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Social network Graph Link Prediction - Facebook Challenge

0.0.1 Problem statement:

Given a directed social graph, have to predict missing links to recommend users (Link Prediction in graph)

0.0.2 Data Overview

Taken data from facebook's recruting challenge on kaggle https://www.kaggle.com/c/FacebookRecruiting data contains two columns source and destination eac edge in graph - Data columns (total 2 columns):

- source node int64
- destination node int64

0.0.3 Mapping the problem into supervised learning problem:

- Generated training samples of good and bad links from given directed graph and for each link got some features like no of followers, is he followed back, page rank, katz score, adar index, some svd fetures of adj matrix, some weight features etc. and trained ml model based on these features to predict link.
- Some reference papers and videos:
 - https://www.cs.cornell.edu/home/kleinber/link-pred.pdf
 - https://www3.nd.edu/~dial/publications/lichtenwalter2010new.pdf
 - https://kaggle2.blob.core.windows.net/forum-messageattachments/2594/supervised_link_prediction.pdf
 - https://www.youtube.com/watch?v=2M77Hgy17cg

0.0.4 Business objectives and constraints:

- No low-latency requirement.
- Probability of prediction is useful to recommend ighest probability links

0.0.5 Performance metric for supervised learning:

• Both precision and recall is important so F1 score is good choice

Confusion matrix

```
In [1]: #Importing Libraries
        # please do go through this python notebook:
        import warnings
        warnings.filterwarnings("ignore")
        import csv
        import pandas as pd#pandas to create small dataframes
        import datetime #Convert to unix time
        import time #Convert to unix time
        # if numpy is not installed already : pip3 install numpy
        import numpy as np#Do aritmetic operations on arrays
        # matplotlib: used to plot graphs
        import matplotlib
        import matplotlib.pylab as plt
        import seaborn as sns#Plots
        from matplotlib import rcParams#Size of plots
        from sklearn.cluster import MiniBatchKMeans, KMeans#Clustering
        import math
        import pickle
        import os
        # to install xgboost: pip3 install xgboost
        import xgboost as xgb
        import warnings
        import networkx as nx
        import pdb
        import pickle
        from pandas import HDFStore, DataFrame
        from pandas import read_hdf
        import gc
        from tqdm import tqdm
        from scipy.sparse.linalg import svds, eigs
        from sklearn.metrics import f1_score
        from sklearn.ensemble import RandomForestClassifier
        from sklearn.metrics import f1 score
        from sklearn.model_selection import RandomizedSearchCV
        from scipy.stats import randint as sp_randint
        from scipy.stats import uniform
        from sklearn.metrics import f1_score
In [2]: #reading graph
        if not os.path.isfile('data/after_eda/train_woheader.csv'):
            traincsv = pd.read_csv('data/train.csv')
```

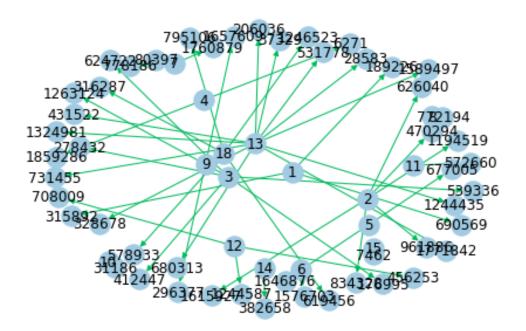
```
print(traincsv[traincsv.isna().any(1)])
            print(traincsv.info())
            print("Number of diplicate entries: ",sum(traincsv.duplicated()))
            traincsv.to_csv('data/after_eda/train_woheader.csv',header=False,index=False)
            print("saved the graph into file")
        else:
            g=nx.read_edgelist('data/after_eda/train_woheader.csv',delimiter=',',create_using=
            print(nx.info(g))
Name:
Type: DiGraph
Number of nodes: 1862220
Number of edges: 9437519
Average in degree:
                     5.0679
Average out degree:
                      5.0679
    Displaying a sub graph
In [3]: if not os.path.isfile('train_woheader_sample.csv'):
            pd.read_csv('data/train.csv', nrows=50).to_csv('train_woheader_sample.csv',header=
        subgraph=nx.read_edgelist('train_woheader_sample.csv',delimiter=',',create_using=nx.Di
        # https://stackoverflow.com/questions/9402255/drawing-a-huge-graph-with-networkx-and-m
        pos=nx.spring_layout(subgraph)
        nx.draw(subgraph,pos,node_color='#AOCBE2',edge_color='#00bb5e',width=1,edge_cmap=plt.cr
        plt.savefig("graph_sample.pdf")
        print(nx.info(subgraph))
Name:
Type: DiGraph
Number of nodes: 66
```

Number of edges: 50 Average in degree:

Average out degree:

0.7576

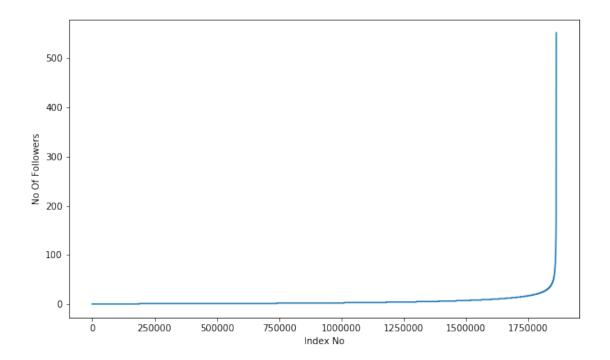
0.7576

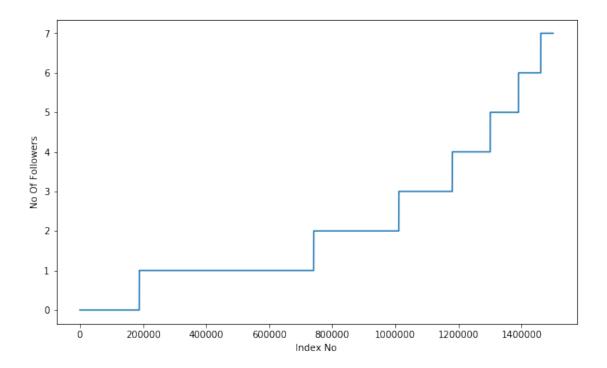


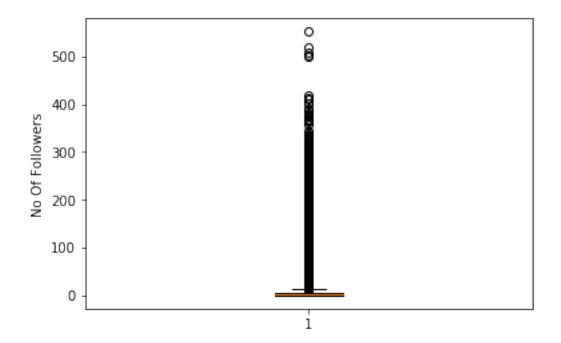
1 1. Exploratory Data Analysis

The number of unique persons 1862220

1.1 1.1 No of followers for each person

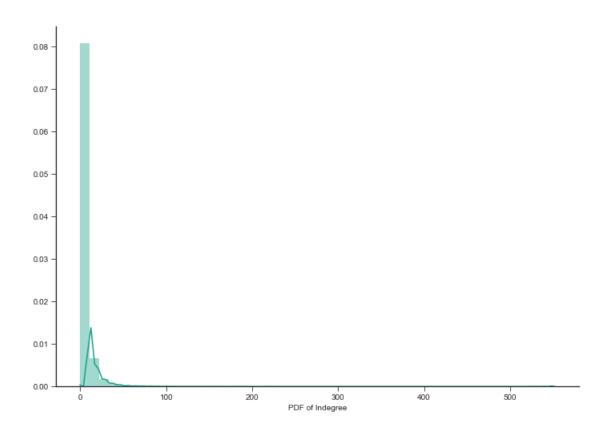




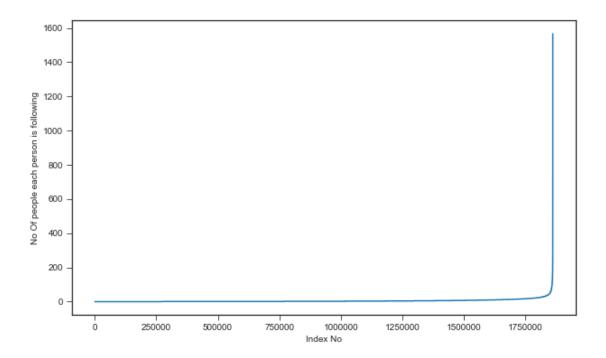


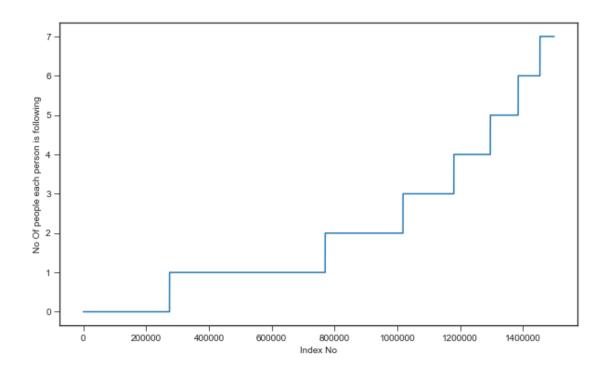
```
In [8]: ### 90-100 percentile
        for i in range(0,11):
            print(90+i,'percentile value is',np.percentile(indegree_dist,90+i))
90 percentile value is 12.0
91 percentile value is 13.0
92 percentile value is 14.0
93 percentile value is 15.0
94 percentile value is 17.0
95 percentile value is 19.0
96 percentile value is 21.0
97 percentile value is 24.0
98 percentile value is 29.0
99 percentile value is 40.0
100 percentile value is 552.0
  99% of data having followers of 40 only.
In [9]: ### 99-100 percentile
        for i in range(10,110,10):
            print(99+(i/100), 'percentile value is', np.percentile(indegree_dist, 99+(i/100)))
99.1 percentile value is 42.0
99.2 percentile value is 44.0
99.3 percentile value is 47.0
99.4 percentile value is 50.0
99.5 percentile value is 55.0
99.6 percentile value is 61.0
99.7 percentile value is 70.0
99.8 percentile value is 84.0
99.9 percentile value is 112.0
100.0 percentile value is 552.0
In [10]: %matplotlib inline
         sns.set_style('ticks')
         fig, ax = plt.subplots()
         fig.set_size_inches(11.7, 8.27)
         sns.distplot(indegree_dist, color='#16A085')
         plt.xlabel('PDF of Indegree')
         sns.despine()
         #plt.show()
D:\installed\Anaconda3\lib\site-packages\matplotlib\axes\_axes.py:6571: UserWarning: The 'norm'
```

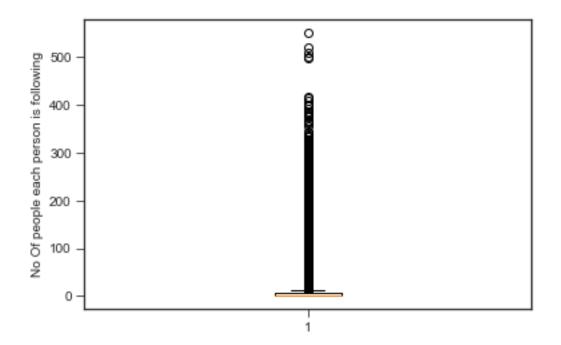
warnings.warn("The 'normed' kwarg is deprecated, and has been "



1.2 No of people each person is following

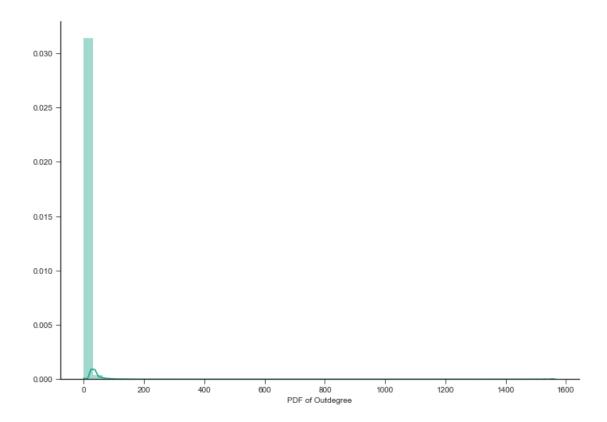






```
In [14]: ### 90-100 percentile
         for i in range(0,11):
             print(90+i, 'percentile value is',np.percentile(outdegree_dist,90+i))
90 percentile value is 12.0
91 percentile value is 13.0
92 percentile value is 14.0
93 percentile value is 15.0
94 percentile value is 17.0
95 percentile value is 19.0
96 percentile value is 21.0
97 percentile value is 24.0
98 percentile value is 29.0
99 percentile value is 40.0
100 percentile value is 1566.0
In [15]: ### 99-100 percentile
         for i in range(10,110,10):
             print(99+(i/100), 'percentile value is', np.percentile(outdegree_dist, 99+(i/100)))
99.1 percentile value is 42.0
99.2 percentile value is 45.0
99.3 percentile value is 48.0
99.4 percentile value is 52.0
99.5 percentile value is 56.0
99.6 percentile value is 63.0
99.7 percentile value is 73.0
99.8 percentile value is 90.0
99.9 percentile value is 123.0
100.0 percentile value is 1566.0
In [16]: sns.set_style('ticks')
         fig, ax = plt.subplots()
         fig.set_size_inches(11.7, 8.27)
         sns.distplot(outdegree_dist, color='#16A085')
         plt.xlabel('PDF of Outdegree')
         sns.despine()
D:\installed\Anaconda3\lib\site-packages\matplotlib\axes\_axes.py:6571: UserWarning: The 'norm'
```

warnings.warn("The 'normed' kwarg is deprecated, and has been "



In [17]: print('No of persons those are not following anyone are', sum(np.array(outdegree_dist sum(np.array(outdegree_dist)==0)*100/len(outdegree_dist)==0)*100/len(outdegree_dist)**

No of persons those are not following anyone are 274512 and % is 14.741115442858524

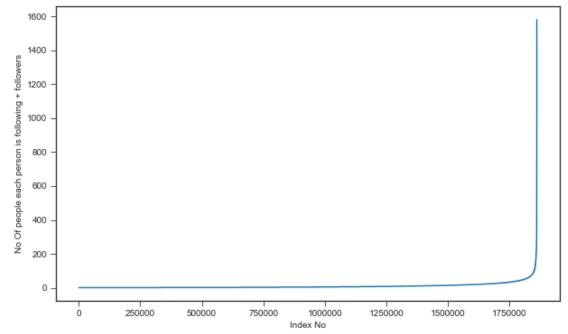
```
In [18]: print('No of persons having zero followers are', sum(np.array(indegree_dist)==0),'and sum(np.array(indegree_dist)==0)*100/len(indegree_dist)
```

No of persons having zero followers are 188043 and % is 10.097786512871734

print('No of persons those are not not following anyone and also not having any following anyone are not not following anyone and also not having any following anyone.

No of persons those are not not following anyone and also not having any followers are 0

1.3 1.3 both followers + following



```
In [23]: ### 90-100 percentile
         for i in range(0,11):
             print(90+i, 'percentile value is',np.percentile(in_out_degree_sort,90+i))
90 percentile value is 24.0
91 percentile value is 26.0
92 percentile value is 28.0
93 percentile value is 31.0
94 percentile value is 33.0
95 percentile value is 37.0
96 percentile value is 41.0
97 percentile value is 48.0
98 percentile value is 58.0
99 percentile value is 79.0
100 percentile value is 1579.0
In [24]: ### 99-100 percentile
         for i in range(10,110,10):
             print(99+(i/100), 'percentile value is', np.percentile(in_out_degree_sort, 99+(i/100))
99.1 percentile value is 83.0
99.2 percentile value is 87.0
99.3 percentile value is 93.0
99.4 percentile value is 99.0
```

```
99.5 percentile value is 108.0
99.6 percentile value is 120.0
99.7 percentile value is 138.0
99.8 percentile value is 168.0
99.9 percentile value is 221.0
100.0 percentile value is 1579.0
In [25]: print('Min of no of followers + following is',in_out_degree.min())
         print(np.sum(in_out_degree==in_out_degree.min()),' persons having minimum no of follow
Min of no of followers + following is 1
334291 persons having minimum no of followers + following
In [26]: print('Max of no of followers + following is',in_out_degree.max())
         print(np.sum(in_out_degree==in_out_degree.max()),' persons having maximum no of follow
Max of no of followers + following is 1579
1 persons having maximum no of followers + following
In [27]: print('No of persons having followers + following less than 10 are',np.sum(in_out_deg
No of persons having followers + following less than 10 are 1320326
In [28]: print('No of weakly connected components',len(list(nx.weakly_connected_components(g))
         count=0
         for i in list(nx.weakly_connected_components(g)):
             if len(i)==2:
                 count+=1
         print('weakly connected components wit 2 nodes',count)
No of weakly connected components 45558
weakly connected components wit 2 nodes 32195
```

2 2. Posing a problem as classification problem

2.1 Generating some edges which are not present in graph for supervised learning

Generated Bad links from graph which are not in graph and whose shortest path is greater than 2.

```
r = csv.reader(open('data/after_eda/train_woheader.csv','r'))
            edges = dict()
            for edge in r:
                edges[(edge[0], edge[1])] = 1
            missing_edges = set([])
            while (len(missing_edges)<9437519):
                a=random.randint(1, 1862220)
                b=random.randint(1, 1862220)
                tmp = edges.get((a,b),-1)
                if tmp == -1 and a!=b:
                    try:
                        if nx.shortest_path_length(g,source=a,target=b) > 2:
                            missing_edges.add((a,b))
                        else:
                            continue
                    except:
                            missing_edges.add((a,b))
                else:
                    continue
            pickle.dump(missing_edges,open('data/after_eda/missing_edges_final.p','wb'))
        else:
            missing_edges = pickle.load(open('data/after_eda/missing_edges_final.p','rb'))
Wall time: 3.17 s
```

2.2 2.2 Training and Test data split:

Removed edges from Graph and used as test data and after removing used that graph for creating features for Train and test data

```
In [48]: from sklearn.model_selection import train_test_split
    if (not os.path.isfile('data/after_eda/train_pos_after_eda.csv')) and (not os.path.is:
        #reading total data df
        df_pos = pd.read_csv('data/train.csv')
        df_neg = pd.DataFrame(list(missing_edges), columns=['source_node', 'destination_n'
        print("Number of nodes in the graph with edges", df_pos.shape[0])
        print("Number of nodes in the graph without edges", df_neg.shape[0])

#Trian test split
    #Spiltted data into 80-20
    #positive links and negative links seperatly because we need positive training da
    #and for feature generation
    X_train_pos, X_test_pos, y_train_pos, y_test_pos = train_test_split(df_pos,np.on.)
```

```
X_train_neg, X_test_neg, y_train_neg, y_test_neg = train_test_split(df_neg,np.ze;
                       print('='*60)
                       print("Number of nodes in the train data graph with edges", X_train_pos.shape[0],
                        print("Number of nodes in the train data graph without edges", X_train_neg.shape[
                        print('='*60)
                        print("Number of nodes in the test data graph with edges", X_test_pos.shape[0],"=
                        print("Number of nodes in the test data graph without edges", X_test_neg.shape[0]
                        #removing header and saving
                        X_train_pos.to_csv('data/after_eda/train_pos_after_eda.csv',header=False, index=F
                        X_test_pos.to_csv('data/after_eda/test_pos_after_eda.csv',header=False, index=False
                        X_train_neg.to_csv('data/after_eda/train_neg_after_eda.csv',header=False, index=False, inde
                        X_test_neg.to_csv('data/after_eda/test_neg_after_eda.csv',header=False, index=False
                else:
                        #Graph from Traing data only
                        del missing_edges
Number of nodes in the graph with edges 9437519
Number of nodes in the graph without edges 9437519
______
Number of nodes in the train data graph with edges 7550015 = 7550015
Number of nodes in the train data graph without edges 7550015 = 7550015
______
Number of nodes in the test data graph with edges 1887504 = 1887504
Number of nodes in the test data graph without edges 1887504 = 1887504
In [49]: if (os.path.isfile('data/after_eda/train_pos_after_eda.csv')) and (os.path.isfile('data/after_eda/train_pos_after_eda.csv'))
                        train_graph=nx.read_edgelist('data/after_eda/train_pos_after_eda.csv',delimiter='
                        test_graph=nx.read_edgelist('data/after_eda/test_pos_after_eda.csv',delimiter=','
                        print(nx.info(train_graph))
                        print(nx.info(test_graph))
                        # finding the unique nodes in the both train and test graphs
                        train_nodes_pos = set(train_graph.nodes())
                        test_nodes_pos = set(test_graph.nodes())
                        trY_teY = len(train_nodes_pos.intersection(test_nodes_pos))
                        trY_teN = len(train_nodes_pos - test_nodes_pos)
                        teY_trN = len(test_nodes_pos - train_nodes_pos)
                       print('no of people common in train and test -- ',trY_teY)
                       print('no of people present in train but not present in test -- ',trY_teN)
                        print('no of people present in test but not present in train -- ',teY_trN)
                        print(' % of people not there in Train but exist in Test in total Test data are {
```

Name:

```
Number of nodes: 1780722
Number of edges: 7550015
Average in degree:
                     4.2399
Average out degree:
                      4.2399
Name:
Type: DiGraph
Number of nodes: 1144623
Number of edges: 1887504
Average in degree:
                     1.6490
Average out degree:
                      1.6490
no of people common in train and test -- 1063125
no of people present in train but not present in test -- 717597
no of people present in test but not present in train -- 81498
\% of people not there in Train but exist in Test in total Test data are 7.1200735962845405 \%
    we have a cold start problem here
In [50]: #final train and test data sets
         if (not os.path.isfile('data/after_eda/train_after_eda.csv')) and \
         (not os.path.isfile('data/after_eda/test_after_eda.csv')) and \
         (not os.path.isfile('data/train_y.csv')) and \
         (not os.path.isfile('data/test_y.csv')) and \
         (os.path.isfile('data/after_eda/train_pos_after_eda.csv')) and \
         (os.path.isfile('data/after_eda/test_pos_after_eda.csv')) and \
         (os.path.isfile('data/after_eda/train_neg_after_eda.csv')) and \
         (os.path.isfile('data/after_eda/test_neg_after_eda.csv')):
             X_train_pos = pd.read_csv('data/after_eda/train_pos_after_eda.csv', names=['source
             X_test_pos = pd.read_csv('data/after_eda/test_pos_after_eda.csv', names=['source_:
             X_train_neg = pd.read_csv('data/after_eda/train_neg_after_eda.csv', names=['source
             X_test_neg = pd.read_csv('data/after_eda/test_neg_after_eda.csv', names=['source_:
             print('='*60)
             print("Number of nodes in the train data graph with edges", X_train_pos.shape[0])
             print("Number of nodes in the train data graph without edges", X_train_neg.shape[
             print('='*60)
             print("Number of nodes in the test data graph with edges", X_test_pos.shape[0])
             print("Number of nodes in the test data graph without edges", X_test_neg.shape[0]
             X_train = X_train_pos.append(X_train_neg,ignore_index=True)
             y_train = np.concatenate((y_train_pos,y_train_neg))
             X_test = X_test_pos.append(X_test_neg,ignore_index=True)
             y_test = np.concatenate((y_test_pos,y_test_neg))
             X_train.to_csv('data/after_eda/train_after_eda.csv',header=False,index=False)
             X_test.to_csv('data/after_eda/test_after_eda.csv',header=False,index=False)
```

Type: DiGraph

```
pd.DataFrame(y_test.astype(int)).to_csv('data/test_y.csv',header=False,index=False
Number of nodes in the train data graph with edges 7550015
Number of nodes in the train data graph without edges 7550015
______
Number of nodes in the test data graph with edges 1887504
Number of nodes in the test data graph without edges 1887504
In [51]: print("Data points in train data",X_train.shape)
        print("Data points in test data", X_test.shape)
        print("Shape of traget variable in train",y_train.shape)
        print("Shape of traget variable in test", y_test.shape)
Data points in train data (15100030, 2)
Data points in test data (3775008, 2)
Shape of traget variable in train (15100030,)
Shape of traget variable in test (3775008,)
In [53]: # computed and store the data for featurization
         # please check out FB_featurization.ipynb
   3. Featurization
In [3]: if os.path.isfile('data/after_eda/train_pos_after_eda.csv'):
           train_graph=nx.read_edgelist('data/after_eda/train_pos_after_eda.csv',delimiter=',
           print(nx.info(train_graph))
       else:
           print("please run the FB_EDA.ipynb or download the files from drive")
Name:
Type: DiGraph
Number of nodes: 1780722
Number of edges: 7550015
Average in degree:
                    4.2399
Average out degree:
                     4.2399
3.1
    3. Similarity measures
   3.1 Jaccard Distance:
http://www.statisticshowto.com/jaccard-index/
In [4]: #for followees
       def jaccard_for_followees(a,b):
```

pd.DataFrame(y_train.astype(int)).to_csv('data/train_y.csv',header=False,index=False)

```
try:
                                                                 if len(set(train_graph.successors(a))) == 0 | len(set(train_graph.successors()))
                                                                                  return 0
                                                                 sim = (len(set(train_graph.successors(a)).intersection(set(train_graph.successors))
                                                                                                                                                                                      (len(set(train_graph.successors(a)).union(set(train_graph.successors(a))).union(set(train_graph.successors(a))).union(set(train_graph.successors(a))).union(set(train_graph.successors(a))).union(set(train_graph.successors(a))).union(set(train_graph.successors(a))).union(set(train_graph.successors(a))).union(set(train_graph.successors(a))).union(set(train_graph.successors(a))).union(set(train_graph.successors(a))).union(set(train_graph.successors(a))).union(set(train_graph.successors(a))).union(set(train_graph.successors(a))).union(set(train_graph.successors(a))).union(set(train_graph.successors(a))).union(set(train_graph.successors(a))).union(set(train_graph.successors(a))).union(set(train_graph.successors(a))).union(set(train_graph.successors(a))).union(set(train_graph.successors(a))).union(set(train_graph.successors(a))).union(set(train_graph.successors(a))).union(set(train_graph.successors(a))).union(set(train_graph.successors(a))).union(set(train_graph.successors(a))).union(set(train_graph.successors(a))).union(set(train_graph.successors(a))).union(set(train_graph.successors(a))).union(set(train_graph.successors(a))).union(set(train_graph.successors(a))).union(set(train_graph.successors(a))).union(set(train_graph.successors(a))).union(set(train_graph.successors(a))).union(set(train_graph.successors(a))).union(set(train_graph.successors(a))).union(set(train_graph.successors(a))).union(set(train_graph.successors(a))).union(set(train_graph.successors(a))).union(set(train_graph.successors(a))).union(set(train_graph.successors(a))).union(set(train_graph.successors(a))).union(set(train_graph.successors(a))).union(set(train_graph.successors(a))).union(set(train_graph.successors(a))).union(set(train_graph.successors(a))).union(set(train_graph.successors(a))).union(set(train_graph.successors(a))).union(set(train_graph.successors(a))).union(set(train_graph.successors(a))).union(set(train_graph.successors(a))).union(set(train_graph.successors(a))).union(set(train_graph.successors(a))).union(set(train_graph.success
                                                 except:
                                                                 return 0
                                                 return sim
In [5]: #for followers
                                def jaccard_for_followers(a,b):
                                                  try:
                                                                 if len(set(train_graph.predecessors(a))) == 0 | len(set(g.predecessors(b))) ==
                                                                 sim = (len(set(train_graph.predecessors(a)).intersection(set(train_graph.prede
                                                                                                                                                                         (len(set(train_graph.predecessors(a)).union(set(train_graph.predecessors(a)).union(set(train_graph.predecessors(a)).union(set(train_graph.predecessors(a)).union(set(train_graph.predecessors(a)).union(set(train_graph.predecessors(a)).union(set(train_graph.predecessors(a)).union(set(train_graph.predecessors(a)).union(set(train_graph.predecessors(a)).union(set(train_graph.predecessors(a)).union(set(train_graph.predecessors(a)).union(set(train_graph.predecessors(a)).union(set(train_graph.predecessors(a)).union(set(train_graph.predecessors(a)).union(set(train_graph.predecessors(a)).union(set(train_graph.predecessors(a)).union(set(train_graph.predecessors(a)).union(set(train_graph.predecessors(a)).union(set(train_graph.predecessors(a)).union(set(train_graph.predecessors(a)).union(set(train_graph.predecessors(a)).union(set(train_graph.predecessors(a))).union(set(train_graph.predecessors(a))).union(set(train_graph.predecessors(a))).union(set(train_graph.predecessors(a))).union(set(train_graph.predecessors(a))).union(set(train_graph.predecessors(a))).union(set(train_graph.predecessors(a))).union(set(train_graph.predecessors(a))).union(set(train_graph.predecessors(a))).union(set(train_graph.predecessors(a))).union(set(train_graph.predecessors(a))).union(set(train_graph.predecessors(a))).union(set(train_graph.predecessors(a))).union(set(train_graph.predecessors(a))).union(set(train_graph.predecessors(a))).union(set(train_graph.predecessors(a))).union(set(train_graph.predecessors(a))).union(set(train_graph.predecessors(a))).union(set(train_graph.predecessors(a))).union(set(train_graph.predecessors(a))).union(set(train_graph.predecessors(a))).union(set(train_graph.predecessors(a))).union(set(train_graph.predecessors(a))).union(set(train_graph.predecessors(a))).union(set(train_graph.predecessors(a))).union(set(train_graph.predecessors(a))).union(set(train_graph.predecessors(a))).union(set(train_graph.predecessors(a))).union(set(train_graph.predecessors(a))).union(set(train_graph.predecessors(a))).union(set(train_graph.p
                                                                 return sim
                                                 except:
                                                                 return 0
3.3 3.2 Cosine distance
In [6]: #for followees
                                def cosine_for_followees(a,b):
                                                 try:
                                                                 if len(set(train_graph.successors(a))) == 0 | len(set(train_graph.successors(
                                                                                  return 0
                                                                 sim = (len(set(train_graph.successors(a)).intersection(set(train_graph.successors(a)).
                                                                                                                                                                                      (math.sqrt(len(set(train_graph.successors(a)))*len
                                                                 return sim
                                                 except:
                                                                 return 0
In [7]: def cosine_for_followers(a,b):
                                                 try:
                                                                 if len(set(train_graph.predecessors(a))) == 0 | len(set(train_graph.predecessors(a)))
                                                                 sim = (len(set(train_graph.predecessors(a)).intersection(set(train_graph.prede
                                                                                                                                                                                          (math.sqrt(len(set(train_graph.predecessors(a))))
                                                                 return sim
                                                 except:
                                                                 return 0
3.4 3.3 Ranking Measures
3.4.1 3.3.1 Page Ranking
In [8]: if not os.path.isfile('data/fea_sample/page_rank.p'):
                                                pr = nx.pagerank(train_graph, alpha=0.85)
```

```
pickle.dump(pr,open('data/fea_sample/page_rank.p','wb'))
        else:
            pr = pickle.load(open('data/fea_sample/page_rank.p','rb'))
In [9]: print('min',pr[min(pr, key=pr.get)])
        print('max',pr[max(pr, key=pr.get)])
        print('mean',float(sum(pr.values())) / len(pr))
min 1.6556497245737814e-07
max 2.7098251341935827e-05
mean 5.615699699389075e-07
In [10]: #for imputing to nodes which are not there in Train data
         mean_pr = float(sum(pr.values())) / len(pr)
         print(mean_pr)
5.615699699389075e-07
3.5 4. Other Graph Features
3.5.1 4.1 Shortest path:
In [11]: #if has direct edge then deleting that edge and calculating shortest path
         def compute_shortest_path_length(a,b):
             p = -1
             try:
                 if train_graph.has_edge(a,b):
                     train_graph.remove_edge(a,b)
                     p= nx.shortest_path_length(train_graph,source=a,target=b)
                     train_graph.add_edge(a,b)
                 else:
                     p= nx.shortest_path_length(train_graph,source=a,target=b)
                 return p
             except:
                 return -1
3.5.2 4.2 Checking for same community
In [12]: #getting weekly connected edges from graph
         wcc=list(nx.weakly_connected_components(train_graph))
         def belongs_to_same_wcc(a,b):
             index = []
             if train_graph.has_edge(b,a):
                 return 1
             if train_graph.has_edge(a,b):
                     for i in wcc:
```

if a in i:

```
index= i
                break
        if (b in index):
            train_graph.remove_edge(a,b)
            if compute_shortest_path_length(a,b)==-1:
                train_graph.add_edge(a,b)
                return 0
            else:
                train_graph.add_edge(a,b)
                return 1
        else:
            return 0
else:
        for i in wcc:
            if a in i:
                index= i
                break
        if(b in index):
            return 1
        else:
            return 0
```

3.5.3 4.3 Adamic/Adar Index:

3.5.4 4.4 Is persion was following back:

return 0

```
3.5.5 4.5 Katz Centrality:
```

```
In [15]: if not os.path.isfile('data/fea_sample/katz.p'):
             katz = nx.katz.katz_centrality(train_graph,alpha=0.005,beta=1)
             pickle.dump(katz,open('data/fea_sample/katz.p','wb'))
         else:
             katz = pickle.load(open('data/fea_sample/katz.p','rb'))
In [16]: print('min',katz[min(katz, key=katz.get)])
         print('max',katz[max(katz, key=katz.get)])
         print('mean',float(sum(katz.values())) / len(katz))
min 0.0007313532484065916
max 0.003394554981699122
mean 0.0007483800935562018
In [17]: mean_katz = float(sum(katz.values())) / len(katz)
         print(mean_katz)
0.0007483800935562018
3.5.6 4.6 Hits Score
In [18]: if not os.path.isfile('data/fea_sample/hits.p'):
             hits = nx.hits(train_graph, max_iter=100, tol=1e-08, nstart=None, normalized=True
             pickle.dump(hits,open('data/fea_sample/hits.p','wb'))
         else:
             hits = pickle.load(open('data/fea_sample/hits.p','rb'))
In [19]: print('min',hits[0][min(hits[0], key=hits[0].get)])
         print('max',hits[0][max(hits[0], key=hits[0].get)])
         print('mean',float(sum(hits[0].values())) / len(hits[0]))
min 0.0
max 0.004868653378780953
mean 5.615699699344123e-07
```

3.6 5. Featurization

3.6.1 5. 1 Reading a sample of Data from both train and test

```
In [20]: import random
         if os.path.isfile('data/after_eda/train_after_eda.csv'):
             filename = "data/after_eda/train_after_eda.csv"
              # you uncomment this line, if you dont know the lentqh of the file name
              # here we have hardcoded the number of lines as 15100030
              \# n_{\underline{}} train = sum(1 for line in open(filename)) \#number of records in file (exclude
```

```
n_{train} = 15100028
                                        s = 100000 #desired sample size
                                        skip_train = sorted(random.sample(range(1,n_train+1),n_train-s))
                                        #https://stackoverflow.com/a/22259008/4084039
In [21]: if os.path.isfile('data/after_eda/test_after_eda.csv'):
                                       filename = "data/after_eda/test_after_eda.csv"
                                        # you uncomment this line, if you dont know the lentgh of the file name
                                        # here we have hardcoded the number of lines as 3775008
                                        # n_test = sum(1 for line in open(filename)) #number of records in file (excludes
                                       n_{test} = 3775006
                                        s = 50000  #desired sample size
                                       skip_test = sorted(random.sample(range(1,n_test+1),n_test-s))
                                        #https://stackoverflow.com/a/22259008/4084039
In [22]: print("Number of rows in the train data file:", n_train)
                           print("Number of rows we are going to elimiate in train data are",len(skip_train))
                           print("Number of rows in the test data file:", n_test)
                           print("Number of rows we are going to elimiate in test data are",len(skip_test))
Number of rows in the train data file: 15100028
Number of rows we are going to elimiate in train data are 15000028
Number of rows in the test data file: 3775006
Number of rows we are going to elimiate in test data are 3725006
In [23]: df_final_train = pd.read_csv('data/after_eda/train_after_eda.csv', skiprows=skip_train_
                           df_final_train['indicator_link'] = pd.read_csv('data/train_y.csv', skiprows=skip_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_train_trai
                           print("Our train matrix size ",df_final_train.shape)
                           df_final_train.head(2)
Our train matrix size (100002, 3)
Out[23]:
                                    source_node destination_node indicator_link
                                                    273084
                                                                                                       1505602
                                                                                                                                                                            1
                                                                                                         325548
                                                                                                                                                                            1
                                                 1371356
In [24]: df_final_test = pd.read_csv('data/after_eda/test_after_eda.csv', skiprows=skip_test, :
                           df_final_test['indicator_link'] = pd.read_csv('data/test_y.csv', skiprows=skip_test, named to the state of the state 
                           print("Our test matrix size ",df_final_test.shape)
                           df_final_test.head(2)
Our test matrix size (50002, 3)
Out [24]:
                                    source_node destination_node indicator_link
                           0
                                                    848424
                                                                                                         784690
                                                    539301
                                                                                                         164255
                                                                                                                                                                            1
```

3.6.2 5.2 Adding a set of features

```
we will create these each of these features for both train and test data points
  jaccard_followers
  jaccard_followees
  cosine_followers
  cosine followees
  num_followers_s
  num_followees_s
  num_followers_d
  num_followees_d
  inter_followers
  inter_followees
In [25]: if not os.path.isfile('data/fea_sample/storage_sample_stage1.h5'):
             print("Inside if")
             #mapping jaccrd followers to train and test data
             df_final_train['jaccard_followers'] = df_final_train.apply(lambda row:
                                                      jaccard_for_followers(row['source_node'],:
             df_final_test['jaccard_followers'] = df_final_test.apply(lambda row:
                                                      jaccard_for_followers(row['source_node'],
             #mapping jaccrd followees to train and test data
             df_final_train['jaccard_followees'] = df_final_train.apply(lambda row:
                                                      jaccard_for_followees(row['source_node'],
             df_final_test['jaccard_followees'] = df_final_test.apply(lambda row:
                                                      jaccard_for_followees(row['source_node'],
                 #mapping jaccrd followers to train and test data
             df_final_train['cosine_followers'] = df_final_train.apply(lambda row:
                                                      cosine_for_followers(row['source_node'],re
             df_final_test['cosine_followers'] = df_final_test.apply(lambda row:
                                                      cosine_for_followers(row['source_node'],re
             #mapping jaccrd followees to train and test data
             df_final_train['cosine_followees'] = df_final_train.apply(lambda row:
                                                      cosine_for_followees(row['source_node'],re
             df_final_test['cosine_followees'] = df_final_test.apply(lambda row:
                                                      cosine_for_followees(row['source_node'],re
Inside if
In [26]: def compute_features_stage1(df_final):
             #calculating no of followers followees for source and destination
             #calculating intersection of followers and followees for source and destination
             num_followers_s=[]
             num_followees_s=[]
```

```
num_followers_d=[]
             num_followees_d=[]
             inter_followers=[]
             inter_followees=[]
             for i,row in df_final.iterrows():
                 try:
                     s1=set(train_graph.predecessors(row['source_node']))
                     s2=set(train_graph.successors(row['source_node']))
                 except:
                     s1 = set()
                     s2 = set()
                     d1=set(train_graph.predecessors(row['destination_node']))
                     d2=set(train_graph.successors(row['destination_node']))
                 except:
                     d1 = set()
                     d2 = set()
                 num_followers_s.append(len(s1))
                 num_followees_s.append(len(s2))
                 num_followers_d.append(len(d1))
                 num_followees_d.append(len(d2))
                 inter_followers.append(len(s1.intersection(d1)))
                 inter_followees.append(len(s2.intersection(d2)))
             return num_followers_s, num_followers_d, num_followees_s, num_followees_d, inter_
In [33]: if not os.path.isfile('storage_sample_stage1.h5'):
             df_final_train['num_followers_s'], df_final_train['num_followers_d'], \
             df_final_train['num_followees_s'], df_final_train['num_followees_d'], \
             df_final_train['inter_followers'], df_final_train['inter_followees'] = compute_fea
             df_final_test['num_followers_s'], df_final_test['num_followers_d'], \
             df_final_test['num_followees_s'], df_final_test['num_followees_d'], \
             df_final_test['inter_followers'], df_final_test['inter_followees'] = compute_featu:
             hdf = HDFStore('storage_sample_stage1.h5')
             hdf.put('train_df',df_final_train, format='table', data_columns=True)
             hdf.put('test_df',df_final_test, format='table', data_columns=True)
             hdf.close()
         else:
             df_final_train = read_hdf('storage_sample_stage1.h5', 'train_df',mode='r')
             df_final_test = read_hdf('storage_sample_stage1.h5', 'test_df',mode='r')
```

3.6.3 5.3 Adding new set of features

we will create these each of these features for both train and test data points

```
adar index
is following back
belongs to same weakly connect components
shortest path between source and destination
```

```
In [28]: if not os.path.isfile('data/fea_sample/storage_sample_stage2.h5'):
            #mapping adar index on train
            df_final_train['adar_index'] = df_final_train.apply(lambda row: calc_adar_in(row[
            #mapping adar index on test
            df_final_test['adar_index'] = df_final_test.apply(lambda row: calc_adar_in(row['s
            #mapping followback or not on train
            df_final_train['follows_back'] = df_final_train.apply(lambda row: follows_back(rows_back))
            #mapping followback or not on test
            df_final_test['follows_back'] = df_final_test.apply(lambda row: follows_back(row[
            #-----
            #mapping same component of wcc or not on train
            df_final_train['same_comp'] = df_final_train.apply(lambda row: belongs_to_same_wc
            ##mapping same component of wcc or not on train
            df_final_test['same_comp'] = df_final_test.apply(lambda row: belongs_to_same_wcc()
            #-----
            #mapping shortest path on train
            df_final_train['shortest_path'] = df_final_train.apply(lambda row: compute_shortest_path')
            #mapping shortest path on test
            df_final_test['shortest_path'] = df_final_test.apply(lambda row: compute_shortest
           hdf = HDFStore('data/fea_sample/storage_sample_stage2.h5')
            hdf.put('train_df',df_final_train, format='table', data_columns=True)
            hdf.put('test_df',df_final_test, format='table', data_columns=True)
            hdf.close()
        else:
            df_final_train = read_hdf('data/fea_sample/storage_sample_stage2.h5', 'train_df','
            df_final_test = read_hdf('data/fea_sample/storage_sample_stage2.h5', 'test_df',more
```

3.6.4 5.4 Adding new set of features

we will create these each of these features for both train and test data points

Weight Features
weight of incoming edges
weight of outgoing edges
weight of incoming edges + weight of outgoing edges
weight of incoming edges * weight of outgoing edges
2*weight of incoming edges + weight of outgoing edges

```
weight of incoming edges + 2*weight of outgoing edges
Page Ranking of source
Page Ranking of dest
katz of source
katz of dest
hubs of source
hubs of dest
authorities_s of source
authorities_s of dest
```

Weight Features

In order to determine the similarity of nodes, an edge weight value was calculated between nodes. Edge weight decreases as the neighbor count goes up. Intuitively, consider one million people following a celebrity on a social network then chances are most of them never met each other or the celebrity. On the other hand, if a user has 30 contacts in his/her social network, the chances are higher that many of them know each other. credit - Graph-based Features for Supervised Link Prediction William Cukierski, Benjamin Hamner, Bo Yang

```
In [29]: #weight for source and destination of each link
         Weight_in = {}
         Weight_out = {}
         for i in tqdm(train_graph.nodes()):
             s1=set(train_graph.predecessors(i))
             w_{in} = 1.0/(np.sqrt(1+len(s1)))
             Weight_in[i]=w_in
             s2=set(train_graph.successors(i))
             w_{out} = 1.0/(np.sqrt(1+len(s2)))
             Weight_out[i]=w_out
         #for imputing with mean
         mean_weight_in = np.mean(list(Weight_in.values()))
         mean_weight_out = np.mean(list(Weight_out.values()))
100%|| 1780722/1780722 [00:13<00:00, 133302.15it/s]
In [30]: if not os.path.isfile('data/fea_sample/storage_sample_stage3.h5'):
             print("File not present")
             #mapping to pandas train
             df_final_train['weight_in'] = df_final_train.destination_node.apply(lambda x: Weight_in')
             df_final_train['weight_out'] = df_final_train.source_node.apply(lambda x: Weight_ender)
             #mapping to pandas test
             df_final_test['weight_in'] = df_final_test.destination_node.apply(lambda x: Weigh
             df_final_test['weight_out'] = df_final_test.source_node.apply(lambda x: Weight_out)
             #some features engineerings on the in and out weights
```

```
df_final_train['weight_f2'] = df_final_train.weight_in * df_final_train.weight_ou
                                 df_final_train['weight_f3'] = (2*df_final_train.weight_in + 1*df_final_train.weight_in + 1*df_final_tra
                                 df_final_train['weight_f4'] = (1*df_final_train.weight_in + 2*df_final_train.weight_in + 2*df_final_tra
                                 #some features engineerings on the in and out weights
                                 df_final_test['weight_f1'] = df_final_test.weight_in + df_final_test.weight_out
                                 df_final_test['weight_f2'] = df_final_test.weight_in * df_final_test.weight_out
                                 df_final_test['weight_f3'] = (2*df_final_test.weight_in + 1*df_final_test.weight_
                                 df_final_test['weight_f4'] = (1*df_final_test.weight_in + 2*df_final_test.weight_
File not present
In [31]: if not os.path.isfile('data/fea_sample/storage_sample_stage3.h5'):
                                 #page rank for source and destination in Train and Test
                                 #if anything not there in train graph then adding mean page rank
                                 df final_train['page rank_s'] = df_final_train.source_node.apply(lambda x:pr.get()
                                 df_final_train['page_rank_d'] = df_final_train.destination_node.apply(lambda x:pr
                                 df_final_test['page_rank_s'] = df_final_test.source_node.apply(lambda x:pr.get(x,))
                                 df_final_test['page_rank_d'] = df_final_test.destination_node.apply(lambda x:pr.g.
                                 #-----
                                 #Katz centrality score for source and destination in Train and test
                                 #if anything not there in train graph then adding mean katz score
                                 df_final_train['katz_s'] = df_final_train.source_node.apply(lambda x: katz.get(x,))
                                 df_final_train['katz_d'] = df_final_train.destination_node.apply(lambda x: katz.g.
                                 df_final_test['katz_s'] = df_final_test.source_node.apply(lambda x: katz.get(x,means.get(x))
                                 df_final_test['katz_d'] = df_final_test.destination_node.apply(lambda x: katz.get
                                 #Hits algorithm score for source and destination in Train and test
                                 #if anything not there in train graph then adding O
                                 df_final_train['hubs_s'] = df_final_train.source_node.apply(lambda x: hits[0].get
                                 df_final_train['hubs_d'] = df_final_train.destination_node.apply(lambda x: hits[0]
                                 df_final_test['hubs_s'] = df_final_test.source_node.apply(lambda x: hits[0].get(x
                                 df_final_test['hubs_d'] = df_final_test.destination_node.apply(lambda x: hits[0].
                                 #Hits algorithm score for source and destination in Train and Test
                                 #if anything not there in train graph then adding O
                                 df_final_train['authorities_s'] = df_final_train.source_node.apply(lambda x: hits
                                 df_final_train['authorities_d'] = df_final_train.destination_node.apply(lambda x:
```

df_final_train['weight_f1'] = df_final_train.weight_in + df_final_train.weight_ou

```
df_final_test['authorities_s'] = df_final_test.source_node.apply(lambda x: hits[1]
             df_final_test['authorities_d'] = df_final_test.destination_node.apply(lambda x: h
             #-----
            hdf = HDFStore('data/fea_sample/storage_sample_stage3.h5')
             hdf.put('train_df',df_final_train, format='table', data_columns=True)
             hdf.put('test_df',df_final_test, format='table', data_columns=True)
             hdf.close()
         else:
             df_final_train = read_hdf('data/fea_sample/storage_sample_stage3.h5', 'train_df','
             df_final_test = read_hdf('data/fea_sample/storage_sample_stage3.h5', 'test_df',modelstage3.h5', 'test_df',modelstage3.h5'
In [34]: df_final_train.head()
Out [34]:
            source_node
                         destination_node
                                           indicator_link
                                                           jaccard_followers
         0
                 273084
                                  1505602
                                                        1
                                                                           0
                                                                           0
         1
                                                        1
                 832016
                                  1543415
         2
                1325247
                                   760242
                                                        1
                                                                           0
         3
                                                        1
                                                                           0
                1368400
                                  1006992
                                                        1
                                                                           0
                 140165
                                  1708748
            jaccard_followees
                               cosine_followers cosine_followees num_followers_s
         0
                     0.000000
                                       0.000000
                                                         0.000000
         1
                     0.187135
                                       0.028382
                                                         0.343828
                                                                                17
         2
                                                                                35
                     0.369565
                                       0.156957
                                                         0.566038
         3
                     0.000000
                                       0.000000
                                                         0.000000
                                                                                 2
         4
                     0.00000
                                                                                 5
                                       0.000000
                                                         0.000000
            num_followees_s
                             num_followees_d ... weight_f3 weight_f4
                                                                          page_rank_s \
         0
                         15
                                           8
                                              . . .
                                                    1.005929
                                                               0.877964
                                                                         2.045290e-06
         1
                         61
                                         142
                                                    0.332196
                                                               0.356598
                                                                         2.353458e-07
         2
                         41
                                                              0.494302 6.211019e-07
                                          22
                                                    0.525694
                                              . . .
         3
                          5
                                           7
                                                    0.985599
                                                               1.105172
                                                                         2.998153e-07
                                              . . .
                         10
                                           3
                                                    2.301511
                                                               1.603023 4.349180e-07
                                              . . .
                                      katz_d
                                                     hubs_s
                                                                    hubs_d \
            page_rank_d
                            \mathtt{katz}_{\mathtt{s}}
         0 3.459963e-07 0.000773 0.000756
                                               1.943132e-13
                                                              1.941103e-13
         1 6.427660e-07 0.000845
                                    0.001317
                                               3.906648e-11
                                                              9.424102e-11
         2 5.179801e-07 0.000885
                                    0.000855 7.730764e-114 4.067322e-114
                                               5.443738e-17
         3 1.704245e-06 0.000739
                                    0.000773
                                                              4.139999e-16
         4 2.089590e-07 0.000751 0.000735
                                               3.887821e-16
                                                              4.721269e-16
            authorities_s authorities_d
         0
             9.226339e-16
                            2.231877e-15
           1.208074e-11
                           1.273080e-10
         2 2.681298e-113 2.199205e-113
         3
           2.413250e-14 6.688064e-15
                           2.734009e-18
            7.552255e-16
```

3.6.5 5.5 Adding new set of features

we will create these each of these features for both train and test data points

SVD features for both source and destination

```
In [35]: def svd(x, S):
           try:
               z = sadj_dict[x]
               return S[z]
           except:
               return [0,0,0,0,0,0]
In [36]: #for svd features to get feature vector creating a dict node val and inedx in svd vec
        sadj_col = sorted(train_graph.nodes())
        sadj_dict = { val:idx for idx,val in enumerate(sadj_col)}
In [37]: Adj = nx.adjacency_matrix(train_graph,nodelist=sorted(train_graph.nodes())).asfptype(
In [38]: U, s, V = svds(Adj, k = 6)
        print('Adjacency matrix Shape', Adj.shape)
        print('U Shape', U.shape)
        print('V Shape', V.shape)
        print('s Shape',s.shape)
Adjacency matrix Shape (1780722, 1780722)
U Shape (1780722, 6)
V Shape (6, 1780722)
s Shape (6,)
In [39]: if not os.path.isfile('data/fea_sample/storage_sample_stage4.h5'):
            #-----
           df_final_train[['svd_u_s_1', 'svd_u_s_2', 'svd_u_s_3', 'svd_u_s_4', 'svd_u_s_5', 'svd_u_s_5']
           df_final_train.source_node.apply(lambda x: svd(x, U)).apply(pd.Series)
           df_final_train[['svd_u_d_1', 'svd_u_d_2', 'svd_u_d_3', 'svd_u_d_4', 'svd_u_d_5','
            df_final_train.destination_node.apply(lambda x: svd(x, U)).apply(pd.Series)
            #-----
            df_final_train[['svd_v_s_1','svd_v_s_2', 'svd_v_s_3', 'svd_v_s_4', 'svd_v_s_5', 's
           df_final_train.source_node.apply(lambda x: svd(x, V.T)).apply(pd.Series)
           df_final_train[['svd_v_d_1', 'svd_v_d_2', 'svd_v_d_3', 'svd_v_d_4', 'svd_v_d_5','s
           df_final_train.destination_node.apply(lambda x: svd(x, V.T)).apply(pd.Series)
```

```
df_final_test[['svd_u_s_1', 'svd_u_s_2', 'svd_u_s_3', 'svd_u_s_4', 'svd_u_s_5', 's
            df_final_test.source_node.apply(lambda x: svd(x, U)).apply(pd.Series)
            df_final_test[['svd_u_d_1', 'svd_u_d_2', 'svd_u_d_3', 'svd_u_d_4', 'svd_u_d_5', 's'
            df_final_test.destination_node.apply(lambda x: svd(x, U)).apply(pd.Series)
            df_final_test[['svd_v_s_1','svd_v_s_2', 'svd_v_s_3', 'svd_v_s_4', 'svd_v_s_5', 's
            df_final_test.source_node.apply(lambda x: svd(x, V.T)).apply(pd.Series)
            df_final_test[['svd_v_d_1', 'svd_v_d_2', 'svd_v_d_3', 'svd_v_d_4', 'svd_v_d_5', 's
            df_final_test.destination_node.apply(lambda x: svd(x, V.T)).apply(pd.Series)
            #-----
            hdf = HDFStore('data/fea_sample/storage_sample_stage4.h5')
            hdf.put('train_df',df_final_train, format='table', data_columns=True)
            hdf.put('test_df',df_final_test, format='table', data_columns=True)
            hdf.close()
In [40]: df_final_train.columns
Out[40]: Index(['source_node', 'destination_node', 'indicator_link',
               'jaccard_followers', 'jaccard_followees', 'cosine_followers',
               'cosine_followees', 'num_followers_s', 'num_followees_s',
               'num_followees_d', 'inter_followers', 'inter_followees',
               'num_followers_d', 'adar_index', 'follows_back', 'same_comp',
               'shortest_path', 'weight_in', 'weight_out', 'weight_f1', 'weight_f2',
               'weight_f3', 'weight_f4', 'page_rank_s', 'page_rank_d', 'katz_s',
               'katz_d', 'hubs_s', 'hubs_d', 'authorities_s', 'authorities_d',
               'svd_u_s_1', 'svd_u_s_2', 'svd_u_s_3', 'svd_u_s_4', 'svd_u_s_5',
               'svd_u_s_6', 'svd_u_d_1', 'svd_u_d_2', 'svd_u_d_3', 'svd_u_d_4',
               'svd_u_d_5', 'svd_u_d_6', 'svd_v_s_1', 'svd_v_s_2', 'svd_v_s_3',
               'svd_v_s_4', 'svd_v_s_5', 'svd_v_s_6', 'svd_v_d_1', 'svd_v_d_2',
               'svd_v_d_3', 'svd_v_d_4', 'svd_v_d_5', 'svd_v_d_6'],
              dtype='object')
```

3.6.6 5.6 Preferential Attachment

Preferential Attachement for followers

```
df final_train['preferential followers'] = preferential followers
         df_final_train.head()
Out [41]:
            source_node
                         destination_node
                                           indicator_link
                                                           jaccard followers
                 273084
                                  1505602
                                                         1
                                                                            0
                                                         1
                                                                            0
         1
                 832016
                                  1543415
         2
                1325247
                                   760242
                                                        1
                                                                            0
         3
                                                         1
                                                                            0
                1368400
                                  1006992
         4
                 140165
                                  1708748
                                                         1
                                                                            0
            jaccard_followees
                               cosine_followers
                                                 cosine_followees
                                                                    num_followers_s
         0
                     0.000000
                                       0.000000
                                                          0.000000
         1
                     0.187135
                                       0.028382
                                                          0.343828
                                                                                 17
         2
                     0.369565
                                       0.156957
                                                          0.566038
                                                                                 35
         3
                     0.000000
                                       0.000000
                                                          0.000000
                                                                                  2
         4
                                                                                  5
                     0.000000
                                       0.000000
                                                          0.000000
            num followees s
                             num followees d ...
                                                      svd v s 4
                                                                     svd v s 5
         0
                         15
                                                   1.545075e-13 8.108434e-13
                         61
                                         142 ... 1.345726e-02 3.703479e-12
         1
                                              ... -7.021227e-19 1.940403e-19
         2
                         41
                                          22
         3
                          5
                                           7
                                              ... 1.514614e-11 1.513483e-12
         4
                         10
                                           3
                                                   1.999809e-14 3.360247e-13
               svd_v_s_6
                             svd_v_d_1
                                           svd_v_d_2
                                                          svd_v_d_3
                                                                        svd_v_d_4
           1.719702e-14 -1.355368e-12
                                        4.675307e-13
                                                      1.128591e-06
                                                                     6.616550e-14
         1 2.251737e-10 1.245101e-12 -1.636948e-10 -3.112650e-10
                                                                     6.738902e-02
         2 -3.365389e-19 -1.238370e-18 1.438175e-19 -1.852863e-19 -5.901864e-19
         3 4.498061e-13 -9.818087e-10 3.454672e-11 5.213635e-08
                                                                   9.595823e-13
         4 1.407670e-14 0.000000e+00 0.000000e+00 0.000000e+00 0.000000e+00
               svd v d 5
                             svd v d 6 preferential followers
         0 9.771077e-13 4.159752e-14
                                                             66
         1 2.607801e-11 2.372904e-09
                                                           1598
         2 1.629341e-19 -2.572452e-19
                                                            980
         3 3.047045e-10 1.246592e-13
                                                             22
         4 0.000000e+00 0.000000e+00
                                                              0
         [5 rows x 56 columns]
In [42]: # for test dataset
         test_followers_s = np.array(df_final_test['num_followers_s'])
         test_followers_d = np.array(df_final_test['num_followers_d'])
         preferential_followers=[]
         for i in range(len(test_followers_s)):
             preferential_followers.append(test_followers_d[i]*test_followers_s[i])
         df_final_test['preferential_followers'] = preferential_followers
         df final test.head()
```

```
Out [42]:
                         destination_node indicator_link
                                                           jaccard_followers
            source_node
                 848424
         0
                                   784690
                                                        1
                                                                            0
                                                                            0
         1
                 483294
                                  1255532
                                                        1
         2
                                                        1
                                                                            0
                 626190
                                  1729265
                                                        1
                                                                            0
         3
                 947219
                                   425228
         4
                                                        1
                                                                            0
                 991374
                                   975044
            jaccard_followees
                               cosine_followers cosine_followees
                                                                    num followers s
         0
                                       0.029161
                                                         0.000000
                          0.0
                          0.0
                                       0.000000
                                                                                  2
         1
                                                         0.000000
                                       0.00000
         2
                          0.0
                                                                                 15
                                                         0.000000
         3
                                       0.000000
                          0.0
                                                         0.000000
                                                                                 11
         4
                          0.2
                                       0.042767
                                                         0.347833
                                                                                 12
            num_followees_s num_followees_d
                                                      svd_v_s_4
                                                                     svd_v_s_5 \
         0
                                                   2.701538e-12 4.341620e-13
                          6
                                           9
                                              . . .
         1
                          1
                                          19
                                                   2.248568e-14 3.600957e-13
                                              . . .
         2
                         16
                                                   1.778927e-12 2.740535e-13
                                           9
                                              . . .
         3
                         10
                                          34
                                                   7.917166e-13 4.020707e-12
         4
                         15
                                          27
                                                   1.361574e-13 1.154623e-12
               svd v s 6
                             svd v d 1
                                           svd v d 2
                                                         svd v d 3
                                                                        svd v d 4 \
         0 5.535503e-14 -9.994076e-10 5.791910e-10 3.512364e-07
                                                                    2.486658e-09
         1 4.701436e-15 -9.360516e-12
                                        3.206809e-10 4.668696e-08
                                                                    6.665777e-12
         2 4.199834e-14 -4.253075e-13 4.789463e-13 3.479824e-07
                                                                     1.630549e-13
         3 2.817657e-13 -2.162590e-11 6.939194e-12 1.879861e-05 4.384816e-12
         4 9.656662e-14 -8.742904e-12 7.467370e-12 1.256880e-05 3.636983e-12
                             svd_v_d_6 preferential_followers
               svd_v_d_5
         0 2.771146e-09 1.727694e-12
                                                            84
           1.495979e-10 9.836670e-14
                                                             34
         2 3.954708e-13 3.875785e-14
                                                            150
         3 1.239414e-11 6.483485e-13
                                                            407
         4 3.948463e-12 2.415863e-13
                                                            324
         [5 rows x 56 columns]
```

Preferential Attachement for followees


```
Out [43]:
                        destination_node indicator_link
                                                           jaccard_followers
            source_node
                 273084
         0
                                   1505602
                                                         1
                                                                             0
                                                                             0
         1
                 832016
                                   1543415
                                                         1
         2
                                                         1
                                                                             0
                1325247
                                   760242
                                                         1
                                                                             0
         3
                1368400
                                   1006992
                                                         1
                                                                             0
         4
                 140165
                                   1708748
            jaccard_followees
                               cosine_followers cosine_followees
                                                                    num followers s
         0
                     0.000000
                                        0.000000
                                                          0.000000
                                                                                  11
         1
                     0.187135
                                        0.028382
                                                          0.343828
                                                                                  17
         2
                                                                                  35
                     0.369565
                                        0.156957
                                                          0.566038
                                                                                   2
         3
                     0.000000
                                        0.000000
                                                          0.000000
         4
                     0.000000
                                        0.000000
                                                          0.000000
                                                                                   5
            num_followees_s
                             num_followees_d
                                                       svd_v_s_5
                                                                     svd_v_s_6
                                              . . .
         0
                                                    8.108434e-13 1.719702e-14
                         15
                                            8
                                               . . .
         1
                         61
                                          142
                                                    3.703479e-12
                                                                  2.251737e-10
         2
                         41
                                           22
                                                    1.940403e-19 -3.365389e-19
                                              . . .
         3
                          5
                                            7
                                                    1.513483e-12 4.498061e-13
         4
                         10
                                            3
                                                    3.360247e-13 1.407670e-14
               svd v d 1
                             svd v d 2
                                            svd v d 3
                                                          svd v d 4
                                                                         svd v d 5
         0 -1.355368e-12 4.675307e-13 1.128591e-06
                                                      6.616550e-14 9.771077e-13
         1 1.245101e-12 -1.636948e-10 -3.112650e-10
                                                       6.738902e-02 2.607801e-11
         2 -1.238370e-18 1.438175e-19 -1.852863e-19 -5.901864e-19 1.629341e-19
         3 -9.818087e-10 3.454672e-11 5.213635e-08
                                                                     3.047045e-10
                                                       9.595823e-13
         4 0.000000e+00 0.000000e+00 0.000000e+00 0.000000e+00
                                                                     0.000000e+00
                                                  preferential_followees
               svd_v_d_6 preferential_followers
           4.159752e-14
                                                                       120
         1 2.372904e-09
                                             1598
                                                                      8662
         2 -2.572452e-19
                                              980
                                                                       902
         3 1.246592e-13
                                               22
                                                                        35
         4 0.00000e+00
                                                0
                                                                        30
         [5 rows x 57 columns]
In [44]: #for test dataset
         test_followees_s = np.array(df_final_test['num_followees_s'])
         test_followees_d = np.array(df_final_test['num_followees_d'])
         preferential_followees=[]
         for i in range(len(test_followees_s)):
             preferential followees.append(test followees d[i]*test followees s[i])
         df_final_test['preferential_followees'] = preferential_followees
         df_final_test.head()
Out [44]:
            source_node destination_node indicator_link jaccard_followers \
         0
                 848424
                                   784690
                                                         1
                                                                             0
```

```
1
                                                         1
                                                                            0
                 483294
                                  1255532
         2
                                                                            0
                 626190
                                  1729265
                                                         1
         3
                 947219
                                                         1
                                                                            0
                                   425228
         4
                                                         1
                                                                            0
                 991374
                                   975044
            jaccard_followees
                               cosine_followers cosine_followees
                                                                    num_followers_s
         0
                          0.0
                                       0.029161
                                                          0.00000
         1
                          0.0
                                       0.000000
                                                          0.000000
                                                                                  2
         2
                          0.0
                                       0.000000
                                                          0.000000
                                                                                 15
         3
                          0.0
                                       0.00000
                                                          0.000000
                                                                                 11
         4
                          0.2
                                       0.042767
                                                          0.347833
                                                                                 12
            num_followees_s num_followees_d
                                                       svd_v_s_5
                                                                     svd_v_s_6
         0
                          6
                                                   4.341620e-13
                                                                  5.535503e-14
                          1
         1
                                          19
                                                   3.600957e-13
                                                                  4.701436e-15
         2
                         16
                                           9
                                              ... 2.740535e-13 4.199834e-14
         3
                         10
                                          34
                                                   4.020707e-12
                                                                  2.817657e-13
                         15
                                          27
                                               ... 1.154623e-12 9.656662e-14
               svd_v_d_1
                             svd_v_d_2
                                           svd_v_d_3
                                                          svd_v_d_4
                                                                        svd_v_d_5
         0 -9.994076e-10 5.791910e-10
                                        3.512364e-07
                                                       2.486658e-09
                                                                     2.771146e-09
         1 -9.360516e-12 3.206809e-10
                                        4.668696e-08
                                                       6.665777e-12
                                                                     1.495979e-10
         2 -4.253075e-13 4.789463e-13 3.479824e-07
                                                       1.630549e-13
                                                                     3.954708e-13
         3 -2.162590e-11 6.939194e-12 1.879861e-05
                                                      4.384816e-12
                                                                    1.239414e-11
         4 -8.742904e-12 7.467370e-12 1.256880e-05 3.636983e-12 3.948463e-12
               svd_v_d_6 preferential_followers preferential_followees
          1.727694e-12
                                              84
                                                                       54
         1 9.836670e-14
                                              34
                                                                       19
         2 3.875785e-14
                                             150
                                                                      144
         3 6.483485e-13
                                             407
                                                                      340
         4 2.415863e-13
                                             324
                                                                      405
         [5 rows x 57 columns]
In [45]: #for train datasets
```

3.6.7 5.7 SVD_dot

```
su1, su2, su3, su4, su5, su6=df_final_train['svd_u_s_1'], df_final_train['svd_u_s_2'], df_fix
sv1,sv2,sv3,sv4,sv5,sv6=df_final_train['svd_v_s_1'],df_final_train['svd_v_s_2'],df_fix
du1,du2,du3,du4,du5,du6=df_final_train['svd_u_d_1'],df_final_train['svd_u_d_2'],df_final_train['svd_u_d_2'],df_final_train['svd_u_d_1']
dv1,dv2,dv3,dv4,dv5,dv6=df_final_train['svd_v_d_1'],df_final_train['svd_v_d_2'],df_fix
```

```
In [46]: su = np.array([su1,su2,su3,su4,su5,su6]).T
         sv = np.array([sv1,sv2,sv3,sv4,sv5,sv6]).T
         print(su.shape)
```

```
print(sv.shape)
(100002, 6)
(100002, 6)
In [48]: du = np.array([du1,du2,du3,du4,du5,du6]).T
                                          dv = np.array([dv1,dv2,dv3,dv4,dv5,dv6]).T
                                          print(du.shape)
                                          print(dv.shape)
(100002, 6)
 (100002, 6)
In [50]: u_dot = []
                                          v_dot = []
                                          for ea in range(su.shape[0]):
                                                              u_dot.append(np.dot(su[ea],du[ea]))
                                                              v_dot.append(np.dot(sv[ea],dv[ea]))
                                          df_final_train['ud_dot']=u_dot
                                          df_final_train['vd_dot']=v_dot
In [51]: #for test datasets
                                          su1, su2, su3, su4, su5, su6=df_final_test['svd_u_s_1'], df_final_test['svd_u_s_2'], df_final_test['svd_u_s_2']
                                           sv1,sv2,sv3,sv4,sv5,sv6=df_final_test['svd_v_s_1'],df_final_test['svd_v_s_2'],df_final_test['svd_v_s_1']
                                          du1,du2,du3,du4,du5,du6=df_final_test['svd_u_d_1'],df_final_test['svd_u_d_2'],df_final_test['svd_u_d_2'],df_final_test['svd_u_d_2'],df_final_test['svd_u_d_1'],df_final_test['svd_u_d_2'],df_final_test['svd_u_d_1'],df_final_test['svd_u_d_2'],df_final_test['svd_u_d_1'],df_final_test['svd_u_d_2'],df_final_test['svd_u_d_1'],df_final_test['svd_u_d_2'],df_final_test['svd_u_d_1'],df_final_test['svd_u_d_2'],df_final_test['svd_u_d_1'],df_final_test['svd_u_d_2'],df_final_test['svd_u_d_2'],df_final_test['svd_u_d_2'],df_final_test['svd_u_d_2'],df_final_test['svd_u_d_2'],df_final_test['svd_u_d_2'],df_final_test['svd_u_d_2'],df_final_test['svd_u_d_2'],df_final_test['svd_u_d_2'],df_final_test['svd_u_d_2'],df_final_test['svd_u_d_2'],df_final_test['svd_u_d_2'],df_final_test['svd_u_d_2'],df_final_test['svd_u_d_2'],df_final_test['svd_u_d_2'],df_final_test['svd_u_d_2'],df_final_test['svd_u_d_2'],df_final_test['svd_u_d_2'],df_final_test['svd_u_d_2'],df_final_test['svd_u_d_2'],df_final_test['svd_u_d_2'],df_final_test['svd_u_d_2'],df_final_test['svd_u_d_2'],df_final_test['svd_u_d_2'],df_final_test['svd_u_d_2'],df_final_test['svd_u_d_2'],df_final_test['svd_u_d_2'],df_final_test['svd_u_d_2'],df_final_test['svd_u_d_2'],df_final_test['svd_u_d_2'],df_final_test['svd_u_d_2'],df_final_test['svd_u_d_2'],df_final_test['svd_u_d_2'],df_final_test['svd_u_d_2'],df_final_test['svd_u_d_2'],df_final_test['svd_u_d_2'],df_final_test['svd_u_d_2'],df_final_test['svd_u_d_2'],df_final_test['svd_u_d_2'],df_final_test['svd_u_d_2'],df_final_test['svd_u_d_2'],df_final_test['svd_u_d_2'],df_final_test['svd_u_d_2'],df_final_test['svd_u_d_2'],df_final_test['svd_u_d_2'],df_final_test['svd_u_d_2'],df_final_test['svd_u_d_2'],df_final_test['svd_u_d_2'],df_final_test['svd_u_d_2'],df_final_test['svd_u_d_2'],df_final_test['svd_u_d_2'],df_final_test['svd_u_d_2'],df_final_test['svd_u_d_2'],df_final_test['svd_u_d_2'],df_final_test['svd_u_d_2'],df_final_test['svd_u_d_2'],df_final_test['svd_u_d_2'],df_final_test['svd_u_d_2'],df_final_test['svd_u_d_2'],df_final_test['svd_u_d_2
                                           dv1,dv2,dv3,dv4,dv5,dv6=df_final_test['svd_v_d_1'],df_final_test['svd_v_d_2'],df_final_test['svd_v_d_2'],df_final_test['svd_v_d_2'],df_final_test['svd_v_d_1'],df_final_test['svd_v_d_2'],df_final_test['svd_v_d_1'],df_final_test['svd_v_d_2'],df_final_test['svd_v_d_1'],df_final_test['svd_v_d_2'],df_final_test['svd_v_d_1'],df_final_test['svd_v_d_2'],df_final_test['svd_v_d_1'],df_final_test['svd_v_d_2'],df_final_test['svd_v_d_1'],df_final_test['svd_v_d_2'],df_final_test['svd_v_d_2'],df_final_test['svd_v_d_2'],df_final_test['svd_v_d_2'],df_final_test['svd_v_d_2'],df_final_test['svd_v_d_2'],df_final_test['svd_v_d_2'],df_final_test['svd_v_d_2'],df_final_test['svd_v_d_2'],df_final_test['svd_v_d_2'],df_final_test['svd_v_d_2'],df_final_test['svd_v_d_2'],df_final_test['svd_v_d_2'],df_final_test['svd_v_d_2'],df_final_test['svd_v_d_2'],df_final_test['svd_v_d_2'],df_final_test['svd_v_d_2'],df_final_test['svd_v_d_2'],df_final_test['svd_v_d_2'],df_final_test['svd_v_d_2'],df_final_test['svd_v_d_2'],df_final_test['svd_v_d_2'],df_final_test['svd_v_d_2'],df_final_test['svd_v_d_2'],df_final_test['svd_v_d_2'],df_final_test['svd_v_d_2'],df_final_test['svd_v_d_2'],df_final_test['svd_v_d_2'],df_final_test['svd_v_d_2'],df_final_test['svd_v_d_2'],df_final_test['svd_v_d_2'],df_final_test['svd_v_d_2'],df_final_test['svd_v_d_2'],df_final_test['svd_v_d_2'],df_final_test['svd_v_d_2'],df_final_test['svd_v_d_2'],df_final_test['svd_v_d_2'],df_final_test['svd_v_d_2'],df_final_test['svd_v_d_2'],df_final_test['svd_v_d_2'],df_final_test['svd_v_d_2'],df_final_test['svd_v_d_2'],df_final_test['svd_v_d_2'],df_final_test['svd_v_d_2'],df_final_test['svd_v_d_2'],df_final_test['svd_v_d_2'],df_final_test['svd_v_d_2'],df_final_test['svd_v_d_2'],df_final_test['svd_v_d_2'],df_final_test['svd_v_d_2'],df_final_test['svd_v_d_2'],df_final_test['svd_v_d_2'],df_final_test['svd_v_d_2'],df_final_test['svd_v_d_2'],df_final_test['svd_v_d_2'],df_final_test['svd_v_d_2'],df_final_test['svd_v_d_2'],df_final_test['svd_v_d_2'],df_final_test['svd_v_d_2'],df_final_test['svd_v_d_2
In [52]: su = np.array([su1,su2,su3,su4,su5,su6]).T
                                           sv = np.array([sv1,sv2,sv3,sv4,sv5,sv6]).T
                                          print(su.shape)
                                          print(sv.shape)
                                          du = np.array([du1,du2,du3,du4,du5,du6]).T
                                          dv = np.array([dv1,dv2,dv3,dv4,dv5,dv6]).T
                                          print(du.shape)
                                          print(dv.shape)
(50002, 6)
 (50002, 6)
(50002, 6)
(50002, 6)
In [53]: u_dot = []
                                          v_{dot} = []
```

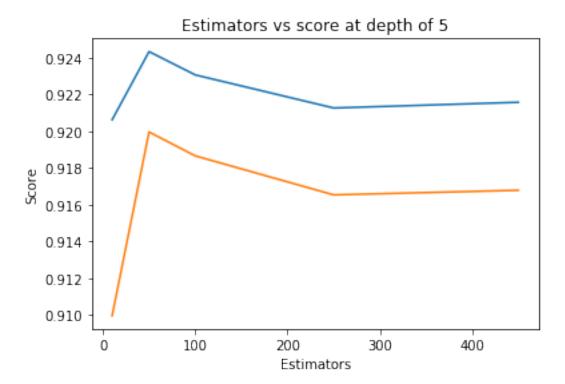
```
for ea in range(su.shape[0]):
             u_dot.append(np.dot(su[ea],du[ea]))
             v_dot.append(np.dot(sv[ea],dv[ea]))
         df_final_test['ud_dot']=u_dot
         df_final_test['vd_dot']=v_dot
In [54]: hdf = HDFStore('storage_sample_stage4.h5')
         hdf.put('train_df',df_final_train, format='table', data_columns=True)
         hdf.put('test_df',df_final_test, format='table', data_columns=True)
         hdf.close()
4 Models
In [92]: #reading
         from pandas import read_hdf
         df_final_train = read_hdf('data/fea_sample/storage_sample_stage4.h5', 'train_df',mode
         df_final_test = read_hdf('data/fea_sample/storage_sample_stage4.h5', 'test_df',mode=':
In [55]: df_final_train.columns
Out[55]: Index(['source_node', 'destination_node', 'indicator_link',
                'jaccard_followers', 'jaccard_followees', 'cosine_followers',
                'cosine_followees', 'num_followers_s', 'num_followees_s',
                'num_followees_d', 'inter_followers', 'inter_followees',
                'num_followers_d', 'adar_index', 'follows_back', 'same_comp',
                'shortest_path', 'weight_in', 'weight_out', 'weight_f1', 'weight_f2',
                'weight_f3', 'weight_f4', 'page_rank_s', 'page_rank_d', 'katz_s',
                'katz_d', 'hubs_s', 'hubs_d', 'authorities_s', 'authorities_d',
                'svd_u_s_1', 'svd_u_s_2', 'svd_u_s_3', 'svd_u_s_4', 'svd_u_s_5',
                'svd_u_s_6', 'svd_u_d_1', 'svd_u_d_2', 'svd_u_d_3', 'svd_u_d_4',
                'svd_u_d_5', 'svd_u_d_6', 'svd_v_s_1', 'svd_v_s_2', 'svd_v_s_3',
                'svd_v_s_4', 'svd_v_s_5', 'svd_v_s_6', 'svd_v_d_1', 'svd_v_d_2',
                'svd_v_d_3', 'svd_v_d_4', 'svd_v_d_5', 'svd_v_d_6',
                'preferential_followers', 'preferential_followees', 'ud_dot', 'vd_dot'],
               dtype='object')
In [56]: y_train = df_final_train.indicator_link
         y_test = df_final_test.indicator_link
In [57]: df_final_train.drop(['source_node', 'destination_node', 'indicator_link'], axis=1, inpla
         df_final_test.drop(['source_node', 'destination_node', 'indicator_link'],axis=1,inplace
```

4.1 6.1 Random Forest

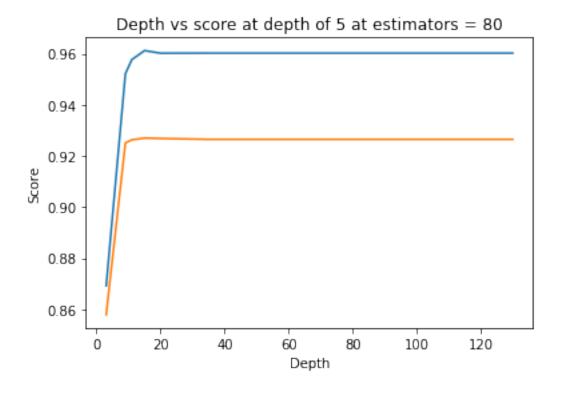
```
In [58]: estimators = [10,50,100,250,450]
         train_scores = []
         test scores = []
         for i in estimators:
```

```
clf = RandomForestClassifier(bootstrap=True, class_weight=None, criterion='gini',
                     max_depth=5, max_features='auto', max_leaf_nodes=None,
                     min_impurity_decrease=0.0, min_impurity_split=None,
                     min_samples_leaf=52, min_samples_split=120,
                     min_weight_fraction_leaf=0.0, n_estimators=i, n_jobs=-1,random_state=25,ve
             clf.fit(df_final_train,y_train)
             train_sc = f1_score(y_train,clf.predict(df_final_train))
             test_sc = f1_score(y_test,clf.predict(df_final_test))
             test_scores.append(test_sc)
             train_scores.append(train_sc)
             print('Estimators = ',i,'Train Score',train_sc,'test Score',test_sc)
        plt.plot(estimators,train_scores,label='Train Score')
        plt.plot(estimators,test_scores,label='Test Score')
        plt.xlabel('Estimators')
        plt.ylabel('Score')
        plt.title('Estimators vs score at depth of 5')
Estimators = 10 Train Score 0.9206276581363669 test Score 0.9099420606264169
Estimators = 50 Train Score 0.9243443808565498 test Score 0.919961264788851
Estimators = 100 Train Score 0.9230737062205958 test Score 0.9186600861073191
Estimators = 250 Train Score 0.9212693899736589 test Score 0.9165319957185133
Estimators = 450 Train Score 0.9215796838126267 test Score 0.9167837299507284
```

Out[58]: Text(0.5, 1.0, 'Estimators vs score at depth of 5')



```
In [61]: depths = [3,9,11,15,20,35,50,70,130]
        train_scores = []
        test_scores = []
        for i in depths:
             clf = RandomForestClassifier(bootstrap=True, class weight=None, criterion='gini',
                     max_depth=i, max_features='auto', max_leaf_nodes=None,
                     min_impurity_decrease=0.0, min_impurity_split=None,
                     min_samples_leaf=52, min_samples_split=120,
                     min_weight_fraction_leaf=0.0, n_estimators=80, n_jobs=-1,random_state=25,
             clf.fit(df_final_train,y_train)
             train_sc = f1_score(y_train,clf.predict(df_final_train))
             test_sc = f1_score(y_test,clf.predict(df_final_test))
             test_scores.append(test_sc)
             train_scores.append(train_sc)
             print('depth = ',i,'Train Score',train_sc,'test Score',test_sc)
        plt.plot(depths,train_scores,label='Train Score')
        plt.plot(depths,test_scores,label='Test Score')
        plt.xlabel('Depth')
        plt.ylabel('Score')
        plt.title('Depth vs score at depth of 5 at estimators = 80')
depth = 3 Train Score 0.8691679564498052 test Score 0.8578205183492174
depth = 9 Train Score 0.9521841009321695 test Score 0.9250940264324586
depth = 11 Train Score 0.9576999204195319 test Score 0.9263131323755233
depth = 15 Train Score 0.9612562252261408 test Score 0.9269964055241419
depth = 20 Train Score 0.9602348599912336 test Score 0.9268426263349693
depth = 35 Train Score 0.9602689486552567 test Score 0.9265046540032852
depth = 50 Train Score 0.9602689486552567 test Score 0.9265046540032852
depth = 70 Train Score 0.9602689486552567 test Score 0.9265046540032852
depth = 130 Train Score 0.9602689486552567 test Score 0.9265046540032852
```



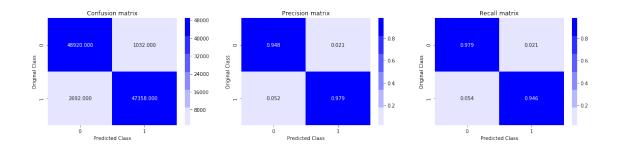
```
In [62]: from sklearn.metrics import f1_score
         from sklearn.ensemble import RandomForestClassifier
         from sklearn.metrics import f1 score
         from sklearn.model_selection import RandomizedSearchCV
         from scipy.stats import randint as sp_randint
         from scipy.stats import uniform
         param_dist = {"n_estimators":sp_randint(50,100),
                       "max_depth": sp_randint(10,20),
                       "min samples split": sp randint(110,190),
                       "min_samples_leaf": sp_randint(25,65)}
         clf = RandomForestClassifier(random_state=25,n_jobs=-1)
         rf_random = RandomizedSearchCV(clf, param_distributions=param_dist,
                                            n_iter=5,cv=10,scoring='f1',random_state=25)
         rf_random.fit(df_final_train,y_train)
         print('mean test scores',rf_random.cv_results_['mean_test_score'])
         print('mean train scores',rf_random.cv_results_['mean_train_score'])
mean test scores [0.95942393 0.95962772 0.9588493 0.96084579 0.9609113 ]
mean train scores [0.96016827 0.96014306 0.95956999 0.96201388 0.96198856]
```

```
In [63]: print(rf_random.best_estimator_)
RandomForestClassifier(bootstrap=True, class weight=None, criterion='gini',
            max_depth=14, max_features='auto', max_leaf_nodes=None,
            min_impurity_decrease=0.0, min_impurity_split=None,
            min_samples_leaf=28, min_samples_split=111,
            min_weight_fraction_leaf=0.0, n_estimators=72, n_jobs=-1,
            oob_score=False, random_state=25, verbose=0, warm_start=False)
  Best Parameters found
  • max depth = 14
  • n estimators = 72
  • min_samples_leaf=28
  • min_samples_split=111
In [64]: clf = RandomForestClassifier(bootstrap=True, class_weight=None, criterion='gini',
                     max_depth=14, max_features='auto', max_leaf_nodes=None,
                     min_impurity_decrease=0.0, min_impurity_split=None,
                     min_samples_leaf=28, min_samples_split=111,
                     min_weight_fraction_leaf=0.0, n_estimators=72, n_jobs=-1,
                     oob_score=False, random_state=25, verbose=0, warm_start=False)
In [65]: clf.fit(df_final_train,y_train)
         y_train_pred = clf.predict(df_final_train)
         y_test_pred = clf.predict(df_final_test)
In [66]: from sklearn.metrics import f1_score
         print('Train f1 score',f1_score(y_train,y_train_pred))
         print('Test f1 score',f1_score(y_test,y_test_pred))
Train f1 score 0.962169849654612
Test f1 score 0.9273067148348071
  Confusion Matrix
In [67]: from sklearn.metrics import confusion_matrix
         def plot_confusion_matrix(test_y, predict_y):
             C = confusion_matrix(test_y, predict_y)
             A = (((C.T)/(C.sum(axis=1))).T)
             B = (C/C.sum(axis=0))
             plt.figure(figsize=(20,4))
             labels = [0,1]
```

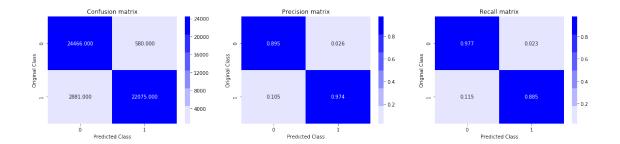
representing A in heatmap format

```
cmap=sns.light_palette("blue")
             plt.subplot(1, 3, 1)
             sns.heatmap(C, annot=True, cmap=cmap, fmt=".3f", xticklabels=labels, yticklabels=
             plt.xlabel('Predicted Class')
             plt.ylabel('Original Class')
             plt.title("Confusion matrix")
             plt.subplot(1, 3, 2)
             sns.heatmap(B, annot=True, cmap=cmap, fmt=".3f", xticklabels=labels, yticklabels=
             plt.xlabel('Predicted Class')
             plt.ylabel('Original Class')
             plt.title("Precision matrix")
             plt.subplot(1, 3, 3)
             # representing B in heatmap format
             sns.heatmap(A, annot=True, cmap=cmap, fmt=".3f", xticklabels=labels, yticklabels=
             plt.xlabel('Predicted Class')
             plt.ylabel('Original Class')
             plt.title("Recall matrix")
             plt.show()
In [68]: print('Train confusion_matrix')
         plot_confusion_matrix(y_train,y_train_pred)
         print('Test confusion_matrix')
         plot_confusion_matrix(y_test,y_test_pred)
```

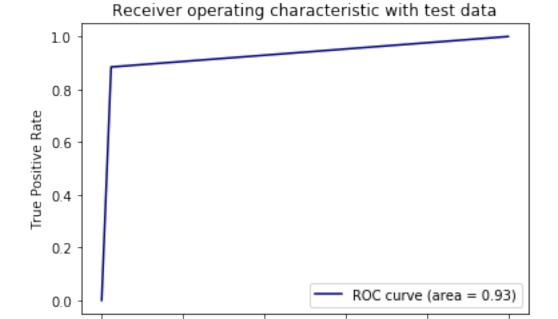
Train confusion_matrix



Test confusion_matrix



ROC/AUC Curve



0.4

False Positive Rate

0.6

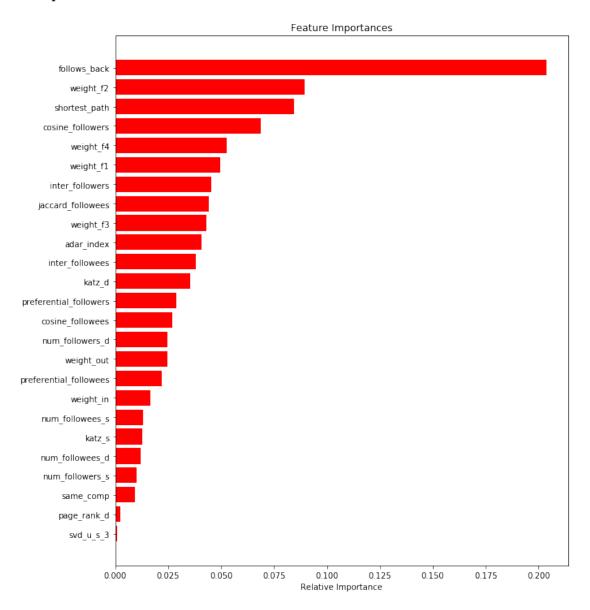
0.8

1.0

0.0

0.2

```
indices = (np.argsort(importances))[-25:]
plt.figure(figsize=(10,12))
plt.title('Feature Importances')
plt.barh(range(len(indices)), importances[indices], color='r', align='center')
plt.yticks(range(len(indices)), [features[i] for i in indices])
plt.xlabel('Relative Importance')
plt.show()
```

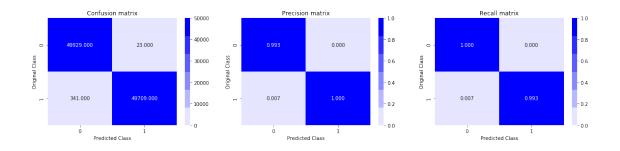


4.2 6.2 XGBOOST (Tuning)

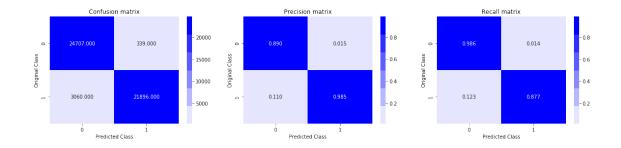
```
param_dist = {"n_estimators":sp_randint(50,100),
                       "max_depth": sp_randint(10,20)
         model = RandomizedSearchCV(clf, param_distributions=param_dist,
                                            n iter=5,cv=3,scoring='f1',random state=25)
         model.fit(df_final_train,y_train)
         print('mean test scores',model.cv_results_['mean_test_score'])
         print('mean train scores',model.cv_results_['mean_train_score'])
mean test scores [0.97826592 0.97824537 0.97757468 0.97824576 0.97728859]
mean train scores [0.99795819 0.99945028 0.99139832 0.99788798 0.99650233]
In [72]: print(model.best_estimator_)
XGBClassifier(base score=0.5, booster='gbtree', colsample_bylevel=1,
       colsample_bynode=1, colsample_bytree=1, gamma=0, learning_rate=0.1,
      max_delta_step=0, max_depth=14, min_child_weight=1, missing=None,
       n_estimators=76, n_jobs=1, nthread=None,
       objective='binary:logistic', random_state=0, reg_alpha=0,
       reg_lambda=1, scale_pos_weight=1, seed=None, silent=None,
       subsample=1, verbosity=1)
  Best Parameter found
  • max_depth = 14
  • n estimators = 76
In [73]: clf=xgb.XGBClassifier(base score=0.5, booster='gbtree', colsample bylevel=1,
                colsample bytree=1, gamma=0, learning rate=0.1, max delta step=0,
                max_depth=14, min_child_weight=1, missing=None, n_estimators=76,
                n_jobs=1, nthread=None, objective='binary:logistic', random_state=0,
                reg_alpha=0, reg_lambda=1, scale_pos_weight=1, seed=None,
                silent=True, subsample=1)
In [74]: clf.fit(df_final_train,y_train)
         y_train_pred = clf.predict(df_final_train)
         y_test_pred = clf.predict(df_final_test)
In [75]: from sklearn.metrics import f1_score
         print('Train f1 score',f1_score(y_train,y_train_pred))
         print('Test f1 score',f1_score(y_test,y_test_pred))
Train f1 score 0.9963520474634704
Test f1 score 0.9279735542794176
```

Confusion Matrix

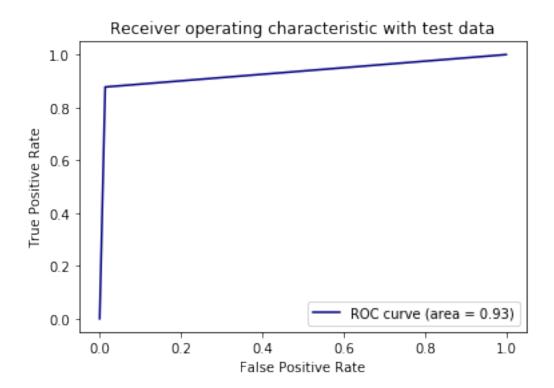
Train confusion_matrix



Test confusion_matrix

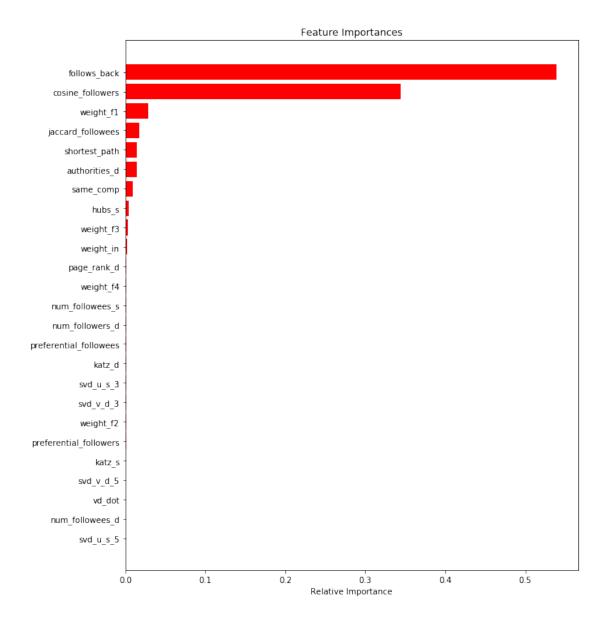


ROC/AUC Curve



Feature Importance

```
In [78]: features = df_final_train.columns
    importances = clf.feature_importances_
    indices = (np.argsort(importances))[-25:]
    plt.figure(figsize=(10,12))
    plt.title('Feature Importances')
    plt.barh(range(len(indices)), importances[indices], color='r', align='center')
    plt.yticks(range(len(indices)), [features[i] for i in indices])
    plt.xlabel('Relative Importance')
    plt.show()
```



5 ## Observations:

- 1. Understanding of graph and feature engineering was the most important part of this case study.
- 2. For Random Forest, Follow_back was the most important feature found, followed by weight_f2 and shortest_path.
- 3. Best result was obtained in case of XGBOOST.
- 4. XGBOOST took most of time.
- 5. For XGBOOST, follows_back was the most important feature. Followed by co-sine_follower and weight_f1.
- 6. XGBOOST gave the best result.

5.1 Summary:

```
In [79]: from prettytable import PrettyTable
      summary = PrettyTable()
      summary.field_names = ["Model", "n_estimators", "max_depth", "Train f1-Score", "Test f
In [80]: summary.add_row(['Random Forest','72','14','0.962','0.926'])
      summary.add row(['XGBOOST','76','14','0.996','0.927'])
      print(summary)
+----+
   Model | n_estimators | max_depth | Train f1-Score | Test f1-Score |
+----+
               72
                    1
                        14 |
| Random Forest |
                                0.962
                                            0.926
               76
                   - 1
                        14
                           0.996
                                       - 1
   XGBOOST |
                                            0.927
  _____+
```

6 ## Case Study Flow:

- 1. The dataset provided is directed graph data
- 2. For the given dataset, We have approx. 1.86M nodes and 9.43M edges.
- 3. Data was obtained from kaggle. You can get data from here https://www.kaggle.com/c/FacebookRecruiting
- 4. We have provided only connected nodes. i.e. 9.43M edges. But for each user among n user's, there is n-1 edges. So, for n nodes total possible edges are of 10^12 order.
- 5. On EDA, it is found that, number of followers are less than 12 for 90% of users.
- 6. The given dataset was highly imbalanced, as only one classification label is present.
- 7. We decided y = 0, is link is not present and took random sample from it.
- 8. In training and test dataset were exactly balanced.
- 9. Featurization is the most important part of this case study. We extracted various features types of features...
 - Similarity measures
 - Ranking Measure
 - Various Graph Features
 - Various Weight Features
 - SVD features using Adjancy matrix. (n_components = 6)
- 10. We Trained two models Random Forest and XGBOOST
- 11. XGBOST took most time for run.

In []: