```
% CODE FOR LINEAR ELEMENTS %
function Project 01 Linear
L=0.5;
                                          % Rod Length %
Le=zeros(5,1);
                                          % Element Size Matrix %
d=zeros(5,1);
                                          % L2 Error Values Matrix %
e=zeros(5,1);
                                          % Energy Error Values Matrix %
                                         % No. of nodes %
nn=[11,41,161,641,2565];
x=zeros(5,1);
                                          % Extra Matrices used for Storage %
y1=zeros(5,1);
y2=zeros(5,1);
for i=1:5
    Le(i)=L/(nn(i)-1);
                                          % Le = Element Length %
    [d(i),e(i)]=solve_fem(nn(i));
                                         % Solves model for given set of values %
    x(i) = log10(Le(i));
    y1(i) = log10(d(i));
    y2(i) = log10(e(i));
end
plot(x,y1,'ro-');
                                         % L2 Error Graph Plotting %
xlabel('Element Size');
ylabel('L2 Error');
title('Linear Element L2 Error');
figure;
plot(x,y2,'bo-');
                                          % Energy Error Graph Plotting %
xlabel('Element Size');
ylabel('Energy Error');
title('Linear Element Energy Error');
Convergence_L2=(y1(4)-y1(3))/(x(4)-x(3))% Calculates rate of Convergence for \checkmark
displacement%
Convergence_EE=(y2(4)-y2(3))/(x(4)-x(3)) % Calculates rate of Convergence for energy%
end
function [L2,EE]=solve_fem(nn)
% Inputs %
N=nn;
L=0.5;
                                        % Length of Al Rod %
Le=L/(N-1);
                                        % Calculation of Element Length %
% Connectivity and Nodes %
connect=[1:N-1;2:N];
nodes=[0:(L/(N-1)):L];
Ae=(pi/4)*0.01*0.01*70e9;
                                        % Area * Elastic Modulus %
% Stiffness Matrix Calculation %
                                        % Time Start %
tic;
k=Ae/Le;
                                        % Individual Element Stiffness (N/m) %
K=zeros(N);
for i=2:N
    K(i,i-1)=(-1)*k;
    K(i-1,i)=(-1)*k;
    K(i,i)=2*k;
end
```

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K(1,1)=k;
K(N,N)=k;
                                         % Time Stop %
toc;
% Apply Traction and Body Force %
                                         % Time Start %
tic;
f=zeros(N,1);
for c=connect
    Xe=nodes(c);
    le=Xe(2)-Xe(1);
for q=[-1,1]/sqrt(3)
    n=0.5*[1-q,1+q];
    x=n*Xe';
    f(c)=f(c)+n'*2000*(sin(10*pi*x))*(le/2);
end
f(N)=f(N)-((pi/4)*0.01*0.01*1000000); % Traction Force %
f(1)=0;
                                         % body force at x=0 %
% Boundary Conditions %
K(1,2)=0;
                                         % Boundary Condition at x=0, u=0 %
K(2,1)=0;
% Solution %
u=zeros(N,1);
u=K\setminus f;
toc;
                                         % Stop Time %
% Calculation of new node positions %
new_nodes=zeros(N,1);
for i=1:N
    new_nodes(i,1) = nodes(i) + u(i,1);
end
% Plotting the Displacement Graphs %
figure;
                                         % Plotting graph for Displacement Field %
plot(nodes,u,'ro');
xlabel('X distance');
ylabel('Displacement U');
title('Displacement Field against X Distance');
legend('Displacement Field',N);
% Elements lengths and strain calculations %
new_length=zeros(N-1,1);
for i=1:N-1
    new_length(i,1)=new_nodes(i+1,1)-new_nodes(i,1);
    strain(i,1)=((new_length(i,1)-Le)/Le);
end
% Plotting the Strain Graphs %
figure;
plot(nodes(1:N-1), strain(1:N-1), 'b');
title('Strain Field against X Distance'); % Plotting Graphs for Strain %
legend('Strain Field FEM');
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xlabel('X distance');
ylabel('Strain Value');
% Calculation of L2 and Energy Error Norm %
L2_error=0;
EE_error=0;
E = 70e9;
A=(pi/4)*0.01*0.01;
for c=connect
   Xe=nodes(c);
   le=Xe(2)-Xe(1);
                                  % Weight Functions for 3 point Gauss Quadrature 🗸
   w=[5/9 8/9 5/9];
응
   mm=1;
   for q=[-1,0,1]/sqrt(3/5)
                                  % 3 point Gauss Quadrature %
       n=0.5*[1-q,1+q];
                                  % Shape Function %
       B=(1/le)*[-1,1];
                                  % Derivative of the Shape Function %
       x=n*Xe';
       u_h=n*u(c);
       strain_h=B*u(c);
       exact_u = ((20*sin(10*pi*x))/(E*A*(pi^2))+(((200/(pi*A*E))-(1e6/E))*x));
       exact_strain=(((200*cos(10*pi*x))/(E*A*pi))+((200/(pi*A*E))-(1e6/E)));
       L2\_error = L2\_error + ((exact_u-u_h)^2)*(le/2)*w(mm);
       mm=mm+1;
   end
end
L2=sqrt(L2_error);
                                   % Final Value of L2_Error %
EE=sqrt(EE_error);
                                   % Final Value of Energy Error %
```

end