

Predictive LL(1) Parser

- This top-down parsing algorithm is of non-recursive type.
- In this of parsing a table is built.
- For LL(1) - the first L means the input is scanned from left to right. The second L means it uses leftmost derivation for input string. And the number (1) in the input symbol means it uses only one input symbol (lookahead) to predict the parsing process.

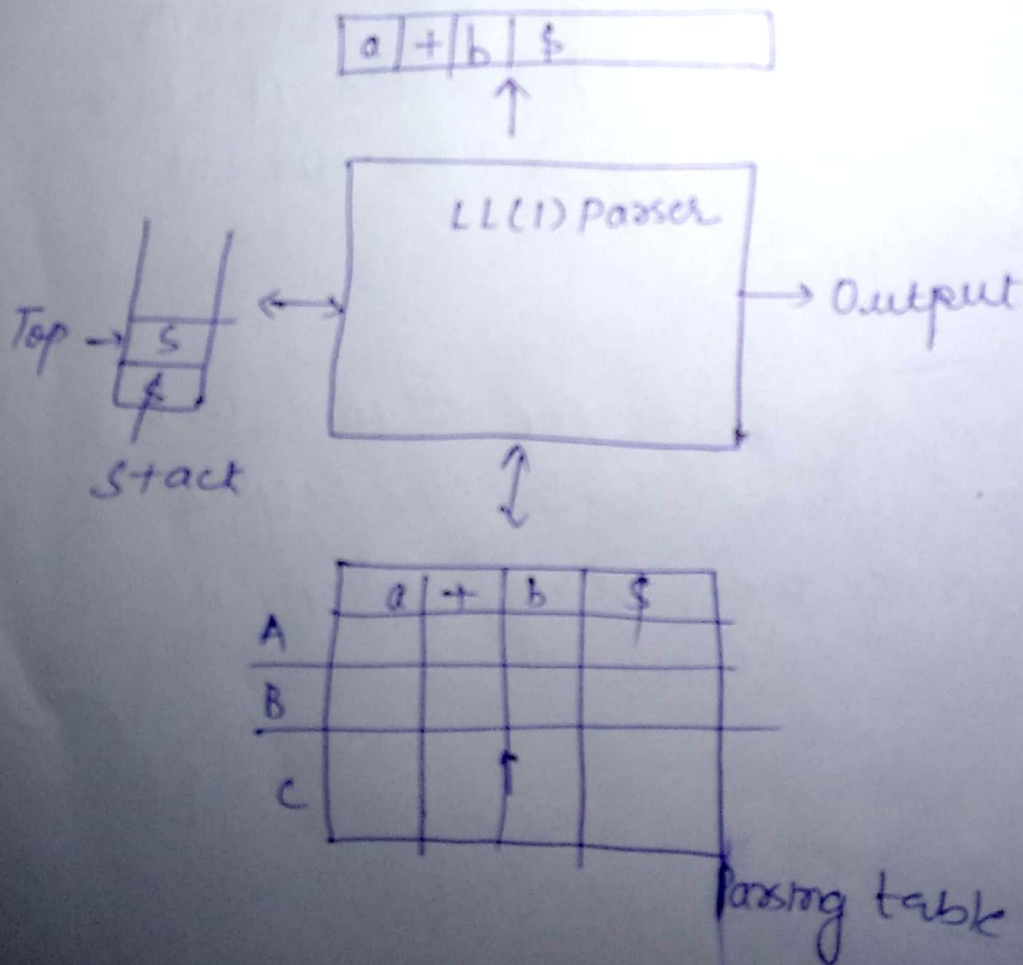


fig: Model for LL(1) Parser

The data structures used by LL(1) are (i) input buffer
(ii) stack (iii) parsing table. The LL(1) parser uses input buffer to store the input tokens.

→ The stack is used to hold the left sentential form. The symbols in R.H.S of rule are pushed into the stack in reverse order i.e. from left to right to left. This use of stack makes this algorithm non-recursive.

→ The table is basically a 2-D array. The table has row for non-terminal & column for terminals. The table can be represented as $M[A, a]$ where A is a non-terminal & a is the current input symbol.

→ The parsing program reads top of the stack & a current i/p symbol. With the help of these two symbols the parsing action is determined.

Construction of Predictive LL(1) Parser

- Step 1 Computation of FIRST & FOLLOW FUNCTION
- Step 2 Construct the Predictive Parsing table using FIRST & FOLLOW functions
- Step 3 Parse the input string with the help of Predictive Parsing table.

Algorithm for predictive Parsing table

Input: Context Free Grammar G .

Output: Predictive Parsing table M .

Algorithm

For the rule $A \rightarrow \alpha$ of grammar G

1) For each a in $\text{FIRST}(\alpha)$ create entry $M[A, a] = A \rightarrow \alpha$ where a is terminal symbol.

2) for ϵ in $\text{FIRST}(\alpha)$ create $M[A, b] = A \rightarrow \alpha$ where b is the symbols from $\text{FOLLOW}(A)$.

3) If ϵ is in $\text{FIRST}(\alpha)$ & $\$$ is in $\text{FOLLOW}(A)$ then create entry in table $M[A, \$] = A \rightarrow \alpha$

(4) All the remaining entries are marked as error.

& create the parsing table for the above grammar.

$$E \rightarrow TE'$$

$$E' \rightarrow +TE' / \epsilon$$

$$T \rightarrow FT'$$

$$T' \rightarrow *FT' / \epsilon$$

$$F \rightarrow (E) / id$$

Sol First check for left recursion & left factoring

There is no left recursion & no left factoring reqn

Now Calculate first & follow

~~first~~ $FIRST(E) = FIRST(T) = FIRST(F)$

As

$$FIRST(F) = \{ (, id \}$$

$$FIRST(E') = \{ +, \epsilon \}$$

$$FIRST(T) = FIRST(F) = \{ (, id \}$$

$$FIRST(T') = \{ *, \epsilon \}$$

$$\therefore FIRST(E) = \{ (, id \}$$

Now calculate follow

$$\text{FOLLOW}(E) = \{ \$,) \}$$

As E is the starting symbol so we add $\$$ in $\text{follow}(E)$.

$$\begin{aligned}\text{FOLLOW}(E') &= \text{FOLLOW}(E) \cup \text{FOLLOW}(E') \\ &= \text{FOLLOW}(E) \\ &= \{ \$,) \}\end{aligned}$$

$$\begin{aligned}\text{FOLLOW}(T') &= \text{FOLLOW}(T) \cup \text{FOLLOW}(T') \\ &= \text{FOLLOW}(T)\end{aligned}$$

$$\begin{aligned}\text{FOLLOW}(T) &= \{ \text{FIRST}(E') - E \} \cup \text{FOLLOW}(E) \cup \text{FOLLOW}(E') \\ &= \{ + \} \cup \{ \$,) \} \cup \{ \$,) \} \\ &= \{ +, \$,) \}\end{aligned}$$

$$\begin{aligned}\text{FOLLOW}(T') &= \text{FOLLOW}(T) \cup \text{FOLLOW}(T') \\ &= \text{FOLLOW}(T) \\ &= \{ \$,) \}\end{aligned}$$

$$\begin{aligned}\text{FOLLOW}(F) &= \{ \text{FIRST}(T') - E \} \cup \text{FOLLOW}(T') \cup \text{FOLLOW}(T) \\ &= \{ * \} \cup \{ \$,) \} \cup \{ +, \$,) \} \\ &= \{ *, +, \$,) \}\end{aligned}$$

| Symbols | FIRST | FOLLOW |
|---------|---------|---------------|
| E | {(, id} | {), \$} |
| E' | {+, ε} | {), \$} |
| T | {(, id} | {+,), \$} |
| T' | {*, ε} | {+,), \$} |
| F | {(, id} | {+, *,), \$} |

Now first create the table

| | id | + | * | (|) | \$ |
|----|----|---|---|---|---|----|
| E | | | | | | |
| E' | | | | | | |
| T | | | | | | |
| T' | | | | | | |
| F | | | | | | |

Now consider each rule one by one to fill the parsing table.

$$E \rightarrow TE'$$

according to parsing table algo we map the above the grammar with the rule $A \rightarrow \alpha$

$$\text{Here } A \rightarrow \alpha \quad A = E, \alpha = TE'$$

$$\text{FIRST}(TE') = \text{FIRST}(T) = \{(, id\}$$

$$M[E, (] = E \rightarrow TE' \quad \& \quad M[E, id] = E \rightarrow TE'$$

| | id | $+$ | $*$ | $($ | $)$ | $\$$ |
|------|----------------------------------------|-----------------------|-----------------------|-----------------------------------------|--------------------|--------------------|
| E | $E \rightarrow TE'$ | error | error | $E \rightarrow TE'$ | error | error |
| E' | error | $E' \rightarrow +TE'$ | error | error | $E' \rightarrow E$ | $E' \rightarrow E$ |
| T | $T \rightarrow FT'$ | error | error | $T \rightarrow FT'$ | error | error |
| T' | error | $T' \rightarrow E$ | $T' \rightarrow *FT'$ | error | $T' \rightarrow E$ | $T' \rightarrow E$ |
| F | error $F \rightarrow id$ | error | error | error $F \rightarrow (E)$ | error | error |

Now ① $E' \rightarrow +TE'$

map the grammar using the rule $A \rightarrow \alpha$

$$A = E'$$

$$\alpha = +TE'$$

$$FIRST(\alpha) \text{ i.e. } FIRST(+TE') = \{+\}$$

$$\therefore M[E', +] = E' \rightarrow +TE'$$

Now ② $E' \rightarrow E$

Here according to rule $A \rightarrow \alpha$

$$A = E'$$

$$\alpha = E$$

$$\text{then } FOLLOW(E') = \{), \$\}$$

$$M[E',)] = E' \rightarrow E$$

$$M[E', \$] = E' \rightarrow E$$

Now

$$\textcircled{3} T \rightarrow FT'$$

Map it according to rule $A \rightarrow \alpha$

$$A = T$$

$$\alpha = FT'$$

$$\text{Now } \text{FIRST}(FT') = \text{FIRST}(F) = \{(, id\}$$

$$\text{Hence } M[\cancel{F}, (] = T \rightarrow FT'$$

$$M[T, id] = T \rightarrow FT'$$

$$\textcircled{4} T' \rightarrow *FT'$$

Map it according to rule $A \rightarrow \alpha$

$$A = T'$$

$$\alpha = *FT'$$

$$\text{FIRST}(\alpha) = \text{FIRST}(*FT')$$

$$= \text{FIRST}(*)$$

$$= *$$

$$\therefore M[T', *] = T' \rightarrow *FT'$$

$$\textcircled{5} T' \rightarrow \epsilon$$

Here
 $A = T'$

$$\alpha = \epsilon$$

$$\therefore \text{FOLLOW}(T') = \{+, \rangle, \$\}$$

$$M[T', +] = T' \rightarrow \epsilon$$

$$M[T', \rangle] = T' \rightarrow \epsilon$$

$$M[T', \$] = T' \rightarrow \epsilon$$

$$\textcircled{6} \quad F \rightarrow (E)$$

Map it according to the rule $A \rightarrow \alpha$

$$A = F$$

$$\alpha = (E)$$

$$\begin{aligned} \text{FIRST}(\alpha) &= \cancel{(E)} \text{FIRST}((E)) \\ &= \{ (\} \end{aligned}$$

$$M[\cancel{F}, (] = F \rightarrow (E)$$

$$\textcircled{7} \quad F \rightarrow id$$

Map it according to rule $A \rightarrow \alpha$

$$A = F$$

$$\alpha = id$$

$$\begin{aligned} \text{FIRST}(\alpha) &= \text{FIRST}(id) \\ &= id \end{aligned}$$

$$M[F, id] = F \rightarrow id$$