



# Data Structures and Algorithms

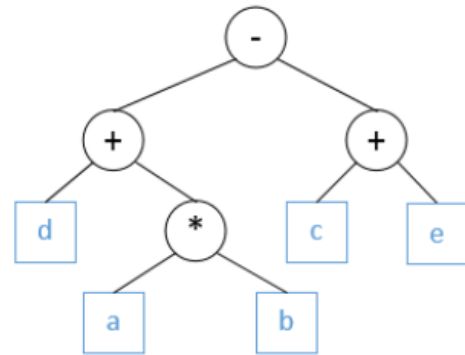
## Tut 5 – Tree

### Question 1

Expression  $(d + (a * b)) - (c + e)$  can be described by the **Expression Tree** below (LNR traverse).

Draw the Expression Trees of the following expressions:

- a)  $(3 - a) * (b + 4)$
- b)  $a - b - c * d - e - f$
- c)  $1 * 3 \div a + (b - c + d) * 7$
- d)  $(8 * 2) + (a + (b - c) * d) \div (5 \div 2)$



Which **Expression Tree** among a) b) c) d) is the complete tree? Explain your answer.

### Question 2

Given an empty Binary Search Tree (BST), the keys are inserted into BST one-by-one. Draw all states of the BST when inserting:

- a) 15, 7, 1, 11, 9, 13, 20
- b) 5, 6, 7, 8, 9
- c) 100, 50, 150, 7, 55, 121, 200

Then, remove the underlined key (7) of the above trees (a, b, c). Draw the final state of the trees after removing.



Given the following data structure

```
class treeNode {
public:
    int data;
    treeNode* left = NULL;
    treeNode* right = NULL;
};
```

### Question 3

a) Write a recursive function to insert a new node into the BST:

```
treeNode* recursiveInsert ( treeNode* subroot, treeNode* newNode ) {
    // YOUR CODE HERE
}
```

b) Write a function to print out the path from root to the node having searchedData

```
void printPath ( treeNode* subroot, int searchedData ) {
    // YOUR CODE HERE
}
```

c) Write a function that print out all leaves of the tree via Breadth First Traverse , LNR and NLR

```
void printLeavesBFT ( treeNode* root ) {
    // YOUR CODE HERE
}
void printLeavesLNR ( treeNode* subroot ) {
    // YOUR CODE HERE
}
void printLeavesNLR ( treeNode* subroot ) {
    // YOUR CODE HERE
}
```

### Question 4\*

Propose an algorithm to check if a given Binary Tree is a BST.

**algorithm** checkBST\_recur (val subroot <BinaryNode>, ref min <DataType>, ref max <DataType>)

*This algorithm check if the input subroot is a BST recursively*

**Pre** subroot points to a root of the subtree

**Post** min and max are the smallest and largest value in the subtree

**Return** true if the subtree is a BST, false otherwise