

Name Gatlin Walker

CSC 325, Assignment #2 – Master Theorem

```
def mergesort3(a):  
    n = len(a)  
    if n <= 1:  
        return a  
  
    mid1 = 1 * n // 3  
    mid2 = 2 * n // 3  
  
    left = mergesort3(a[0:mid1])  
    middle = mergesort3(a[mid1:mid2])  
    right = mergesort3(a[mid2:n])  
  
    # merge3: T(m) <= 12n + 8  
    return merge3(left, middle, right)
```

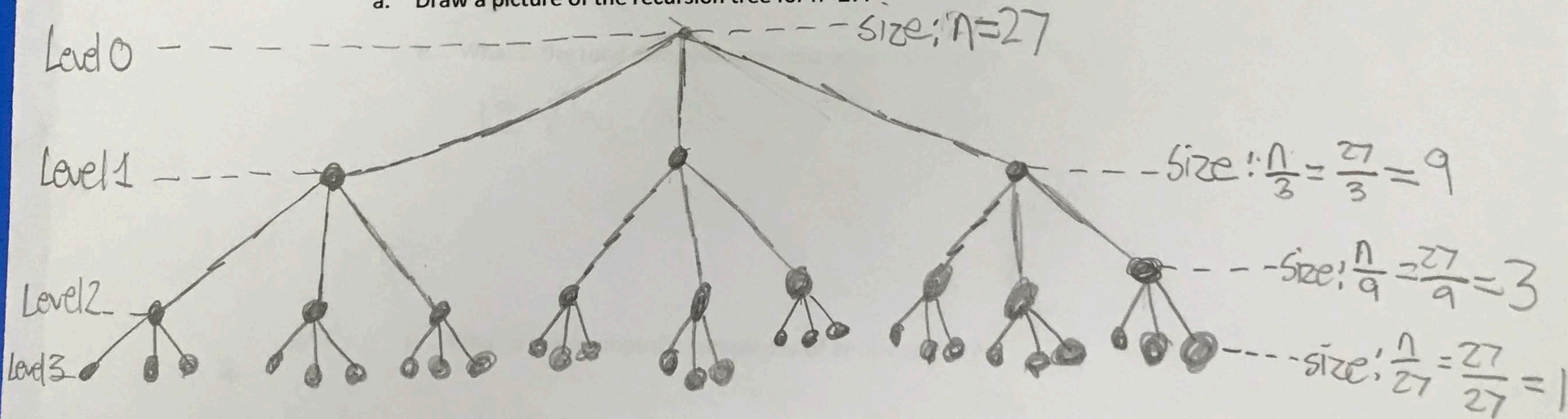
1. The easy way: use the master theorem to get the asymptotic running time of
are the values of a , b , and d , and what case does that lead to?

. (What

$$\begin{array}{lll} a=3 & a=b^d & \text{asymptotic } R_t = O(n^d \lg n) \\ b=3 & 3=3^1 & \text{Case 1} \\ d=1 & & \end{array}$$

2. The hard way (this question continues on the next page):

a. Draw a picture of the recursion tree for $n=27$.



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- b. How many sub-problems are there at any given level (use L in your equation)?
 Note1: root is Level 0, the second level is Level 1, and leaves are at Level $\log_2(n)$.

$$\boxed{\frac{n}{3^L}}$$

$$1$$

$$3$$

Levels
0
1
2
3
4

Sub P's
1
3
9
27

- c. How many elements are there for a given sub-problem found in level L ?

$$\boxed{\frac{n}{3^L}}$$

$$n=27$$

Levels

Elements

$$0$$

$$27$$

$$1$$

$$27/3$$

or

$$27/3^1$$

$$2$$

$$27/9$$

or

$$27/3^2$$

$$3$$

$$27/27$$

or

$$27/3^3$$

- d. How much work is performed at a given level L ?

$$3^L \cdot 12\left(\frac{n}{3^L}\right) + 8 \Rightarrow 12n$$

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- e. What is the total computational cost of mergesort3?

$$12n(\log_2(n) + 1)$$

- f. What is the asymptotic complexity of mergesort3?

$$n \lg n$$