

## 1 Find Limits Graphically

1. 
$$\begin{cases} f(1) = \\ \lim_{x \rightarrow 1^-} f(x) = \\ \lim_{x \rightarrow 1^+} f(x) = \\ \lim_{x \rightarrow 1} f(x) = \end{cases}$$

4. 
$$\begin{cases} f(4) = \\ \lim_{x \rightarrow 4^-} f(x) = \\ \lim_{x \rightarrow 4^+} f(x) = \\ \lim_{x \rightarrow 4} f(x) = \end{cases}$$

7. 
$$\begin{cases} f(7) = \\ \lim_{x \rightarrow 7^-} f(x) = \\ \lim_{x \rightarrow 7^+} f(x) = \\ \lim_{x \rightarrow 7} f(x) = \end{cases}$$

2. 
$$\begin{cases} f(2) = \\ \lim_{x \rightarrow 2^-} f(x) = \\ \lim_{x \rightarrow 2^+} f(x) = \\ \lim_{x \rightarrow 2} f(x) = \end{cases}$$

5. 
$$\begin{cases} f(5) = \\ \lim_{x \rightarrow 5^-} f(x) = \\ \lim_{x \rightarrow 5^+} f(x) = \\ \lim_{x \rightarrow 5} f(x) = \end{cases}$$

3. 
$$\begin{cases} f(3) = \\ \lim_{x \rightarrow 3^-} f(x) = \\ \lim_{x \rightarrow 3^+} f(x) = \\ \lim_{x \rightarrow 3} f(x) = \end{cases}$$

6. 
$$\begin{cases} f(6) = \\ \lim_{x \rightarrow 6^-} f(x) = \\ \lim_{x \rightarrow 6^+} f(x) = \\ \lim_{x \rightarrow 6} f(x) = \end{cases}$$

## 2 Find Limits Involving Infinity Graphically

8. 
$$\begin{cases} f(8) = \\ \lim_{x \rightarrow 8^-} f(x) = \\ \lim_{x \rightarrow 8^+} f(x) = \\ \lim_{x \rightarrow 8} f(x) = \end{cases}$$

10. 
$$\begin{cases} f(10) = \\ \lim_{x \rightarrow 10^-} f(x) = \\ \lim_{x \rightarrow 10^+} f(x) = \\ \lim_{x \rightarrow 10} f(x) = \end{cases}$$

12. 
$$\begin{cases} f(12) = \\ \lim_{x \rightarrow 12^-} f(x) = \\ \lim_{x \rightarrow 12^+} f(x) = \\ \lim_{x \rightarrow 12} f(x) = \end{cases}$$

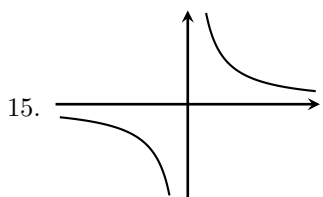
9. 
$$\begin{cases} f(9) = \\ \lim_{x \rightarrow 9^-} f(x) = \\ \lim_{x \rightarrow 9^+} f(x) = \\ \lim_{x \rightarrow 9} f(x) = \end{cases}$$

11. 
$$\begin{cases} f(11) = \\ \lim_{x \rightarrow 11^-} f(x) = \\ \lim_{x \rightarrow 11^+} f(x) = \\ \lim_{x \rightarrow 11} f(x) = \end{cases}$$

13. 
$$\lim_{x \rightarrow -\infty} f(x) =$$

14. 
$$\lim_{x \rightarrow +\infty} f(x) =$$

### 3 Famous Functions



$$f(x) = 1/x$$

$$f(0) =$$

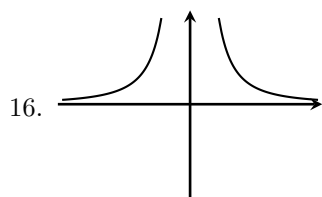
$$\lim_{x \rightarrow 0^-} f(x) =$$

$$\lim_{x \rightarrow 0^+} f(x) =$$

$$\lim_{x \rightarrow 0} f(x) =$$

$$\lim_{x \rightarrow -\infty} f(x) =$$

$$\lim_{x \rightarrow +\infty} f(x) =$$



$$f(x) = 1/x^2$$

$$f(0) =$$

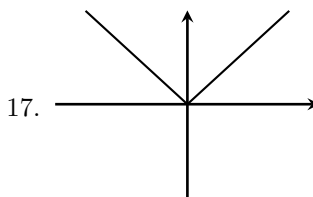
$$\lim_{x \rightarrow 0^-} f(x) =$$

$$\lim_{x \rightarrow 0^+} f(x) =$$

$$\lim_{x \rightarrow 0} f(x) =$$

$$\lim_{x \rightarrow -\infty} f(x) =$$

$$\lim_{x \rightarrow +\infty} f(x) =$$



$$f(x) = |x|$$

$$f(0) =$$

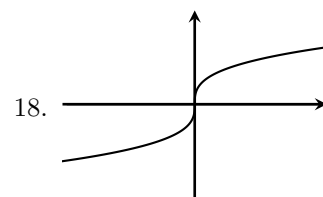
$$\lim_{x \rightarrow 0^-} f(x) =$$

$$\lim_{x \rightarrow 0^+} f(x) =$$

$$\lim_{x \rightarrow 0} f(x) =$$

$$\lim_{x \rightarrow -\infty} f(x) =$$

$$\lim_{x \rightarrow +\infty} f(x) =$$



$$f(x) = \sqrt[3]{x}$$

$$f(0) =$$

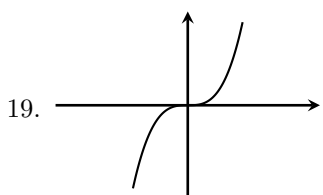
$$\lim_{x \rightarrow 0^-} f(x) =$$

$$\lim_{x \rightarrow 0^+} f(x) =$$

$$\lim_{x \rightarrow 0} f(x) =$$

$$\lim_{x \rightarrow -\infty} f(x) =$$

$$\lim_{x \rightarrow +\infty} f(x) =$$



$$f(x) = x^3$$

$$f(0) =$$

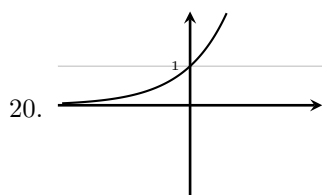
$$\lim_{x \rightarrow 0^-} f(x) =$$

$$\lim_{x \rightarrow 0^+} f(x) =$$

$$\lim_{x \rightarrow 0} f(x) =$$

$$\lim_{x \rightarrow -\infty} f(x) =$$

$$\lim_{x \rightarrow +\infty} f(x) =$$



$$f(x) = e^x$$

$$f(0) =$$

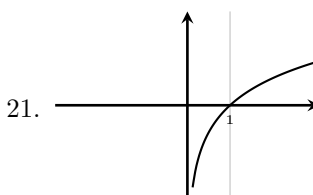
$$\lim_{x \rightarrow 0^-} f(x) =$$

$$\lim_{x \rightarrow 0^+} f(x) =$$

$$\lim_{x \rightarrow 0} f(x) =$$

$$\lim_{x \rightarrow -\infty} f(x) =$$

$$\lim_{x \rightarrow +\infty} f(x) =$$



$$f(x) = \ln(x)$$

$$f(0) =$$

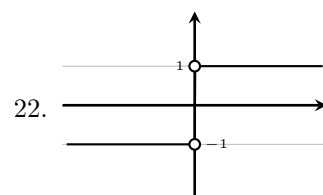
$$\lim_{x \rightarrow 0^-} f(x) =$$

$$\lim_{x \rightarrow 0^+} f(x) =$$

$$\lim_{x \rightarrow 0} f(x) =$$

$$\lim_{x \rightarrow -\infty} f(x) =$$

$$\lim_{x \rightarrow +\infty} f(x) =$$



$$f(x) = \frac{|x|}{x}$$

$$f(0) =$$

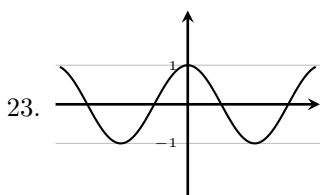
$$\lim_{x \rightarrow 0^-} f(x) =$$

$$\lim_{x \rightarrow 0^+} f(x) =$$

$$\lim_{x \rightarrow 0} f(x) =$$

$$\lim_{x \rightarrow -\infty} f(x) =$$

$$\lim_{x \rightarrow +\infty} f(x) =$$



$$f(x) = \cos(x)$$

$$f(0) =$$

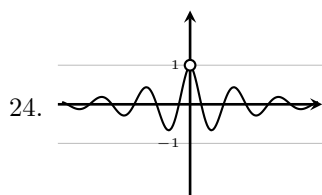
$$\lim_{x \rightarrow 0^-} f(x) =$$

$$\lim_{x \rightarrow 0^+} f(x) =$$

$$\lim_{x \rightarrow 0} f(x) =$$

$$\lim_{x \rightarrow -\infty} f(x) = \text{DNE}$$

$$\lim_{x \rightarrow +\infty} f(x) = \text{DNE}$$



$$f(x) = \frac{\sin(x)}{x}$$

$$f(0) =$$

$$\lim_{x \rightarrow 0^-} f(x) =$$

$$\lim_{x \rightarrow 0^+} f(x) =$$

$$\lim_{x \rightarrow 0} f(x) =$$

$$\lim_{x \rightarrow -\infty} f(x) =$$

$$\lim_{x \rightarrow +\infty} f(x) =$$



$$f(x) = \sin(1/x)$$

$$f(0) = \text{DNE}$$

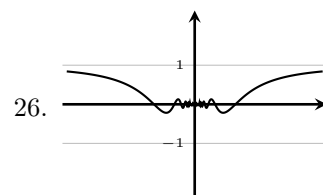
$$\lim_{x \rightarrow 0^-} f(x) = \text{DNE}$$

$$\lim_{x \rightarrow 0^+} f(x) = \text{DNE}$$

$$\lim_{x \rightarrow 0} f(x) = \text{DNE}$$

$$\lim_{x \rightarrow -\infty} f(x) =$$

$$\lim_{x \rightarrow +\infty} f(x) =$$



$$f(x) = x \sin(1/x)$$

$$f(0) =$$

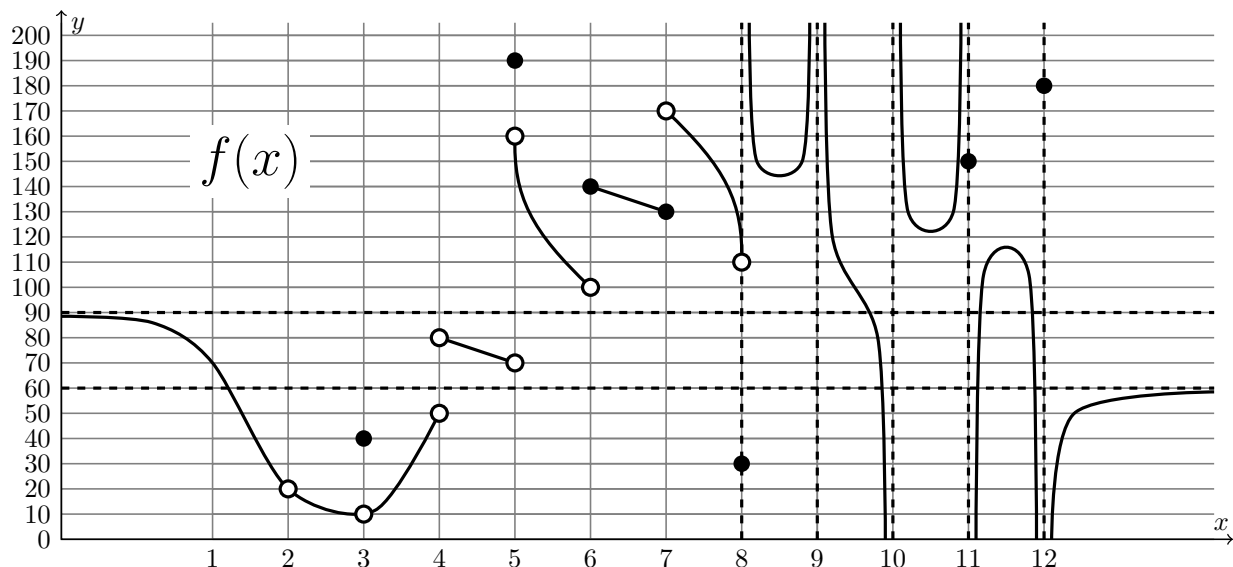
$$\lim_{x \rightarrow 0^-} f(x) =$$

$$\lim_{x \rightarrow 0^+} f(x) =$$

$$\lim_{x \rightarrow 0} f(x) =$$

$$\lim_{x \rightarrow -\infty} f(x) =$$

$$\lim_{x \rightarrow +\infty} f(x) =$$



## 4 Identify Infinite, Jump, Removable Discontinuities Graphically

27. We say  $f$  is **continuous** (cts) at  $x = a$  if  $\lim_{x \rightarrow a} f(x)$  is finite and equals  $f(a)$ .

The function  $f$  above is continuous at integers  $x =$  \_\_\_\_\_.

28. We say  $f$  has a \_\_\_\_\_ discontinuity at \_\_\_\_\_ if  $\lim_{x \rightarrow a} f(x)$  is finite and *unequal* to  $f(a)$ .

The function  $f$  above has this type of discontinuity at integers  $x =$  \_\_\_\_\_.

29. We say  $f$  has a \_\_\_\_\_ discontinuity at \_\_\_\_\_ if  $\lim_{x \rightarrow a^+} f(x)$  and  $\lim_{x \rightarrow a^-} f(x)$  are finite but *unequal*.

The function  $f$  above has this type of discontinuity at integers  $x =$  \_\_\_\_\_.

30. We say  $f$  has an \_\_\_\_\_ discontinuity at \_\_\_\_\_ if  $\lim_{x \rightarrow a^+} f(x)$  or  $\lim_{x \rightarrow a^-} f(x)$  is infinite.

The function  $f$  above has this type of discontinuity at integers  $x =$  \_\_\_\_\_.

## 5 Continuity on an Interval

31. We say  $f$  is **continuous on the open interval**  $(a, b)$  if  $f$  is continuous at every  $x$  in  $(a, b)$ .

Find the union of all open intervals **on which**  $f$  is **continuous**.

(Set-builder notation) \_\_\_\_\_

(Interval notation) \_\_\_\_\_

32. We say  $f$  is **continuous everywhere** if  $f$  is continuous at every  $x$  in \_\_\_\_\_.

33. We say  $f$  is a **continuous function** if  $f$  is continuous at every  $x$  in its \_\_\_\_\_.

## 6 Left and Right Continuity

34. We say  $f$  is \_\_\_\_\_ continuous at  $x = a$  if  $\lim_{x \rightarrow a^+} f(x)$  is finite and equals  $f(a)$ .

The function  $f$  above has this type of continuity at integers  $x =$  \_\_\_\_\_.

35. We say  $f$  is \_\_\_\_\_ continuous at  $x = a$  if  $\lim_{x \rightarrow a^-} f(x)$  is finite and equals  $f(a)$ .

The function  $f$  above has this type of continuity at integers  $x =$  \_\_\_\_\_.

36. We say  $f$  is **continuous on the closed interval**  $[a, b]$  if  $f$  is continuous at every  $x$  in the *open* interval  $(a, b)$

and is \_\_\_\_\_ at  $x = a$  and is \_\_\_\_\_ at  $x = b$ .