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January 19, 2017



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- Using a stack, you can only access the object at the top of the stack; you cannot access, add to, or remove from any other point in the stack.
- Stacks are an abstraction, or general idea, of how the data structure functions, and do not have specific implementations. Therefore, a stack is an Abstract Data Type (ADT) which has more than one implementation.

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 - object top(): returns the last inserted element without removing it
 - integer size(): returns the number of elements stored
 - boolean isEmpty(): indicates whether no elements are stored

Example

Operation	Return value	Stack
push(5)	-	(5)
push(3)	-	(3, 5)
size()	2	(3, 5)
pop()	3	(5)
isEmpty()	false	(5)
pop()	5	()
isEmpty()	true	()
pop()	null	()
push(7)	-	(7)
push(9)	_	(9, 7)
top()	9	(9, 7)
push(4)	_	(4, 9, 7)
size()	3	(4, 9, 7)



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- We add elements from left to right and remove elements from right to left.
- A variable keeps track of the index of the top element.
 (Alternatively, a variable representing the size of the stack could also be used to determine where to add the next item.)
- The array storing the stack elements may become full. A push() operation may then throw an implementation-defined exception or resize the backing array. This behavior is not defined or forced by the ADT.

 Example of an array implementation for Stack ADT where the top of the stack is index 3, the size of the stack is 4, and if you "pop" the top of the stack data 2 will come off the stack.

```
procedure PUSH(o)

arr[size] \leftarrow o

size \leftarrow size + 1

end procedure

procedure POP

size \leftarrow size - 1

item \leftarrow arr[size]

arr[size] \leftarrow NULL

return item

end procedure
```

Linked List-backed Stack

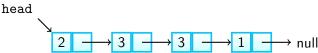
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- A linked list could also be used as the backing data structure of a stack.
- Elements would be added and removed to the same end of the list. For a stack, this usually means that the most efficient way to do this would be to add to and remove from the front of a linked list, as this would be O(1) in most cases.

Linked List-backed Stack

 Example of a linked list implementation for Stack ADT where the top of the stack is at the head, the size of the stack is 4, and if you "pop" the top of the stack data 2 will come off the stack.



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- For an array-backed stack, if the backing array is to resized when it becomes full, this would then be an O(n) operation (but the push() operation itself would be considered amortized O(1)).
- Linked list-backed stacks do not have either of the above two limitations

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- This stack also allows for recursion to work correctly.
- This is known in general as the activation stack.

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