

## 1 Finding Limits Graphically

1. 
$$\begin{cases} f(1) = \\ \lim_{x \to 1^{-}} f(x) = \\ \lim_{x \to 1^{+}} f(x) = \\ \lim_{x \to 1} f(x) = \end{cases}$$

4. 
$$\begin{cases} f(4) = \\ \lim_{x \to 4^{-}} f(x) = \\ \lim_{x \to 4^{+}} f(x) = \\ \lim_{x \to 4} f(x) = \end{cases}$$

7. 
$$\begin{cases} f(7) = \\ \lim_{x \to \mathbf{7}^{-}} f(x) = \\ \lim_{x \to \mathbf{7}^{+}} f(x) = \\ \lim_{x \to \mathbf{7}} f(x) = \end{cases}$$

2. 
$$\begin{cases} f(2) = \\ \lim_{x \to \mathbf{2}^{-}} f(x) = \\ \lim_{x \to \mathbf{2}^{+}} f(x) = \\ \lim_{x \to \mathbf{2}} f(x) = \end{cases}$$

5. 
$$\begin{cases} f(5) = \\ \lim_{x \to \mathbf{5}^{-}} f(x) = \\ \lim_{x \to \mathbf{5}^{+}} f(x) = \\ \lim_{x \to \mathbf{5}} f(x) = \end{cases}$$

3. 
$$\begin{cases} f(3) = \\ \lim_{x \to 3^{-}} f(x) = \\ \lim_{x \to 3^{+}} f(x) = \\ \lim_{x \to 3} f(x) = \end{cases}$$

6. 
$$\begin{cases} f(6) = \\ \lim_{x \to \mathbf{6}^{-}} f(x) = \\ \lim_{x \to \mathbf{6}^{+}} f(x) = \\ \lim_{x \to \mathbf{6}} f(x) = \end{cases}$$

# 2 Finding Limits Involving Infinity Graphically

8. 
$$\begin{cases} f(8) = \\ \lim_{x \to 8^{-}} f(x) = \\ \lim_{x \to 8^{+}} f(x) = \\ \lim_{x \to 8} f(x) = \end{cases}$$

10. 
$$\begin{cases} f(10) = \\ \lim_{x \to \mathbf{10}^{-}} f(x) = \\ \lim_{x \to \mathbf{10}^{+}} f(x) = \\ \lim_{x \to \mathbf{10}} f(x) = \end{cases}$$

12. 
$$\begin{cases} f(12) = \\ \lim_{x \to 12^{-}} f(x) = \\ \lim_{x \to 12^{+}} f(x) = \\ \lim_{x \to 12} f(x) = \end{cases}$$

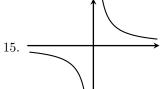
9. 
$$\begin{cases} f(9) = \\ \lim_{x \to 9^{-}} f(x) = \\ \lim_{x \to 9^{+}} f(x) = \\ \lim_{x \to 9} f(x) = \end{cases}$$

11. 
$$\begin{cases} x \to \mathbf{10} \\ f(11) = \\ \lim_{x \to \mathbf{11}^{-}} f(x) = \\ \lim_{x \to \mathbf{11}^{+}} f(x) = \\ \lim_{x \to \mathbf{11}^{+}} f(x) = \end{cases}$$

$$13. \lim_{x \to -\infty} f(x) =$$

$$14. \lim_{x \to +\infty} f(x) =$$

#### **Famous Functions** 3

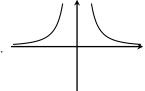


$$f(x) = 1/x$$

$$f(0) = \lim_{x \to \mathbf{0}^{-}} f(x) = \lim_{x \to \mathbf{0}^{+}} f(x) = \lim_{x \to \mathbf{0}} f(x) = \lim_{x \to \mathbf{$$

 $\lim f(x) =$ 

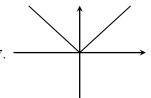
 $x \rightarrow +\infty$ 



$$f(x) = 1/x^2$$

$$f(0) = \lim_{x \to \mathbf{0}^{-}} f(x) =$$

$$\lim_{x \to \mathbf{0}^{-}} f(x) = \\ \lim_{x \to \mathbf{0}^{+}} f(x) = \\ \lim_{x \to \mathbf{0}^{+}} f(x) = \\ \lim_{x \to -\infty} f(x) = \\ \lim_{x \to -\infty} f(x) = \\ \\ x \to +\infty$$

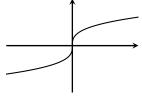


$$f(x) = |x|$$

$$f(0) =$$

$$\lim_{x \to \mathbf{0}^{-}} f(x) = \lim_{x \to \mathbf{0}^{+}} f(x) = \lim_{x \to \mathbf{0}} f(x) = \lim_{x \to -\infty} f(x$$

 $x \rightarrow +\infty$ 



$$f(x) = \sqrt[3]{x}$$

$$f(0) =$$

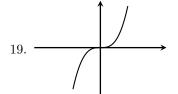
$$\lim_{x \to \mathbf{0}^{-}} f(x) =$$

$$\lim_{x \to \mathbf{0}^{+}} f(x) =$$

$$\lim_{x \to \mathbf{0}} f(x) =$$

$$\lim_{x \to -\infty} f(x) =$$

$$\lim_{x \to -\infty} f(x) = \lim_{x \to +\infty} f(x) = 0$$



$$f(x) = x^3$$

$$f(0) =$$

$$\lim_{x \to \mathbf{0}^-} f(x) =$$

$$\lim_{x \to \mathbf{0}^+} f(x) = \lim_{x \to \mathbf{0}^+} f(x)$$

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$$\lim_{x \to -\infty} f(x) =$$

$$\lim_{\substack{x \to 0 \\ \text{lim } f(x) = \\ x \to -\infty \\ \text{lim } f(x) = \\ x \to +\infty}} f(x) =$$



$$f(x) = e^x$$

$$f(0) =$$

$$\lim_{x \to \mathbf{0}^{-}} f(x) = \lim_{x \to \mathbf{0}^{+}} f(x) = \lim_{x \to \mathbf{0}} f(x$$

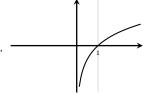
$$\lim_{x \to \mathbf{0}} f(x) = \lim_{x \to \mathbf{0}} f(x) = \lim_{x$$

$$\lim_{x \to -\infty} f(x) = \lim_{x \to -\infty}$$

$$\lim_{x \to -\infty} f(x) =$$

$$\lim_{x \to -\infty} f(x) =$$

$$\lim_{x \to +\infty} f(x) =$$



$$f(x) = \ln(x)$$

$$f(0) =$$

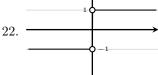
$$\lim_{x \to \mathbf{0}^-} f(x) =$$

$$\lim_{x \to \mathbf{0}^+} f(x) = \lim_{x \to \mathbf{0}^+} f(x)$$

$$\lim_{x \to \mathbf{0}} f(x) =$$

$$\lim f(x) =$$

$$\lim_{x \to +\infty} f(x) =$$



$$f(x) = \frac{|x|}{x}$$

$$f(0) =$$

$$\lim_{x \to \mathbf{0}^{-}} f(x) =$$

$$\lim_{x \to \mathbf{0}^+} f(x) =$$

$$\lim_{x \to \mathbf{0}^+} f(x) =$$

$$\lim_{x \to \mathbf{0}} f(x) =$$

$$\lim_{x \to 0} f(x) =$$

$$\lim_{x \to +\infty} f(x) =$$

$$f(x) = \cos(x)$$

$$f(0) =$$

$$\lim_{x \to 0} f(x) = 0$$

$$\lim_{x \to \mathbf{0}^+} f(x) =$$

$$\lim_{x \to 0} f(x) =$$

$$\lim_{x \to -\infty} f(x) =$$

$$\lim_{x \to +\infty} f(x) =$$



$$f(x) = \frac{\sin(x)}{x}$$

$$f(0) = \lim_{x \to 0^{-}} f(x) =$$

$$\lim_{x \to \mathbf{0}^-} f(x) =$$

$$\lim_{x \to \mathbf{0}} f(x) =$$

$$\lim_{x \to -\infty} f(x) =$$

$$\lim_{x \to +\infty} f(x) =$$





$$f(x) = \sin(1/x)$$

$$f(0) =$$

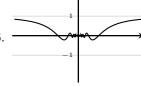
$$\lim_{x \to \mathbf{0}^-} f(x) =$$

$$\lim_{x \to \mathbf{0}^+} f(x) = \lim_{x \to \mathbf{0}^+} f(x)$$

$$\lim_{x \to 0} f(x) =$$

$$\lim_{x \to +\infty} f(x) =$$





$$f(x) = x\sin(1/x)$$

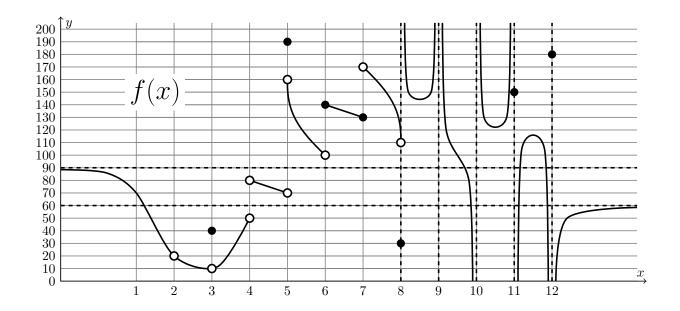
$$f(0) =$$

$$\lim_{x \to \mathbf{0}^{-}} f(x) = \lim_{x \to \mathbf{0}^{+}} f(x) =$$

$$\lim_{x \to 0} f(x) =$$

$$\lim_{x \to \mathbf{0}} f(x) =$$

$$\lim_{x \to +\infty} f(x) =$$



#### Identify Continuity/Discontinuity at a Point 4

| 27. | We say $f(x)$ is  | if $\lim_{x\to a} f(x)$ exists and equals $f(a)$ .   |  |
|-----|---|--|--|
| 28. | We say $f(x)$ has a   | at $x = a$ if $\lim_{x \to a} f(x)$ exists and does <i>not</i> equal $f(a)$ .                    |  |
| 29. | We say $f(x)$ has a   | if $\lim_{x\to a^+} f(x)$ and $\lim_{x\to a^-} f(x)$ exist and are <i>un</i> equal.              |  |
| 30. | We say $f(x)$ has an  | if either $\lim_{x\to a^+} f(x)$ or $\lim_{x\to a^-} f(x)$ equals either $\infty$ or $-\infty$ . |  |
| 31. | The function $f(x)$ is <b>continuous at</b> $x = $                |  |  |
| 32. | 2. The function $f(x)$ is has a removable discontinuity at $x = $ |  |  |
| 33. | . The function $f(x)$ is has a jump discontinuity at $x = $       |  |  |

#### Identify Left and Right Continuity at a Point 5

34. The function f(x) is has an **infinite discontinuity at** x = 1

| 35. | We say $f(x)$ is   | if $\lim_{x\to a^-} f(x)$ exists and equals $f(a)$ . |
|-----|--|--|
| 36. | We say $f(x)$ is   | if $\lim_{x\to a^+} f(x)$ exists and equals $f(a)$ . |
| 37. | The function $f(x)$ is <b>left continuous at</b> $x = $  | ·  |
| 38. | The function $f(x)$ is <b>right continuous at</b> $x = $ |  |

### Continuity on an Interval 6

We say f(x) is **continuous on** (a, b) if f(x) is continuous at x = c for all c in (a, b). 39. We say f(x) is **continuous on** [a, b] if f(x) is continuous at x = c for all c in (a, b), \_\_\_\_\_ and \_\_\_ 40. We say f(x) is **continuous everywhere** if f(x) is continuous at x = c for all c in \_\_\_\_\_\_. 41. We say f(x) is **continuous** if it is continuous on every open interval in \_\_\_\_ 42. Find the union of all open intervals (a, b) such that f(x) is **continuous on (a, b)**. Use interval notation.

43. The function f(x) fails to be **continuous** (on every open interval in its domain). It fails at  $x = \bot$