Matrix theory Assignment 1

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Abstract—This document contains the solution to cal- So, we get $\cos\theta$ to be, culate the angle between 2 vectors $\bar{\mathbf{a}}$ and $\bar{\mathbf{b}}$.

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1 Problem

Find the angle between 2 vectors $\mathbf{a} = \begin{pmatrix} 1 \\ 1 \\ -1 \end{pmatrix}$ and Therefore, the angle between the 2 vectors is 109.47° .

$$\mathbf{b} = \begin{pmatrix} 1 \\ -1 \\ 1 \end{pmatrix}$$

2 Solution

The angle between 2 vectors is given by

$$cos\theta = \frac{\mathbf{a}^T \mathbf{b}}{\|\mathbf{a}\| * \|\mathbf{b}\|}$$

Computing the numerator

$$\mathbf{a}^{T}\mathbf{b} = \begin{pmatrix} 1 & 1 & -1 \end{pmatrix} * \begin{pmatrix} 1 \\ -1 \\ 1 \end{pmatrix}$$
$$\implies \mathbf{a}^{T}\mathbf{b} = -1$$

Computing the denominator

$$\|\mathbf{a}\| * \|\mathbf{b}\| = \sqrt{(1)^2 + (1)^2 + (-1)^2} * \sqrt{(1)^2 + (-1)^2 + (1)^2}$$

 $\implies \|\mathbf{a}\| * \|\mathbf{b}\| = \sqrt{3} * \sqrt{3}$
 $\implies \|\mathbf{a}\| * \|\mathbf{b}\| = 3$

$$\cos\theta = \frac{-1}{3}$$

Therefore,

$$\theta = \cos^{-1}\left(\frac{-1}{3}\right)$$

$$\implies \theta = 1.9106^{c}$$

$$\implies \theta = 109.47^{\circ}$$