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Surface effects and CO/CO₂ influence in the H₂ permeation through a Pd–Ag membrane: A comprehensive model

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ABSTRACT

The permeability of a 0.175 mm thick Pd–Ag tubular membrane to pure H₂ and binary mixtures of H₂/CO or H₂/CO₂ was studied. The tests were performed in a wide range of temperature (523–723 K) and pressure (200–800 kPa).

Pure H₂-permeation through a dense metal membrane is described by the Sieverts' law. However, it was already found that the H₂ permeation does not follow the Sieverts' law when other components are present in the feed and namely CO or CO₂. In this work, it is proposed a new permeation model based on the Sieverts' law considering: i) the mass transfer resistance due to the surface effects and ii) the barrier effect due to the presence of either CO or CO₂. The model was successfully validated against experimental data of hydrogen permeation for binary (H₂/CO and H₂/CO₂) experiments for every working temperature and pressure.

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Introduction

The exploitation of fossil fuels is not sustainable for a long time because of their impact on the environment. In fact, the combustion of these fuels generates greenhouse gases that contribute to global warming, caused by their accumulation in

the atmosphere, for example CO₂ [1]. In this context the need comes up for a global action to decrease the pollution levels and implement environmentally friendly energy technologies (e.g. solar, wind, geothermal, etc.). There are some types of applications (e.g. propulsion of cars, buses, laptop batteries, cell phones, etc.) where it is necessary to use an intermediate energy carrier. It is in this sense that hydrogen is so attractive

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[2]. The use of hydrogen as a clean energy vector is every day more recurrent: combustion of hydrogen results in water and, particularly, its environmental impact is very limited when produced from renewables [3–5]. Currently, the principal source of hydrogen is the reforming of hydrocarbons, mainly methane [6]. As a result of the methane steam reforming some compounds like CO, CO₂, H₂O, etc. are obtained together with H₂. In several uses, high purity hydrogen streams are important, for example for fuel cells or nuclear applications. In these cases is mandatory purifying and separating the hydrogen from the syngas stream. For this purpose, several technologies can be applied such as, cryogenic cooling, PSA and H₂-selective membranes [7].

Methods of separation/purification by H₂-selective membranes are increasingly attractive as compared to other technologies because of their modularity, low energy consumption, possibility for continuous and easy operation, and finally cost effectiveness [8]. Pd-based membranes are particularly interesting due to their high hydrogen permeance and good selectivity [9]. Pure palladium membranes are prone to suffer from the embrittlement phenomenon that can be significantly reduced by alloying Pd with other metals (Ag, Au, Cu, etc.). Self-supported Pd–Ag membranes consisting of dense tubes have been developed for separating ultra-pure hydrogen. Particularly, Pd–Ag thin wall permeator tubes produced via cold-rolling and diffusion welding of metal foils have been produced and characterized in long term permeation tests, demonstrating their complete hydrogen selectivity and durability [10–12]. These dense Pd–Ag tubes have been used in membrane reactors where several dehydrogenation reactions take place; ultra-pure hydrogen production as well as high hydrogen yields have been obtained [13,14].

In most cases, the H₂-permeation through a Pd-membrane is described by the Sieverts' law (Eq. (1)):

$$J_{H_2} = \frac{P_e}{d} (p_{H_2,up}^{0.5} - p_{H_2,down}^{0.5}) \quad (1)$$

where J_{H_2} is the H₂-flux through the membrane (mol s^{−1} m^{−2}), P_e is the permeability of the membrane (mol s^{−1} m^{−1} Pa^{−0.5}), d is the membrane thickness (m), $p_{H_2,up}$ is the upstream H₂-partial pressure (in the feed stream, Pa) and $p_{H_2,down}$ is the downstream H₂-partial pressure (in the permeate side, Pa). According to the Sieverts' law, the pressure dependence factor (n) of the hydrogen flux on the H₂-partial pressure has the value of 0.5.

However, there are several references in the literature about deviations from this law. Deviations from the ideal behavior predicted by the Sieverts' law are due to different factors: poisoning of the membrane surface, membrane defects, mass transfer resistance phenomena related to the surface effect, etc. [15–18].

In this work, a comprehensive approach derived from the Sieverts' law is proposed. This new model takes into account two of the main reasons for deviation of Sieverts' law: i) the barrier effect of CO or CO₂ on the surface of the membrane and ii) the mass transfer resistance due to hydrogen adsorption/desorption over the metal surface. Species such as CO and CO₂

cause the deactivation of the membrane because they can block the hydrogen adsorption sites. On the other hand, the mechanism of hydrogen transport through a dense membrane comprises several stages and, practically, it is controlled by the adsorption/desorption rates over the metal surface and by the diffusion through the metal lattice. Therefore, the effects of surface reactions should be considered in the hydrogen permeation models since they can significantly affect the hydrogen mass transfer resistance. The novel approach proposed in this work was validated by experimental data in a wide range of operating conditions.

Experimental

In order to characterize a tubular Pd/25%Ag-membrane several permeation tests were carried out. The permeation tests were conducted at ENEA Frascati laboratories using a dense Pd–Ag tubular membrane having the following dimensions: 10 mm of internal diameter, 0.175 mm (175 μm) of wall thickness and 125 mm of length. The membrane tube was joined at its ends to two stainless steel tubes in order to form the permeator tube shown in Fig. 1.

In all cases, for H₂-pure as for binary mixtures tests (H₂/CO and H₂/CO₂), the hydrogen flux permeating through the membrane has been measured in the pressure and temperature ranges of 200–800 kPa and 523–723 K, respectively. All experiments were carried out at a constant total feed flow rate (F_T) of 700 mL_N min^{−1} and the hydrogen permeated through the membrane was collected by a constant sweep gas stream of nitrogen (50 mL_N min^{−1}) sent in counter-current mode in the shell side (Fig. 2).

The permeator tube was wrapped by a Pt-wire electric resistance, which was used to heat the membrane until the working temperature; a thermocouple was located very near from the permeator tube external surface to measure the temperature. All this was assembled inside a Pyrex tube (in the shell) in a finger-like configuration accordingly to a well-established and proven membrane module design [19]. One end of the permeator tube is sealed while the other one allows the placing of a stainless steel channel which is responsible for supplying the feed gas mixture. More details about the module and the experimental set-up are given in Fig. 2. In order to thermally isolate the membrane module and keep constant the working temperature, the Pyrex shell was covered with a quartz wool blanket. The feed stream consisting of high purity gases enters into the permeator lumen side through a mass flow controller (MFC). The permeate stream flow rate consisting of ultra-pure hydrogen was measured by a mass flow meter (MFM). Pressure was measured at the inlet/outlet of the permeator lumen and at the shell outside (PI) by pressure gages. The lumen pressure was controlled through a throttle valve (TV).

Selectivity to hydrogen of the membrane has been verified by gas-chromatographic measurements of the permeate and its tightness checked by pressuring the membrane lumen with inert gas during the night.

For the binary mixtures, tests were performed by feeding the membrane with streams of different compositions of H₂/CO or H₂/CO₂, as shown in Table 1.

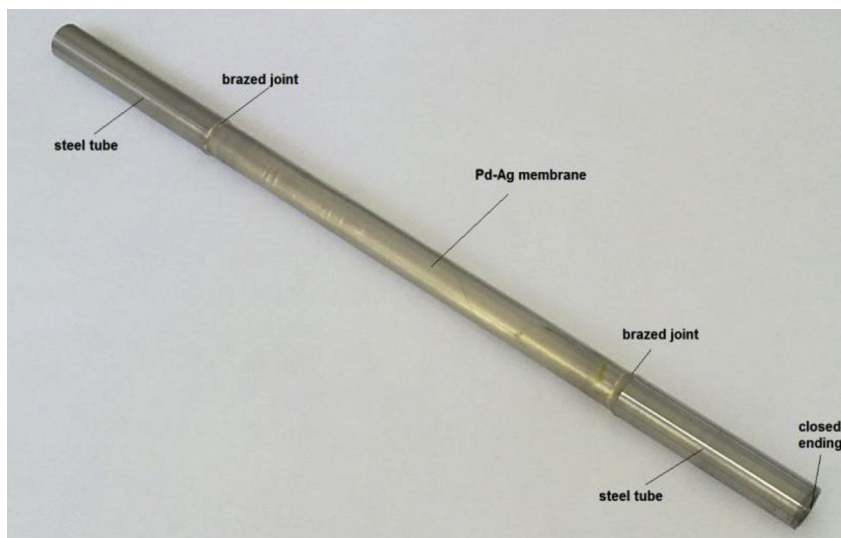


Fig. 1 – Pd–Ag permeator tube.

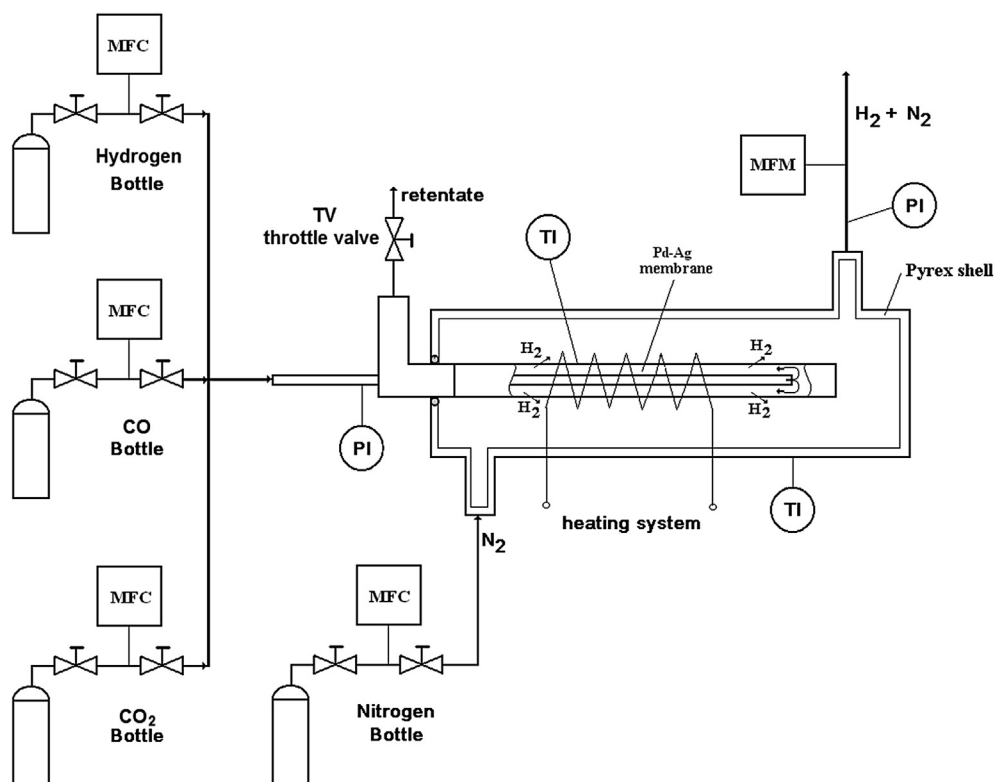


Fig. 2 – Scheme of the membrane module and of the experimental set-up.

Table 1 – Composition of the feed stream during the binary experiments^a.

Composition	CO (%)	CO ₂ (%)	H ₂ (%)
CO/H ₂	1.5–8.0	–	98.5–92.0
CO ₂ /H ₂	–	7.5–30.0	92.5–70.0

^a $F_T = 700 \text{ mL}_N \text{ min}^{-1}$, sweep gas ($50 \text{ mL}_N \text{ min}^{-1}$).

Results and discussion

Pure hydrogen permeation tests

Pure hydrogen tests were conducted to measure the hydrogen permeability under specific and controlled temperature and pressure conditions.

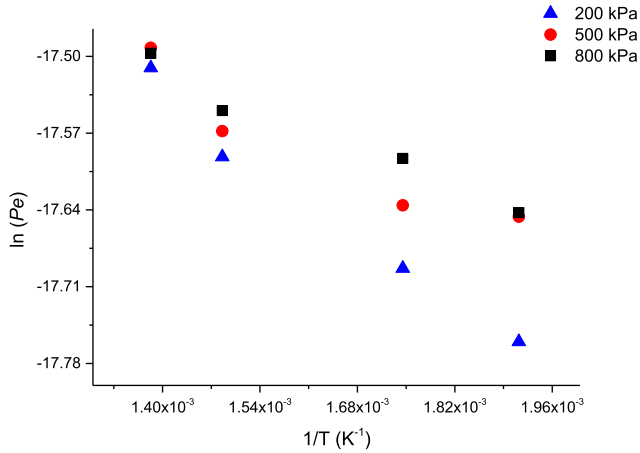


Fig. 3 – Arrhenius plot of the permeability obtained using the Sieverts' law (Eq. (1)) at different hydrogen feed pressures.

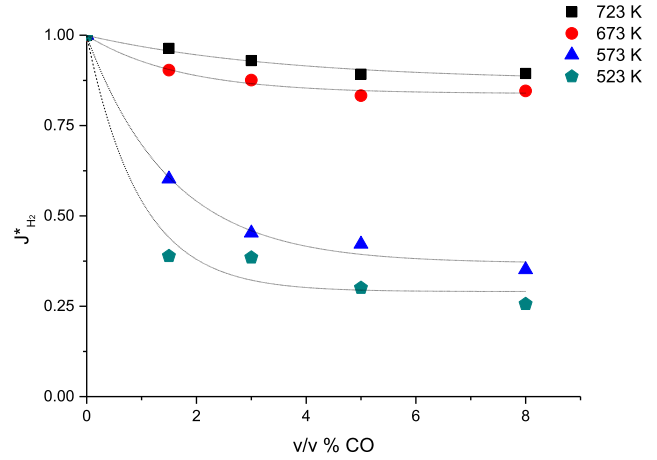


Fig. 4 – Normalized H₂-flux vs %CO in the feed stream. The fitted function (dashed lines) is based on the new model (Eq. (6)).

Table 2 – Values of mass transfer resistance (R_s) obtained from literature [20,22] and permeability (P_e) calculated in this work by Eqs. (2)–(4).

T (K)	R_s (mol ⁻¹ m ² s Pa)	P_e (mol m ⁻¹ s ⁻¹ Pa ^{-0.5})
723	1.10×10^4	1.88×10^{-8}
673	1.46×10^4	1.77×10^{-8}
573	3.00×10^4	1.66×10^{-8}
523	78.78×10^4	1.64×10^{-8}

Fig. 3 shows that the Arrhenius' plot of the H₂-permeability is represented by different curves for each feed pressure when applying the Sieverts' law model of Eq. (1).

Actually, from the Sieverts' law the permeability should be independent of the total pressure, thus demonstrating that such a model is not effective to describe the permeation phenomena in the experienced pressure range (200–800 kPa). This effect is more noticeable for lower temperatures; similar results have been reported elsewhere [20].

In order to more accurately calculate the permeability of the membrane, a modified model that introduces in the Sieverts' law the surface mass transfer resistance and the logarithmic mean driving force was considered (Eqs. (2)–(4)). The surface mass transfer resistance is due to the hydrogen adsorption/desorption reactions over the metal surfaces. Further, the hydrogen partial pressure in the permeate side is not constant along the axial coordinate because of the continuous removal of hydrogen and an appropriate expression of the driving force has to be used. By analogy of the mathematical equation used to describe the temperature gradient in a heat exchanger, it is possible to express the H₂-permeating driving force as a similar expression but, in terms of pressure gradient, that is as a log mean of the H₂-partial pressure difference [21].

$$J_{H_2} = \frac{P_e}{d} \Delta P_{ln} \quad (2)$$

where:

$$\Delta P_{ln} = \frac{\left[(p_{H_2, feed} - J_{H_2} R_s)^{0.5} - (p_{H_2, perm out} + J_{H_2} R_s)^{0.5} \right] - \left[(p_{H_2, ret} - J_{H_2} R_s)^{0.5} - (p_{H_2, perm in} + J_{H_2} R_s)^{0.5} \right]}{A} \quad (3)$$

Table 3 – - Calculated hydrogen permeability and comparison with literature.

P_{e0} (mol m ⁻¹ s ⁻¹ Pa ^{-0.5})	E_a (J mol ⁻¹)	P_{feed} (kPa)	T (K)	d (μm)	Ref.
2.06×10^{-8}	2.59×10^3	200–800	473–623	200	[20]
5.58×10^{-8}	6.30×10^3	1–100	50–500	198	[22]
7.73×10^{-8}	6.60×10^3	680–6800	300–500	125	[24]
3.85×10^{-8}	5.75×10^3	120–870	380–580	80	[25]
2.61×10^{-8}	2.09×10^3	200–800	523–723	175	(This work)

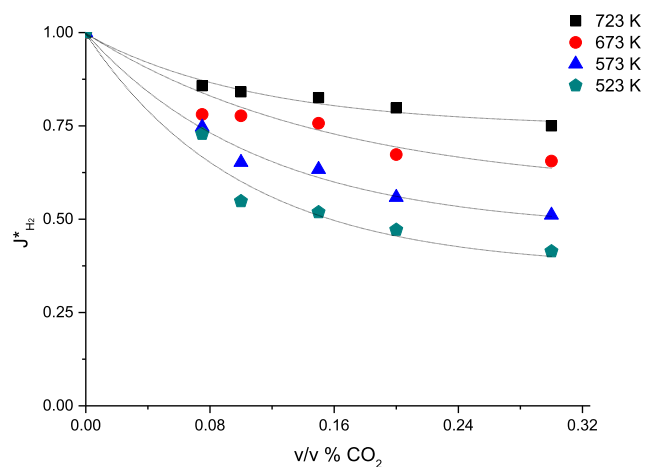


Fig. 5 – Normalized H₂-flux vs %CO₂ in the feed stream. The fitted function (dashed lines) is based on the new model (Eq. (6)).

and:

$$A = \ln \left\{ \frac{(p_{H_2,feed} - J_{H_2} R_s)^{0.5} - (p_{H_2,perm out} + J_{H_2} R_s)^{0.5}}{(p_{H_2,ret} - J_{H_2} R_s)^{0.5} - (p_{H_2,perm in} + J_{H_2} R_s)^{0.5}} \right\} \quad (4)$$

In Eqs. (2)–(4), $p_{H_2,feed}$ is the H₂-partial pressure at the inlet of membrane lumen (Pa), $p_{H_2,ret}$ is the H₂-partial pressure at the outlet of membrane lumen (Pa), $p_{H_2,perm in}$ is the H₂-partial pressure at the inlet of permeate side (Pa), $p_{H_2,perm out}$ is the H₂-partial pressure at the outlet of the permeate side (Pa), R_s is the surface mass transfer resistance (mol⁻¹ m² s Pa). According to the Sieverts' law, the pressure dependence factor (n) of the hydrogen flux on the H₂-partial pressure has the value of 0.5. Particularly, for pure-hydrogen tests, $p_{H_2,feed} = p_{H_2,ret}$; for our configuration (sweep gas stream in counter-current mode), $p_{H_2,perm in}$ is null.

Then, the permeability of the membrane can be assessed from this new expression (Eqs. (2)–(4)) as long as R_s is known. In this work, the values of R_s were taken as an average for ranges according to the literature for membranes of identical composition and similar thicknesses (ca. 200 μm) [20,22] – see Table 2 where the calculated values of hydrogen permeability are also reported.

Contrarily to what happens with P_e values, R_s increases when the temperature decreases (Table 2); actually, the resistance to the H₂-permeation increases exponentially with the temperature decrease.

Accordingly, the permeability vs. temperature can be written by the expression [23]:

$$P_e = P_{e0} e^{-\frac{E_a}{RT}} \quad (5)$$

where P_{e0} is the pre-exponential coefficient (mol m⁻¹ s⁻¹ Pa^{-0.5}), E_a is the activation energy of permeation (J mol⁻¹), R is the universal gas constant (J mol⁻¹ K⁻¹) and T is the absolute temperature (K). Through the fitting, it was determined the values of P_{e0} and E_a to be

2.61×10^{-8} mol m⁻¹ s⁻¹ Pa^{-0.5} and 2.09×10^3 J mol⁻¹, respectively.

Values of the hydrogen permeability obtained in this work are comparable with those reported in the literature for similar membranes as shown in Table 3.

Effect of CO or CO₂ in the H₂ permeation tests

Some species like CO and CO₂ interact with the metals and are adsorbed on their surface. As a consequence some sites available for the hydrogen dissociation over the metal surface may be blocked, thus causing a reduction of the membrane active area.

In a previous work, the presence of poisoning gases on the hydrogen permeation through Pd-membranes has been taken into account by a model described therein [21]. Such a model has been now further modified by introducing the logarithmic mean driving force defined by Eqs. (3) and (4), thus obtaining a comprehensive expression accounting for both the surface and poisoning effects:

$$J_{H_2} = \frac{P_e}{d} \left(1 - \alpha \frac{K_i \bar{p}_i}{1 + K_i \bar{p}_i} \right) \Delta P_{ln} \quad (6)$$

where the parameter α (dimensionless) depends only on the temperature and accounts for additional effects of the adsorbed gas, K_i is the adsorption equilibrium constant (Pa⁻¹) and \bar{p}_i is the average partial pressure (Pa) of species i .

In order to account the inhibitor effect of the CO or CO₂ on the hydrogen permeability, the α and K_i parameters were determined for every H₂/CO and H₂/CO₂ composition by non-linear fitting of the experimental data reported in Figs. 4 and 5; the values obtained are shown in Table 4.

As expected, both α and K decrease with temperature (the last one corresponding to a van't Hoff behavior) being the adsorption equilibrium constants much larger for CO than for CO₂, as reported elsewhere [21].

The poisoning effect of CO/CO₂ on the H₂-permeation flux can be highlighted by assessing the normalized fluxes of H₂ (Eq. (7)) versus the percentage of each of these substances in the feed stream. The normalized flux of hydrogen $J_{H_2}^*$ is calculated by the following expression:

$$J_{H_2}^* = \frac{J_{H_2/CO \text{ or } CO_2}}{J_{H_2}} \quad (7)$$

where: $J_{H_2/CO \text{ or } CO_2}$ (mol s⁻¹ m⁻²) is the hydrogen permeation flux measured in the H₂/CO or H₂/CO₂ tests and J_{H_2} is the hydrogen permeation flux calculated via Eq. (2) with the

Table 4 – The α and K_i parameters of Eq. (6) obtained by fitting the experimental data of Figs. 4 and 5.

T (K)	CO		CO ₂	
	α	K (Pa ⁻¹)	α	K (Pa ⁻¹)
723	0.12	1.00×10^{-4}	0.62	4.93×10^{-6}
673	0.20	1.03×10^{-4}	0.77	6.30×10^{-6}
573	0.77	1.34×10^{-4}	0.80	1.17×10^{-5}
523	0.78	3.35×10^{-4}	0.90	1.50×10^{-5}

values of the hydrogen partial pressures measured in the CO/CO₂ tests (i.e., taking into account the decrease of the hydrogen partial pressure when increasing the feed concentration of such gases); this way the driving force is the same in both terms.

The experimental data shown by Figs. 4 and 5 were obtained at a feed total pressure of 500 kPa. The fitting obtained by the novel approach (Eq. (6)) and with the parameters given in Tables 2 and 4 is shown as dashed lines. A very good adherence is observed. The same happens for other pressures (data not shown).

In both graphs the H₂-permeation fluxes are lower than the ones reached with pure H₂. The inhibitory effect is in general more pronounced for CO than for CO₂; this result suggests that the interaction of CO with the Pd–Ag surface is stronger than that of CO₂ in the range of temperature studied. Also, the inhibitory effect increases with the amount of CO (or CO₂) in the mixed feed because, in the tested conditions, the CO (or CO₂) coverage of the metal surface is directly related to the CO (or CO₂) concentration in the gas phase. Finally, at high CO concentration it is perceptible that an asymptotic trend is observed, not seen for the curves of CO₂ mixtures. A similar trend has been reported before in the literature [21], and is related with the much higher adsorption equilibrium constants for CO (cf. Table 4).

Figs. 4 and 5 show that, in agreement with the literature [21,26], the inhibition effect of CO/CO₂ decreases with temperature. Moreover, it is observed that for CO there is a high gap between the normalized hydrogen fluxes at 673 and 573 K as compared with other temperatures. This is related with the mechanism of the gases interaction with the metallic surface (as inferred from the adsorption enthalpies), as detailed below.

The adsorption enthalpy for each gas (ΔH_i) was determined by using the van't Hoff equation.

$$\frac{d \ln(K_i)}{d\left(\frac{1}{T}\right)} = -\frac{\Delta H_i}{R} \quad (8)$$

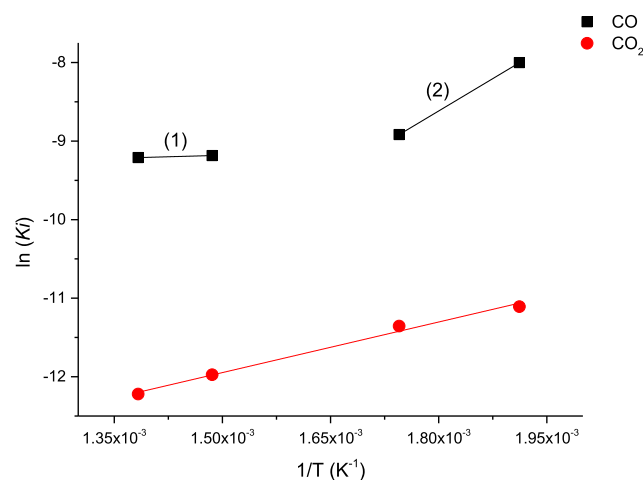


Fig. 6 – Linear regression between the determined adsorption constants of CO and CO₂ versus the inverse of temperature.

According with Fig. 6, the adsorption enthalpy obtained for CO₂ is $-17.85 \text{ kJ mol}^{-1}$. This value is higher than that reported previously for a 50 μm thick Pd–Ag membrane ($-5.41 \text{ kJ mol}^{-1}$) [21], thus indicating that some contribution of chemical sorption might occur in the herein obtained data [27,28], recorded at higher temperatures. For CO, it seems that there is a change in the mechanism with temperature, with an adsorption enthalpy of $-2.10 \text{ kJ mol}^{-1}$ at higher temperatures (Section 1), and $-45.63 \text{ kJ mol}^{-1}$ at lower ones (Section 2). This explains the gap observed in Fig. 4.

In a previous work the reversibility of the CO/CO₂ effects was analyzed [21]. In the case of CO₂ it was possible to recover completely the initial flux by passing N₂ on both sides of the membrane, while after using CO a treatment with synthetic air at 573 K was required to restore the membrane permeance towards H₂. In this work the same procedure was required. It appears that the reaction of oxygen with the adsorbed CO produces CO₂ that is purged, leading to complete membrane regeneration.

Conclusions

The hydrogen permeation flux through dense metal membranes is normally studied using the Sieverts' law but, this model is not always accurate enough. This is the case when other effects prevail, like presence of inhibitor gases (e.g. CO and CO₂) and/or surface mass transfer resistances. Because of this, it has been proposed a new model able to predict the H₂-permeation tendency with a high level of accuracy for the studied conditions (presence of inhibitor gases, wide ranges of pressure and temperature).

The model has shown an adequate fit to the experimental data (CO/H₂ and CO₂/H₂ mixtures) by successful validation in the large range of experienced conditions. Permeability towards pure hydrogen of a Pd–Ag self-supported membrane has been determined, taking the surface transfer resistance coefficients as the average from literature values. Particularly, in experiments with pure hydrogen the P_{e0} and E_a values were calculated, which were consistent with those reported in the literature. It was equally proved the inhibitory effect of CO and CO₂ on the H₂-permeating flux. Such an effect decreases with temperature and increases with the CO/CO₂ composition in the feed.

The adsorption enthalpy values obtained, ΔH_{CO} , ΔH_{CO_2} , are low, suggesting that weak physical sorption phenomena occur.

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