8 QUEENS PROBLEM USING BACK TRACKING

BACK TRACKING

✓ **Backtracking** is a general algorithm for finding all (or some) solutions to some computational problem, that *incrementally builds candidates to the solutions*, and abandons each partial candidate '*c*' ("backtracks") as soon as it determines that '*c*' cannot possibly be completed to a valid solution.

✓ Backtracking is an important tool for solving constraint satisfaction problems, such as *crosswords, verbal arithmetic, Sudoku, and many other puzzles.*

✓ It is also the basis of the so-called logic programming languages such as *Planner and Prolog.*

✓ The term "backtrack" was coined by American mathematicia D. H. Lehmer in the 1950s.

✓ The pioneer string-processing language SNOBOL (1962) may have been the first to provide a built-in general backtracking facility.

✓ The good example of the use of backtracking is the eight queens puzzle, that asks for all arrangements of eight queens on a standard chessboard so that no queen attacks any other.

✓ In the common backtracking approach, the partial candidates are arrangements of k queens in the first k rows of the board, all in different rows and columns.

✓ Any partial solution that contains two mutually attacking queens can be abandoned, since it cannot possibly be completed to a valid solution

WHAT IS 8 QUEEN PROBLEM?

- ✓ The **eight queens puzzle** is the problem of placing eight chess queens on an 8 8 chessboard so that no two queens attack each other.

- ✓ Thus, a solution requires that no two queens share the same row, column, or diagonal.

- ✓ The eight queens puzzle is an example of the more general *n*-**queens problem** of placing *n* queens on an *n n* chessboard, where solutions exist for all natural numbers *n* with the exception of *1, 2 and 3*.

- ✓ The solution possibilities are discovered only up to *28 queen*

PROBLEM INVENTOR

✓ The puzzle was originally proposed in 1848 by the chess
player ***Max Bezzel***, and over the
years, many mathematicians, including Gauss, have worked on
this puzzle and its generalized n-queens problem.

SOLUTION INVENTOR

✓ The first solution for 8 queens were provided by ***Franz Nauck*** in 1850. Nauck also extended the puzzle to n-queens problem (on an n n board—a chessboard of arbitrary size).

✓ In 1874, S. ***Günther*** proposed a method of finding solutions by using determinants, and ***J.W.L. Glaisher*** refined this approach.

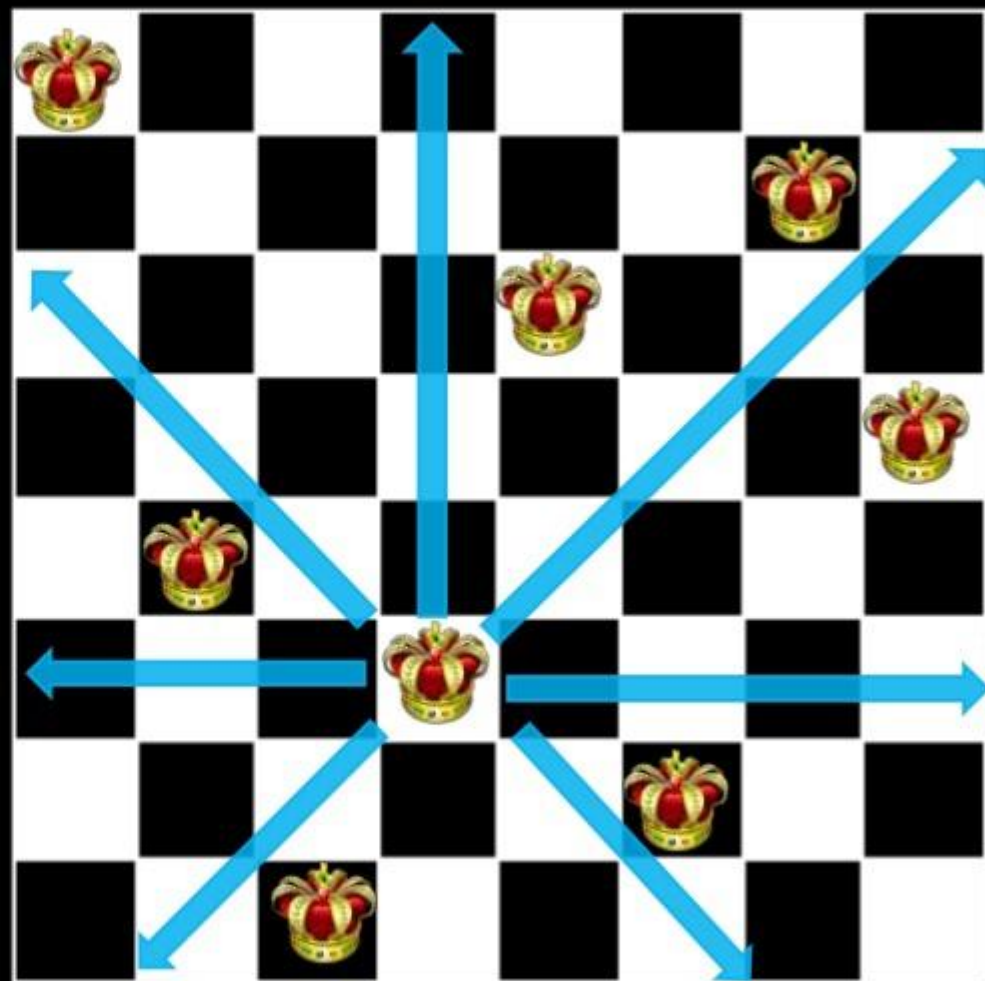✓ ***Edsger Dijkstra*** used this problem in 1972 to illustrate the

Formulation :

States: any arrangement of 0 to 8 queens on the board

Initial state: 0 queens on the board

Successor function: add a queen in any square

Goal test: 8 queens on the board, none attacked

BACKTRACKING CONCEPT

✓   Each recursive call attempts to place a queen in a specific column.

✓   For a given call, the state of the board from previous placements is known (i.e. where are the other queens?)

✓   *Current step backtracking*: If a placement within the column does not lead to a solution, the queen is removed and moved *"down"* the column

✓   *Previous step backtracking*: When all rows in a column

CONTINU..

➢**Pruning:** If a queen cannot be placed into column i, do not even try to place one onto column i+1 − rather, backtrack to column i−1 and move the queen that had been placed there.

➢Using this approach we can reduce the number of potential solutions even more
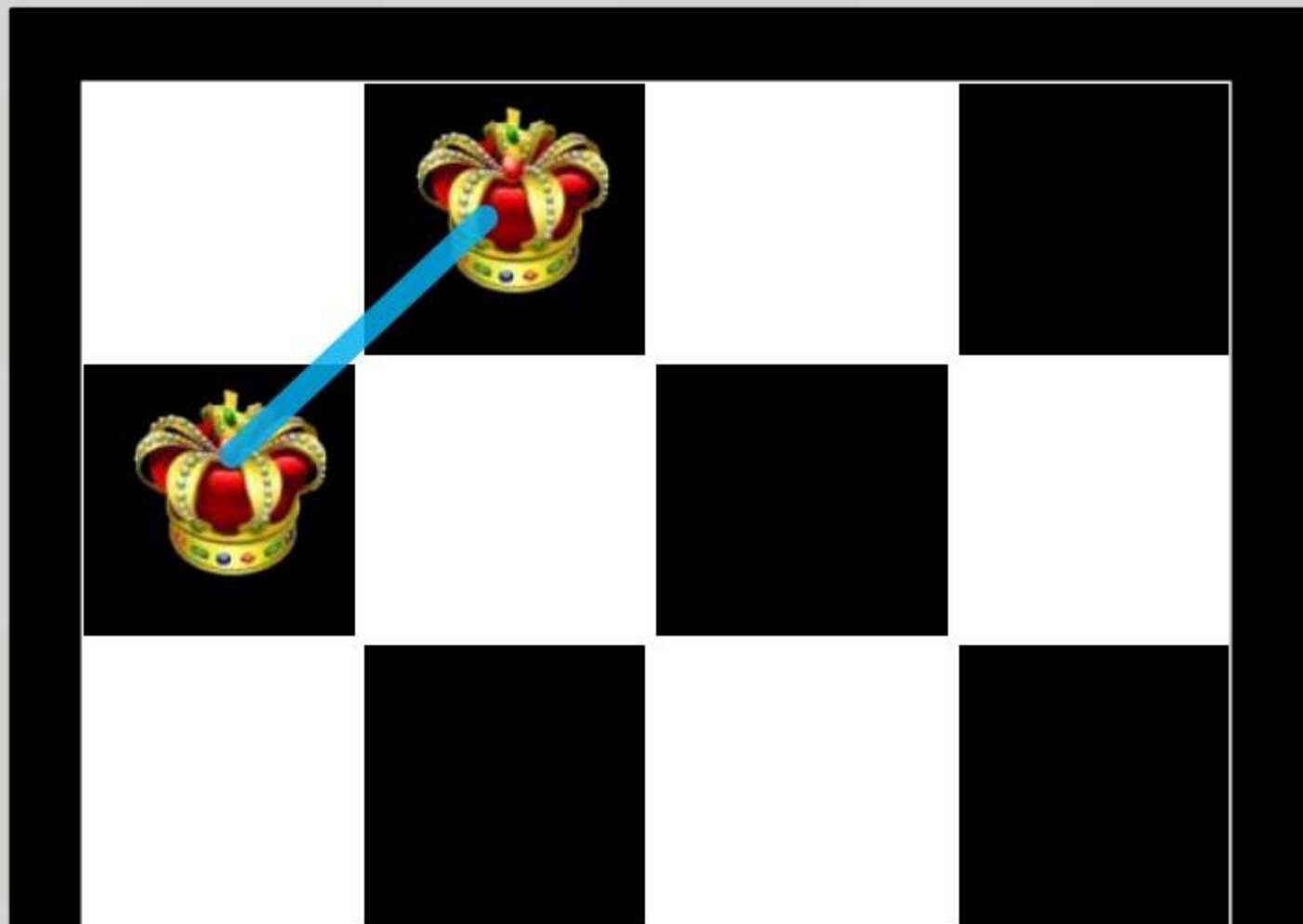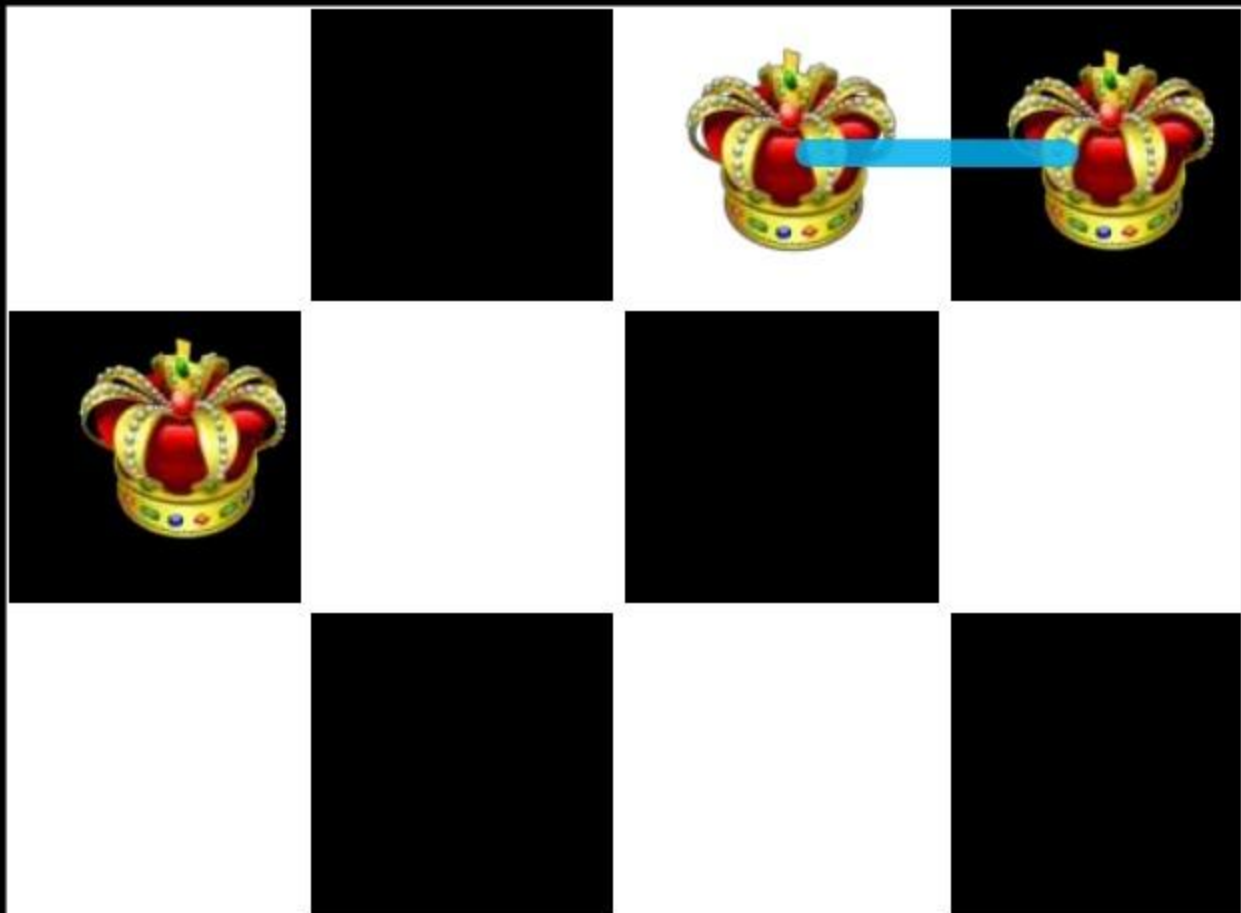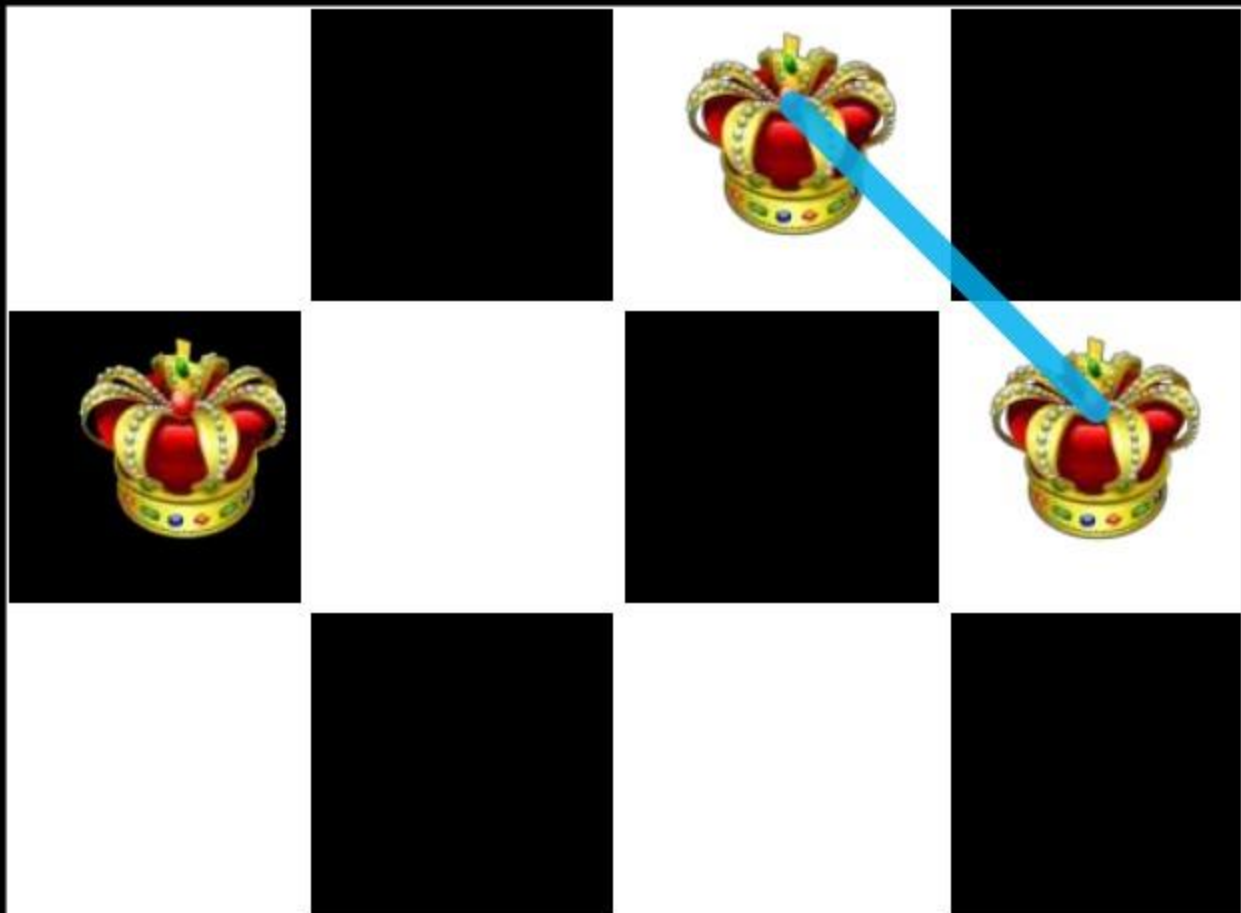
BACKTRACKING DEMO FOR 4 QUEENS

1 UNIQUE SOLUTION

STEPS REVISITED – BACKTRACKING

1. Place the first queen in the left upper corner of the table.

2. Save the attacked positions.

3. Move to the next queen (which can only be placed to the next line).

4. Search for a valid position. If there is one go to step 8.

5. There is not a valid position for the queen. Delete it (the x coordinate is 0).

6. Move to the previous queen.

EIGHT QUEEN PROBLEM: ALGORITHM

```
putQueen(row)
{
    for every position col on the same row
        if  position col is available
            place the next queen in position col
        if (row<8)
            putQueen(row+1);
        else  success;
```

THE PUTQUEEN RECURSIVE METHOD

```
void putQueen(int row)
  {
    for (int col=0;col<squares;col++)

        if (column[col]==available &&
        leftDiagonal[row+col]==available &&
        rightDiagonal[row-col]== available)
          {
```

```
        rightDiagonal[row-col]=!available;
         if (row< squares-1)
                 putQueen(row+1);
      else
                 print(" solution found");
      column[col]=available;
       leftDiagonal[row+col]=available;
       rightDiagonal[row-col]= available;
    }
```

WHY NOT NESTED LOOP

✓   The nested loops are not so preferred because . It Does not scale to different sized boards

✓   You must duplicate identical code (place and remove). and error in one spot is hard to find

✓   The problem with this is that it's not very programmer-friendly. We can't vary at runtime the size of the board we're searching

✓ The major advantage of the backtracking algorithm is the abillity to find and count all the possible solutions rather than just one while offering decent speed.

✓ If we go through the algorithm for 8 queens 981 queen moves (876 position tests plus 105 backtracks) are required for the first solution alone. 16,704 moves (14,852 tests and 1852 backtracks) are needed to find all 92 solutions.

✓ Given those figures, it's easy to see why the solution is best left to computers.

THANK YOU