## CSMM: Lesson 1.5 HW

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For the following questions, use these function definitions, along with the function definitions from previous homeworks:

$$G := \lambda abc.abc$$

$$Y := \lambda a.(\lambda b.a(bb))(\lambda b.a(bb))$$

$$\chi := \lambda rn.G(\lor (= n0)(= n1))1(+(r(-n1))(r(-n2)))$$

$$\delta := \lambda x.\Phi(xF)(+(xT)(xF))$$

$$\chi_1 := \lambda n.(n\delta(\Phi 01))F$$

(1-2) For each of the following,

Find the normal form of the following  $\lambda$ -expressions (show work)

- 1.  $(Y\chi)^3$
- 2.  $\chi_1 3$
- 3. Define a function ! such that (Y!)n returns n!. Try it on a few different values of n to convince yourself that it works.

## **ANSWERS**

Derivations vary, just be careful with parens and variables.

- 1. 3
- 2. 3

Several possible formulations exist, one such answer is:

3. 
$$! := \lambda rn.G(=n0)1(\times n(r(-n1)))$$