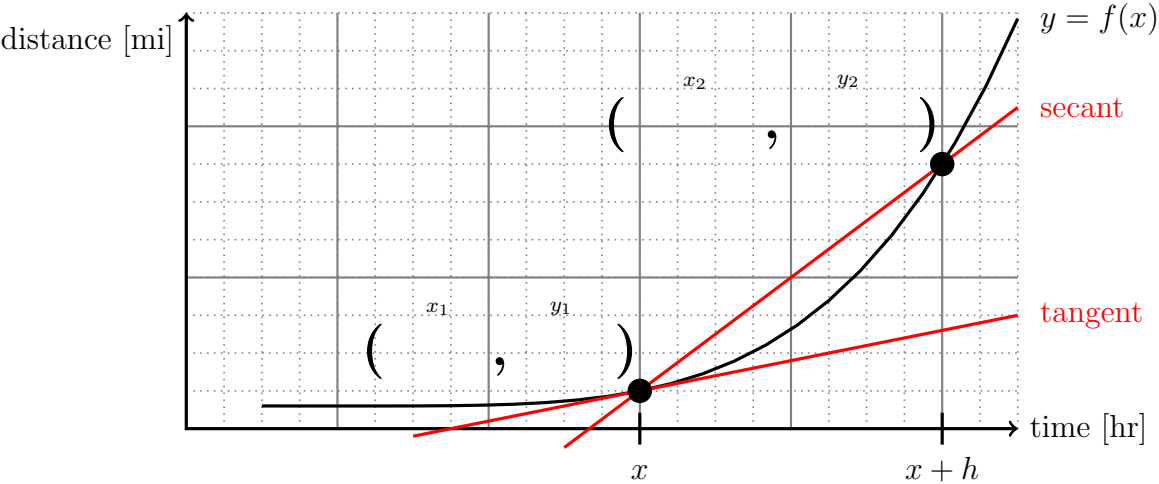


# The Limit Definition of Derivative

Suppose the distance a train has traveled is a function of time  $y = f(x)$ .

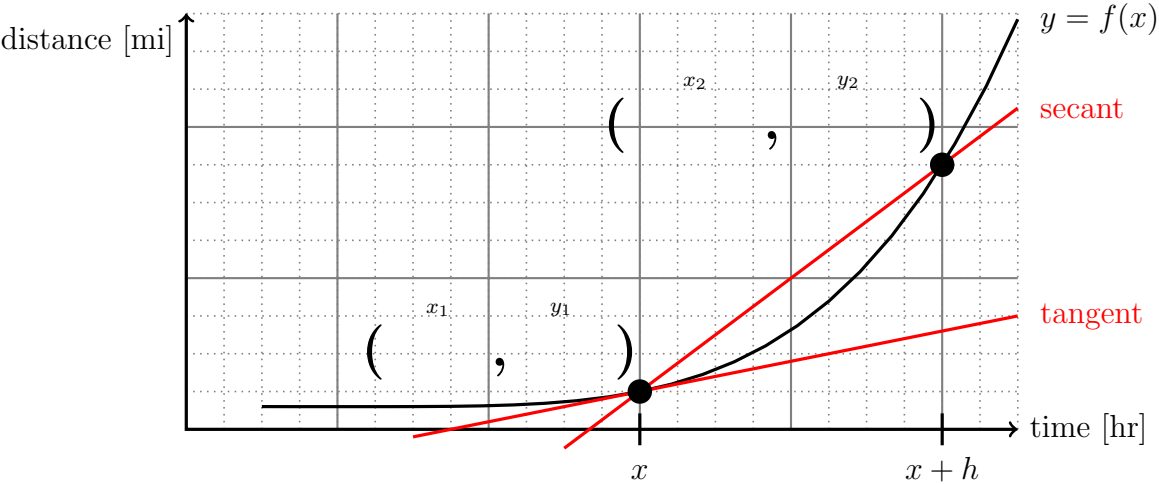


average velocity over  $[x, x+h]$  = average rate of change over  $[x, x+h]$  = slope of secant between  $x, x+h$  =  $\frac{\Delta y}{\Delta x} = \frac{y_2 - y_1}{x_2 - x_1} =$   = definition of difference quotient

velocity at  $x$  = rate of change at  $x$  = slope of tangent at  $x$  =  $\lim_{h \rightarrow 0}$   = definition of derivative  $f'(x)$

# The Limit Definition of Derivative

Suppose the distance a train has traveled is a function of time  $y = f(x)$ .



average velocity over  $[x, x+h]$  = average rate of change over  $[x, x+h]$  = slope of secant between  $x, x+h$  =  $\frac{\Delta y}{\Delta x} = \frac{y_2 - y_1}{x_2 - x_1} =$   = definition of difference quotient

velocity at  $x$  = rate of change at  $x$  = slope of tangent at  $x$  =  $\lim_{h \rightarrow 0}$   = definition of derivative  $f'(x)$