

$$1. \quad H_0 : P = 0.7$$

$$H_1 : P \neq 0.7$$

Level of Significance  $= \alpha = 0.10$

Test Statistic : Binomial Variable  $X$  with  $P = 0.7$  and  $n$

$$X = 8 \text{ and } np_0 = 15 \times 0.7 = 10.5$$

$$\therefore P = 2P(X \leq 8 \text{ when } p = 0.7)$$

$$= 2 \sum_{x=0}^8 b(x; 15, 0.7)$$

$$= 2 \times 0.1311 \text{ (From Binomial Prob. Table)}$$

$$= 0.2622$$

$$\therefore P > 0.10 \text{ i.e. } P > \alpha$$

$\therefore$  Don't reject to conclude that there is insufficient evidence to doubt the builder's claim

$$2. \quad H_0 : P = 0.6$$

$$H_1 : P > 0.6$$

Level of Significance  $= \alpha = 0.05$

$$\text{Given : } x = 70, n = 100, P = 0.6$$

$$Z = \frac{x - np_0}{\sqrt{np_0q_0}}$$

$$Z = 2.04$$

$$P = P(Z > 2.04)$$

As,  $P < \alpha$ , reject  $H_0$  and conclude that new drug is superior.

3. Let  $P_1$  be the proportion of Mumbai voters and  $P_2$  be the proportion of surrounding area residents.

$$\hat{P}_1 = \frac{120}{200} = 0.6$$

$$\hat{P}_2 = \frac{240}{500} = 0.48$$

$$\alpha = 5\%$$

$$\hat{P}_p = \frac{120 + 240}{200 + 500} = 0.514$$

$\alpha_2$  Hypothesis

$$H_0: P_1 \leq P_2$$

$$H_1: P_1 > P_2$$

$$Z = \frac{\hat{P}_1 - \hat{P}_2}{\sqrt{\hat{P}_p \cdot (1 - \hat{P}_p) \left( \frac{1}{n_1} + \frac{1}{n_2} \right)}}$$

$$Z = \frac{0.6 - 0.48}{\sqrt{0.514 (1 - 0.514) \left( \frac{1}{200} + \frac{1}{500} \right)}}$$

$$Z = 2.869$$

$$P = P(Z > 2.869) = 0.0044$$



4. a Null Hypothesis  
 $H_0: p = 0.20$

Alternate Hypothesis  
 $H_1: p > 0.20$

The critical region is in right Tail

b Null Hypothesis  
 $H_0: \mu = 3$

Alternate Hypothesis  
 $H_1: \mu \neq 3$

The critical region is in both tails

c Null Hypothesis  
 $H_0: \mu = 500$

Alternative Hypothesis  
 $H_1: \mu > 500$

The critical region is in right tail

d Null Hypothesis  
 $H_0: \mu = 15$

Alternative Hypothesis  
 $H_1: \mu \neq 15$

The critical region is in both tails

5. Let  $\mu_1$  and  $\mu_2$  be the population mean 'robustness' of laptops supplied by company A and company B respectively

$$H_0: \mu_1 = \mu_2$$

$$H_1: \mu_1 \neq \mu_2$$

Significance level  $\alpha = 0.05$

$$\bar{X}_1 = \frac{1}{n_1} \sum_{i=1}^{n_1} x_{1i}$$

$$\bar{X}_1 = \frac{9.3 + 8.8 + 6.8 + 8.7 + 8.5 + 6.7 + 8.0 + 6.5 + 9.2 + 7.0}{10}$$

$$\bar{X}_1 = 7.95$$

$$\bar{X}_2 = \frac{1}{n_2} \sum_{i=1}^{n_2} x_{2i}$$

$$\bar{X}_2 = \frac{11.0 + 9.8 + 9.9 + 10.2 + 10.1 + 9.9 + 11.0 + 11.1 + 10.2 + 9.6}{10}$$

$$\bar{X}_2 = 10.26$$

$$S_1^2 = \frac{1}{n_1 - 1} \left[ \sum_{i=1}^{n_1} x_{1i}^2 - n_1 \bar{X}_1^2 \right]$$

$$S_1^2 = 1.207$$

$$\text{Similarly } S_2^2 = 0.325$$

Since Sample Variances are quite different, we cannot assume that population variances are equal, so we will use the unpooled