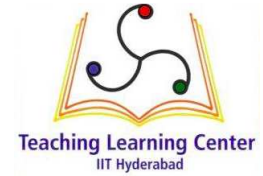




## Gate problems in DSP



**Abstract :** *These problems have been selected from GATE question papers and can be used for conducting tutorials in courses related to a first course in Digital Signal Processing.*

- 1) The trigonometric Fourier series of an even function of time does not have the
  - (A) dc term
  - (B) cosine terms
  - (C) sine terms
  - (D) odd harmonic terms
- 2) The Fourier transform of a real valued time signal
  - (A) odd symmetry
  - (B) even symmetry
  - (C) conjugate symmetry
  - (D) no symmetry
- 3) The function  $f(t)$  has the Fourier transform  $g(w)$ . The Fourier Transform
  - (A)  $\frac{1}{2\pi}f(w)$
  - (B)  $\frac{1}{2\pi}f(-w)$
  - (C)  $2\pi f(-w)$
  - (D) None of the above
- 4) The Laplace Transform of  $e^{\alpha t} \cos \alpha t u(t)$ 
  - (A)  $\frac{(s - \alpha)}{(s - \alpha)^2 + \alpha^2}$
  - (B)  $\frac{(s + \alpha)}{(s - \alpha)^2 + \alpha^2}$
  - (C)  $\frac{1}{(s - \alpha)^2}$
  - (D) None of the above
- 5) A deterministic signal has the power spectrum given in the figure is, The minimum sampling rate needed to completely represent this signal is
  - (A) 1 kHz
  - (B) 2 kHz
  - (C) 3 kHz
  - (D) None of the above
- 6) If the Fourier Transform of deterministic signal  $g(t)$  is  $G(f)$ , then
  1. The fourier Transform of  $g(t - 2)$  is.
    - (a)  $G(f)e^{-j(4\pi f)}$
  2. The fourier Transform of  $g(\frac{t}{2})$  is.
    - (b)  $G(2f)$  (c)  $2G(2f)$  (d)  $G(f - 2)$
- 7) The transfer function of a system is given by  $H(s) = \frac{1}{s^2(s - 2)}$ . The impulse response of the system is : ( \* denotes convolution, and  $U(t)$  is unit step function)
  - (A)  $(t^2 * e^{-2t})U(t)$
  - (B)  $(t * e^{2t})U(t)$
  - (C)  $(te^{-2t})U(t)$
  - (D)  $(te^{-2t})U(t)$

- 8) Let  $\delta(t)$  denote the delta function. The value of the integral  $\int_{-\infty}^{+\infty} \delta(t) \cos\left(\frac{3t}{2}\right) dt$  is
- (A) 1      (B) -1      (C) 0      (D)  $\frac{\pi}{2}$
- 9) A band limited signal is sampled at the Nyquist rate. The signal can be recovered by passing the samples through
- (A) An RC filter
- (B) an envelope detector
- (C) a PLL
- (D) an ideal low-pass filter with appropriate bandwidth
- 10) The impulse response functions of four linear systems  $S_1, S_2, S_3$  and  $S_4$  are given respectively by
- $$h_1(t) = 1$$
- $$h_2(t) = U(t)$$
- $$h_3(t) = \frac{U(t)}{t+1}$$
- $$h_4(t) = e^{-3t}U(t)$$
- Where  $U(t)$  is the unit step function. Which of these systems is time invariant, causal and Stable ?
- (A)  $S_1$       (B)  $S_2$       (C)  $S_3$       (D)  $S_4$
- 11) The open-loop DC gain of a unity negative feedback system with close-loop transfer function  $\frac{s+4}{s^2+7s+13}$  is
- (A)  $\frac{4}{13}$       (B)  $\frac{4}{13}$       (C) 4      (D) 13
- 12) The Nyquist sampling interval, for the signal  $\text{Sinc}(700t) + \text{Sinc}(500t)$  is ( in seconds)
- (A)  $\frac{1}{350}$       (B)  $\frac{\pi}{350}$       (C)  $\frac{1}{700}$       (D)  $\frac{\pi}{175}$
- 13) Which of the following cannot be the Fourier series of a periodic signal ?
- (A)  $x(t) = 2\cos t + 3\cos 3t$
- (B)  $x(t) = 2\cos \pi t + 7\cos t$
- (C)  $x(t) = \cos t + 0.5$
- (D)  $x(t) = 2\cos 1.5\pi t + \sin 3.5\pi t$
- 14) The fourier transform  $F(e^{-1}u(t))$  is equal to  $\frac{1}{a+j2\pi f}$ . Therefore,  $F\left\{\frac{1}{a+j2\pi t}\right\}$
- (A)  $e^f u(f)$       (C)  $e^f u(-f)$
- (B)  $e^{-f} u(f)$       (D)  $e^{-f} u(-f)$
- 15) A linear phase channel with phase delay  $T_p$  and group delay  $T_g$  must have
- (A)  $T_p = T_g = \text{Constant}$
- (B)  $T_p \propto f$  and  $T_g \propto f$
- (C)  $T_p = \text{constant}$  and  $T_g \propto f$
- (D)  $T_p \propto f$  and  $T_g = \text{constant}$
- 16) A 1 MHz sinusoidal carrier is amplitude modulated by a symmetrical square wave of period 100  $\mu\text{sec}$ . Which of the following frequencies will NOT be present in the modulated signal ?

- (A) 990KHz (C) 1020KHz  
(B) 1010KHz (D) 1030KHz

17) Consider a sampled signal  $y(t) = 5 \times 10^{-6} x(t) \sum_{n=-\infty}^{+\infty} \delta(t - nT_s)$  is

- (A)  $5 \times 10^{-6} \cos(8\pi \times 10^3 t)$   
(B)  $5 \times 10^{-5} \cos(8\pi \times 10^3 t)$   
(C)  $5 \times 10^{-1} \cos(8\pi \times 10^3 t)$   
(D)  $10 \cos(8\pi \times 10^3 t)$

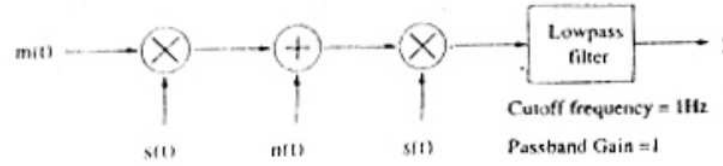
18) The Laplace transform of a continuous-time signal  $x(t)$  is  $X(s) = \frac{5-s}{s^2-s-2}$ . If the Fourier transform of this signal exists, then  $x(t)$  is

- (A)  $e^{2t}u(t) - 2e^{-t}u(t)$   
(B)  $-e^{2t}u(-t) + 2e^{-t}u(t)$   
(C)  $-e^{2t}u(-t) - 2e^{-t}u(t)$   
(D)  $e^{2t}u(-t) - 2e^{-t}u(t)$

19) If the impulse response of a discrete-time system is  $h[n] = -5^n u[-n-1]$ , then the system function  $H(z)$  is equal to

- (A)  $\frac{-z}{z-5}$  and the system is stable  
(B)  $\frac{z}{z-5}$  and the system is stable  
(C)  $\frac{-z}{z-5}$  and the system is unstable  
(D)  $\frac{z}{z-5}$  and the system is unstable

20) In below figure,  $m(t) = \frac{2\sin 2\pi t}{t}$ ,  $s(t) = \cos 200\pi t$  and  $n(t) = \frac{\sin 199\pi t}{t}$ . The output is



- (A)  $\frac{\sin 2\pi t}{t}$   
(B)  $\frac{\sin 2\pi t}{t} + \frac{\sin 2\pi t}{t} \cos(3\pi t)$   
(C)  $\frac{\sin 2\pi t}{t} + \frac{\sin 0.5\pi t}{t} \cos(1.5\pi t)$   
(D)  $\frac{\sin 2\pi t}{t} + \frac{\sin \pi t}{t} \cos(0.75\pi t)$

21) A signal  $x(t) = 100 \cos(24\pi \times 10^3 t)$  is ideally sampled with a sampling period of  $50 \mu\text{sec}$  and then passed through an ideal low-pass filter with cutoff frequency of 15 KHz. Which of the following frequencies is/are present at the filter output?

- (A) 12 KHz only (C) 12 KHz and 9 KHz  
(B) 8 KHz only (D) 12 KHz and 8 KHz

22) The Fourier series expansion of a real periodic signal with fundamental frequency  $f_0$  is given by  $g_p(t) = \sum_{n=-\infty}^{+\infty} c_n e^{j2\pi n f_0 t}$  is given that  $C_3 = 3 + j5$ . Then  $C_{-3}$  is

- (A)  $5 + j3$  (C)  $-5 - j3$   
(B)  $-3 - j5$  (D)  $3 - j5$

23) Let  $x(t)$  be the input to a linear, time-invariant system. The required output is  $4x(t-2)$ . The

transfer function of the system should be

- (A)  $4e^{j4\pi f}$  (B)  $2e^{-j8\pi f}$  (C)  $4e^{-j4\pi f}$  (D)  $2e^{j8\pi f}$

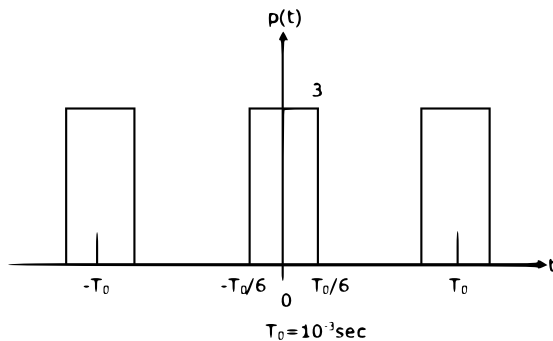
- 24) A sequence  $x(n)$  with the z-transform  $X(z) = z^4 + z^2 - 2z + 2 - 3z^{-4}$  is applied as an input to a linear, time-invariant system with the impulse response  $h(n) = 2\delta(n - 3)$  where

$$\delta(n) = \begin{cases} 1, & \text{if } n=0 \\ 0, & \text{otherwise} \end{cases}$$

The output at  $n=4$  is

- (A) -6 (B) 0 (C) 2 (D) -4

- 25) Let  $x(t) = 2\cos(800\pi t) + \cos(1400\pi t)$ ,  $x(t)$  sampled with the rectangular pulse train shown in figure. The only spectral components (in kHz) present in the sampled signal in the frequency range 2.5 kHz to 3.5 kHz are



- (A) 2.7, 3.4 (C) 2.6, 2.7, 3.3, 3.4, 3.6  
(B) 3.3, 3.6 (D) 2.7, 3.3

Data for **Q.2-24** are given below. Solve the problems and choose the correct answers. The system under consideration is an RC low-pass filter (RC-LPF) with  $R=1.0K\Omega$  and  $C=1.0\mu F$

- 26) Let  $H(f)$  denote the frequency response of the RC-LPF. Let  $f_1$  be the highest frequency such that  $0 \leq |f| \leq f_1$ ,  $\frac{|H(f_1)|}{H(0)} \geq 0.95$ . Then  $f_1$  (in HZ) is

- (A) 327.8 (B) 163.9 (C) 52.2 (D) 104.4

- 27) Let  $t_g(f)$  be the group delay function of the given RC-LPF and  $f_2 = 100\text{Hz}$ . Then  $t_g(f_2)$  in ms, is

- (A) 0.717 (B) 7.17 (C) 71.7 (D) 4.505

- 28) The impulse response  $h[n]$  of a linear time-invariant system is given by  $h[n] = u[n+3] + u[n-2] - 2u[n-7]$  where  $u[n]$  is the unit step sequence. The above system is

- (A) Stable but not causal

- (B) Stable and Causal

- (C) Causal but unstable

- (D) Unstable and not Causal

- 29) The z-transform of a system is  $H(z) = \frac{z}{z-0.2}$ . If the ROC is  $|z| < 0.2$ , then the impulse response of the system is

- (A)  $(0.2)^n u[n]$  (C)  $-(0.2)^n u[n]$

- (B)  $(0.2)^n u[-n-1]$  (D)  $-(0.2)^n u[-n-1]$

- 30) The Fourier transform of a conjugate symmetric function is always

- (A) real

- (B) conjugate anti-symmetric

- (C) real

- (D) conjugate symmetric

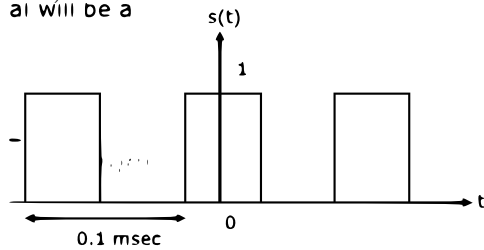
- 31) The gain margin for the system with open-loop transfer function  $G(s)H(z) = \frac{2(1+z)}{s^2}$

(A)  $\infty$  (B) 0 (C) 1 (D)  $-\infty$

- 32) A 1 kHz sinusoidal signal is ideally sampled at 1500 samples/sec and the sampled signal is passed through an ideal low-pass filter with cut-off frequency 800 Hz. The output signal has the frequency ?

(A) 0 Hz (C) 0.5 kHz  
(B) 0.75 kHz (D) 0.25 kHz

- 33) A rectangular pulse train  $s(t)$  as shown in figure, is convolved with the signal  $\cos^2(4\pi \times 10^3)t$ . The result will be a



(A) DC (C) 8 kHz sinusoid  
(B) 12 kHz sinusoid (D) 14 kHz sinusoid

- 34) consider the sequence  $x[n] = [4 - j5 \ 1 + j2 \ 4]$ . The conjugate anti-symmetric part of the sequence is

(A)  $[-4 - j2.5 \ j2 \ 4 - j2.5]$   
(B)  $[-j2.5 \ 1 \ j2.5]$   
(C)  $[-j5 \ j2 \ 0]$   
(D)  $[-4 \ 1 \ 4]$

- 35) A causal LTI system is described by the difference equation  $2y[n] = ay[n-2] - 2x[n] +$

$bx[n-1]$ . The system is stable only if

(A)  $|a| = 2, |b| < 2$

(B)  $|a| > 2, |b| > 2$

(C)  $|a| < 2$ , any value of  $b$

(D)  $|b| < 2$ , any value of  $a$

- 36) A causal system having the transfer function  $H(s) = \frac{1}{s+2}$  is excited with  $10u(t)$ . The time at which the output reaches 99% of its steady state value is

(A) 2.7 sec (C) 2.4 sec  
(B) 2.5 sec (D) 2.1 sec

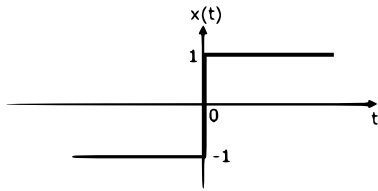
- 37) The impulse response  $h[n]$  of a linear time invariant system is given as

$$h[n] = \begin{cases} -2\sqrt{2}, & \text{if } n=1, -1 \\ 4\sqrt{2}, & \text{if } n=2, -2 \\ 0, & \text{otherwise.} \end{cases}$$

If the input to the above system is the sequence  $\frac{jpn}{e^4}$ , then the output is

(A)  $4\sqrt{2}e^{\frac{jpn}{4}}$  (C)  $4e^{\frac{jpn}{4}}$   
(B)  $4\sqrt{2}e^{-\frac{jpn}{4}}$  (D)  $-4e^{\frac{jpn}{4}}$

- 38) The function  $x(t)$  is shown in figure. Even and odd parts of a unit-step function  $u(t)$  are respectively.



(A)  $\frac{1}{2}, \frac{1}{2}x(t)$  (C)  $\frac{1}{2}, -\frac{1}{2}x(t)$

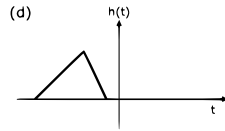
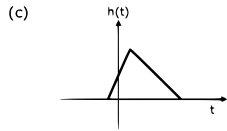
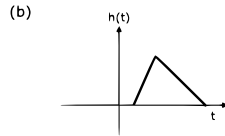
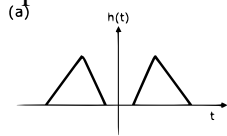
(B)  $-\frac{1}{2}, \frac{1}{2}x(t)$  (D)  $-\frac{1}{2}, -\frac{1}{2}x(t)$

- 39) The region of convergence of Z-transform of the sequence  $(\frac{5}{6})^n u(n) - (\frac{6}{5})^n u(-n-1)$  must be

(A)  $|z| < \frac{5}{6}$  (C)  $\frac{5}{6} < |z| < \frac{5}{6}$

(B)  $|z| > \frac{6}{5}$  (D)  $\frac{6}{5} < |z| < \infty$

- 40) Which of the following can be impulse response of causal system?



- 41) Let  $x(n) = (\frac{1}{2})^n$ ,  $y(n) = x^2(n)$  and  $Y(e^{j\omega})$  be the fourier transform of  $y(n)$ . Then  $Y(e^{j0})$

(A)  $\frac{1}{4}$  (C) 4

(B) 2 (D)  $\frac{4}{3}$

- 42) The output  $y(t)$  of a linear time invariant system is related to its input  $x(t)$  by the following equation.  $y(t) = 0.5x(t - t_d + T) + x(t - t_d) + 0.5x(t - t_d - T)$ . The filter transfer function  $H(\omega)$  of such a system is given by

(A)  $(1 + \cos \omega T)e^{-j\omega t_d}$

(B)  $(1 + 0.5\cos \omega T)e^{-j\omega t_d}$

(C)  $(1 + \cos \omega T)e^{j\omega t_d}$

(D)  $(1 - 0.5\cos \omega T)e^{-j\omega t_d}$

- 43) A signal  $x(n) = \sin(\omega_0 n + \phi)$  is the input to a LTI system frequency response  $H(e^{j\omega})$ . If the output of the system is  $Ax(n - n_0)$ , then the most general form of  $\angle H(e^{j\omega})$  will be

(A)  $-n_0\omega_0 + \beta$  for any arbitrary real  $\beta$

(B)  $-n_0\omega_0 + 2\pi k$  for any arbitrary integer k.

(C)  $n_0\omega_0 + 2\pi k$  for any arbitrary integer k.

(D)  $-n_0\omega_0 + \phi$

- 44) For a signal  $x(t)$  the Fourier transform is  $X(f)$ . Then the inverse Fourier transform of  $X(3f + 2)$  is given by

(A)  $\frac{1}{2}x(\frac{1}{2})e^{j3\pi t}$

(B)  $3x(3t)e^{-j4\pi t}$

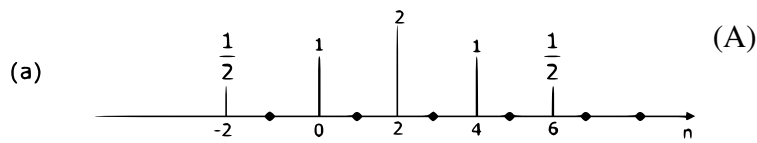
(C)  $\frac{1}{3}x(\frac{1}{3})e^{\frac{-j4\pi t}{3}}$

(D)  $x(3t + 2)$

- 45) (A) The Sequence

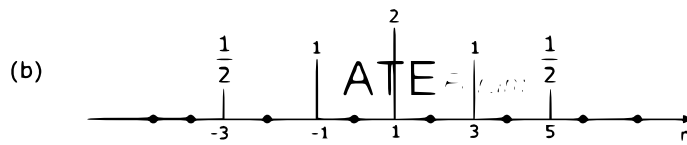
$$y(n) = \begin{cases} x(\frac{n}{2} - 1), & \text{for } n \text{ even} \\ 0, & \text{odd} \end{cases}$$

will be



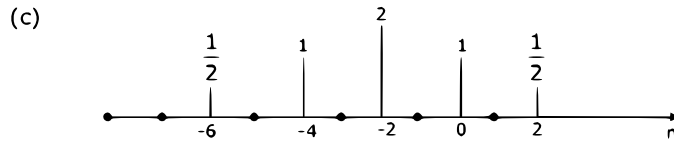
(A)

$$\delta(t) = \begin{cases} 1, & t=0 \\ 0, & \text{otherwise} \end{cases}.$$



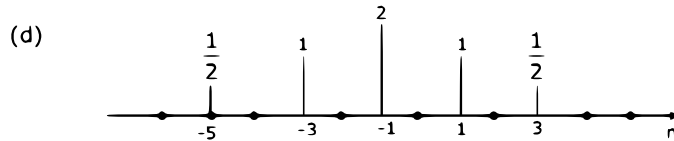
(B)

$$\delta(t) = \begin{cases} \infty, & t=0 \\ 0, & \text{otherwise} \end{cases}.$$



(C)

$$\delta(t) = \begin{cases} 1, & t=0 \\ 0, & \text{otherwise} \end{cases}.$$



and  $\int_{-\infty}^{+\infty} \delta(t) dt$

(B) The Fourier transform of  $y(2n)$  will be

(D)

(A)  $e^{-2j\omega} [\cos 4\omega + 2\cos 2\omega + 2]$

$$\delta(t) = \begin{cases} \infty, & t=0 \\ 0, & \text{otherwise} \end{cases}.$$

and  $\int_{-\infty}^{+\infty} \delta(t) dt$

(B)  $[\cos 2\omega + 2\cos \omega + 2]$

(C)  $e^{-j\omega} [\cos 2\omega + 2\cos \omega + 2]$

(D)  $e^{j\omega} [\cos 2\omega + 2\cos \omega + 2]$

46) Let  $x(t) \leftrightarrow X(j\omega)$  be Fourier Transform pair. The Fourier Transform of the signal  $x(5t - 3)$  in terms of  $X(j\omega)$  is given as

(A)  $\frac{1}{5} e^{\frac{-j3\omega}{5}} X\left(\frac{j\omega}{5}\right)$

(B)  $\frac{1}{5} e^{\frac{j3\omega}{5}} X\left(\frac{j\omega}{5}\right)$

(C)  $\frac{1}{5} e^{-j3\omega} X\left(\frac{j\omega}{5}\right)$

(D)  $\frac{1}{5} e^{j3\omega} X\left(\frac{j\omega}{5}\right)$

47) The dirac delta function  $\delta(t)$  is defined as

48) A signal  $m(t)$  with bandwidth 500 Hz is first multiplied by a signal  $g(t)$  where  $g(t) = \sum_{k=-\infty}^{\infty} (-1)^k \delta(t - 0.5 \times 10^{-4} k)$ . The resulting signal is then passed through an ideal lowpass filter with bandwidth 1 kHz. The output of the lowpass filter would be:

(A)  $\delta(t)$

(C) 0

(B)  $m(t)$

(D)  $m(t)\delta(t)$

49) The minimum sampling frequency (in samples/sec) required to reconstruct the following signal from its samples without distortion.

$$x(t) = 5\left(\frac{\sin 2\pi 1000t}{\pi t}\right)^3 + 7\left(\frac{\sin 2\pi 1000t}{\pi t}\right)^2$$

(A)  $2 \times 10^3$

(C)  $6 \times 10^3$

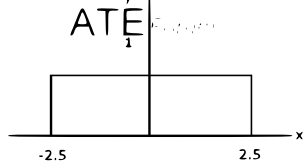
(B)  $4 \times 10^3$

(D)  $8 \times 10^3$

50) A uniformly distributed random variable  $x$  with probability density function  $f_X(x) = \frac{1}{10}(u(x +$

$$5) - u(x - 5))$$

Where  $u(\cdot)$  is the unit step function is passed through a transformation given in the figure below. The probability density function of the transformed random variable  $Y$  would be



(A)  $f_Y(y) = \frac{1}{5}(u(y + 2.5) - u(y - 2.5))$

(B)  $f_Y(y) = \frac{1}{2}(\delta(y) - \delta(y - 1))$

(C)  $f_Y(y) = \frac{1}{4}(\delta(y + 2.5) - \delta(y - 2.5)) + \frac{1}{2}\delta(y)$

(D)  $f_Y(y) = \frac{1}{4}(\delta(y + 2.5) - \delta(y - 2.5)) + \frac{1}{10}(u(y + 2.5) - u(y - 2.5))$

51) A system with input  $x[n]$  and the output  $y[n]$  is given as  $y[n] = (\sin \frac{5}{6}\pi n)x[n]$ . The system is

(A) Linear, stable and invertible

(B) non-linear, stable and non-invertible

(C) linear, stable and non-invertible

(D) linear, unstable and invertible

52) The 3-dB bandwidth of the low-pass signal  $e^{-t}u(t)$ , where  $u(t)$  is the unit step function, is given by

(A)  $\frac{1}{2\pi}$  Hz (C)  $\infty$

(B)  $\frac{1}{2\pi}\sqrt{\sqrt{2}-1}$  Hz (D) 1 Hz

53) The unit-step response of a system starting from rest is given by

$$c(t) = 1 - e^{-2t} \text{ for } t \geq 0$$

The transfer function of the system is:

(A)  $\frac{1}{1+2s}$  (C)  $\frac{1}{2+s}$

(B)  $\frac{2}{2+s}$  (D)  $\frac{2s}{1+2s}$

54) A Hilbert transformer is a

(A) non-linear system

(B) non-causal system

(C) time-varying system

(D) low-pass system

55) The frequency response of linear, time-invariant system is given by  $H(f) = \frac{5}{1+j10\pi f}$ . The step response of the system is

(A)  $5(1 - e^{-5t})u(t)$

(B)  $5(1 - e^{-\frac{t}{5}})u(t)$

(C)  $\frac{1}{5}(1 - e^{-5t})u(t)$

(D)  $\frac{1}{5}(1 - e^{-\frac{t}{5}})u(t)$

56) A 5-point sequence  $x[n]$  is given as

$x[-3] = 1, x[-2] = 1, x[-1] = 0, x[0] = 5, x[1] = 1$ . Let  $X(e^{j\omega})$  denote the discrete-time Fourier transform of  $x[n]$ . The value of  $\int_{-\pi}^{\pi} X(e^{j\omega})d\omega$  is :



- (A) 5      (B)  $10\pi$     (C)  $16\pi$     (D)  $5 + j10\pi$

57) The  $z$ -transform  $X[z]$  of a sequence  $x[n]$  is given by  $X[z] = \frac{0.5}{1 - 2z^{-1}}$ . It is given that the region of convergence of  $X[z]$  includes the unit circle. The value of  $x[0]$  is:

- (A) -0.5    (B) 0      (C) 0.25    (D) 0.5

58) The input and output of a continuous time systems are respectively denoted by  $x(t)$  and  $y(t)$ . Which of the following descriptions corresponds to a causal system?

(A)  $y(t) = x(t - 2) + x(t + 4)$

(B)  $y(t) = (t - 4)x(t + 1)$

(C)  $y(t) = (t + 4)x(t - 1)$

(D)  $y(t) = (t + 5)x(t + 5)$

59) The impulse response  $h(t)$  of a linear time-invariant continuous time system is described by  $h(t) = e^{\alpha t}u(t) + e^{\beta t}u(-t)$ , where  $u(t)$  denotes the unit step function, and  $\alpha$  and  $\beta$  are real constants. This system is stable if

(A)  $\alpha$  is positive and  $\beta$  is positive

(B)  $\alpha$  is negative and  $\beta$  is negative

(C)  $\alpha$  is positive and  $\beta$  is negative

(D)  $\alpha$  is negative and  $\beta$  is positive

60) A linear, time-invariant, causal continuous time system has a rational transfer function with simple poles at  $s = -2$  and  $s = -4$ , and one simple zero at  $s = -1$ . A unit step  $u(t)$  is applied at the input of the system. At steady state, the output

has constant value of 1. The impulse response of this system is

(A)  $[e^{-2t} + e^{-4t}]u(t)$

(B)  $[-4e^{-2t} + 12e^{-4t} - e^{-t}]u(t)$

(C)  $[-4e^{-2t} + 12e^{-4t}]u(t)$

(D)  $[-0.5e^{-2t} + 1.5e^{-4t}]u(t)$

61) The signal  $x(t)$  is described by

$$x(t) = \begin{cases} 1, & \text{for } -1 \leq t \leq 1 \\ 0, & \text{otherwise} \end{cases}$$

(A)  $\pi, 2\pi$

(C)  $0, \pi$

(B)  $0.5\pi, 1.5\pi$

(D)  $2\pi, 2.5\pi$

62) A discrete time linear shift-invariant system has an impulse response  $h[n]$  with  $h[0] = 1, h[1] = -1, h[2] = -2$  and zero otherwise. The system is given an input sequence  $x[n]$  with  $x[0] = x[2] = 1$ , and zero otherwise. The number of nonzero samples in the output sequence  $y[n]$ , and the value of  $y[2]$  are, respectively

(A) 5, 2

(C) 6, 1

(B) 6, 2

(D) 5, 3

63)  $\{x(n)\}$  is real-valued periodic sequence with a period  $N$ .  $x(n)$  and  $X(k)$  form N-point Discrete Fourier Transform (DFT) pairs. The DFT  $Y(k)$  of the sequence  $y(n) = \frac{1}{N} \sum_{r=0}^{N-1} x(r)x(n+r)$

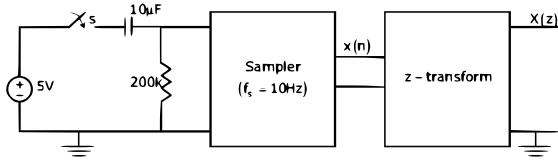
(A)  $|X(k)|^2$

(B)  $\frac{1}{N} \sum_{r=0}^{N-1} X(r) * X(k+r)$

(C)  $\frac{1}{N} \sum_{r=0}^{N-1} X(r)X(k+r)$

(D) 0

In the following network, the switch is closed at  $t=0^-$  and the sampling starts from  $t=0$ . The sampling frequency is 10Hz.



64) The samples  $x(n)$  at  $n=0,1,2,\dots$  given by

(A)  $5(1 - e^{-0.05n})$

(B)  $5e^{-0.05n}$

(C)  $5(1 - e^{-5n})$

(D)  $5e^{-5n}$

65) The expression and the region of convergence of the z-transform of the sampled signal are

(A)  $\frac{5z}{z - e^{-5}}, |z| < e^{-5}$

(B)  $\frac{5z}{z - e^{-0.05}}, |z| < e^{-0.05}$

(C)  $\frac{5z}{z - e^{-5}}, |z| > e^{-0.05}$

(D)  $\frac{5z}{z - e^{-5}}, |z| > e^{-5}$

66) A function is given by  $f(t) = \sin^2 t + \cos 2t$ . Which of the following is true ?

(A)  $f$  has frequency components at 0 and  $\frac{1}{2\pi}$  Hz

(B)  $f$  has frequency components at 0 and  $\frac{1}{\pi}$  Hz

(C)  $f$  has frequency components at  $\frac{1}{2\pi}$  and  $\frac{1}{\pi}$  Hz

(D)  $f$  has frequency components at 0,  $\frac{1}{2\pi}$  and  $\frac{1}{\pi}$  Hz

67) The ROC of Z-transform of the discrete time sequence  $x(n) = (\frac{1}{3})^n u(n) - (\frac{1}{2})^n u(-n-1)$  is

(A)  $\frac{1}{3} < |z| < \frac{1}{2}$  (C)  $|z| < \frac{1}{3}$

(B)  $|z| > \frac{1}{2}$  (D)  $2 < |z| < 3$

68) A system with transfer function  $H(z)$  has impulse response  $h(x)$  defined as  $h(2)=1, h(3)=-1$  and  $h(k)=0$  otherwise. Consider the following statements.

S1:  $H(z)$  is a low pass filter

S2:  $H(z)$  is a FIR filter

which of the following is correct ?

(A) Only S2 is true

(B) Both S1 and S2 are false.

(C) Both S1 and S2 are true, and S2 is a reason for S1

(D) Both S1 and S2 are true, but S2 is not a reason for S1

69) The Fourier series of a real periodic function has only

(P) Cosine terms if it is even

(P) Sine terms if it is even

(P) Cosine terms if it is odd

(P) Sine terms if it is odd.

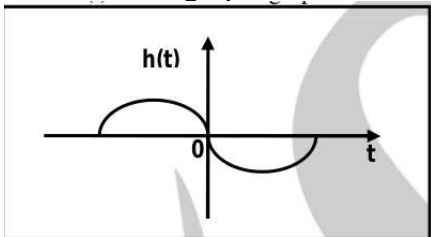
Which of the above statements are correct ?

(A) P AND S (C) Q AND S

(B) P AND R (D) Q AND R

70) Consider a system whose input  $x$  and output  $y$  are related by the equation.

$y(t) = \int_{-\infty}^{+\infty} x(t - \tau)h(2\tau)d\tau$  Where  $h(t)$  is shown in the graph.



Which of the following four properties are possessed by the system ?

**BIBO:**Bounded Input gives Bounded Output

**Causal:**The system is Causal.

**LP:**The system is Lowpass.

**LTI:**The system is Linear and Time-Invariant.

(A) Causal, LP (C) BIBO, Causal, LTI

(B) BIBO, LTI (D) LP,LTI

71) The 4-point Discrete Fourier Transform (DFT) of a discrete time sequence 1,0,2,3 is

(A)  $[0, -2 + 2j, 2, -2 - 2j]$

(B)  $[2, 2 + 2j, 6, -2 - 2j]$

(C)  $[6, 1 - 3j, 2, 1 + 3j]$

(D)  $[6, -1 + 3j, 0, -1 - 3j]$

72) An LTI system having transfer function  $\frac{s^2+1}{s^2+2s+1}$  and input  $x(t) = \sin x(t)$  is in steady state. The output is sampled at a rate of  $\omega_w$  rad/s to obtain the final output  $\{y(k)\}$ . Which

of the following is true ?

(A)  $y(x)$  is zero for all sampling frequencies  $\omega_s$

(B)  $y(x)$  is nonzero for all sampling frequencies  $\omega_s$

(C)  $y(x)$  is nonzero for all sampling frequencies  $\omega_s > 2$ , but zero for all  $\omega_s < 2$

(D)  $y(x)$  is zero for all sampling frequencies  $\omega_s > 2$ , but nonzero for all  $\omega_s < 2$

73) The unit step response of an under-damped second order system has steady state value of -2. Which one of the following transfer functions has these properties ?

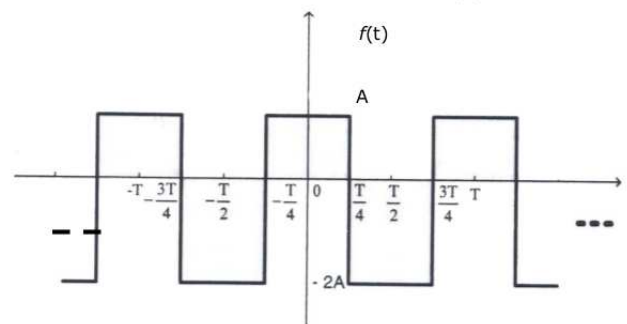
(A)  $\frac{-2.24}{s^2 + 2.59s + 1.12}$

(B)  $\frac{-3.82}{s^2 + 1.91s + 1.91}$

(C)  $\frac{-2.24}{s^2 - 2.59s + 1.12}$

(D)  $\frac{-2.24}{s^2 + 2.59s + 1.12}$

74) The trigonometric Fourier series for the waveform  $f(t)$  shown below contains



(A) only cosine terms and zero value for the dc component

(B) only cosine terms and a positive value for the dc component

(C) only cosine terms and a negative value for the dc component

(D) only sine terms and a negative for the dc component

75) Consider the z-transform  $X(z) = 5z^2 + 4z^{-1} + 3$ ;  $0 < |z| < \infty$ . The inverse z-transform  $x[n]$

(A)  $5\delta[n+2] + 3\delta[n] + 4\delta[n-1]$

(B)  $5\delta[n-2] + 3\delta[n] + 4\delta[n+1]$

(C)  $5u[n+2] + 3u[n] + 4u[n-1]$

(D)  $5u[n-2] + 3u[n] + 4u[n+1]$

76) Two discrete time systems with impulse responses  $h_1[n] = \delta[n-1]$  and  $h_2[n] = \delta[n-2]$  are cascade. The overall impulse response of the cascaded system is

(A)  $\delta[n-1] + \delta[n-2]$

(B)  $\delta[n-4]$  (C)  $\delta[n-3]$

77) For an N-point FFT algorithm with  $N = 2^m$  which one of the following statement is TRUE?

(A) It is not possible to construct a signal flow graph with both input and output in normal order.

(B) The number of butterflies in the  $m^{th}$  stage is N/m

(C) In-place computation requires storage of only 2N node data

(D) Computation of a butterfly requires only

one complex multiplication

78) A system with transfer function  $\frac{Y(s)}{X(s)} = \frac{s}{s+p}$  has an output  $y(t) = \cos(2t - \frac{\pi}{3})$  for the input signal  $x(t) = p\cos(2t - \frac{\pi}{2})$ . Then, the system parameter 'p' is  
(A)  $\sqrt{3}$

(B)  $\frac{2}{\sqrt{3}}$

(C) 1

(D)  $\frac{\sqrt{3}}{2}$

79) A continuous time LTI system is described by  $\frac{d^2y(t)}{dt^2} + 4\frac{dy(t)}{dt} + 3y(t) = 2\frac{dx(t)}{dt} + 4x(t)$   
(A)  $(e^t - e^{3t})u(t)$

(B)  $(e^{-t} - e^{-3t})u(t)$

(C)  $(e^{-t} + e^{-3t})u(t)$

(D)  $(e^t + e^{3t})u(t)$

80) The transfer function of a discrete time LTI system is given by  $H(z) = \frac{2 - \frac{3}{4}z^{-1}}{1 - \frac{3}{4}z^{-1} + \frac{1}{8}z^{-2}}$

Consider the following statements:

**S1:** The system is stable and causal for ROC:  $|z| > \frac{1}{2}$

**S2:** The system is stable but not causal for ROC:  $|z| < \frac{1}{4}$

**S3:** The system is neither stable nor causal for ROC:  $\frac{1}{4} < |z| < \frac{1}{2}$

Which one of the following statements is valid?

(A) Both S1 and S2 are true.

(B) Both S2 and S3 are true.

(C) sine terms

(C) Both S1 and S3 are true.

(D) odd harmonic terms

(D) S1, S2 and S3 are all true.

81) The Nyquist sampling rate for the signal  $s(t) = \frac{\sin(500\pi t)}{\pi t} \times \frac{\sin(700\pi t)}{\pi t}$  is given by

(A) 400 Hz

(C) 1200 Hz

(B) 600 Hz

(D) 1400 Hz

82) A system is defined by its impulse response  $h(n) = 2^n u(n-2)$ . The system is

(A) stable and causal

(B) causal but not stable

(C) stable but not causal

(D) unstable and non-causal

83) If the unit step response of a network is  $1 - e^{-\alpha t}$ , then its unit impulse response

(A)  $\alpha e^{-\alpha t}$

(B)  $\alpha^{-1} e^{-\alpha t}$

(C)  $(1 - \alpha^{-1}) e^{-\alpha t}$

(D)  $(1 - \alpha) e^{-\alpha t}$

84) The trigonometric Fourier series of an even function does not have the

(A) dc term

(B) cosine terms

85) An input  $x(t) = e^{-2t}u(t) + \delta(t-6)$  is applied to an LTI system with impulse response  $h(t) = u(t)$ . The output is

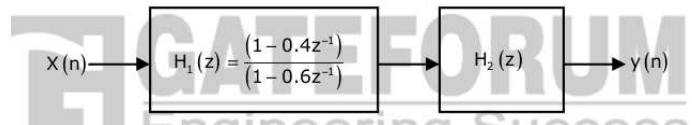
(A)  $[1 - e^{-2t}]u(t) + u(t+6)$

(B)  $[1 - e^{-2t}]u(t) + u(t-6)$

(C)  $0.5[1 - e^{-2t}]u(t) + u(t+6)$

(D)  $0.5[1 - e^{-2t}]u(t) + u(t-6)$

86) Two systems  $H_1(z)$  and  $H_2(z)$  are connected in cascade as shown below. The overall output  $y(n)$  is the same as the input  $x(n)$  with a one unit delay. The transfer function of the second system  $H_2(z)$  is



(A)  $\frac{(1-0.6z^{-1})}{z^{-1}(1-0.4z^{-1})}$

(C)  $\frac{z^{-1}(1-0.4z^{-1})}{(1-0.6z^{-1})}$

(B)  $\frac{z^{-1}(1-0.6z^{-1})}{(1-0.4z^{-1})}$

(D)  $\frac{(1-0.4z^{-1})}{z^{-1}(1-0.6z^{-1})}$

87) The first 6 points of the 8-point DFT of a real valued sequence are  $5, 1-j3, 0, 3-j4, 0$  and  $3+j4$ . The last two points of the DFT are respectively

(A)  $0, 1-j3$

(C)  $1+j3, 5$

(B)  $0, 1+j3$

(D)  $1-j3, 5$

88) The systems with impulse responses  $h_1(t)$  and  $h_2(t)$  are connected in cascade. Then the overall impulse response of the cascaded system is given by

(A) product of  $h_1(t)$  and  $h_2(t)$

(B) sum of  $h_1(t)$  and  $h_2(t)$ (A)  $0.5 - j0.25$ (C)  $\frac{1}{0.5-j0.25}$ (C) convolution of  $h_1(t)$  and  $h_2(t)$ (B)  $\frac{1}{0.5+j0.25}$ (D)  $2 + j4$ (D) Substraction of  $h_2(t)$  and  $h_1(t)$ 

89) A band-limited signal with a maximum frequency of 5 kHz is to be sampled. According to the sampling theorem, the sampling frequency which is not valid is

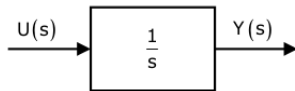
(A) 5 kHz

(C) 15 kHz

(B) 12 kHz

(D) 20 kHz

90) Assuming zero initial condition, the response  $y(t)$  of the system given below to a unit step input  $u(t)$  is

(A)  $u(t)$ (C)  $\frac{t^2}{2}u(t)$ (B)  $tu(t)$ (D)  $e^{-t}u(t)$ 

91) A system is described by the differential equation  $\frac{d^2y}{dt^2} + 5\frac{dy}{dt} + 6y(t) = x(t)$ . Let  $x(t)$  be a rectangular pulse given by

$$x(t) = \begin{cases} 1, & 0 < t < 2 \\ 0, & \text{otherwise} \end{cases}$$

Assuming that  $y(0) = 0$  and  $\frac{dy}{dt} = 0$  at  $t=0$ , the Laplace transform of  $y(t)$  is

(A)  $\frac{e^{-2s}}{s(s+2)(s+3)}$ (C)  $\frac{e^{-2s}}{(s+2)(s+3)}$ (B)  $\frac{1-e^{-2s}}{s(s+2)(s+3)}$ (D)  $\frac{1-e^{-2s}}{(s+2)(s+3)}$ 

92) Let  $x[n]=x[-n]$ . Let  $X(z)$  be the z-transform of  $x[n]$ . If  $0.5+j0.25$  is a zero of  $X(z)$  then one of the following must be a zero of  $X(z)$ .

93) An FIR system is described by the system function  $H(z) = 1 + \frac{7}{2}z^{-1} + \frac{3}{2z^{-2}}$ . The system is

(A) maximum phase (C) mixed phase

(B) minimum phase (D) zero phase

94) The input-output relationship of a causal stable LTI system is given as  $y[n] = \alpha y[n-1] + \beta x[n]$ . If the impulse response  $h[n]$  of this system satisfies the condition  $\sum_{n=0}^{\infty} h[n] = 2$ , the relationship between  $\alpha$  and  $\beta$  is

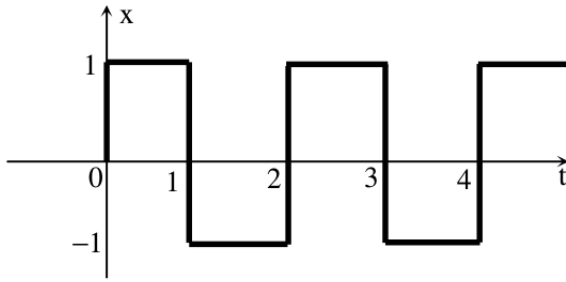
(A)  $\alpha = 1 - \frac{\beta}{2}$ (C)  $\alpha = 2\beta$ (B)  $\alpha = 1 + \frac{\beta}{2}$ (D)  $\alpha = -2\beta$ 

95) The impulse response of a system is  $h(t) = tu(t)$ . For an input  $u(t-1)$ , the output is

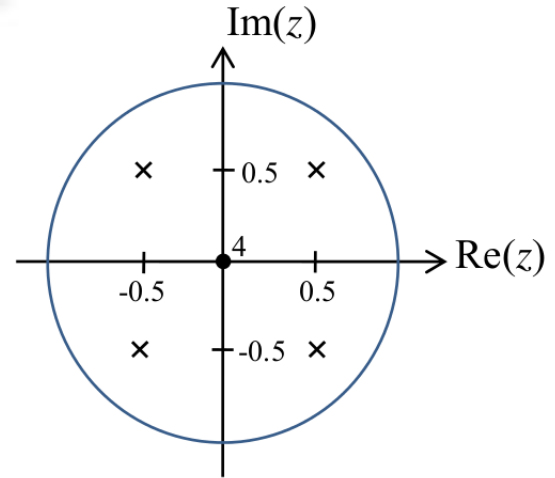
(A)  $\frac{t^2}{2}u(t)$ (B)  $\frac{t \times (t-1)}{2}u(t-1)$ (C)  $\frac{(t-1)^2}{2}u(t-1)$ (D)  $\frac{t^2-1}{2}u(t-1)$ 

96) The value of the integral  $\int_{-\infty}^{+\infty} \text{sinc}^2(5t)dt$  is

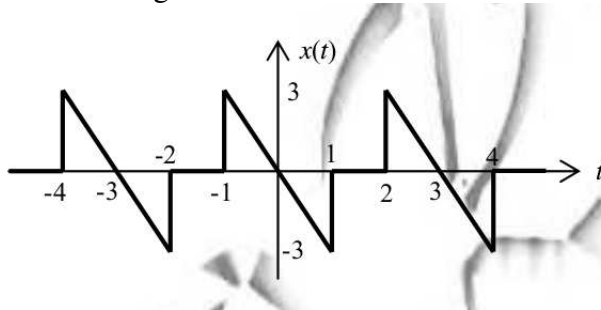
97) Consider the periodic square wave in the figure shown.



The ratio of the power in the 7<sup>th</sup> harmonic to the power in the 5<sup>th</sup> harmonic for this waveform is closest in value to \_\_\_\_\_



- 98) The waveform of a periodic signal  $x(t)$  is shown in the figure.



A signal  $g(t)$  is defined by  $g(t) = x(\frac{t-1}{2})$ . The average power of  $g(t)$  is \_\_\_\_\_

- (A)  $h[n]$  is real for all  $n$   
 (B)  $h[n]$  is purely imaginary for all  $n$   
 (C)  $h[n]$  is real for only even  $n$   
 (D)  $h[n]$  is purely imaginary for only odd  $n$

- 99) Consider the signal  $s(t) = m(t)\cos(2\pi f_c t) + \hat{m}(t)\sin(2\pi f_c t)$  where  $\hat{m}(t)$  denotes the Hilbert transform of  $m(t)$  and the bandwidth of  $m(t)$  is very small compared to  $f_c$ . The signal  $s(t)$  is a

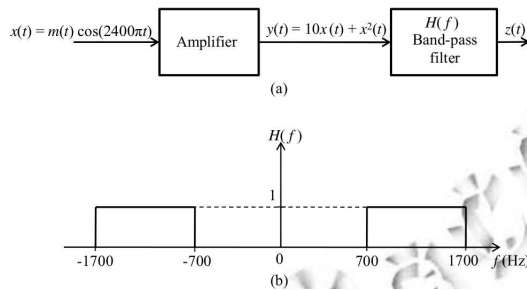
- (A) high-pass signal  
 (B) low-pass signal  
 (C) band-pass signal  
 (D) double sideband suppressed carrier signal

- 100) The pole-zero diagram of causal and stable discrete-time system is shown in figure. The zero at the origin has multiplicity 4. The impulse response of the system is  $h[n]$ . If  $h[0] = 1$ , we can conclude

- 101) A continuous-time sinusoid of frequency 33 Hz is multiplied with a periodic Dirac impulse train of frequency 46 Hz. The resulting signal is passed through an ideal analog low-pass filter with a cutoff frequency of 23 Hz. The fundamental frequency (in Hz) of the output is \_\_\_\_\_

- 102) Consider the signal  $x[n] = 6\delta[n+2] + 3\delta[n+1] + 8\delta[n] + 7\delta[n-1] + 4\delta[n-2]$ . If  $X(e^{j\omega})$  is the discrete-time Fourier transform of  $x[n]$ . Then  $\frac{1}{\pi} \int_{-\pi}^{\pi} X(e^{j\omega}) \sin^2(2\omega) d\omega$  is equal to \_\_\_\_\_

- 103) In the system shown in Figure(a),  $m(t)$  is a low-pass signal with bandwidth  $W$  Hz. The frequency response of the band-pass filter  $H(f)$  is shown in Figure(b). If it is described that the output signal  $z(t) = 10x(t)$ , the maximum value of  $W$  (in Hz) should be strictly less than \_\_\_\_\_



Data for **Q.108-109** are given below.

The impulse response  $h(t)$  of a linear time invariant continuous time system is given by  $h(t) = e^{-2t}u(t)$ , where  $u(t)$  denotes the unit step function.

- 104) The frequency response  $H(\omega)$  of this system in terms of angular frequency  $\omega$  is give by  $H(\omega)$

(A)  $\frac{1}{1 + j2\omega}$  (C)  $\frac{1}{2 + j\omega}$

(B)  $\frac{\sin(\omega)}{\omega}$  (D)  $\frac{j\omega}{2 + j\omega}$

- 105) The output of this system to the sinusoidal input  $x(t) = 2\cos(2t) \forall t$ , is

(A) 0

(B)  $2^{-0.25}\cos(2t - 0.125\pi)$

(C)  $2^{-0.5}\cos(2t - 0.125\pi)$ .

(D)  $2^{-0.5}\cos(2t - 0.25\pi)$

- 106) A system described by a linear, constant coefficient, ordinary, first order differential equation has an exact solution given by  $y(t)$  for  $t > 0$ , when the forcing function is  $x(t)$  and the initial condition is  $y(0)$ . If one wishes to modify the system so that the solution becomes  $-2y(t)$  for  $t > 0$ , we need to

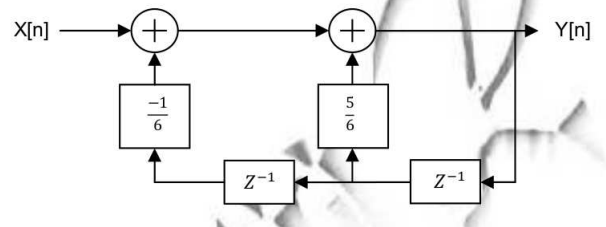
(A) change the initial condition to  $-y(0)$  and the forcing function to  $2x(t)$

(B) change the initial condition to  $2y(0)$  and the forcing function to  $-x(t)$

(C) change the initial condition to  $j\sqrt{2y(0)}$  and the forcing function to  $j\sqrt{x(t)}$

(D) change the initial condition to  $-2y(0)$  and the forcing function to  $-2x(t)$

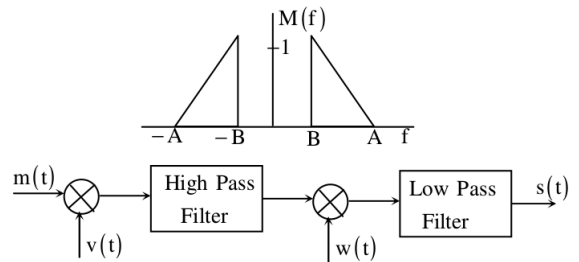
- 107) For the discrete-time shown in the figure, the poles of the system transfer function are located at



(A) 2, 3 (C)  $\frac{1}{2}, \frac{1}{3}$

(B)  $\frac{1}{2}, 3$  (D)  $2, \frac{1}{3}$

- 108) In the figure,  $M(f)$  is the Fourier transform of the message signal,  $m(t)$  where  $A=100$  Hz and  $B=40$  Hz. Given  $v(t) = \cos(2\pi f_c t)$  and  $w(t) = \cos(2\pi(f_c + A))$ , where  $f_c > A$ . The cutoff frequencies of the both filters are \_\_\_\_\_  $f_c$



- 109) The result of the convolution  $x(-t) * \delta(-t - t_0)$  is

(A)  $x(t + t_0)$  (C)  $x(-t + t_0)$

(B)  $x(t - t_0)$  (D)  $x(-t - t_0)$