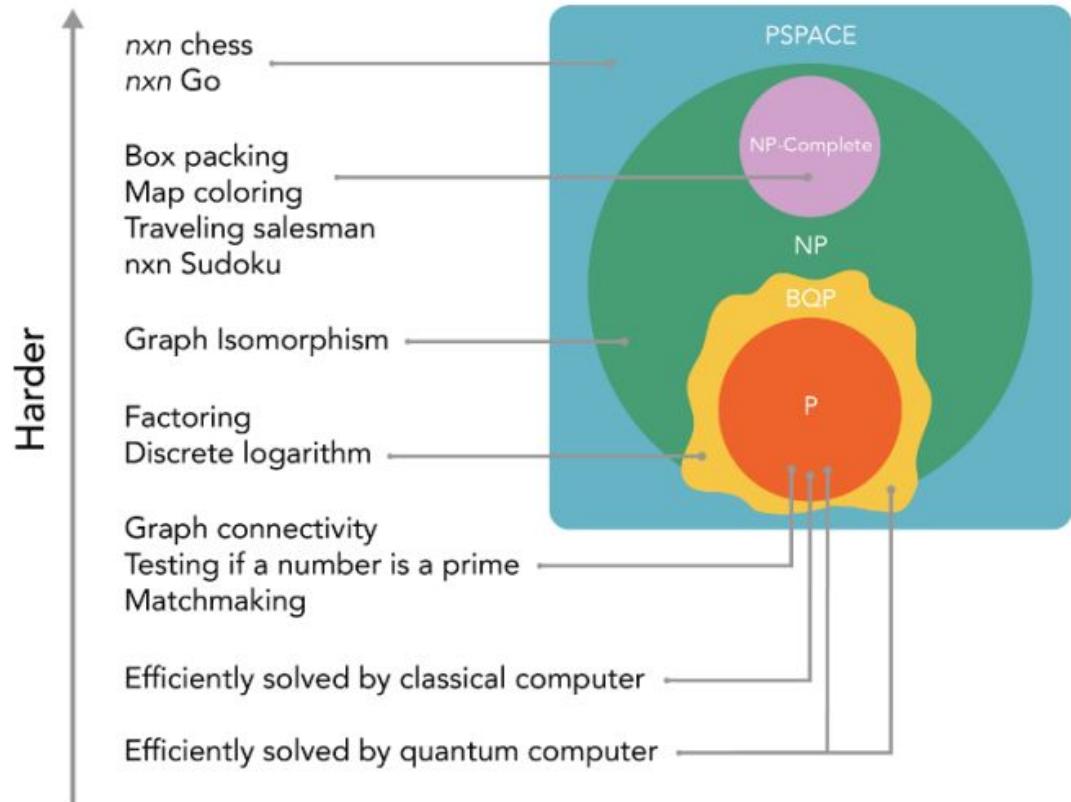
Measurement





What Problems Can Be Solved by QC?

Example Problems



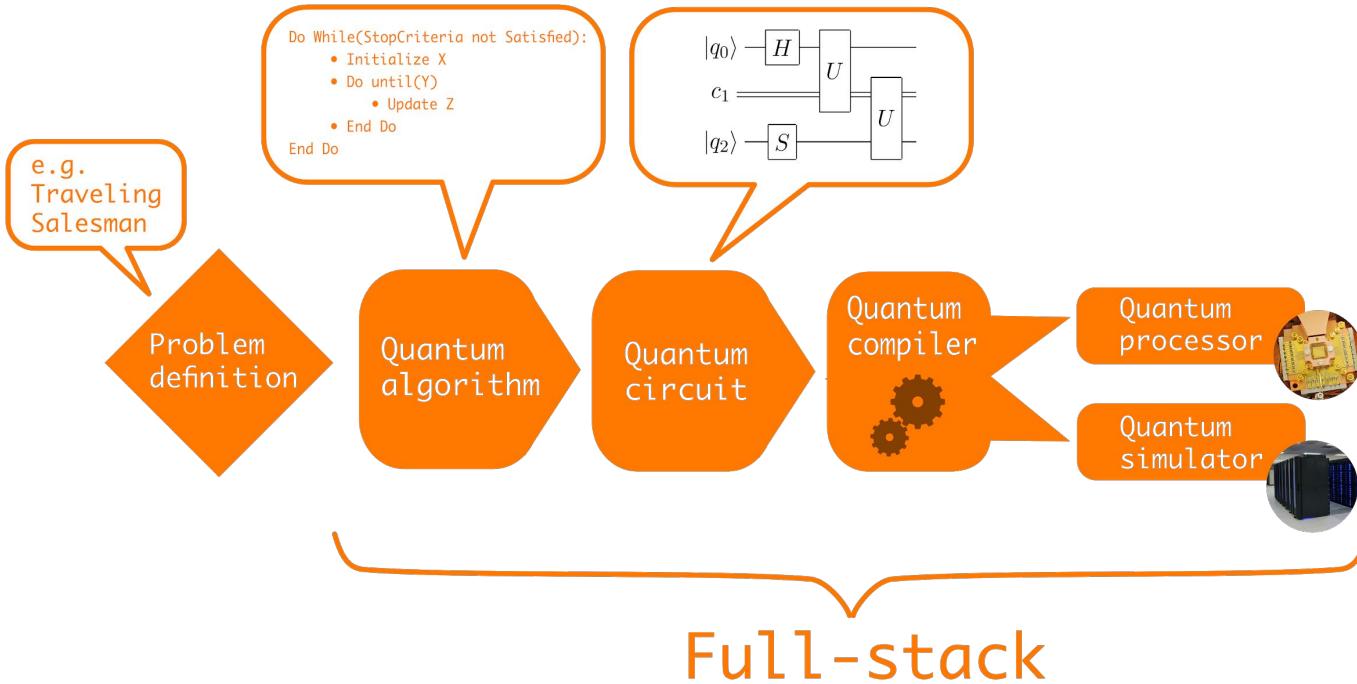
1. **Cybersecurity (NP)**
2. **Materials science (NP, PSPACE)**
3. **Chemistry (NP, PSPACE)**
4. **Nitrogen fixation (PSPACE)**
5. **Pharmaceuticals (PSPACE)**
6. **Machine learning (NP)**
7. **Optimization (NP)**

QUANTUM ALGORITHM SPEEDUPS

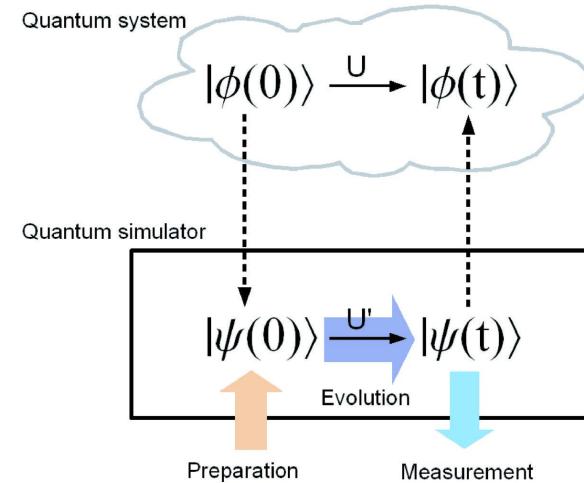
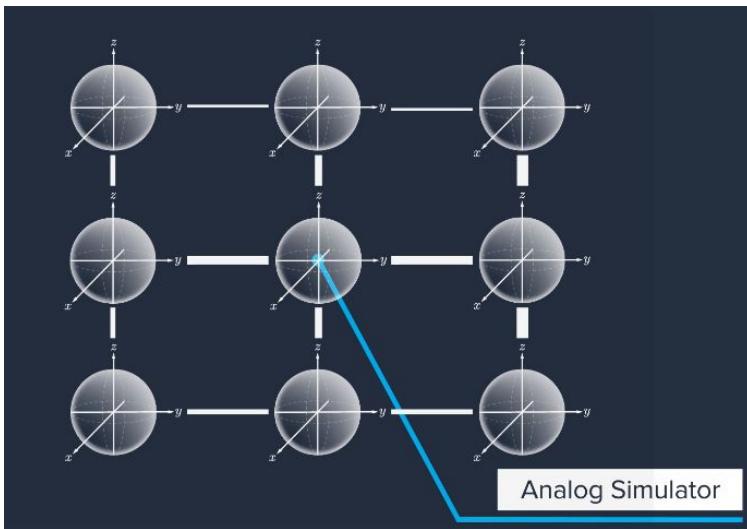
ALGORITHM	CLASSICAL RESOURCES	QUANTUM RESOURCES	QUANTUM ADVANTAGE	LIMITATION
Simulation (quantum chemistry)	2^N (for N atoms)	N^C	Exponential*	Mapping problem to qubits
Factoring (+ related number theoretic)	2^N (for N digits)	N^3	Exponential	Classical runtime limit unproven
Linear systems ($Ax=b$)	2^N (for N digits)	$\sim N$	Exponential	Strict conditions, e.g. sparse matrix
Optimization	2^N (for N items)	?	?	Empirical
Search (unsorted/unstructured data)	N (for N entries)	\sqrt{N}	Polynomial (\sqrt{N})	Data loading

Types of Quantum Computers

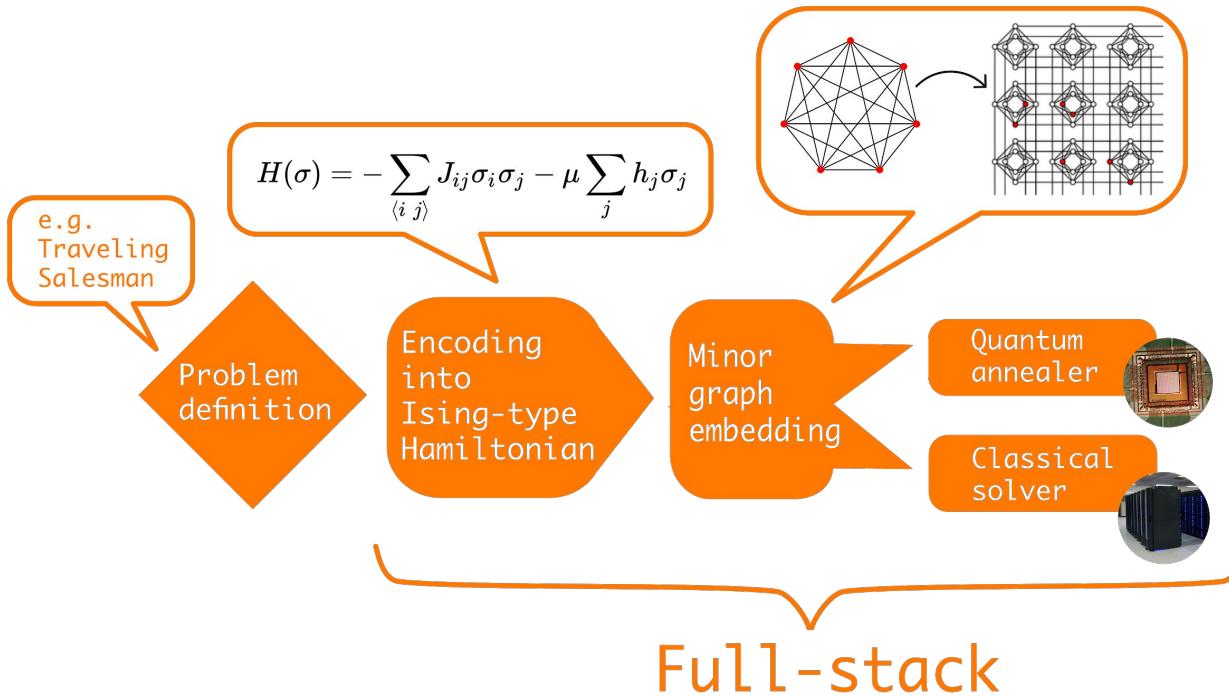
Universal Gate Model Fault Tolerant



Quantum Simulator



Quantum Annealer

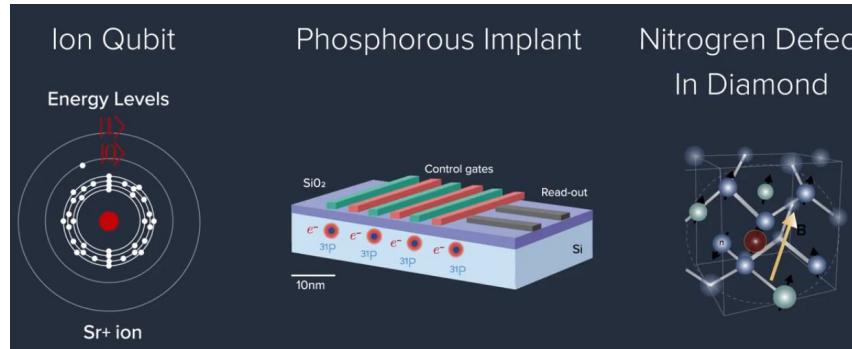


How to Build One?

Qubit Modalities and Di Vincenzo Criteria

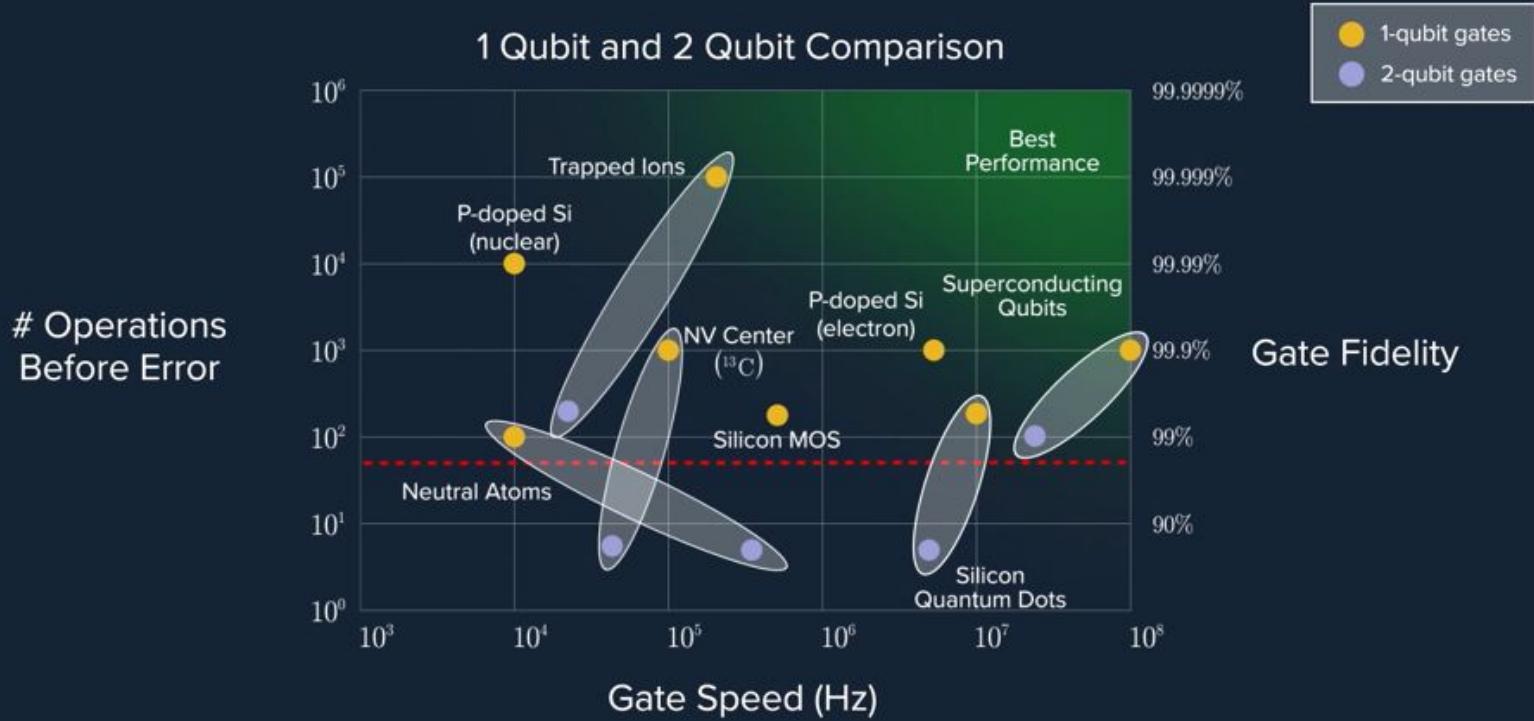
	D1 SCALABLE SYSTEM	D2 INITIALIZATION	D3 MEASUREMENT	D4 UNIVERSAL GATES	D5 COHERENCE	D6 INTERCONVERSION	D7 COMMUNICATION
SiGe Quantum Dots	Yellow	Green	Green	Yellow	Green	Yellow	Yellow
Doped Silicon	Yellow	Yellow	Green	Yellow	Green	Yellow	Yellow
NV Centers	Yellow	Yellow	Green	Yellow	Green	Green	Green
Neutral Atoms	Green	Green	Yellow	Yellow	Green	Green	Green
Trapped Ions	Green	Green	Green	Green	Green	Yellow	Yellow
Superconductors	Yellow	Green	Green	Green	Yellow	Yellow	Green

- █ Sufficient demonstrations exist to proceed to the 100 qubit level
- █ Concepts and/or first demonstrations exist



		SUPER-CONDUCTING	TRAPPED IONS	SILICON QUANTUM DOTS		IMPURITY-DOPED SILICON		IMPURITY CENTERS	TRAPPED NEUTRAL IONS
QUBIT MODALITY	MATERIALS	Al	Yb+, Ca+, Sr+, Be+, Ba+, Mg+	isotopically purified Si, SiGe	isotopically purified Si	Phosphorus doped isotopically purified silicon	Nitrogen vacancies in diamond	Rb, Cs, Ho	
	TYPE	transmon	hyperfine & optical transitions	quantum dot 2DEG	quantum dot Si MOS	implanted dopant	nuclear + electron spin	Rydberg states	
	CONTROL/RO	microwaves	microwaves & optics	baseband or microwave	baseband or microwave	microwaves	microwaves & optics	uwave	
	STATE	junction phase	atomic state of electron	electron spin	electron spin	electron spin	nuclear spin	nuclear + electron spin	Rydberg state
STATE-OF-ART TIMES (ns)	T1	50,000	>1E14 (years)	1,000,000,000	2,000,000,000	5,000,000,000	>1E14	100,000,000	5,000,000,000
	T2	100,000	50,000,000,000	400,000	1,200,000	100,000	1,000,000,000	20,000,000	1,000,000,000
	1QB GATE	10	5,000	100	2,000	200	100,000	10,000	100,000
	2QB GATE	40	50,000	200	1,000	TBD	TBD	25,000	3,000
	RO	200	30,000	1,000	100,000	1,000,000	50,000,000	50,000	10,000,000
FIDELITY	1QB	99.90%	99.999%	99.60%	99.5%	99.90%	99.99%	99.90%	99%
	2QB	99.0%	99.5%	80%	TBD	TBD	TBD	82%	80%
	RO	99%	99.99%	99%	95%	95.00%	99.90%	94%	99.90%
CLOCK (MHz)	1QB GATE	100.00	0.20	10.00	0.50	5.00	0.01	0.10	0.01
	2QB GATE	25.00	0.02	5.00	1.00	TBD	TBD	0.04	0.33
	READOUT	5.00	0.03	1.0E+00	1.0E-02	1.0E-03	2.0E-05	2.00E-02	1.00E-04

1 Qubit and 2 Qubit Fidelity and Gate Speed

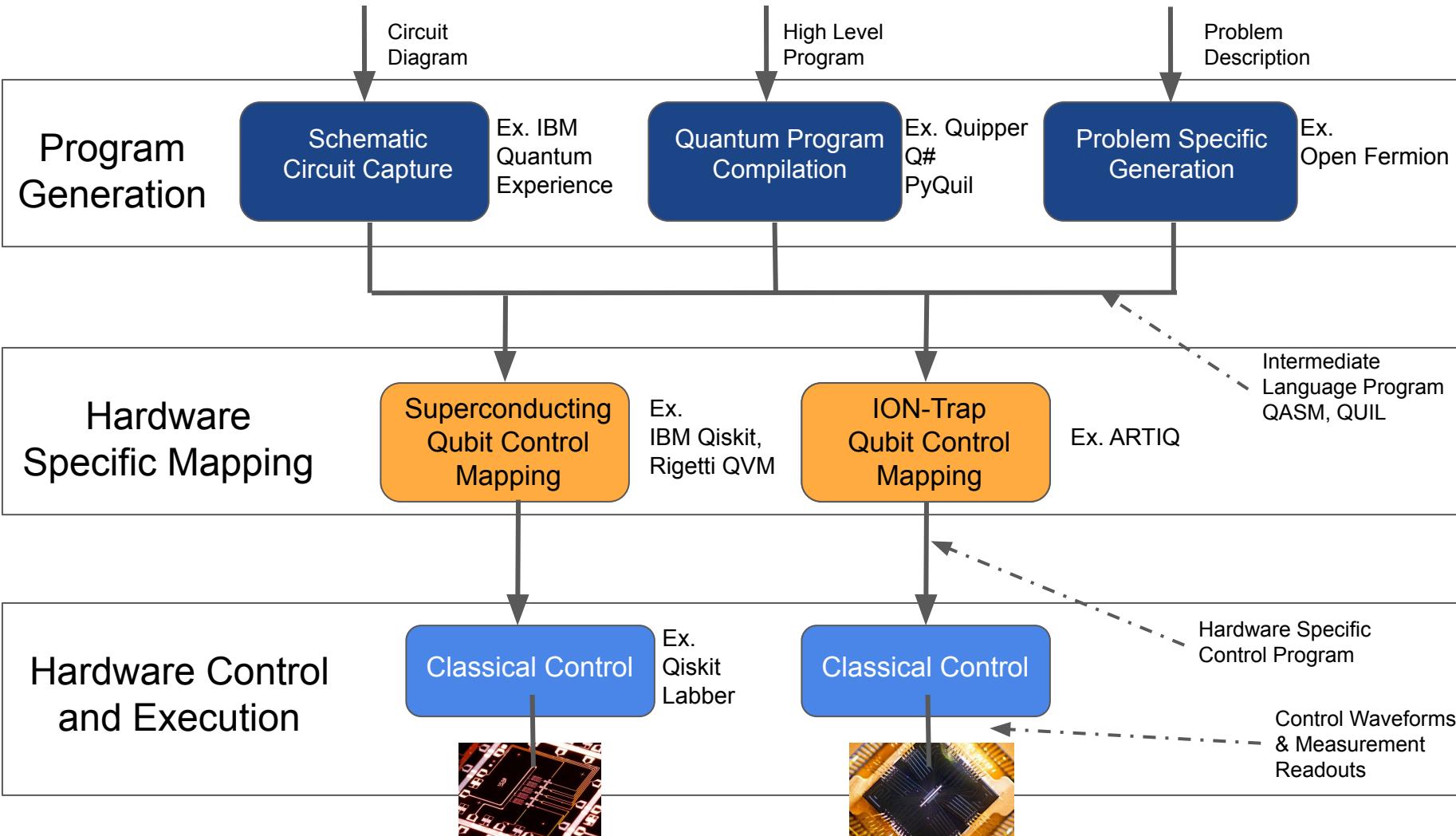


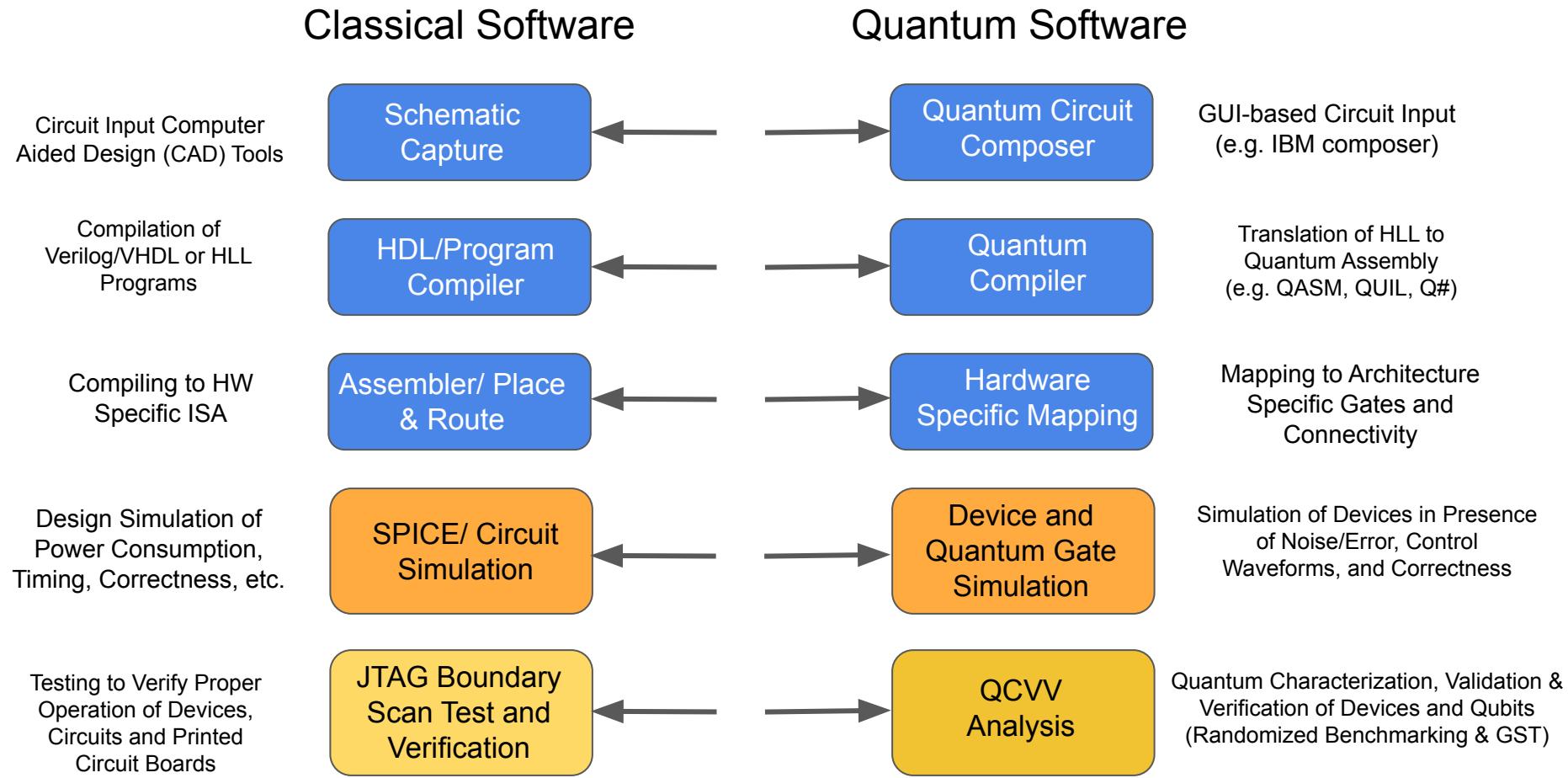
Quantum Software

- **How do we efficiently design a quantum processor?**
- **How do we validate that it is working properly?**
- **How we do program it?**

The 3 primary types of software

- 1. Program generation software (technology agnostic)**
 - Schematic capture (generally related to the quantum circuit model)
 - HLL: high-level programming languages -- (C, Fortran, Pascal - abstracting away subroutines)
 - Lower-level assembly languages (abstracting away specific hardware controls and subroutines)
 - Problem-specific platforms
- 2. Circuit mapping software (require knowledge of the hardware architecture)**
- 3. Control and execution software (require knowledge on hardware architecture)**





Open Source Development Libraries for QC Programming

1. Build a quantum circuit consisting of quantum and/or classical registers
2. Add operations to the circuit
3. Simulate the circuit

Company	Name	Links	OS	Classical Language	Quantum Language
IBM	Qiskit	https://qiskit.org/	Mac, Windows, Linux	Python	OpenQASM
Rigetti	Forest	https://www.rigetti.com/forest	Mac, Windows, Linux	Python	QUIL
Google	CirQ	https://github.com/quantumlib/Cirq	Mac, Windows, Linux	Python	
Xanadu	StrawberryFields	https://strawberryfields.readthedocs.io/en/latest/	Mac, Windows, Linux	Python	Blackbird
D-Wave	Ocean SDK	https://www.dwavesys.com/take-leap	Mac, Windows, Linux	Python	QMASM
Microsoft	QDK	https://www.microsoft.com/en-us/quantum/development-kit	Mac, Windows, Linux	Python	Q#

All available software platforms at <https://quantiki.org/wiki/list-qc-simulators>