

ENGINEERING PHYSICS

BT - 201

$$\lambda = \frac{h}{mv}$$

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Properties of matter waves :-

①

$$\lambda = \frac{h}{mv}$$

• $h = \text{constant}$

$$v = \frac{h}{\lambda m} = u$$

②

$$m=0, \lambda=\infty$$

For the existence of wave, $m \neq 0$
(It should be material particle)

iii

For the existence of wave, $v \neq 0$ (i.e., particle should be moving particle)

iv (particular should be moving particle)

Wavelength $\lambda = h/v$ (at, if anti node in input)

with m taking $1, 2, 3, \dots$ Node (amplitude zero)

at m anti node, wavelength won't change

③

Not EM wave (does not depend on charge)

④

Velocity of matter wave is greater than speed of light 'c'.

Relation in particle velocity, phase velocity, wave velocity
(phase velocity)

• Particle Velocity :- Let we consider a particle of mass 'm' and velocity 'v', then it's kinetic energy 'E' will be equal to

$$E = (mc^2 + \frac{1}{2}mv^2) \text{ or } E = \gamma mc^2$$

$$F = \frac{1}{\gamma} mv^2$$

$$(F = \gamma - 1) mv^2 \text{ or } F = \gamma v^2$$

$$v = \sqrt{\frac{2E}{m}} \quad \text{--- ①} \quad E + P = \gamma$$

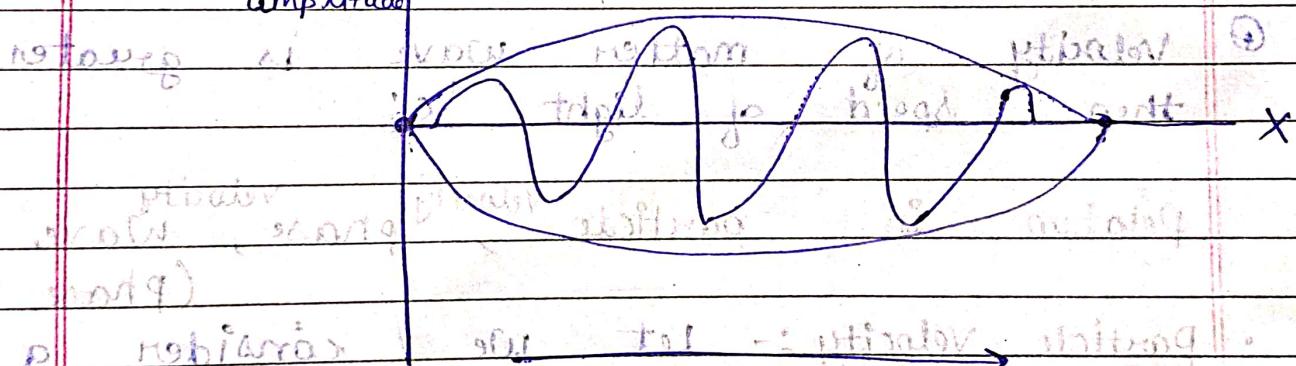
PSO and

$E = h\nu$ ~~per unit time~~ ^{constant} Planck's law of radiation.

$$N = \frac{f \text{ atoms}}{m} \cdot \frac{d}{\lambda} \quad (1)$$
$$\nu = \frac{c}{\lambda} \quad (2)$$
$$\omega = 2\pi\nu \quad (3)$$

* Grouping, wave (phase) & velocity (v) \rightarrow

Let we consider a wave packet in which two waves moving with same amplitude and slightly difference in angular frequencies ω_1 and ω_2 and propagation constant (k_1, k_2) propagates in direction then displacement equations for the waves will be:



$$y_1 = A \sin(\omega_1 t - k_1 x) \quad (1)$$

$$y_2 = A \sin(\omega_2 t - k_2 x) \quad (2)$$

$$y = y_1 + y_2 \quad (3)$$

$$\textcircled{a) } y = A [\sin(\omega_1 t - k_1 x) + \sin(\omega_2 t - k_2 x)]$$

$$\begin{aligned} & \omega = \frac{\pi}{L} \quad \sin c + \sin Q \leftarrow \sin \frac{c}{2} \cos \frac{C-D}{2} \\ & \frac{\omega}{k} = \frac{\pi}{L} \quad y = A \left[\sin \left(\frac{\omega_1 t + \omega_2 t}{2} + \frac{(-k_1 x + k_2 x)}{2} \right) \cos \frac{(\omega_1 - \omega_2)t}{2} - \right. \\ & \left. \frac{\omega}{k} = \frac{\pi}{L} \right] \end{aligned}$$

Consider $\frac{\omega_1 + \omega_2}{2} t - \frac{k_1 + k_2}{2} x$ works.

$$\frac{\omega_1 - \omega_2}{2} t - \frac{k_1 - k_2}{2} x = \frac{d\omega}{2} t + \frac{dk}{2} x$$

$$y = A \left[\sin(\omega t - kx) \cos \left(\frac{d\omega t - dk x}{2} \right) \right] \quad \text{--- (3)}$$

Standard equation for displacement is

$$y \stackrel{\text{arbitrary phase}}{\Rightarrow} A \sin(\omega t - kx) \quad \text{--- (4)}$$

Compare eq. (3), (4)

$$y = A \cos \left(\frac{d\omega t - dk x}{2} \right) \sin(\omega t - kx) \quad \text{--- (5)}$$

eq. (5) $A \cos \left(\frac{d\omega t - dk x}{2} \right)$ is

Cosine term or amplitude.

From $y = A \sin(kx + \omega t)$ equation (3)

$$y = A \sin(\omega t - kx) \quad \text{or} \quad y = A \sin(\omega t + \phi)$$

wave (phase) velocity $v_p = \frac{\omega}{k}$

$$\begin{cases} \omega t = ku \\ x = \frac{\omega t}{k} \\ v_p = \frac{\omega}{k} \end{cases}$$

$$y(x, t) = v_p t = \frac{\omega}{k} t \quad \text{--- (6)}$$

from $y = A \cos(kx + \omega t)$

$$y = A \cos\left(\frac{d\omega}{dk} t - \frac{d\omega}{dk} k - n\right) \quad \text{or} \quad y = A \cos\left(\frac{d\omega}{dk} t + \phi\right)$$

$$y = A \cos\left(\frac{d\omega}{dk} t + \phi\right) \quad \text{velocity} = \frac{d\omega}{dk}$$

group velocity of sinusoidal wave?

$$\text{group velocity } v_g = \frac{d\omega}{dk}$$

$$v_g = \frac{d\omega}{dk} \quad \text{--- (7)}$$

$$(nA - kA) \sin\left(\frac{d\omega}{dk} t - \frac{d\omega}{dk} k - n\right) \cos AR = v$$

$$(nA - kA) \cos\left(\frac{d\omega}{dk} t - \frac{d\omega}{dk} k - n\right) \cos AR = v$$

shifting to most simple

Relation between particle and group velocity. (non-relativistic)

From the definition of group velocity

$$\text{top } v_g = \frac{d\omega}{dk} \quad \text{(1)}$$

A wave packet moves with its own velocity known as group velocity.

$$\text{from } d\omega = 2\pi D, \quad k = \frac{2\pi}{\lambda} \quad \text{(2)}$$

$$v_g = \frac{d(2\pi D)}{d(\frac{2\pi}{\lambda})}$$

$$v_g = \frac{2\pi (dD)}{2\pi d(\frac{1}{\lambda})}$$

$$v_g = \frac{d(\frac{1}{\lambda})}{dD} \quad \text{(3)}$$

from de-Broglie hypothesis

$$p\lambda = \frac{h\nu}{P} \quad \text{(3)}$$

$$\lambda = \frac{h}{mv}$$

$$\lambda = \frac{h}{\sqrt{2mE}}$$

$$E = h\nu \quad \text{--- Planck's law}$$

$$\lambda = \frac{h}{\sqrt{2mE}} \quad [v = \nu]$$

$$\frac{1}{v_{\text{g}} \text{ (from eq. 4)}} = \frac{(2m h D)^{1/2}}{D} \quad (4)$$

(char. velocity - eq. 4)

From eq. ② and ④ we get

$$\text{mean vel. after } \frac{d}{D} \text{ over } (2m h D)^{1/2} \text{ sec. is}$$

(char. velocity - eq. 4)

$$v_{\text{g}} = \frac{1}{h} \left[\frac{(2m h D)^{1/2} \times 2m h}{2} \right] \text{ m/s.}$$

$$\frac{1}{v_g} = \frac{1}{h} \times \frac{(2m h D)^{1/2} \times 1}{2m h} \quad \text{eq. 5}$$

$$\frac{1}{v_g} = \sqrt{\frac{m^2 h D}{2m h D_1^2 h}} \quad \text{eq. 5}$$

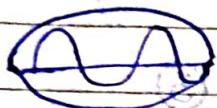
$$\frac{1}{v_g} = \sqrt{\frac{m}{2h D_1^2}} \quad \text{eq. 5}$$

($\frac{1}{v_g}$ from particle velocity)

$$\omega = \sqrt{\frac{2h D}{m^2 h D_1^2}} = \text{eq. 6}$$

$$\frac{1}{v_{\text{g, final}}} = \frac{1}{\omega D_1^2 h} \quad \text{eq. 7}$$

$$v_g = v \quad \text{eq. 7}$$



$$\text{group velocity } v_g = \frac{d\omega}{dk} = \frac{dv_b}{dk}$$

group velocity is equal to v_p particle velocity

- relation b/w particle length and group Velocities (relativistic).

put

$$m = m_0$$

$$\sqrt{1 - v^2/c^2}$$

$$v_b = \frac{E_b}{mc^2}$$

Same derivation of non relativistic only change in m

* Relation b/w v_p and v_g from phase $\rightarrow v_p = \omega/k$ \rightarrow group

$$\text{or } \omega = v_p \cdot k$$

$$\text{diff. w.r.t. } k \Rightarrow \frac{d\omega}{dk} = v_p$$

$$\frac{d\omega}{dk} = v_p \frac{dk}{dk} + k \frac{dv_p}{dk} \Rightarrow \frac{d\omega}{dk} = v_p + k \frac{dv_p}{dk}$$

$$\text{or } v_g = v_p + k \frac{\frac{dv_p}{dk}}{\frac{dk}{k}}$$

where $v_g = \omega/k = v_p + k \frac{dv_p}{dk}$

$$v_g = \frac{d\omega}{dk}$$

$$K = \frac{2\pi}{\lambda} \Rightarrow K = \frac{d\omega}{dk} = \frac{d\omega}{d(\frac{2\pi}{\lambda})} \Rightarrow \frac{d\omega}{d\lambda} = \frac{d\omega}{dk} \cdot \frac{dk}{d\lambda} = \frac{d\omega}{dk} \cdot \frac{2\pi}{\lambda}$$

$$dK = 2\pi \left[-1 \left(\frac{2\pi}{\lambda} \right) d\lambda \right] = \frac{d\omega}{dk} \cdot \frac{2\pi}{\lambda} = 0$$

$$v_g = v_p + \frac{2\pi}{\lambda} \int d\lambda \frac{dv_p}{d\lambda} = v_p + \frac{2\pi}{\lambda} (-\frac{dv_p}{d\lambda})$$

from eqn (A)

$$v_g = v_p - \lambda \frac{dv_p}{d\lambda} \quad \textcircled{5}$$

if $\frac{dv_p}{d\lambda} = 0$, $v_g = v_p$ $\textcircled{6}$ (non dispersive)

v_p independent of λ non dispersive medium.

For dispersive medium:

$$\frac{dv_p}{d\lambda} \neq 0 \quad \text{so } v_g \neq v_p$$

$$v_g = v_p - \lambda \frac{dv_p}{d\lambda}$$

dispersion can be written as

$$v_p > v_g$$

* Relation in wave (phase) velocity v_p and

particle velocity = $v = \omega r$

from wave velocity $v_p = \frac{\omega}{k}$ $\textcircled{1}$

$$\omega = 2\pi\nu, \quad k = \frac{2\pi}{\lambda} \quad \text{so } v_p = \frac{2\pi\nu}{\lambda} \quad \textcircled{2}$$

$$v_p = \frac{\omega}{k} = \frac{2\pi\nu}{\lambda} \quad \text{from } \nu = \frac{c}{\lambda} \quad \text{so } v_p = \frac{2\pi c}{\lambda} \quad \text{or } v_p = D \quad \text{where } D = 2\pi c$$

$$v_p = D \quad \text{--- (2)}$$

from

$$E = h\nu \quad \frac{h\nu}{kT} = \frac{1}{kT} \quad \text{Planck's law}$$

$$D = \frac{E}{h} = \frac{(4\pi n V^2 \lambda)}{h^2} \quad \text{so } D = \frac{4\pi n V^2}{h^2} \quad \text{or } V = \sqrt{\frac{D h^2}{4\pi n}}$$

$$\lambda = \frac{h}{p}$$

$$\lambda = \frac{h}{mv} \rightarrow \text{de Broglie hypothesis.}$$

$$v_p = \left(\frac{1}{2} mv^2 \right) \left(\frac{h}{mv} \right) \quad \frac{1}{2} mv = \frac{1}{2} h v$$

$$v_p = \frac{1}{2} v \quad \text{---} \quad \text{Ansatz}$$

Phase velocity v_p is half of particle velocity

Q. Show that wave velocity & ~~is~~ greater than speed of light.

$$\text{Wave velocity } v_p = \frac{\omega}{k} \quad \text{---} \quad \text{Ansatz}$$

$$\omega = 2\pi\nu \quad (, \text{ and } k = 2\pi \text{ rad/m}) \quad \nu \leftarrow m, \text{ then}$$

$$v_p = \frac{\omega}{k} = \frac{2\pi\nu}{2\pi} = \nu \quad \text{Ansatz}$$

$$v_p = \frac{2\pi\nu}{2\pi} = \nu \quad \text{Ansatz}$$

$$v_p = \frac{2\pi\nu}{\lambda} \quad \lambda \rightarrow \text{length of wave}$$

$$v_p = \nu \lambda \quad \text{Ansatz}$$

$$v_p = \nu \lambda$$

$$v_p = \nu \lambda \quad \text{Ansatz}$$

$$E = h\nu \quad \text{Ansatz}$$

$$E = \frac{h\nu}{h} \quad \text{Ansatz}$$

$$\lambda = \frac{h}{mv} \quad \text{---} \quad \text{Ansatz}$$

$$E = \frac{h\nu}{h} = \nu \lambda \quad (\nu \propto E, \lambda \propto 1/E)$$

$$\text{de Broglie Eqn} = \frac{h}{\lambda} = \frac{h}{mv} \quad \lambda = \frac{h}{mv}$$

$$V_p = \frac{mc^2}{h} \times \frac{\lambda}{m} = \frac{c^2}{\lambda} = E = m c^2$$

$$V_p = c^2$$

$$\lambda = \frac{h}{mv} \Rightarrow \frac{h}{mv} = \frac{c^2}{V_p}$$

Optical velocity V_o & longitudinal velocity V

or

$$V_p \cdot V = cV \quad \text{--- (6)}$$

Now Always $V < c$, then $V_p > c$

It is impossible, $V_p > c$ (then $V_p > c$)
mass, $m \rightarrow 0$ (micro particle)

Particle should be micro particle.



Heisenberg's Uncertainty principle:-

If it is impossible to determine exact position and momentum of microparticle simultaneously.

Let we consider a wave packet at the boundary of wave packet (assume) position are x_1 and x_2 then change in position is $\Delta x = (x_2 - x_1)$ and if charge

\hbar (h not)

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in velocity be $A\vec{v}$ or momentum

$$\Delta P^{\parallel} (= m A \vec{v}) \text{ when } t = 0 \text{ and } A = \lambda$$

mathematically

$$\text{or, } \Delta P^{\parallel} = \frac{\Delta E}{4\pi}$$

where, h is Planck's constant,

$$h = 6.6 \times 10^{-34} \text{ Joule sec.}$$

$$\left\{ \frac{h}{4\pi} = \hbar \text{ (h not)} \right\}$$

$$\text{or, } \frac{h}{4\pi} = \frac{(K_1 + K_2) \lambda}{2}$$

$$(K_1 - K_2) - (A - A') P \geq \frac{\hbar}{2}$$

Proof:-

Let we consider two waves in a wave packet of amplitude 'A', and w , k_1 and w_2 , k_2 are angular frequencies and propagation constants respectively.

Displacement eqn of the wave are

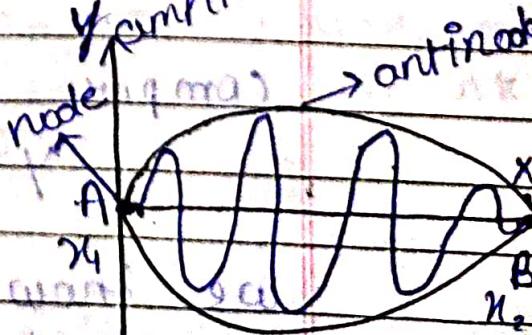
$$y_1 = A \sin(w_1 t - k_1 x) + \Phi_1$$

$$y_2 = A_2 \sin(w_2 t - k_2 x) + \Phi_2$$

$$y = y_1 + y_2$$

$$(w_1 t - k_1 x) \text{ and } w_2 t - k_2 x$$

(about a string) due to both waves in buildings



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$$y = A \left[\sin(\omega_1 t - k_1 x) + \sin\left(\frac{\omega_1 + \omega_2}{2}t - \frac{k_1 + k_2}{2}x\right) \right]$$

$$\sin(C+D) = 2 \cdot \frac{\sin C \cos D + \cos C \sin D}{2}$$

$$y = A \left[2 \sin\left(\frac{\omega_1 + \omega_2}{2}t - \frac{k_1 + k_2}{2}x\right) \right]$$

$$y = A \left[\sin\left(\frac{\omega_1 + \omega_2}{2}t - \frac{k_1 + k_2}{2}x\right) + \cos\left(\frac{\omega_1 + \omega_2}{2}t - \frac{k_1 + k_2}{2}x\right) \right]$$

$$y = A \left[\sin\left(\frac{\omega_1 + \omega_2}{2}t - \frac{k_1 + k_2}{2}x\right) + \cos\left(\frac{\omega_1 + \omega_2}{2}t - \frac{k_1 + k_2}{2}x\right) \right]$$

$$y = A \left[\sin\left(\frac{\omega_1 + \omega_2}{2}t - \frac{k_1 + k_2}{2}x\right) + \cos\left(\frac{\omega_1 + \omega_2}{2}t - \frac{k_1 + k_2}{2}x\right) \right]$$

$$y = A \left[\sin\left(\frac{\omega_1 + \omega_2}{2}t - \frac{k_1 + k_2}{2}x\right) + \cos\left(\frac{\omega_1 + \omega_2}{2}t - \frac{k_1 + k_2}{2}x\right) \right]$$

In above eqⁿ A is amplitude

$$y = A \cos\left(\frac{d\omega}{2}t + \frac{dk}{2}x\right) \sin(\omega t - kx)$$

compare with

$$y = A \sin(\omega t - kx)$$

we know that at node (Point A and B) amplitude is zero or

$$\text{or } 2A \cos\left(\frac{dw}{2} + -\frac{dk}{2}x_1\right) = 0 \quad (1)$$

$$\text{or } \cos\left(\frac{dw}{2} + -\frac{dk}{2}x_1\right) = \cos \frac{\pi}{2}$$

$$\frac{dw}{2} + -\frac{dk}{2}x_1 = \frac{\pi}{2} \quad (2)$$

$$\text{or At point } A' \quad r = 9A \cdot x_A$$

$$\frac{dw}{2} + -\frac{dk}{2}x_1 = \frac{\pi}{2}$$

position of θ towards to the left
At point A' minimum in tri (left)

$$\frac{dw}{2} + -\frac{dk}{2}x_2 = 3\frac{\pi}{2}$$

for another point A'

by elimination method.

$$\frac{dw}{2} + -\frac{dk}{2}x_1 = \frac{\pi}{2} \quad \text{and} \quad \frac{dw}{2} + -\frac{dk}{2}x_2 = 3\frac{\pi}{2}$$

$$x_2 - x_1 = 3\Delta x$$

$$\frac{dw}{2} + -\frac{dk}{2}x_2 = 3\frac{\pi}{2}$$

$$\Rightarrow \frac{dk}{2}(x_2 - x_1) = -\pi \Rightarrow \frac{dk}{2}(x_2 - x_1) = -\pi$$

$$\Rightarrow \frac{dk}{2} \Delta x = \pi \Rightarrow \frac{dk}{2} \Delta x = \pi \quad \begin{cases} x_2 - x_1 = \Delta x \\ dk = \Delta k \end{cases}$$

$$\Rightarrow k = \frac{2\pi}{\Delta x}$$

$$k = \frac{2\pi P}{h}$$

or

$$1 = \frac{h}{P} \quad \text{or } h = P \quad \text{and } \Delta K = \frac{2\pi}{h} \Delta P$$

method de Broglie hypothesis

$$\frac{2\pi}{n} \Delta p_0 = (\pi d_b - \pi a_b) \quad \text{or} \quad \Delta x = \frac{\pi}{2\pi} \Delta p_0$$

~~$$\Delta x = \frac{(\pi d_b - \pi a_b) \cdot \cos \theta}{2\pi}$$~~

$$\Delta x \cdot \Delta p = h \quad \text{or} \quad \Delta x \cdot \Delta p = \frac{\pi \times 2 \times h}{2\pi}$$

$$\Delta x \cdot \Delta p = h \quad \text{or} \quad \Delta x \cdot \Delta p = \frac{\pi \times 2 \times h}{2\pi}$$

hence proved.

Product of change in position and change in momentum is in order of Planck's constant 'h'.

* Verifications:-

1. Electron can not exist in the nucleus we know that, radius of nucleus = 10^{-15} m max K.E. = 4 MeV .

Using Heisenberg's Uncertainty principle,

$$\Delta x \cdot \Delta p = h \quad \text{or} \quad \Delta x \cdot \frac{h}{4\pi} = h$$

$$\Delta x = \frac{h}{4\pi \Delta p} \quad \Delta x = \frac{h}{4\pi \times 10^{-15}} = 2 \times 10^{-4} \text{ m}$$

$$\Delta p = \frac{h}{4\pi \times \Delta x}$$

$$\Delta p = \frac{6.6 \times 10^{-34}}{4 \times 3.14 \times 2 \times 10^{-4}} = 0.262 \times 10^{-20} \text{ kg m/s}$$

$$E = \sqrt{(m_0 c^2)^2 + (pc)^2} \Rightarrow 60 \text{ MeV}$$

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$$\Delta p = 2.627 \times 10^{-21} \text{ kg m/sec.}$$

$$E = \Delta p/c \text{ (convertion to unit in MeV)}$$

$$= 2.62 \times 10^{-21} \frac{\text{J sec}}{\text{kg}} \times 3 \times 10^8 \frac{\text{m}}{\text{sec}}$$

unit conversion $\frac{\text{m}}{\text{kg sec}} \times \frac{\text{sec}}{\text{m}} = \frac{\text{J}}{\text{kg}}$

$$= 7.86 \times 10^{-13} \text{ J}$$

$$= 7.86 \times 10^{-13} \text{ J} \times 10^6 \text{ eV} = 7.86 \times 10^{-7} \text{ MeV}$$

$$E = 4.91 \times 10^6 \text{ eV}$$

(in terms of energy) which is less than the binding energy of the nucleus.

$$E = 4.91 \text{ MeV} \quad 10^6 \text{ eV} = 1 \text{ MeV}$$

It is clear that $[4.9 \text{ MeV} > 4 \text{ MeV}]$, electron does not exist in the nucleus.

$$E = \sqrt{(m_0 c^2)^2 + (pc)^2}$$

$$(d = 9A \cdot r_A)$$

$$d = 9r_A \approx x_A$$

$$r_A = 0.5r_A : \text{fix atomic radius } r_A$$

$$d = 9 = x_A$$

platinum

$$r_A = (anisotropy) + r_{min} = 9A$$

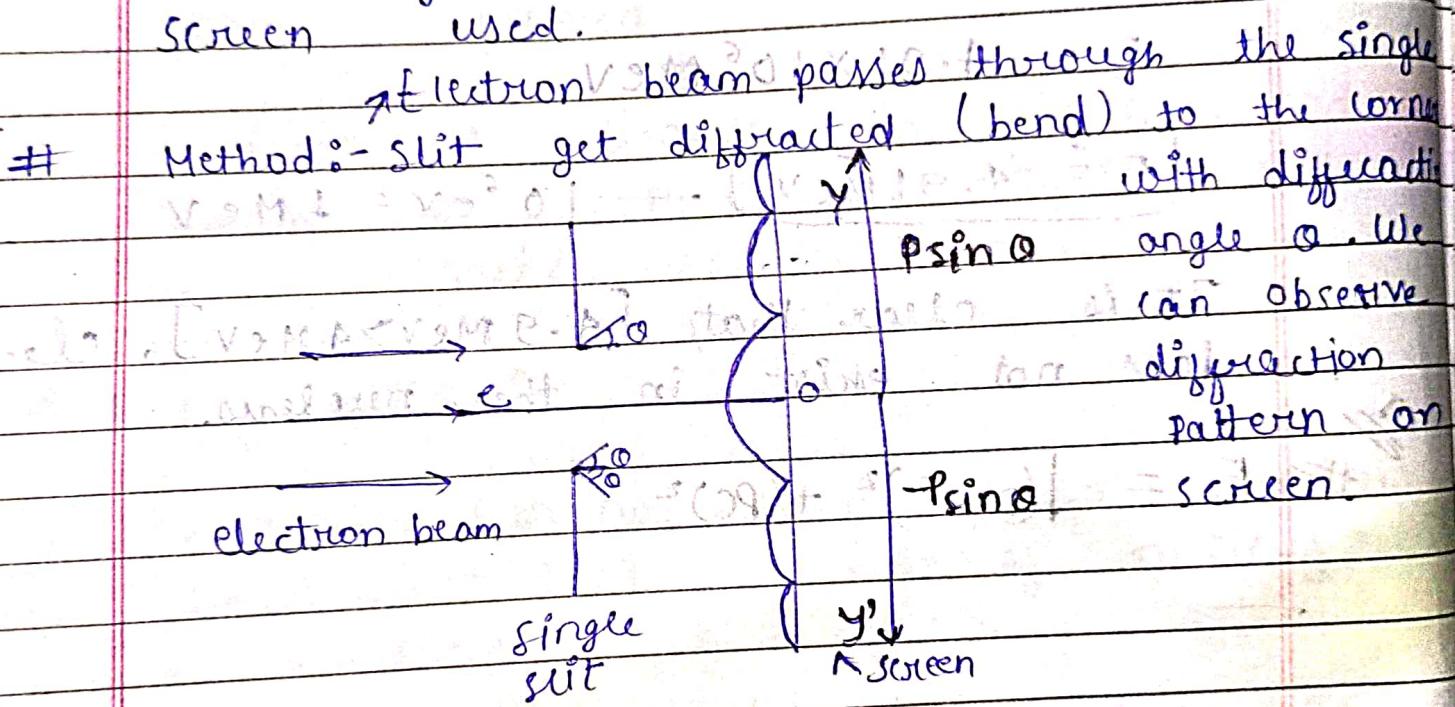
$$V \cdot M = 0.2 \leftarrow \text{size of slit in } \text{opp} \text{ (dark)} \quad b = 1$$

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* Verification :-

2. Diffraction at single slit :-

Parts:- It based on diffraction phenomena in this experiment an electron beam a single slit (of size 'e') and a screen used.



Using Heisenberg's uncertainty principle.

$$\Delta x \cdot \Delta p \geq \frac{h}{4\pi}$$

$\Delta x = e$, and from diffraction at single slit : $e \sin \theta = n\lambda$

or $\Delta x = e = \frac{\lambda}{\sin \theta}$ [$n=1$ for maximum intensity]

$$\Delta p = psin \theta - (-psin \theta) = 2p \sin \theta$$

We can find $\Delta n \cdot \Delta p$ by using

$$= \frac{d}{\sin\theta} \times 2p \sin\theta$$

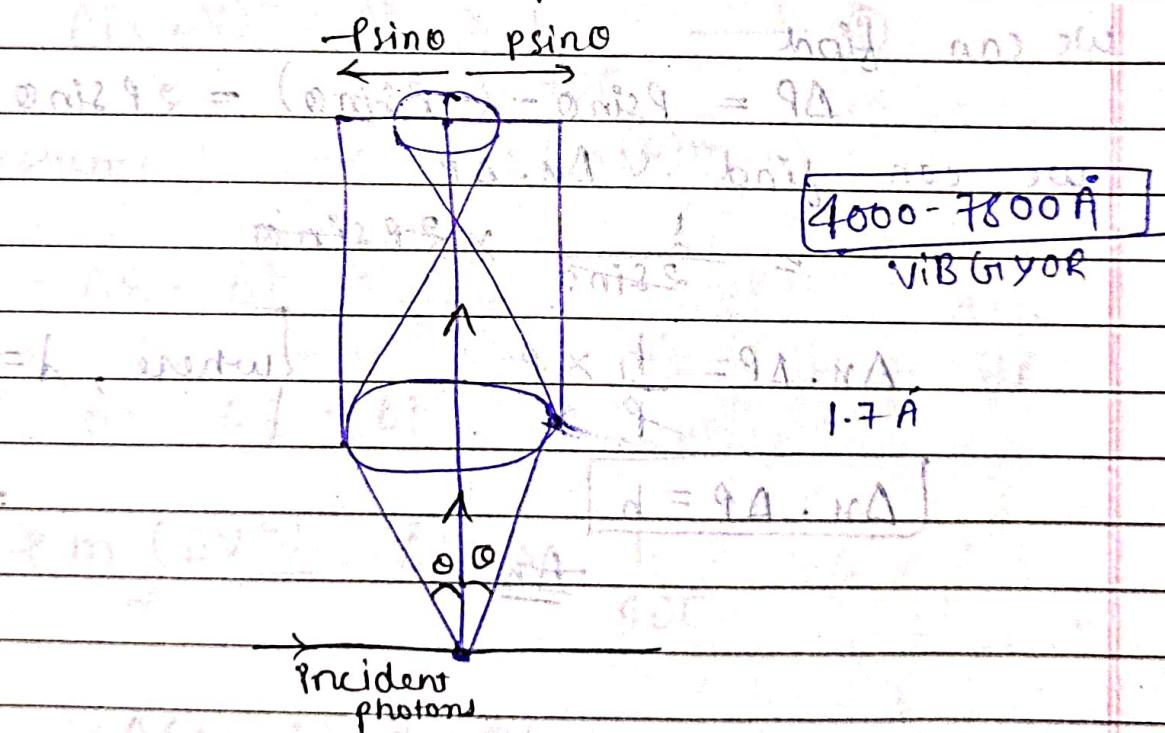
$$\Delta n \cdot \Delta p = 2p d = 2p \times \frac{h}{P} = 2h \quad \left\{ \lambda = \frac{h}{P} \right.$$

$$(\Delta n \cdot \Delta p = 2h)$$

$$\lambda = 0.03 \text{ nm}$$

* Verification :-

3. Electron Microscope:-



Using 'uncertainty' principle

$$\Delta n \cdot \Delta p \geq \frac{h}{4\pi}$$

$\Delta n = e$ and from electron microscope

$$\therefore 2d \sin \theta = \lambda$$

or

$$\Delta n = d = \frac{\lambda}{2 \sin \theta}$$

We can find

$$\Delta p = p \sin \theta - (-p \sin \theta) = 2p \sin \theta$$

We can find $\Delta n \cdot \Delta p$

$$= \frac{\lambda}{2 \sin \theta} \times 2p \sin \theta$$

$$\Delta n \cdot \Delta p = \frac{h}{p} \times p \quad \left\{ \text{where, } \lambda = \frac{h}{p} \right.$$

$$\boxed{\Delta n \cdot \Delta p = h}$$

Answ

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* Prove that $\Delta E \cdot \Delta t \sim h$ using Heisenberg's uncertainty principle.



$$\Delta x \cdot \Delta p \geq \frac{h}{4\pi}$$

①

$$\Delta v = \frac{\Delta x}{\Delta t}, \quad \Delta p = m \Delta v$$

$$\Delta E \cdot \Delta t \cdot m \Delta v \geq \frac{h}{4\pi} \quad d \leq 9A \cdot nA$$

$$m (\Delta v)^2 \cdot \Delta t \geq \frac{h}{4\pi} \quad ②$$

$$\text{assume } \Delta E = m (\Delta v)^2 \cdot 9A$$

$$\Delta E \cdot \Delta t \geq \frac{h}{4\pi} \quad d \leq 9A$$

$$\text{or } \Delta E \cdot (\Delta t) \sim h$$



$$2 m (\Delta v^2) \cdot \Delta t \geq \frac{2h}{4\pi} \quad d \leq 9A$$

$$2 \Delta E \cdot \Delta t \geq \frac{1}{2} \frac{h}{4\pi} \quad d \leq 9A$$

$$\text{or } \Delta E \cdot \Delta t \sim h \times 9A$$

$$m \times p_s \cdot \Delta t =$$

$$m \times v_s \cdot \Delta t =$$

$$m \times p_s \times p_s \cdot \Delta t =$$

Ques. Calculate Uncertainty in position for an electron if its velocity is 300 m/s with accuracy 0.001%.

$$\Delta n = ?$$

$$\Delta v = 300 \text{ m/s}$$

$$\text{accuracy} = 0.001\%$$

$$m_e = 9.1 \times 10^{-31} \text{ kg}$$

$$\Delta n = ?$$

$$\Delta n \cdot \Delta p \geq \frac{h}{4\pi}$$

$$\Delta n \geq \frac{h}{4\pi \cdot \Delta p}$$

$$\Delta n \geq \frac{h}{\Delta p \cdot 4\pi}$$

$$\Delta p = M \cdot \Delta v$$

$$\Delta v = v \times \text{limit of accuracy}$$

$$= 300 \text{ m/s} \times \frac{0.001}{100}$$

$$\Delta v = 0.003 \text{ m/s}$$

$$\Delta n = \frac{6.6 \times 10^{-34} \text{ J/sec}}{4 \times 3.14 \times 9.1 \times 10^{-31} \text{ kg} \times 0.003 \text{ m/s}}$$

$$= \frac{6.6 \times 10^{-34} \text{ J/sec}}{0.342 \times 10^{-31} \text{ (kg m/s)}}$$

$$= 19.29 \times 10^{-34+31} \text{ m}$$

$$= 19.29 \times 10^{-3} \text{ m}$$

$$= 1.929 \times 10^{-2} \text{ m}$$



Operators

* E and P operators.

Wave function Ψ can be written as

$$\Psi = A e^{-i(\omega t - kx)} \quad \text{--- (1)}$$

where, ω and k are angular frequency and propagation constant respectively.

Ψ has real, imaginary, root, negative, and positive valued.

Therefore, Ψ is not observable and not acceptable.

$$\Psi = A + iB \quad \text{--- (2)}$$

$$\omega = 2\pi\nu \quad , \quad k = \frac{2\pi}{\lambda}$$

eqn (1) becomes,

$$\Psi = A e^{-i(2\pi\nu t - \frac{2\pi}{\lambda} x)} \quad \text{--- (3)}$$

$$\epsilon = h\nu \quad \text{--- (4)}$$

$$\nu = \frac{\epsilon}{h} \quad \text{--- (5)}$$

$$\lambda = \frac{h}{p} \quad \text{--- (6)}$$

de Broglie hypothesis

$$\frac{1}{i} = \frac{p}{\hbar}$$

$$\psi = A e^{-i\left(\frac{2\pi}{n}\epsilon t + \frac{-2\pi}{\hbar}px\right)}$$

$$\psi = A e^{-i\left(\epsilon t - px\right)} \quad (3) \quad \left[\hbar = \frac{\hbar}{2\pi} \right]$$

eqn (3) diff. w.r.t. 't'

$$\frac{d\psi}{dt} = A e^{-i\left(\epsilon t - px\right)} \left[-i\frac{\epsilon}{\hbar} (e-0) \right]$$

$$\frac{d\psi}{dt} = -i\frac{\epsilon}{\hbar} \psi \quad \epsilon\psi = \hbar i \cdot \frac{d\psi}{dt}$$

$$E\psi = \hbar i \cdot \frac{d\psi}{dt}$$

$$\epsilon\psi = i\hbar \frac{d\psi}{dt} \quad \{i^2 = -1\}$$

ϵ - operator $= i\hbar \frac{d}{dt}$

Again diff. eq. (3) w.r.t. 'x'

$$\frac{d\psi}{dx} = A e^{-i\left(\epsilon t - px\right)} \left[-i\frac{\epsilon}{\hbar} (0-p) \right]$$

$$\frac{d\psi}{dx} = -i\frac{\epsilon}{\hbar} p \psi$$

$$i\hbar p \psi = i\hbar \frac{d\psi}{dx}$$

(E) n) phasor at top

$$A = \sin(\omega t + \phi)$$

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again bin $\frac{dV}{dx}$ and ψ

~~but P-operator is $\frac{d}{dx}$~~ \rightarrow $\frac{d\psi}{dx}$ \rightarrow $\frac{d}{dx} \psi$

points

~~Ans~~* Wave function ψ :- if $|\psi| <$

~~unit no~~ \rightarrow matrix

\rightarrow To stabilise diff eqn for de-Broglie we need a function known as wavefunction and it denoted by ' ψ ' where, ' ψ ' is

$$\psi = A e^{-i(\omega t - kx)} \quad \text{--- (1)}$$

Anal ' ψ ' is a complex quantity.

$$\psi = A + iB \quad \text{--- (2)}$$

' ψ ' has a real, imaginary, root (+)ve & negative valued, which is not observable and acceptable.

Strength (magnitude) is total

$$\psi^* = A - iB \quad \text{--- (3)}$$

where ' ψ^* ' is complex conjugate of ' ψ '

$$\psi \psi^* = A^2 + B^2 \quad \text{--- (4)}$$

$$\text{and } \psi \psi^* = (\psi)^2$$

or $|\psi|^2 = A^2 + B^2 \quad \text{--- (5)}$

for 4th Property in 3D

$$\int_{-\infty}^{\infty} |\psi|^2 dxdydz = 1$$

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$|\psi|^2$ has real, (+)ve and single valued. It is observable and acceptable.

$\Rightarrow |\psi|^2$ is probability of finding electron anywhere, any time.

- ① It must be finite.
- ② It is continuous.
- ③ (+)ve and single valued
- ④ Normalized.

According to Max Born interpretation
Normalization is $\int_{-\infty}^{+\infty} |\psi|^2 dn = 1$



What is Orthogonal Property?

$$\int_{-\infty}^{+\infty} |\psi|^2 dn = 0$$

if ψ is orthogonal to ψ' then $\int_{-\infty}^{+\infty} \psi \psi' dn = 0$

$$① \rightarrow {}^* \psi + {}^* A = {}^* \psi \psi$$

$$f(\psi) = {}^* \psi \psi, \text{ then}$$

$$② \rightarrow {}^* \psi + {}^* A = {}^* |\psi|$$

Schrodinger wave equation:

- It is differential form of de-braglie wave.
- Schrodinger wave eqn is eqn for describing or describe motion of particle (or wave) in quantum mechanics.
- which is similar to newton's law of motion in classical mechanics.
- Wave function $\psi = A e^{-i(\omega t - kx)}$ and $\psi = A e^{-i(Et - Px)}$
- and we have ψ -operator $\frac{d}{dt}$ and P -operator $= \frac{i}{\hbar} \frac{d}{dx}$
- Total energy (of particle ψ is equal to K.E. ($= \frac{1}{2}mv^2$) and potential energy (V)

$$\text{Total Energy} = \frac{1}{2}mv^2 + V \quad (1)$$

1st term of R.H.S. ψ

$$\psi = \psi(E - V) \quad \text{and} \quad \psi^* \psi = 1$$

$$\frac{1}{2}mv^2 = \frac{P^2}{2m} \quad \{ \hbar P = mv \}$$

$$E = \frac{P^2}{2m} + V \quad (2)$$

APPLY ψ in eq. (2) ψ is wave function

$$E\psi = \frac{P^2\psi}{2m} + V\psi \quad (3)$$

P-operator is $i \frac{d}{dx}$

$$P^2 = \left(\frac{\hbar}{i} \frac{d}{dx} \right) \left(\frac{\hbar}{i} \frac{d}{dx} \right)$$

$$E\Psi = \frac{-\hbar^2}{2m} \frac{d^2\Psi}{dx^2} + V\Psi$$

total equation of motion is given by

$$E\Psi = -\frac{\hbar^2}{2m} \frac{d^2\Psi}{dx^2} + V\Psi$$

$$\frac{\hbar^2}{2m} \frac{d^2\Psi}{dx^2} + (E-V)\Psi = 0$$

$$\frac{\hbar^2}{2m} \frac{d^2\Psi}{dx^2} + (E-V)\Psi = 0$$

divide (÷) by $\left(\frac{\hbar^2}{2m}\right)$ in eq. above = eq. both side

$$\frac{d^2\Psi}{dx^2} + \frac{2m}{\hbar^2} (E-V)\Psi = 0 \quad \text{--- (4)}$$

eqn (4) known as 1-D Time Independent SWE. (schrodinger wave equation)

In above eqn Ψ is not a function of time $(\Psi \rightarrow \Psi_0)$

$$\Psi_0 + \Psi_1 = \Psi$$

For a free particle

$$V=0$$

$$\frac{d^2\psi}{dx^2} + \frac{2m}{\hbar^2} E \psi = 0 \quad \text{(5) 1D Schrödinger Eqn}$$

$$\frac{d^2\psi}{dx^2} + \frac{d^2\psi}{dy^2} + \frac{d^2\psi}{dz^2} + \frac{2m}{\hbar^2} (E-V) \psi = 0 \quad \text{(6) 3D Schrödinger Eqn}$$

~~Eqn (6)~~ is 3D time independent SWE (Schrodinger wave equation)

From $E\psi = -\frac{\hbar^2}{2m} \frac{d^2\psi}{dx^2}$

Put E -operator with $\frac{d}{dt}$ in above eqn

$$i\hbar \frac{d\psi}{dt} = -\frac{\hbar^2}{2m} \frac{d^2\psi}{dx^2} + V\psi \quad \text{(7)}$$

Eqn (7) is 1-Dimensional Time dependent Schrodinger wave equation (SWE)

In above eqn ' ψ ' is function of position x & time t ; $\psi \rightarrow \Psi(x, t)$

$$[\psi \rightarrow \Psi(x, t)]$$

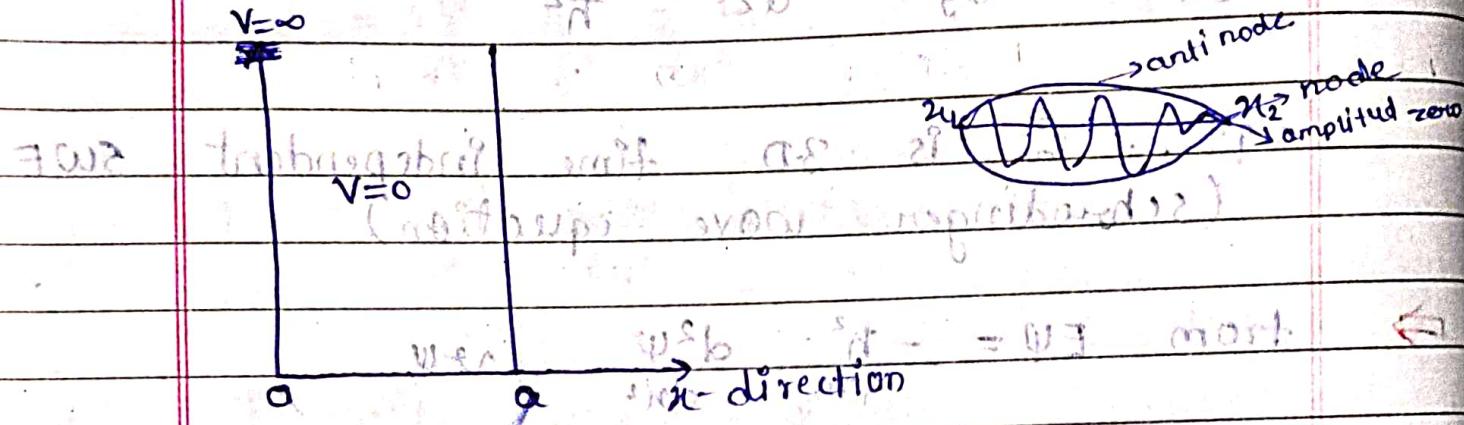
(read as ψ is a function of x & t)

$$\text{Eqn (7)} \rightarrow 0 = \psi \exists \text{ ms} + i\psi \frac{\partial}{\partial t} + \frac{\hbar^2}{2m} \frac{\partial^2\psi}{\partial x^2}$$

Particle in a box with size 'a'

or Application of Time Independent Schrödinger wave equation (TISWE)

Q Let's consider a 1D box of size 'a'



Now an electron moves in x-direction

E Inside the box \rightarrow K.E. \rightarrow 0 (min) $V \rightarrow 0$ (max)

At boundary, $K.E. \rightarrow 0$ (min) $V \rightarrow \infty$ (max)

From time independent Schrödinger wave equation.

$$\frac{d^2\psi}{dx^2} + \frac{2m}{\hbar^2}(E - V)\psi = 0 \quad \text{(1)}$$

for free particle (inside a box)

$$\frac{d^2\psi}{dx^2} + \frac{2m}{\hbar^2} E \psi = 0 \quad \text{(2)}$$

$$\frac{d^2 \Psi}{dx^2} + k^2 \Psi = 0 \quad \text{--- (3)}$$

(1) bndy (2) app. model

$$\text{Where } k^2 = \frac{2mE}{\hbar^2} \quad \text{--- (4)}$$

General solution of equation (3)

$$\Psi = A \sin kx + B \cos kx \quad \text{--- (5)}$$

Boundary conditions are

$$x=0 ; \Psi = 0 \quad \text{--- (6)}$$

$$x=a ; \Psi = 0 \quad \text{--- (7)}$$

from (5) and (6)

$$0 = A \sin kx_0 + B \cos kx_0$$

$$0 = 0 + B$$

$$(5) \boxed{B=0} \quad (8) \boxed{\sin kx_0 = 0}$$

Put $B=0$ in eq. (5)

$$\Psi = A \sin kx \quad \text{--- (9)}$$

Apply boundary condition using eqn (7) and (9)

$$(7) \boxed{\sin ka = 0}$$

$$0 = A \sin ka \sin n\pi$$

$$\{\sin 0^\circ = \sin n\pi\}$$

$$0 \neq 0 \sin n\pi \Rightarrow \sin n\pi = 0$$

$$ka = n\pi - \text{arbitrary}$$

$$ka = n\pi - \text{arbitrary}$$

$$k = \frac{n\pi}{a} \quad (10)$$

from eqn (9) and (10)

$$\Psi = A \sin \frac{n\pi x}{a} + B \cos \frac{n\pi x}{a} \quad (11)$$

(11) satisfies the boundary condition

(from eqn 2 (4) & (10))

$$k^2 = \frac{2mE}{\hbar^2}$$

$$\left(\frac{n\pi}{a}\right)^2 = \frac{2mE}{\hbar^2} \quad \left\{ \begin{array}{l} \hbar = \frac{h}{2\pi} \\ E = \frac{n^2 h^2}{8a^2 m} \end{array} \right.$$

$$E = \frac{n^2 \pi^2}{8a^2} \times \frac{\hbar^2}{2^2 m^2 e^2 \pi^2} \times \frac{1}{2m}$$

$$E = \frac{n^2 \hbar^2}{8a^2 m} \quad (12)$$

$$E \propto n^2$$

$$\Psi = A \sin kx \quad (12)$$

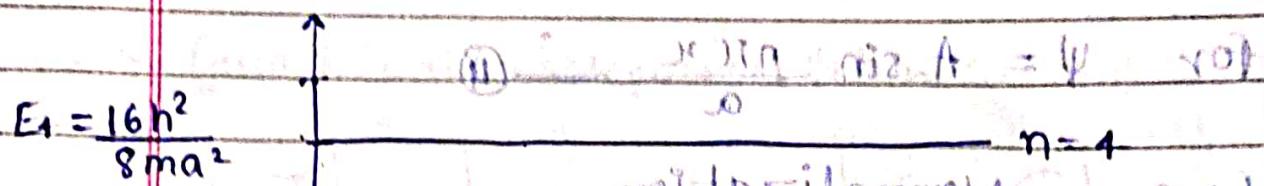
$$E_n \rightarrow E_{n0} \quad (12)$$

$$E_n = \frac{n^2 \hbar^2}{8ma^2} \quad (13)$$

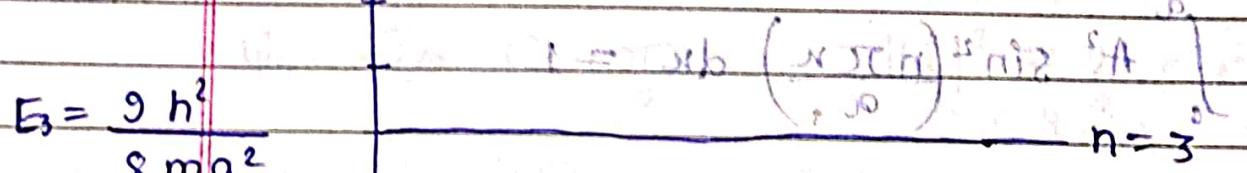
$$\{ \sin kx = 0 \}$$

(13) is eqn for eigenvalue for a particle in 1-D box

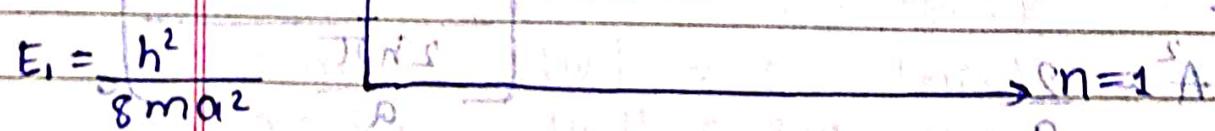
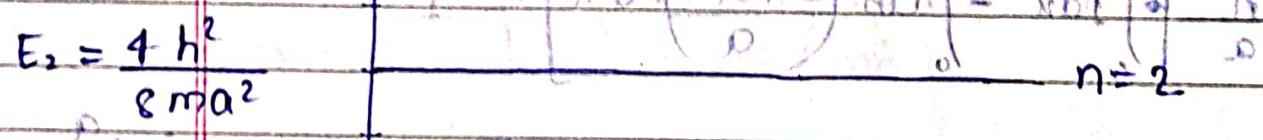
plot a graph in (i) E , eV (in terms)



$$L = \sqrt{h^2 / (\mu)} \quad (1)$$



$$\Delta E_3 = E_3 - E_1 = 9\ h^2 / (8\ ma^2)$$



from graph, $E_2 - E_1 = E_3 - E_2 = E_4 - E_3 = \Delta E$

$$E_2 - E_1 \neq E_3 - E_2 \neq E_4 - E_3 \quad (1)$$

If is clear that, energy spectrum of particle in a box is discrete
 $\Psi \leftarrow \Psi$

(contd.)

Conform neg? Eqn (1) ni deno a taki

$$\text{for } \psi = A \sin \frac{n\pi x}{a} \quad (1)$$

from Normalization

$$\int_{-\infty}^{+\infty} |\psi|^2 dx = 1$$

$$\int_0^a A^2 \sin^2 \left(\frac{n\pi x}{a} \right) dx = 1$$

$$\sin^2 \theta = \frac{1 - \cos^2 \theta}{2}$$

$$\frac{A^2}{a} \left[\int_0^a 1 dx - \int_0^a \cos \left(\frac{2n\pi x}{a} \right) dx \right] = 1$$

$$\frac{A^2}{a} [a - 0] = 1$$

$$A^2 = \frac{a}{2}$$

$$A = \sqrt{\frac{a}{2}}$$

Eqn (1) becomes $\psi = \sqrt{\frac{a}{2}} \sin \frac{n\pi x}{a}$

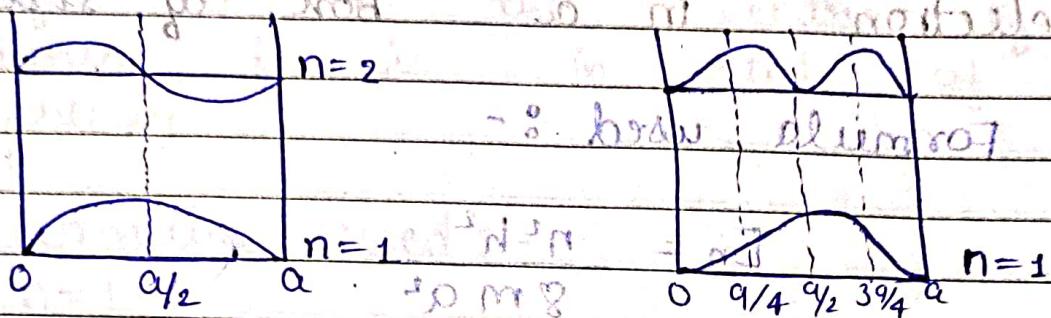
$$\text{Ansatz } \psi_{1,2} = \sqrt{\frac{a}{2}} \sin \frac{n\pi x}{a} \quad \text{for } n=1, 2, \dots \quad (14)$$

if $n \neq 0$ mod 2

$$\psi \rightarrow \psi_n$$

and. $|\psi|^2 = \frac{2}{a} \sin^2 n\pi x : \text{In } 13 \text{ u/1}$

\rightarrow (Graphical representation: (a) column)



$$\psi_n = \sqrt{2/a} \sin \frac{n\pi x}{a} \quad |\psi_n|^2 = 2 \sin^2 \frac{n\pi x}{a}$$

$$\rightarrow n=1, \quad |\psi_1|^2 = \frac{2}{a} \sin^2 \frac{\pi x}{a} = 2 \sin^2 \frac{\pi x}{a} = 2 \times 0.5 = 1$$

$$n=0; \quad |\psi_0|^2 = 0 \text{ (min)}$$

$$n=a/2; \quad |\psi_{a/2}|^2 = 2/a \text{ (max)} = 1$$

$$n=a; \quad |\psi_a|^2 = 0 \text{ (min)} = 0$$

$$\rightarrow n=2, \quad |\psi_2|^2 = \frac{2}{a} \sin^2 \frac{2\pi x}{a} = 2 \times 0.5 \times 0.5 = 0.5$$

$$n=0; \quad |\psi_0|^2 = 0 \text{ (min.)}$$

$$n=a/4; \quad |\psi_{a/4}|^2 = 2/a \times 0.5 = 0.5$$

$$n=a/2; \quad |\psi_{a/2}|^2 = 0 \text{ (min.)}$$

$$n=3a/4; \quad |\psi_{3a/4}|^2 = 2/a \times 0.5 = 0.5$$

$$n=a; \quad |\psi_a|^2 = 0 \text{ (min.)}$$

$|\psi_n|^2$ has real, single valued and positive.

Numerical :-

Q. 1 Calculate zero energy state for an electron in a box of size 1 Å

Solve →

Formula used :-

$$E_n = \frac{n^2 h^2}{8 m a^2}$$

$$n = 1, E_1 = \frac{h^2}{8 m a^2}$$

$$h = 6.6 \times 10^{-34} \text{ J sec.}$$

$$m = 9.1 \times 10^{-31} \text{ kg}$$

$$a = 1 \text{ Å} = 10^{-10} \text{ m}$$

$$E_1 = \frac{1^2 \times (6.6)^2 \times (10^{-34})^2}{8 \times 9.1 \times 10^{-31} \times (10^{-10})^2}$$

$$E_1 = \frac{43.56 \times 10^{-68}}{72.8 \times 10^{-310} \times 10^{-20}}$$

$$E_1 = (0.598 \times 10^{-17} \text{ J})$$

$$E_1 = (5.98 \times 10^{-18} \text{ J})$$

$$E_1 = (5.98 \times 10^{-18} \text{ J}) \quad \left\{ \text{for unit conversion divide by charge}\right.$$

Ans $E_1 = 37.837 \text{ ev.} \text{ and } 5.98 \text{ J}$

$$\frac{P}{\Delta P} = \frac{V_9}{\Delta V_9}$$

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Q.3 What is minimum uncertainty in the frequency of a photon whose life time is about 10^{-8} sec?

Solve =

Formulae used -

By Heisenberg uncertainty principle

$$(\Delta E)^2 \cdot (\Delta t) = \frac{h \times 1.8 \times 8}{4\pi} \quad \text{①}$$

$$\text{put } \Delta E = h \Delta V \quad (0.1 \times 0.8 \times 10^{-8}) = \text{?}$$

$$\text{Formula } \Delta V \cdot \Delta t = \frac{h}{4\pi}$$

$$\Delta V = \frac{h}{4\pi \times 1.8 \times 10^{-8}} \quad \text{?}$$

$$\Delta V = \frac{1}{12.56} \times \frac{1}{10^{-8}}$$

$$\Delta V = \frac{1}{12.56} \times \frac{1}{10^{-8}} \quad \text{?}$$

$$\Delta V = 0.0796 \times 10^8 \quad \text{?}$$

$$\Delta V = 8.0796 \times 10^6 \text{ Hz.}$$

$$\Delta V = 8.0796 \times 10^6 \text{ Hz.}$$

Q.4 An electron ~~is~~ is bound by a potential which closely approaches in infinite square well ~~of width~~ $a = 2.5 \times 10^{-10} \text{ m}$. Calculate the three energies the electron can have.

Ans

$$eV = \frac{J}{c}$$

electron volt

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Solve $\Rightarrow E_n = \frac{n^2 h^2}{8 \pi^2 m a^2}$ nuciently = 1, 2, 3 etc.

$a = 2.5 \times 10^{-10} \text{ m}$

$h = 6.6 \times 10^{-34} \text{ J sec}$

$m = 9.1 \times 10^{-31} \text{ kg}$

$$E_1 = \frac{1 \times (6.6 \times 10^{-34})^2}{8 \times 9.1 \times 10^{-31} \times (2.5 \times 10^{-10})^2}$$

$$E_1 = 43.56 \times 10^{-68} \text{ J} = 3.56 \times 10^{-17} \text{ eV}$$

$$E_1 = 0.0957 \times 10^{-17}$$

$$E_1 = \frac{0.0957 \times 10^{-17}}{1.6 \times 10^{-19} \text{ C}} \text{ J} \quad \left\{ \begin{array}{l} \text{for convert the unit} \\ \text{divide by 1 electron charge} \end{array} \right.$$

$$E_1 = 5.983 \text{ eV}$$

$$\frac{1}{2} \times 1 = 6 \text{ eV} \quad \underline{\text{Ans}}$$

$$E_2 = 2 \times (2)^2 \times 0.0957 \times 10^{-17} = 6 \text{ eV}$$

$$E_2 = 0.9 \times 5.983 \text{ eV}$$

$$E_2 = 23.932 \text{ eV}$$

Similarly for 3rd orbit Ans

$$E_3 = 3^2 \times 0.0957 \times 10^{-17} = 81 \times 5.983 \text{ eV}$$

$$E_3 = 9 \times 5.983 \text{ eV}$$

$$E_3 = 53.847 \text{ eV}$$

Ans

WAVE OPTICS

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★ Interference of light:-

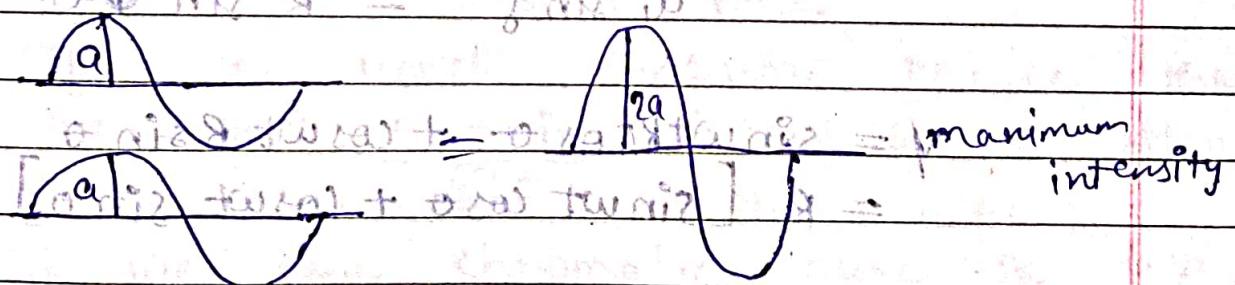
→ When two or more than two waves of same amplitude, coherent and monochromatic source, superimpose then resultant amplitude of the new wave is different from the original waves.

This redistribution is known as interference of light.

(1) Constructive interference :-

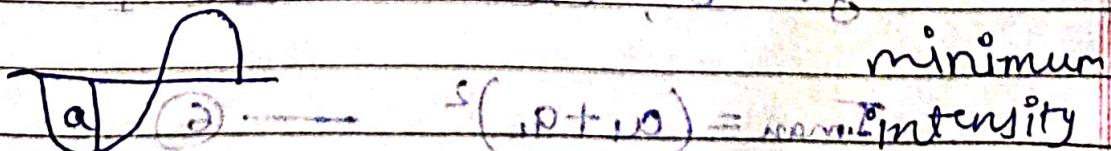
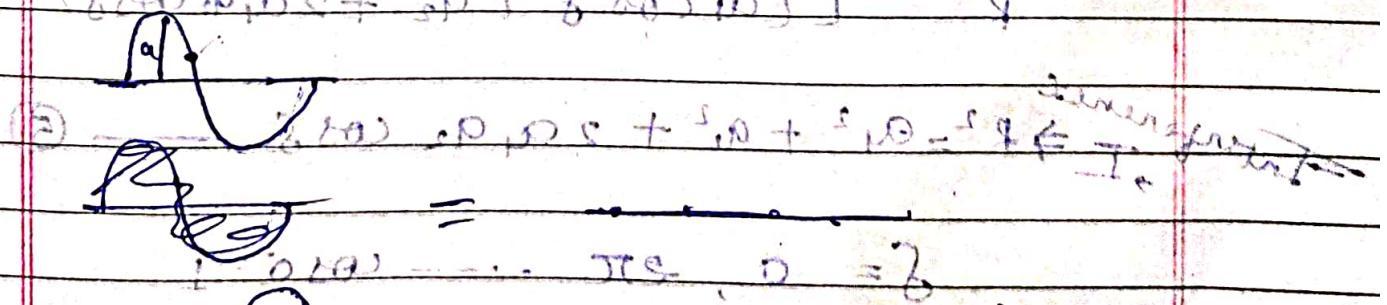
Phase difference between two waves are $0, \pi$

$$\Delta\phi = 0 \text{ or } \pi$$



(2) Destructive interference :-

$$\Delta\phi = \pi, 2\pi, 0, \pi + \pi, \pi + 2\pi, \dots$$



$$(+) \rightarrow (\pi, \pi) = \text{min. Int}$$

★ Superposition of waves :-

$$y_1 = a_1 \sin(\omega t + \delta) \quad \text{--- (1)}$$

for now out will come to find earth

$$y_2 = a_2 \sin \omega t \quad \rightarrow \text{filament}$$

add, synthesis, sum = minimum distance

$$y = y_1 + y_2 \quad \text{for filament translation}$$

above to find amplitude & phase

$$y = a_1 [\sin \omega t \cos \delta + \cos \omega t \sin \delta] + a_2 \sin \omega t$$

$$y = a_1 \sin \omega t \cos \delta + a_2 \sin \omega t + a_1 \cos \omega t \sin \delta$$

$$y = \sin \omega t [a_1 \cos \delta + a_2] + \cos \omega t (a_1 \sin \delta)$$

$$(x, 0), \text{now} \quad \text{Assume}, a_1 \cos \delta + a_2 = R \cos \theta \quad \text{--- (3)}$$

$$a_1 \sin \delta = R \sin \theta \quad \text{--- (4)}$$

$$\text{therefore } y = \sin \omega t \cos \theta + \cos \omega t R \sin \theta \\ = R [\sin \omega t \cos \theta + \cos \omega t \sin \theta]$$

$$y = R [\sin(\omega t + \phi)] \quad \text{--- (2)}$$

$$R^2 = [(a_1^2 \cos^2 \delta + a_2^2 + 2a_1 a_2 \cos \delta) + a_1^2 \sin^2 \delta]$$

$$\text{Interference, I} \Rightarrow R^2 = a_1^2 + a_2^2 + 2a_1 a_2 \cos \delta \quad \text{--- (5)}$$

$$\delta = 0, 2\pi, \dots \cos 0 = 1$$

minimum

$$\text{Intensity, } I_{\text{max}} = (a_1 + a_2)^2 \quad \text{--- (6)}$$

$$\delta = \pi, 3\pi$$

$$I_{\text{min}} = (a_1 - a_2)^2 \quad \text{--- (7)}$$

Coherent source:- phase difference is constant with time.

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Conditions for interference of light:

1. Amplitude of waves should be same. \Rightarrow $a_1 = a_2$, $I_{max} = (a_1 + a_2)^2 = 4a^2$ Bright $I_{min} = (a_1 - a_2)^2 = 0$ Dark

2. Source should be coherent. Intensity min.

3. Source should be monochromatic.

1 \rightarrow for becoming perfect interference pattern amplitude should be same.

2 \rightarrow Coherent source:- Phase difference is constant with time.

If we use coherent source then we get sustained interference pattern.

3 \rightarrow If we use chromatic source in interference of light then colored pattern will form and it get overlapped.

2) wave off set vary - λ (wave length)

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Young's double slit experiment :-

→ young's double slit experiment.
first demonstration of interference
of light.

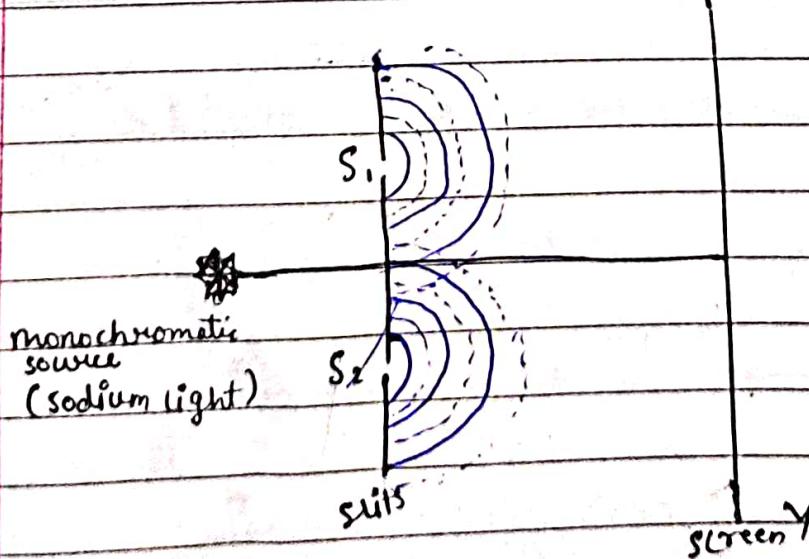
→ It consist monochromatic source
of sodium light, slits and screen.

→ Slits s_1 and s_2 and screen.

→ Sodium light when passes through
slits s_1 and s_2 for alternate place

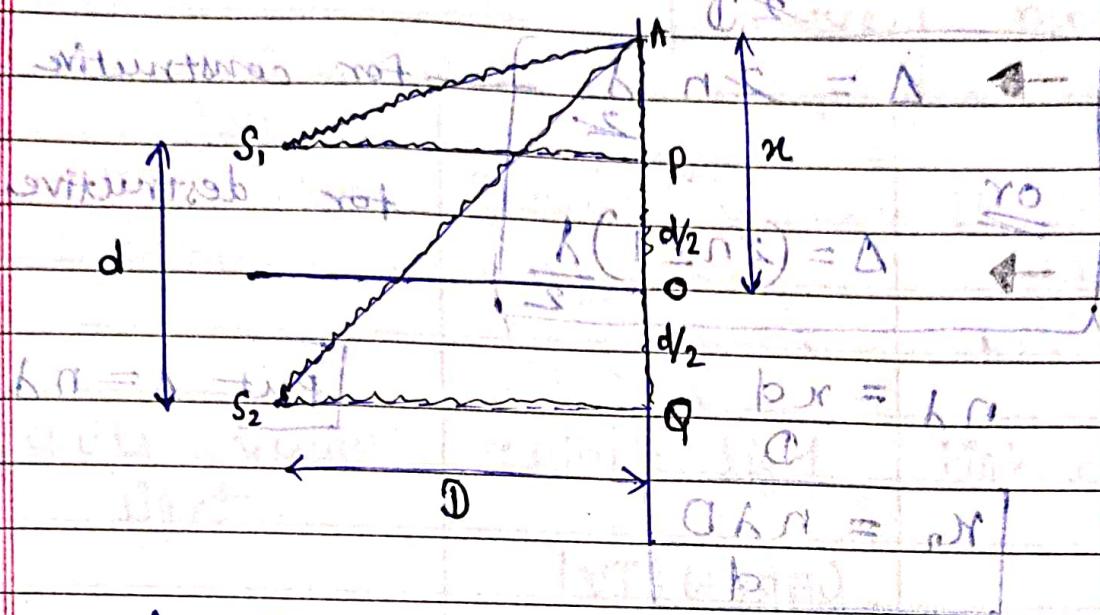
the bright fringes.

→ We can observe interference pattern
and can determine wavelength of
light with the help of observation



#

Derivation for fringe width.



$$\Delta = S_2 A - S_1 A \quad \text{In } \Delta S_1 A P.$$

$$S_1 A^2 = S_1 P^2 + A P^2 \quad \text{OK} (1+n)$$

$$= D^2 + (n - d/2)^2$$

$$= D^2 + \left[n^2 + d^2/4 - 2nd \right] \quad \text{OK} = n^2$$

$$= D^2 + n^2 + d^2/4 - nd.$$

$$(Nth binomial) \quad 8 = n - 1, n$$

$$S_2 A^2 = S_2 Q^2 + Q A^2$$

$$= D^2 + (n + d/2)^2 \quad \text{OK} = s$$

$$= D^2 + \left[n^2 + d^2/4 + 2nd \right].$$

$$= D^2 + n^2 + d^2/4 + nd. = k$$

$$S_2 A^2 - S_1 A^2 = (S_2 A + S_1 A)(S_2 A - S_1 A)$$

$$[(D^2 + n^2 + d^2/4 + nd) - (D^2 + n^2 + d^2/4 - nd)] = 2nd$$

$$S_1 A \approx S_2 A \approx S_1 P \approx S_2 Q \approx 0$$

$$\Delta = \text{the } 2\text{nd diff. in } \text{path difference} \quad \textcircled{1}$$

$$\rightarrow \Delta = 2n \frac{d}{2} \quad \text{for constructive}$$

or

$$\rightarrow \Delta = (2n \pm 1) \frac{\lambda}{2} \quad \text{for destructive}$$

$$n\lambda = nd$$

$$\boxed{\text{put } d = n\lambda}$$

$$\boxed{n_1 = n_2 D} \quad \textcircled{1}$$

$$(A_{12} - A_{22}) - (A_{12} + A_{22}) = A_{12} - A_{22}$$

$$n_{n+1} = (n+1) \lambda D - (A_{12} + A_{22}) = A_{12} - A_{22}$$

$$n_{n+1} - n_n = \lambda D$$

$$n_{n+1} - n_n = \beta \quad (\text{fringe width})$$

$$\beta = \frac{\lambda D}{D} \left(\frac{s_{12} - s_{22}}{s_{12} + s_{22}} \right) =$$

$$\boxed{\lambda = \frac{\beta D}{D + \beta s_{12} + s_{22}}} \quad \textcircled{3}$$

$$(A_{12} - A_{22}) (A_{12} + A_{22}) = A_{12} - A_{22}$$

$$\Delta OS = [(b_n - p)(s_b + s_n + s_C) - (b_n + p)(s_B + s_N + s_C)]$$

$\textcircled{1} \otimes \textcircled{2} \otimes \textcircled{3} \otimes A_{12} \otimes A_{22}$

Mono chromatic source	chromatic source	Highly monochromatic source
Sodium vapour lamp	Mercury vapour lamp	He-Ne laser
emits yellow light	White light (VIBGYOR)	Pink red color
D ₁ Line 5890 Å	4000° to 7800 Å	6328 Å
D ₂ Line 5896 Å		Wavelength
Average wavelength		
5893 Å		
610.387 nm		
transit. in air	transit. in vacuum	
transit. in glass	transit. in air	

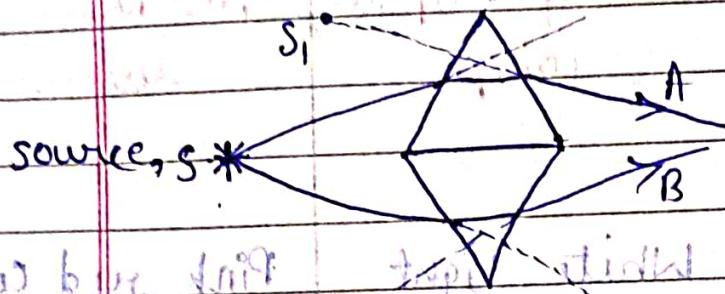
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13/04/23

(1) division of wave front.
(2) division of amplitude.

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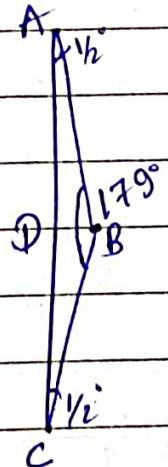
Types :-

(1) Division of wave front :-



(Biprism IV)

Biprism is a combination of two point sources joined above to a base, its obtuse angle is about 179° and other two acute angles are of $\frac{1}{2}^\circ$.



Biprism is used to divide source 'S' into 's' & 's'', where 's' and 's'' are coherent slits or images of the 'S' (source).

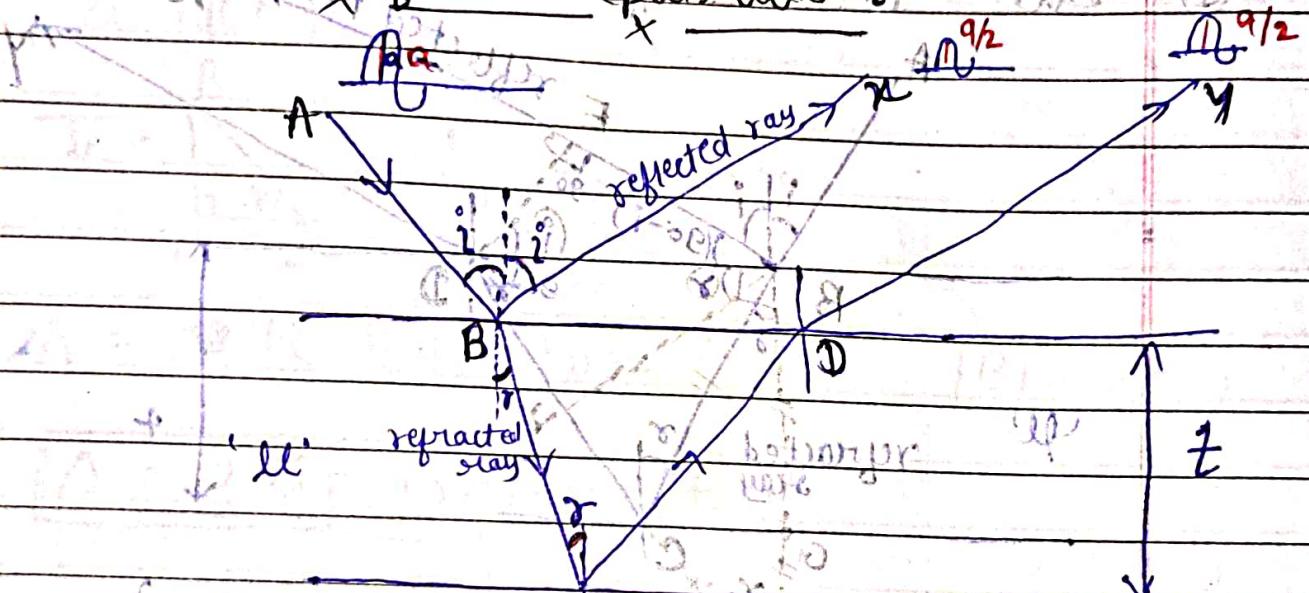
→ Experiment based on division of wave front is Fresel's Biprism experiment.

→ A source (wavefront) divides into 's' and 's'' by means of an optical device.

Prism or biprism based on deviation of light.

(2)

Division of amplitude



→ When a beam of light AB, incident on the surface of a thin film, it divides into two beams in different directions (BX & BY). After some time they travel in same direction, and $as = BX$ and DY (where as of same amplitude and nearly parallel, divisions of amplitude) takes place.

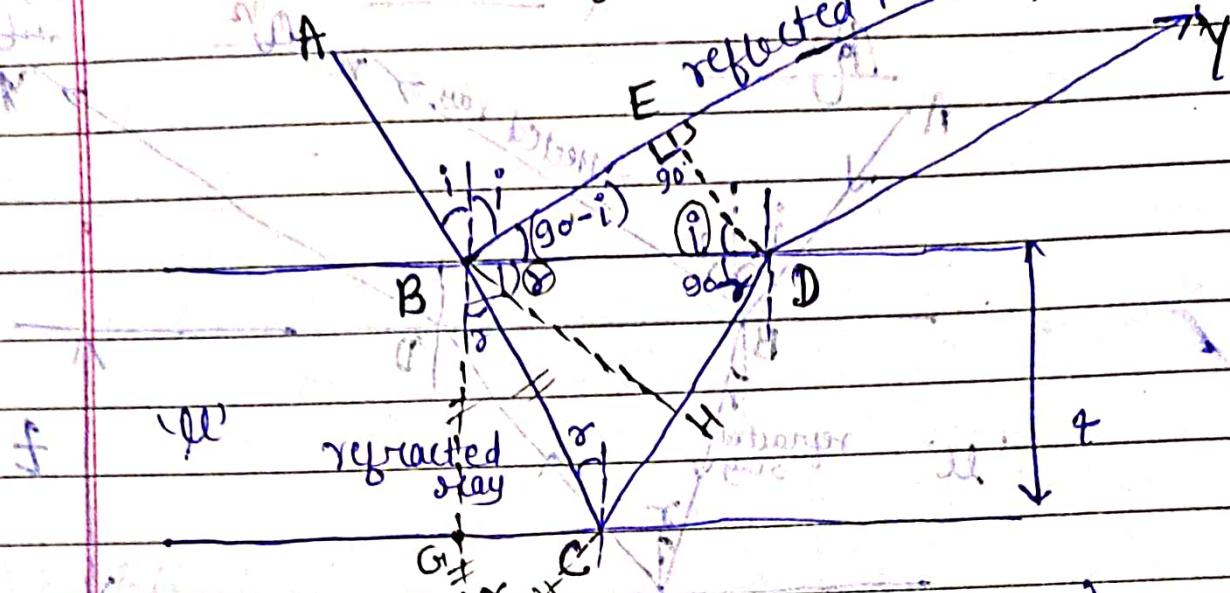
$$\textcircled{S} \rightarrow as = BX = n_1(n_2 + n_3) d = \Delta$$

$$\therefore (nd)n = \Delta \quad \text{or} \quad n_1(n_2 + n_3) d = \Delta$$

$$\textcircled{D} \rightarrow n_1 d = (n_2 + n_3) \Delta = \Delta$$

Interference of light in thin film

(1) Due to reflected light



$$(BC + CD)_{\text{film}} + DY_{\text{air}} - (BE + EN)_{\text{air}}$$

$$\Delta_{\text{air}} = (BC + CD)_{\text{film}} - BE_{\text{air}} \quad \text{--- (1)}$$

From diagram, $DE \parallel BX$. And $EN = DY$ (construction)

$$CD \text{ produces back side} \quad BG = GF, \quad BF = 2t$$

$$BH \perp CD$$

$$\Delta = \alpha (BC + CD)_{\text{air}} - BE_{\text{air}} \quad \text{--- (2)}$$

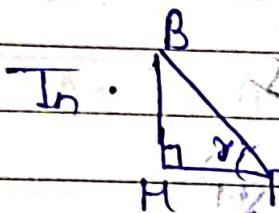
$$\alpha = \frac{\sin i}{\sin r} \quad \frac{BE}{BG} = \frac{DH}{BD} \quad BE = \mu(DH), P$$

$$\Delta = \alpha (BC + CD) - \mu DH \quad \text{--- (3)}$$

$$\Delta = EI [BC + CO - OH]$$

$$\Delta = EI [CF + DR + HC - DH]$$

$$\Delta = EI [FH]$$

 I_D I_D

$$\Delta = EI [BF] \cos r \quad [BF = 2t]$$

$$\boxed{\Delta = 2EI t \cos r} \quad \text{④④}$$

practice diagram

$$\textcircled{1} \rightarrow \sin \theta + \sin(\theta + \alpha) = \Delta$$

$$\textcircled{2} \rightarrow \sin \theta + \sin(\theta + \alpha) 10 = \Delta$$

$$\frac{EI}{EI} \frac{3I/72}{EI/72} - \frac{\sin \theta}{\sin 2} = 10$$

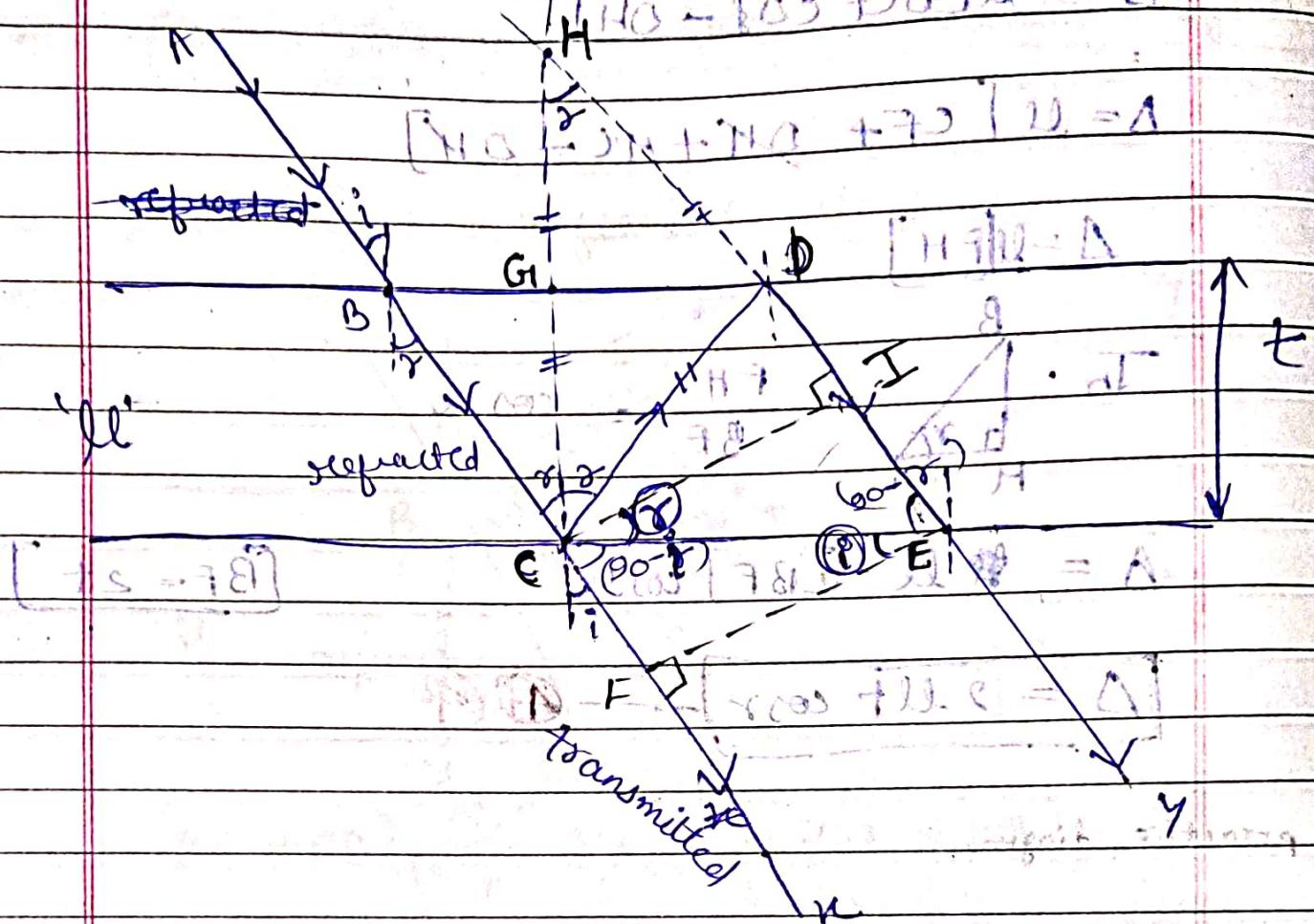
$$\textcircled{3} \rightarrow (3I/10 = 7)$$

$$(3I)u + (3\alpha + \beta)u^2 = \Delta$$

②

Due to transmitted light

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$$EF \perp CX; EY = FX$$

produce DE in back side as $CD = DH$,
 $HC = 2t$

$$\Delta = (CD + DE)_{\text{film}} + CF_{\text{air}} - ①$$

$$\Delta = ll (CD + DE)_{\text{air}} + CF_{\text{air}} - ②$$

$$ll = \frac{\sin i}{\sin r} = \frac{CF/CE}{EI/CE} = \frac{CF}{EI}$$

$$(F = ll(IE)) - ③$$

$$\Delta = ll(CD + DE) + ll(IE)$$

$$\Delta = ll (\cot D + \cot E + \cot H)$$

$$\Delta = ll (DH + DI + IE - IC)$$

$$\Delta = ll (DH + DI)$$

$$\Delta = ll (HC)$$



$$\text{CJH}, \frac{HI}{HG} = \cos \alpha$$

$$HC = 25$$

$$\Delta = ll (HC) \cos \alpha.$$

$$\Delta = 2ll + \cos \alpha.$$

Practice diagram

O due to wedge shaped film (non-parallel)

$$(S\Gamma \rightarrow E\Gamma + IC + BG) \downarrow \text{A}$$

$$I = (i + H\alpha) \cdot D = A$$

$$(i + H\alpha) \cdot D = A$$

$$-C(H) = -TH \cdot HD \quad \text{or} \quad C(H) = TH \cdot HD$$

$$+ S \rightarrow N$$

$$-C(H) = (i + H\alpha) \cdot D = A$$

$$-C(H) = (i + H\alpha) \cdot D = A$$

$$-C(H) = (i + H\alpha) \cdot D = A$$

$$-C(H) = (i + H\alpha) \cdot D = A$$

$$-C(H) = (i + H\alpha) \cdot D = A$$

$$-C(H) = (i + H\alpha) \cdot D = A$$

$$-C(H) = (i + H\alpha) \cdot D = A$$

$$\Delta = (Bc + (D)_{\text{film}} + BE_{\text{air}}) \rightarrow \text{Eqn } ①$$

$$= \mu (Bc + (D)_{\text{air}} - BE_{\text{air}}) \rightarrow \text{Eqn } ②$$

$$ll = \frac{\sin i}{\sin r} = \frac{BE / BD}{BH / BD}$$

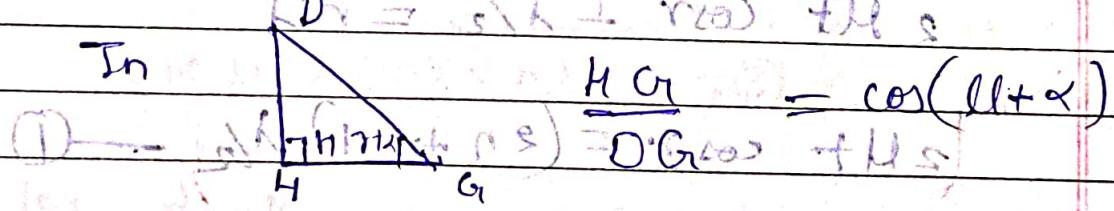
$$BE = \mu BH \rightarrow \text{Eqn } ③ = A \cdot \text{Hib} \cdot \text{Hdg} \quad \text{Eqn } ④$$

$$\Delta = \mu \rho_i (Bc + (D)) - \mu BH \quad \text{Eqn } ⑤$$

$$= \mu ((Bc + (D) - BH))$$

$$= \mu E_{\text{BA}} + H_c + (G_i - BH)$$

$$D = ll H G_i$$



$$\Delta = \mu Hc, \quad Hc = D \cdot \cos(\alpha + \theta)$$

$$\therefore \Delta = \mu D (1 + \mu \tan(\theta + \alpha)) + \mu S$$

$$\boxed{\Delta = 2 \cdot \mu \cdot \cos(\theta + \alpha) + \mu S} \quad \text{Eqn } ⑥$$

* show that results for Δ in reflected and transmitted light are complementary

$$\text{Ansatz: } \Delta = \pi(n - 1) + \varphi$$

Due to reflected light.

$$\begin{array}{c} \text{Ansatz: } \Delta = \pi(n - 1) + \varphi \\ \text{Ansatz: } \Delta = \pi(n - 1) + \frac{\pi}{2} \end{array}$$

① Diagram

$$\text{② Path diff. } \Delta = 2nl\sin\theta = 180^\circ$$

③ In case of reflected light, a phase change of π or $\lambda/2$ occurs.

or

$$\boxed{\Delta = 2nl\sin\theta + \lambda/2}$$

$$(n-1)l\sin\theta + \lambda/2 = k\lambda$$

④ for bright

$$x \quad \Delta = k\lambda$$

$$2nl\sin\theta + \lambda/2 = n\lambda$$

$$(n+1)l\sin\theta = (2n+1)\lambda/2 \quad \text{--- (1)}$$

⑤ for dark: $n\lambda - (n+1)\lambda/2 = \Delta$

$$2nl\sin\theta + \lambda/2 = (2n+1)\lambda/2$$

or

$$\boxed{2nl\sin\theta + \lambda/2 = n\lambda} \quad \text{--- (2)}$$

selected
Elementary

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Due to transmitted light.

① Explain and draw diagram. (Board IT)

② $\Delta = \ell n t \cdot \cos r$ (IT) (Diagram)

2. small normal angle between two parallel rays of light (IT)

③ In case of transmitted light phase change of π (or in same phase) occurs it means no change.

$$\ell n t \cdot \cos r = \Delta$$

④ Diagram for bright fringes (IT)

$$\ell n t \cdot \cos r = n \lambda \quad (3)$$

for dark.

$$2 \ell n t \cdot \cos r = (n \pm 1) \lambda/2 \quad (4)$$

The diff. in path length = $\lambda/2$. (obstruction)

Ans. glass reflection for bright most

as nothing has much ed

prism to make for most

prism is not much an error

* Newton's Ring Experiment:

- It is based on phenomena of interference of light.
- Its type is division of amplitude.
- When a plano convex lens is placed of large focal length is placed it over the glass plate.
- Convex surface of the plano convex lens is towards the glass plate.
- Then an air film is formed between convex surface and upper surface of the glass plate.
- At the point of contact of thickness of air film is zero. And it gradually increases towards the outside. (wedge-shaped film)
- From point of contact, circles can be drawn. and pattern in form of circular or ring, known as Newton's ring.

$$99 \times (f_C - nD) = R$$

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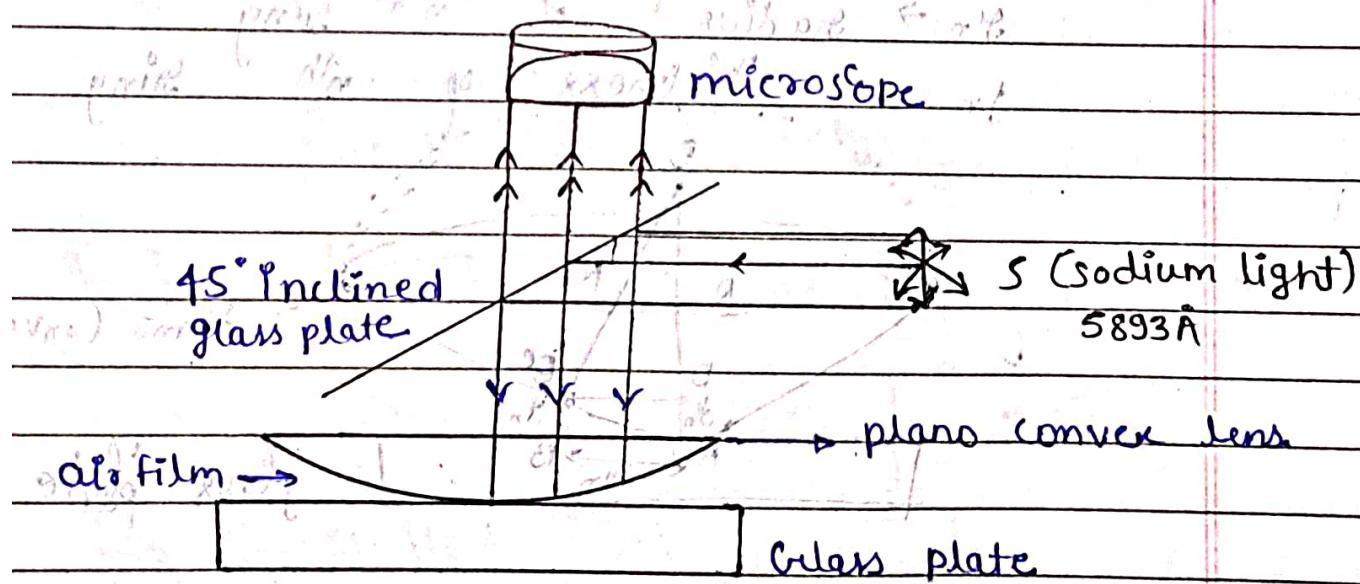
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If we use chromatic source in place of sodium light (monochromatic source), then few coloured rings observed and then forget overlap.

Experimental arrangement:

It consists of plano convex lens and glass plate, monochromatic source (sodium light) 5893 Å.

45° inclined glass plate on a microscope.



Division of amplitude:

$$\begin{aligned}
 & \text{Div. of amp.} : f(A) \quad f(B) \\
 & \text{Div. of amp.} : f(A) + f(B) \\
 & L \text{ at } D = f(A) + f(B) \\
 & \text{Div. of amp.} : f(A) + f(B) = f(D)
 \end{aligned}$$

$$D_n^2 = 4 R n \lambda$$

$$\lambda = \frac{D_{n+p}^2 - D_n^2}{4 PR}$$

where, D_{n+p}^2 is square of diameter of $(n+p)^{th}$ ring. $\lambda = \frac{(D_{n+p})^2 - (D_n)^2}{4 PR} = \frac{R \Delta C}{4 P} = \lambda \Delta$

D_n^2 is ——————
 p is integer, and it is difference
— of $(n+p)^{th}$ and n^{th} ring.

R is radius of curvature of
— plane convex lens.

In Newton's ring experiment the diameters of 4th and 12th dark rings are 0.4 cm and 0.7 cm respectively. Deduce the direct diameters to 20th ring.

Given,

$$D_4 = 0.4\text{ cm}$$

$$D_{12} = 0.7\text{ cm}$$

formula used

$$\lambda = \frac{D_{n+p}^2 - D_n^2}{4 PR} \text{ if ring no. is } 20$$

$$k \propto = \cos \theta + \sin \theta$$

$$\lambda = D_{12}^2 - D_4^2 / 4 \times 8 \times R$$

$$k \propto = \pm \infty$$

$$\lambda R = (0.7)^2 - (0.4)^2 / 4 \times 8$$

$$R\lambda = 0.4$$

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$$R\lambda = 0.49 - 0.16 \text{ cm}^2$$

$$R\lambda = 0.0103$$

$$D_n^2 = 4R\lambda n\lambda = 4 \times 0.0103 \times 2(0+1) \text{ cm}^2$$

$$D_{20} = \sqrt{0.824} \text{ cm}^2$$

$$D_{20} = 0.908 \text{ cm}$$

from formula $D_{20} = \frac{4R\lambda n\lambda}{(n+1)^2}$ for refractive index

Determination of RI (n) of a liquid which is introduced in between convex surface and upper surface of glass plate.

$$n_1 - n_2 = n\theta$$

air - liquid

for an air film $n_1 = 1.00$, $\cos r = 1$

$$2lt \cos r = n\lambda$$

$$2lt_n = n\lambda \frac{8 \times 8 \times 4}{8 \times 8 \times 4} = 4\lambda$$

$$[D_n^2]_{\text{air}} = (4R\lambda n\lambda)^2 (F.O) = 8\lambda$$

$$n_{\text{air}} = 1$$

$$n_{\text{water}} = 1.33 = 4/3$$

$$n_{\text{glass}} = 1.5$$

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$$\mu_{\text{fringe}} = \frac{\lambda}{2} n_{\text{air}}^2 \sin^2 \alpha$$

$$[\Delta n^2]_{\text{liquid}} = 4Rn^2 - \textcircled{2}$$

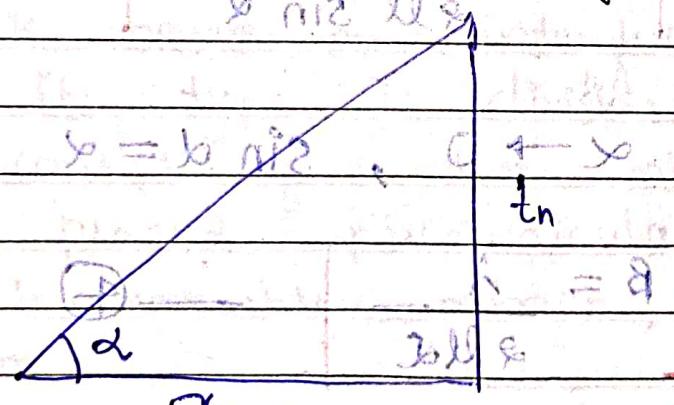
$$[\Delta n^2]_{\text{liquid}} = [\Delta n^2]_{\text{air}}$$

$$\lambda (1 + \mu) = 1.6 \lambda$$

$$\mu = [\Delta n^2]_{\text{air}}$$

$$[\Delta n^2]_{\text{liquid}} = (1 + \mu) \lambda$$

→ Establish relation between β (fringe width) and α (angle of wedge)



$$\tan \alpha = \frac{t_n}{n}$$

$$\tan \alpha = \frac{t_n}{n} \quad \text{where } n = \lambda$$

$$m \sin \theta = \lambda \cos(\theta + \alpha) = \lambda \cos \theta - \textcircled{1}$$

$$1 = \lambda$$

$$m \sin \theta \tan \alpha \cos(\theta + \alpha) = F m \lambda^2 - \textcircled{2}$$

$$2 m \sin \theta \tan \alpha \cos \alpha \lambda^2 = \lambda$$

$\theta = 0^\circ$ for Unormal incidence

$\perp = \text{real}$

$$\lambda P = GE - I = \omega ll$$

$$E - I = \omega ll$$

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$$2 ll n_n \sin \alpha \times \frac{\cos \alpha}{\sin \alpha} = n \lambda$$

$$2 ll n_n \sin \alpha = n \lambda$$

$$\textcircled{2} \quad \frac{n_{n+1}}{n_n} = \frac{\sin \alpha}{\sin \alpha}$$

$$n_n = \frac{n \lambda}{2 ll \sin \alpha}$$

$$\frac{n_{n+1}}{n_n} = \frac{\sin \alpha}{\sin \alpha}$$

$$n_{n+1} = \frac{(n+1) \lambda}{2 ll \sin \alpha}$$

$$\frac{n_{n+1}}{n_n} = \frac{\lambda}{\lambda}$$

$$n_{n+1} - n_n = \frac{\lambda}{\lambda}$$

(After solving) λ is constant λ is constant

$$\boxed{B = \frac{\lambda}{2 ll \sin \alpha}}$$

$$\alpha \rightarrow 0, \sin \alpha = \alpha$$

$$\boxed{B = \frac{\lambda}{2 ll \alpha}} \quad \textcircled{4}$$

Q find α if B is 3 mm and $ll = 1$ and

$$\lambda = 5893 \text{ Å}$$

$\alpha = 0.001$

Solve given,

$$B = 3 \text{ mm} = (3 + x) 10^{-3} \text{ cm} = 0.3 \text{ cm}$$

$$ll = 1$$

$$\lambda = 5893 \text{ Å} = 5893 \times 10^{-8} \text{ cm}$$

$$\alpha = \frac{B}{ll} = \frac{0.3}{1} \times 10^8 = 3 \times 10^7 \text{ rad}$$

and $\tan \alpha = 0$

$$\text{bnd} \cdot 1000 \alpha = 5.883 \times 10^{-8} + \frac{\text{cm}}{\text{cm}^2 \text{ radian}} \text{ at } 630$$

$$2 \times 1 \times 3 \times 10^{-1} \frac{\text{cm}}{\text{cm}^2 \text{ radian}} \text{ at } 630$$

$$\alpha = 9.8216 \times 10^{-5} \text{ radian}$$

multizinc no $\alpha = 9.8216 \times 10^{-5} \times 180^\circ \pi$

$$\alpha = 562.98 \times 10^{-5}$$

$$\alpha = (0.056)$$

* Michelson's Interferometer (MI):-

- It is based on interference of light.
- And its type is division of amplitude.
- It consists of two mirrors M_1 and M_2 placed perpendicular to each other.
- M_1 is moveable mirror, & M_2 is fixed mirror.
- Two glass plates P & Q , of same type place parallel to each other and 45° to the mirrors.
- One surface of glass plate 'P' is semi-silvered which is toward glass plate 'Q'.
- If source of monochromatic light with convex lens is used, roll of convex lens

is to make the \times beam parallel, and
a telescope $\times 1 \times 5 \times 10$.

→ Working ~~2018~~²⁰¹⁹ 01/02/2018.8 = 30

→ Light from source incident on semisilve surface, division of amplitude takes place.

\rightarrow Division of amplitude: $(280 \cdot 9) \Rightarrow$

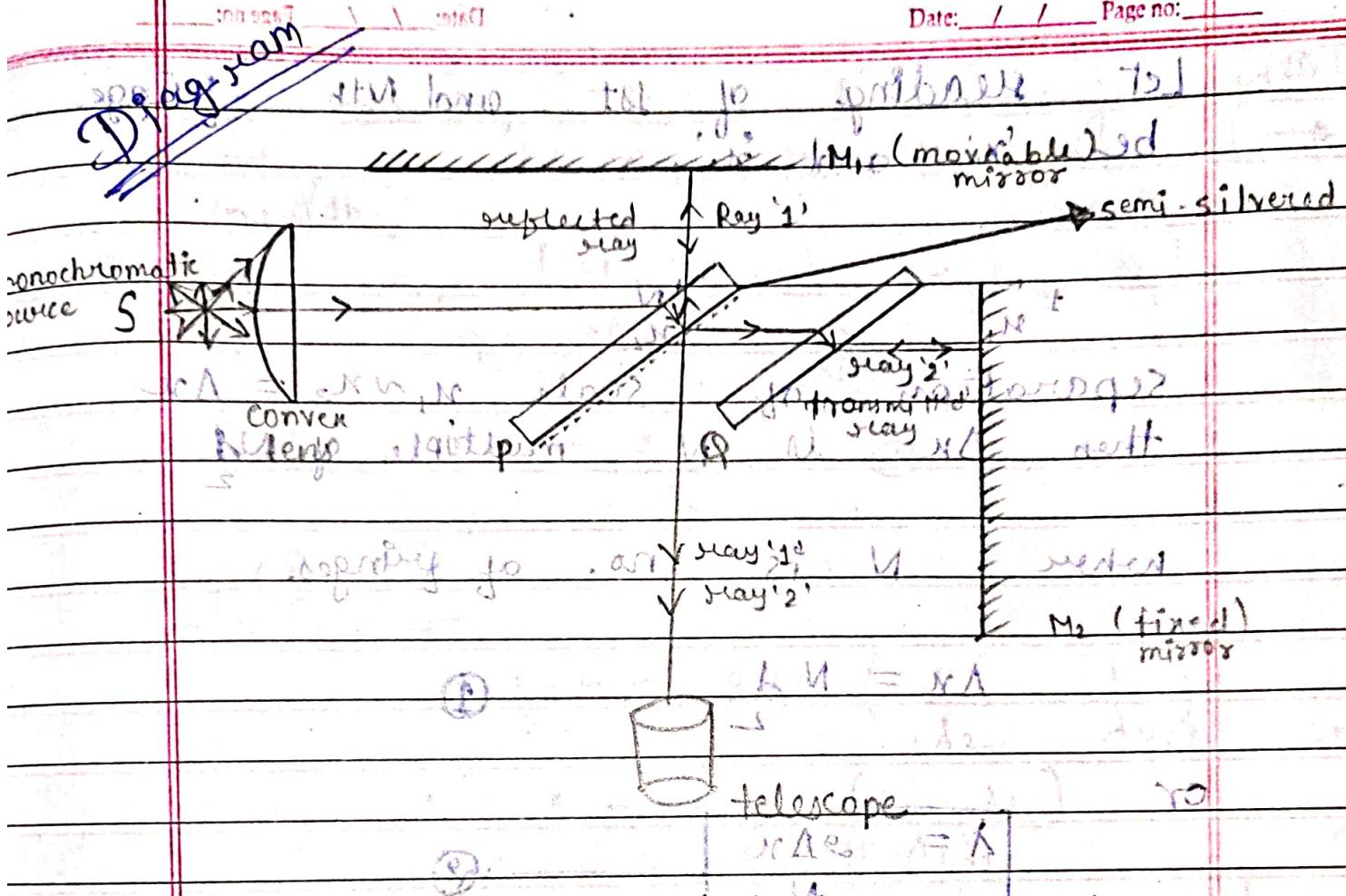
(IM) Maternidade - Ambulatório

total go nonfracture no hand 21 FF 4-
shortlimb go ambulib N right all bad 4-
long M fracture out go ambulib FT 4-
nonfracture at nonambulib hand 21 M 4-
hand 21 M L forearm olecranon 21 M 4-

Next card for P-19 is already ready out
but want to add at library info
mention int of 24

~~S'is' italq Nalp fo nofwd 200~~ 4-
~~nalp bndot si diitw bswrdz-inse~~
~~'n' italq~~

~~stet tipil illorenchonam go munk ET
and munk go half, buss i (red writing)~~



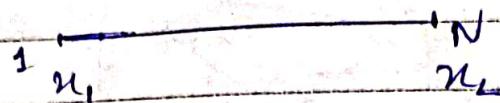
* Role of glass plate :- Q:- In absence of glass plate Q, ray '1' passes twice through glass whereas ray '2' does not even once. For out compensating the path difference in this two rays, a compensating glass plate of some type (some RI, dimension) introduced.

Applications :-

(A) Determination of wavelength λ of light source.

$$\text{R} = \frac{\lambda}{\sin \theta}$$

Let reading of 1st and Nth fringe be x_1 and x_N .



separation of scale $n, n_2 = \Delta n$
then, Δn is N multiple of $\frac{\lambda}{2}$

where N is no. of fringes.

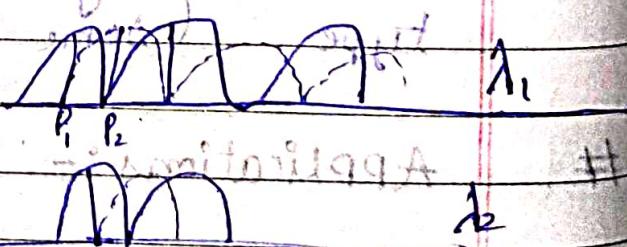
$$\Delta n = N \frac{\lambda}{2} \quad \textcircled{1}$$

or

$$\lambda = \frac{2\Delta n}{N} \quad \textcircled{2}$$

(B) Determination of change in wavelength

If source has two wavelengths λ_1 and λ_2 such as sodium light.



Top set of fringes due to scattering (A)

$$(P_1, P_2 - \text{scattering}) \cdot n (n+1)$$

$$+(1-n) = \Delta$$

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We can say 'F' if λ_2 formed wavelength $n^{(th)}$ fringe observed then therefore $\lambda_2 \rightarrow n(n+1)^{th}$. therefore, from eqn, $\lambda = \frac{2\Delta x}{N}$

$$n = \frac{2\Delta x}{\lambda} \quad (1)$$

$$[\lambda = \lambda_1 + (1-n) \lambda_2]$$

$$\text{and } n+1 = \frac{2\Delta x}{\lambda_2} \quad (2)$$

$$\text{eq. (2)} \rightarrow (1) \quad \text{After the calculation we get}$$

$$n + 1 - n = \frac{2\Delta x}{\lambda_1} (\lambda_1 - \lambda_2)$$

$$1 = \frac{2\Delta x}{\lambda_1} (\lambda_1 - \lambda_2)$$

$$\lambda_1 - \lambda_2 = \frac{\lambda_1 \lambda_2}{2\Delta x}$$

$$2\Delta x = 1.2 - 9.2$$

$$\text{or } \Delta \lambda = \frac{\lambda_1 \lambda_2}{1.2 - 9.2} \quad (3)$$

$$\lambda_1 \approx \lambda_2, \text{ then } \frac{\lambda_1 \lambda_2}{1.2 - 9.2} = \frac{\lambda^2}{1.2 - 9.2} = \Delta$$

$$\Delta = \frac{\lambda(1.2 - 9.2)}{2\Delta x} \quad (4)$$

$$\Delta = \frac{1.2 - 9.2}{2\Delta x} = \frac{1.2 - 9.2}{2 \times 10^{-3}} = \Delta$$

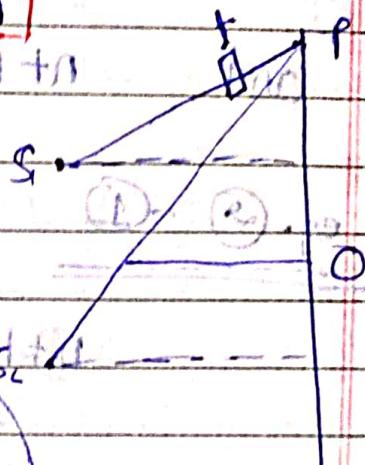
$$\Delta = (\mu - 1)t$$

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(c) Determination of 't' (thickness) of glass plate which is introduced in between one path of interference fringes.

$$(\mu - 1)t \pm N\lambda$$

$$N\lambda = t(\mu - 1)$$



In MI, ray sh passes twice

$$(\mu - 1)t = 2N\lambda$$

$$S_2P - S_1P = \Delta$$

$$S_2P = (S_1P + t)_{\text{air}} + t_{\text{film}}$$

$$= (S_1P + t)_{\text{air}} + \mu t$$

$$S_1P = S_1P + (\mu - 1)t$$

$$\Delta = S_2P - S_1P$$

$$= S_2P - [S_1P + (\mu - 1)t]$$

$$\Delta = S_2P - S_1P - (\mu - 1)t \quad \text{in glass plate}$$

$$\Delta = S_2P - S_1P = \frac{n d}{D} \quad \text{--- (1)}$$

Types of fringes in MI

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Numericals-

- Q. 1 In MI 200 fringes cross the field of view when a moveable mirror displays through 0.0589 mm. Calculate wavelength of light. $\lambda = \frac{2 \Delta n}{N}$

- Q. 2 A glass plate of refractive index 1.5 is introduced normally in one of the path of light in MI which is eliminated by the wavelength of 5893 Å. Determine 't' of glass plate 500 dark fringes across the view.

$$t = \frac{N \lambda}{2 \Delta n}$$

$$t = \frac{200 \times 5893 \times 10^{-10}}{2(1.5 - 1)} = t$$

Solve - 1 Given,

$$N = 200 \text{ m}^{-1} \Rightarrow 200 \text{ m}^{-1} = \frac{1}{\Delta n}$$

$$\Delta n = \frac{1}{N} = \frac{1}{200} = 0.005 \text{ m}^{-1} \Rightarrow 0.005 \text{ m}^{-1} = \frac{1}{\Delta n} \quad [m^{-1} \Rightarrow 10^{-3} \text{ m}^{-1}]$$

$$\lambda = \frac{2 \Delta n}{N} = \frac{2 \times 0.005 \times 10^{-3}}{200} \text{ m}$$

$$\lambda = \frac{0.005 \times 10^{-3}}{200} \text{ m}$$

$$\lambda = 5890 \times 10^{-10} \text{ m}$$

$$\boxed{\lambda = 5890 \text{ Å}}$$

$$\{ 10^{-10} \text{ m} = 1 \text{ Å} \}$$

Solve - Q-2

$$2(11-1)t = N \lambda$$

$$\text{Solve } \frac{N}{2} = 1000 \text{ for } N \Rightarrow N = 2000$$

where \Rightarrow $\exists \forall x \exists y \exists z$ $\neg P(x) \wedge Q(y) \wedge R(z)$

$$\lambda = 5893 \text{ } \text{Å} = 5893 \times 10^{-8} \text{ cm}$$

$$7.1 \text{ m} \times 500 \text{ cm}^2 = 3550 \text{ cm}^3$$

(approximate value)

$$f = \frac{500 \times 5.893 \times 10^{-8}}{2 \times 0.5} \text{ cm}$$

$$t = 2.946500 \times 10^{-8} \text{ cm}$$

$$f = 0.0294 \text{ cm}^{-1} \text{ eV}^{-1}$$

$$x 20.0 = \text{mm} (220.0 = \text{m}) \quad \{ 1 \text{ mm} = 10 \text{ cm} \}$$

t = 0.294 mm

701X P820.0 X-8 - NA S = 2
002

$$\text{m} \stackrel{s=8}{=} 01 \times 8820.0 = 8$$

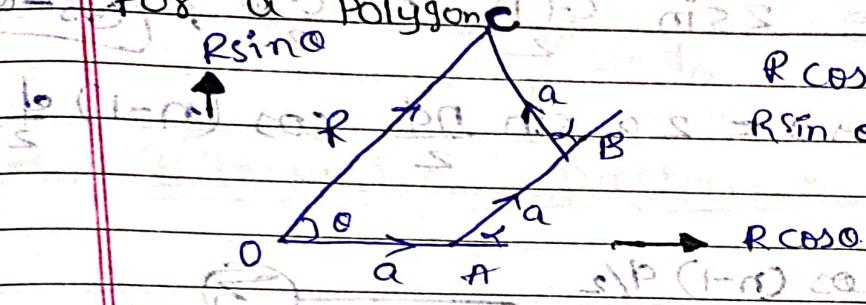
$$m^{01-01x0e8e} = k$$

$$\{ \lambda_1 = \mu^{01-01} \} \quad (\tilde{\lambda} \circ p_{\mathcal{B}} = \lambda)$$

$$\frac{(1+\alpha-\beta)b}{s} = \frac{b(1-\alpha)^2 + b}{s} = \frac{(1-\alpha)^2 b}{s} = \frac{(1-\alpha)^2 b}{s}$$

Derivation for resultant amplitude

for a Polygon



In a polygon, a is amplitude of each subslit (part) and d is common phase difference and R is resultant amplitude

$$R \cos \theta = a [1 + \cos d + \cos 2d + \dots + \cos(n-1)d] \quad (1)$$

$$R \sin \theta = a [\sin d + \sin 2d + \dots + \sin(n-1)d] \quad (2)$$

Multiply (2) by $\sin d/2$ on both the sides

$$2 \sin d/2 R \cos \theta = a [2 \sin d/2 + 2 \cos d \sin d/2 + 2 \cos 2d \sin d/2 + \dots + 2 \cos(n-1)d \sin d/2]$$

$$= \sin d/2 + (\sin 3d/2 - \sin d/2) + 2 \cos(n-1)d \sin d/2$$

$$= a [2 \sin d/2 + (\sin 3d/2 - \sin d/2) + \dots + (\sin 5d/2 - \sin 3d/2) + \dots + (\sin(n-3)d/2 - \sin(n-1)d/2)]$$

$$= a [2 \sin d/2 + (\sin 3d/2 - \sin d/2) + \dots + (\sin 5d/2 - \sin 3d/2) + \dots + (\sin(n-3)d/2 - \sin(n-1)d/2)]$$

$$= a [\sin d/2 + \sin(n-1)d/2]$$

$$\sin(C+D) = 2 \sin \frac{C+D}{2} \cos \frac{C-D}{2}$$

~~$$2 \sin \frac{d}{2} \cos \theta = 2 a \sin \frac{nd}{2} \cos \frac{(n-1)d}{2}$$~~

$$R \cos \theta = a \sin \frac{nd}{2} \cos \frac{(n-1)d}{2}$$

Similarly, if $\sin d/2$ has magnitude

$$(1) - \sin(\theta) = -ab \sin \frac{nd}{2} + b \sin \frac{(n-1)d}{2}$$

$$(2) - [a(n-1)d/2 + b(n-1)d/2]$$

Squaring ab eqn ③ & ④ then sum eqn ③ & ④

$$[a^2 n^2 + b^2 n^2 + 2ab n^2] = a^2 \sin^2 \frac{nd}{2} + \cos^2 \frac{(n-1)d}{2}$$

$$(8-a^2)n^2 + (8-b^2)n^2 = 8n^2 \text{ since } a^2 + b^2 = 1$$

$$a^2 \sin^2 \frac{nd}{2} + \sin^2 \frac{(n-1)d}{2}$$

$$+ [a^2 b^2 n^2 + b^2 n^2] = \sin^2 \frac{d}{2} + b^2 n^2$$

$$R^2 = a^2 \sin^2 \frac{nd}{2} + \cos^2 \frac{(n-1)d}{2} + a^2 b^2 n^2 + \sin^2 \frac{d}{2}$$

$$(a^2 b^2 n^2 - b^2 n^2) + \sin^2 \frac{d}{2} =$$

$$+ (a^2 b^2 n^2 - a^2 n^2) +$$

$$[a^2 b^2 n^2 + a^2 n^2] R^2 = a^2 \sin^2 \frac{nd}{2} + \cos^2 \frac{(n-1)d}{2} + \sin^2 \frac{(n-1)d}{2}$$

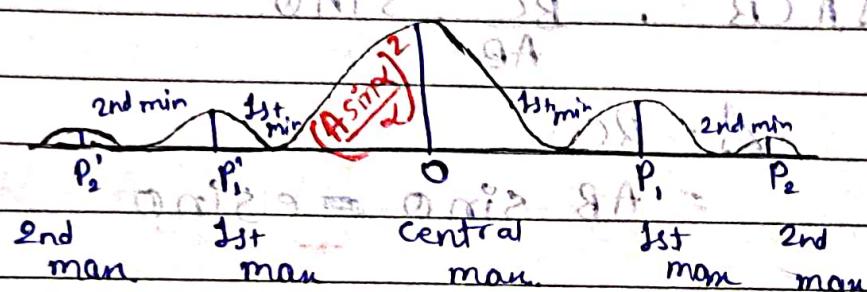
$$[a^2 b^2 (n^2 - 1) + a^2 n^2] R^2 =$$

$$R^2 = \frac{a^2 \sin^2 \frac{nd}{2}}{\sin^2 \frac{d}{2}} = \text{Intensity} \rightarrow (5)$$

$$R = \frac{a \sin(\pi d)}{2} \quad \text{for half wave} \quad \uparrow \quad \text{6}$$

at which $d = \lambda$, $R = \lambda$ or 98.1 nm

Diffraction pattern :-



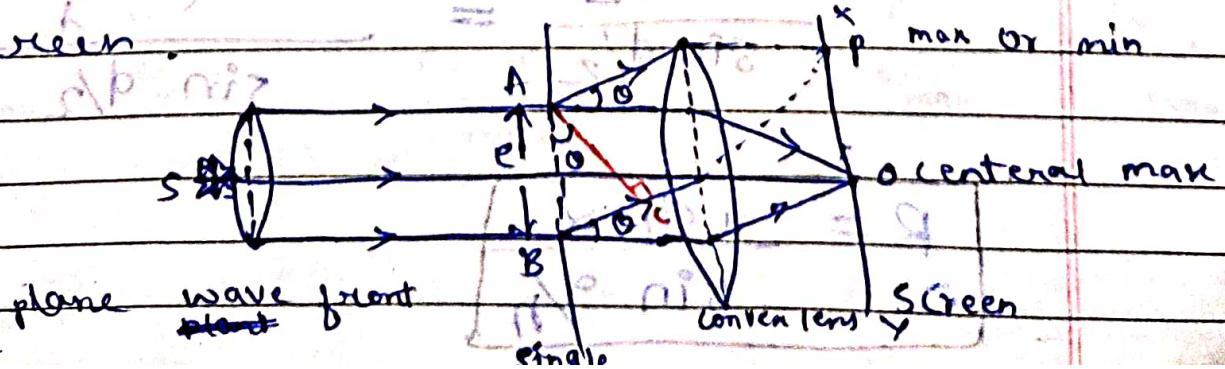
- (1) central principle max
- (2) secondary max. minima
- (3) — II — maxima

Home work
Distinguish b/w
interference
and diffraction
of light.

Definition
Diagram
Interfer-
ence
diffraction

Diffraction at Single slit :-

It based on Fraunhofer diffraction and it consist of plan wave front and a single slit of size λ and a converging lens and a screen.



When $\theta \uparrow$ then Intensity \downarrow

$AC \perp BP$ as $AP = CP$, AB slit divides in n equal parts

$$\Delta = BC$$

In $\triangle ACB$, $\frac{BC}{AB} = \sin \theta$.

$$\Delta = BC$$

$$= AB \sin \theta = e \sin \theta$$

Phase difference = $2\pi \Delta$

wild oscillations \rightarrow minimum intensity (i)

phase diff. $(AB)_{\text{min}} = 2\pi \times e \sin \theta$ (ii)

minimum phase \rightarrow maximum intensity (iii)

phase diff for 1-part = $\frac{2\pi}{\lambda} \times \frac{e \sin \theta}{n}$

$$d = \frac{2\pi}{\lambda} \times \frac{e \sin \theta}{n}$$

$$\frac{n d}{2} = \frac{\pi e \sin \theta}{\lambda} \rightarrow \alpha \quad (\text{Assume})$$

Now position $d/2 = \frac{\pi e \sin \theta}{\lambda n}$ on hand if
true \rightarrow α only go towards ii.

Using eqn for resultant amplitude.

$$R = a \sin \frac{\pi e \sin \theta}{\lambda n} = a \sin \left(\frac{2\pi}{\lambda} e \sin \theta \right)$$

$$\dim \text{reqd} \quad \sin d/2 = \sin d/2$$

$$R = a \sin \frac{\pi e \sin \theta}{\lambda n}$$

$$I = R$$

$$R^2 = I$$

where, R is an resultant amplitude of single slit
 I is Intensity.

Date: / / Page no:

$$R = a \sin \alpha$$

$$\frac{a}{n}$$

maximum $\rightarrow 0$
minimum $\rightarrow \pi$

$$\lim_{n \rightarrow \infty} \sin \frac{\alpha}{n} = \frac{\alpha}{n}$$

$$R = \alpha \rightarrow 0$$

$$(d = \text{slit width})$$
$$R = n a \sin \alpha$$

$$R = A \sin \alpha$$

(1)

where $A (=na)$ is amplitude of slit AB.

$na \Rightarrow$ no of parts
of amplitude

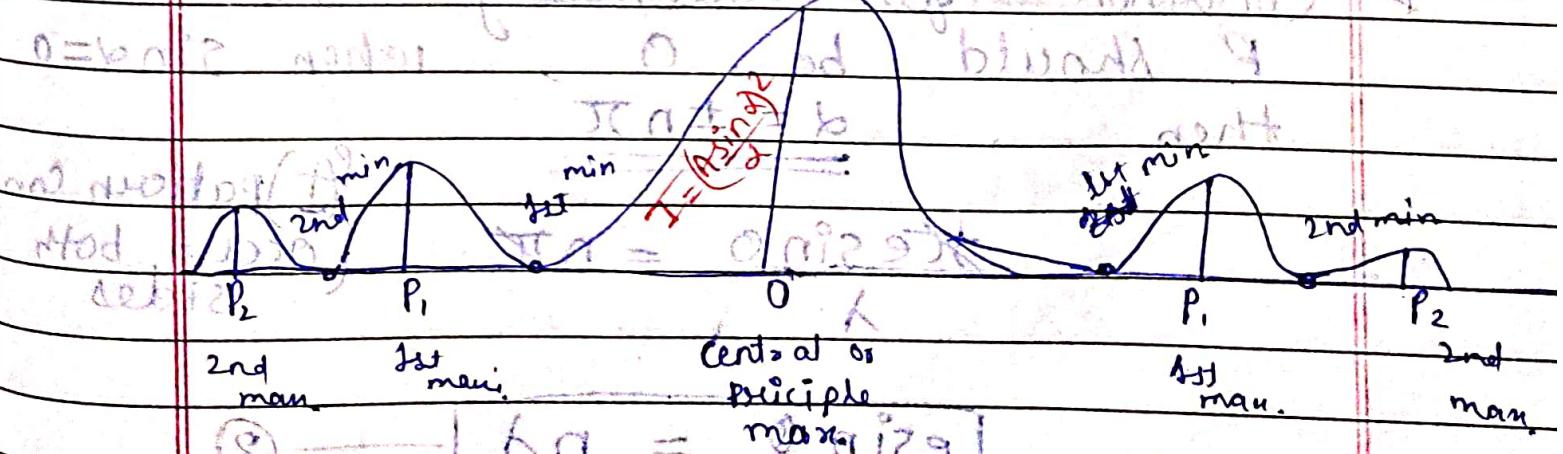
a = amplitude of 1-part

$I = R^2$ resultant amplitude of single slit

$$I = \left(\frac{A \sin \alpha}{\alpha} \right)^2$$

Diffracton pattern:-

Central maximum (principal maximum)



$$m = 1$$

$$\lambda = d \sin \alpha / m$$



$$\theta \approx \alpha = \lambda / D$$

Date: / / Page no: _____



Condition for central maxima
R should be maximum.

$$R = A^2 \sin^2 \alpha, \quad A + \alpha = 0$$

$$I = \left(\frac{A \sin \alpha}{\alpha} \right)^2 \Rightarrow \alpha \sin \alpha = A$$

or.

$$R = A \sin \alpha$$

at $\alpha = 0$

then R is to be substituted in

$$R = A \lim_{\alpha \rightarrow 0} \frac{\sin \alpha}{\alpha} = 1 \lim_{\alpha \rightarrow 0} \frac{\sin \alpha}{\alpha} = 1$$

$$\boxed{R = A}$$

$$\boxed{I = A^2}$$

Condition for secondary minima
R should be 0, when $\sin \alpha = 0$
then, $\alpha = \pm n\pi$

$$\text{so } \sin \alpha = n\pi$$

$$\boxed{\sin \alpha = n\lambda} \quad (2)$$

or

$$\lambda = \frac{\sin \alpha}{n} \quad (3)$$

(+) pattern occurs both sides

condition for secondary maxima

$\frac{dI}{d\alpha} = 0$ when maximum

$$\frac{d}{d\alpha} \left(A \sin \alpha \right)^2 = 0$$

$$A^2 \sin^2 \alpha = I_{\text{max}}$$

$$\Rightarrow A^2 \left[\frac{d}{d\alpha} (\sin \alpha)^2 \right] = 0 \quad \alpha = \frac{\pi}{2}, \frac{3\pi}{2}$$

$$\Rightarrow A^2 \sin \alpha \left[\frac{d}{d\alpha} \left(\frac{\sin \alpha}{\alpha} \right) \right] = 0$$

$$\Rightarrow 2A^2 \sin \alpha \left[\alpha \cos \alpha - \sin \alpha \right] = 0$$

$$\sin \alpha \neq 0, \text{ for } \alpha \cos \alpha - \sin \alpha = 0$$

because it is the condition of secondary minima $\sin \alpha = 0$

$$\alpha = \tan \alpha$$

(4)

Intensity decreases exponentially

Q.

Show that in single slit the relative intensity of successive maxima are nearly

$$1 : \frac{1}{2} : \frac{1}{6} : \frac{1}{21} \dots$$

$$\text{Soln} \Rightarrow I = \left(\frac{A \sin \alpha}{\alpha} \right)^2$$

$$\alpha = \frac{\pi r \sin \theta}{\lambda} \quad [r = \sqrt{x^2 + y^2}]$$

$$\theta = \sin^{-1} \left(\frac{y}{r} \right) \quad [r = \sqrt{x^2 + y^2}]$$

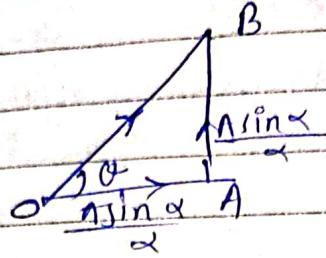
$$\text{or } \alpha = \pi n \frac{\lambda}{r} ; \quad \alpha = (n + \frac{1}{2}) \frac{\lambda}{r}$$

$$\alpha = 3\pi/2, 5\pi/2, 7\pi/2, \dots$$

$$I_1 = A^2 \left(\frac{\sin 3\pi/2}{3\pi/2} \right)^2 = A^2 \frac{4}{9\pi^2} = \frac{1}{9\pi^2/4}$$

$$I_{10} = A^2 \left(\frac{\sin 5\pi/2}{5\pi/2} \right)^2 = A^2 \frac{4}{25\pi^2} = \frac{1}{625\pi^2} = \frac{1}{61.68}$$

Double Slit :-



$$R^2 = a_1^2 + a_2^2 + 2a_1 a_2 \cos \delta$$

$$= \left(\frac{A \sin \alpha}{\alpha} \right)^2 + \left(\frac{A \sin 2\alpha}{\alpha} \right)^2 + 2 \left(\frac{A \sin \alpha}{\alpha} \right) \left(\frac{A \sin 2\alpha}{\alpha} \right) \cos \delta$$

$$= 2 \left(\frac{A \sin \alpha}{\alpha} \right)^2 + 2 \left(\frac{A \sin \alpha}{\alpha} \right)^2 \cos 2\delta$$

$$R^2 = (1 + \cos \delta) 2 \left(\frac{A \sin \alpha}{\alpha} \right)^2$$

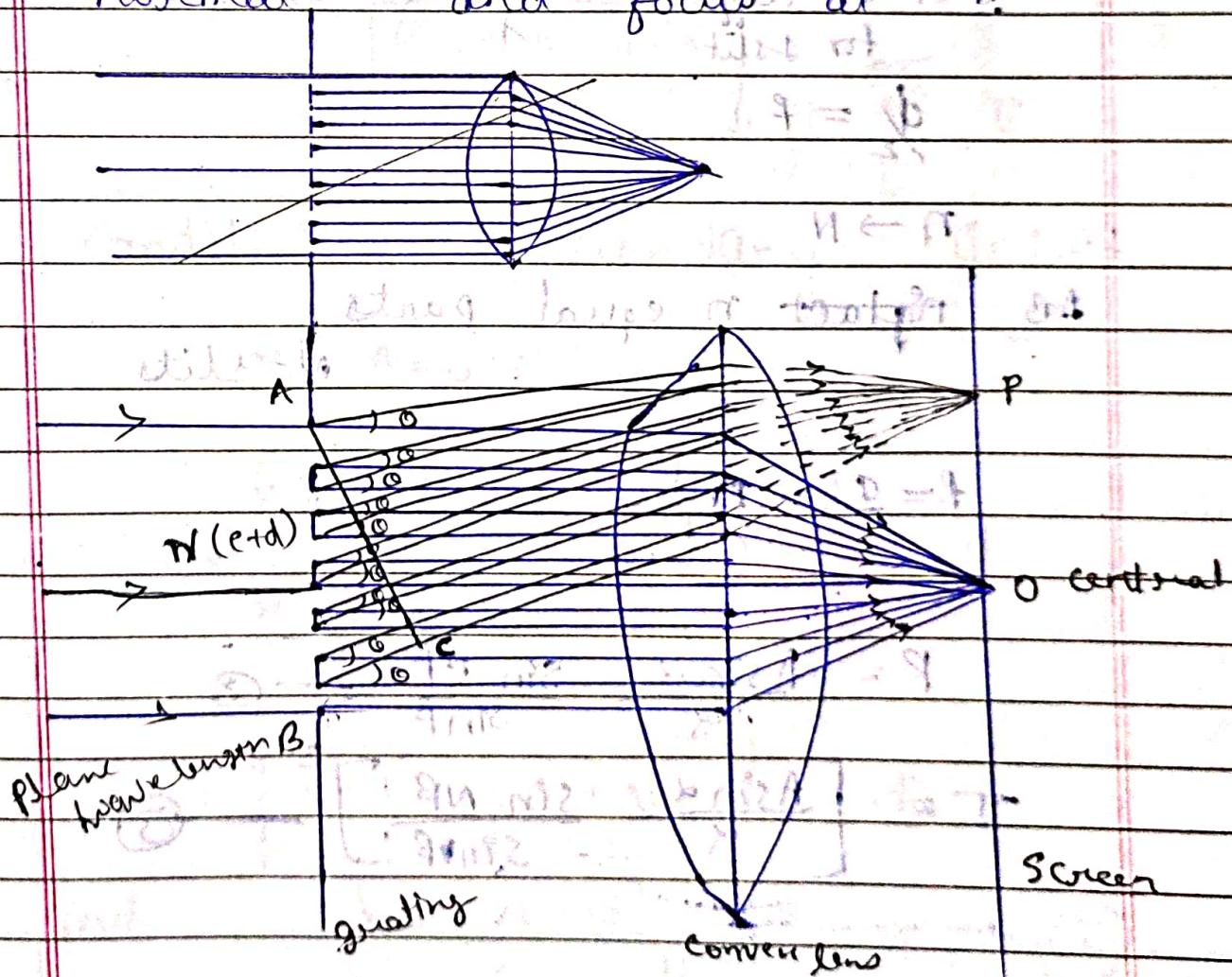
$$R = \sqrt{1 + \cos \delta} \times \sqrt{2} \times \left(\frac{A \sin \alpha}{\alpha} \right)$$

→ Fraunhofer diffraction at N-slits (grating)

Grating is larger no. of parallel slit.

It consists of plan wave front and grating of grating element $e+2$ ($AB = n$ times of $e+2$) and a convex lens and screen.

According to Huygen's Principle plan wave fronts travel normally and focus at 'o' and secondary wave fronts deviates its angle θ to the normal and focus at 'P'.



Theory:- In Young's double slit experiment

Path difference b/w AP and BP.

Path difference b/w AP and CP. (in prism)

$$\Delta = BC, \quad \frac{BC}{AB} = \sin \alpha$$



$$\Delta = ABS \sin \theta$$

$$\Delta = N(e+d) \sin \alpha \quad \text{--- (1)}$$

$$\text{Phase diff.} = \frac{2\pi}{\lambda} \Delta$$

Phase difference $= \frac{2\pi}{\lambda} N(e+d) \sin \alpha$

for AB polarization

$$d^* (\text{phase diff.}) = \frac{2\pi}{\lambda} (e+d) \sin \alpha$$

for g slit

$$\frac{d}{2} = \beta$$

$$n \rightarrow N$$

AB - reflect n equal parts

\sqrt{n} -slit

$$R = \frac{\alpha \sin n d \beta}{\sin d \beta}$$

$$R = \frac{A \sin \alpha}{\alpha} \frac{\sin N \beta}{\sin \beta} \quad \text{--- (2)}$$

$$T = \left[\frac{A \sin \alpha}{\alpha} \quad \frac{\sin N \beta}{\sin \beta} \right] \quad \text{--- (3)}$$

→ condition of first central minimum

$$\beta = \pi(e+d) \sin \theta$$

Then, $R = N A \sin \alpha$ (right) $\beta = 0^\circ$

$$R = A \sin \alpha \times \frac{\sin N\beta}{\sin \beta}$$

$$R = A \sin \alpha \times \frac{\sin N\beta}{N\beta} \times N\beta$$

$$R = N A \sin \alpha \times \frac{1}{1}$$

$$R = N A \sin \alpha$$

→ condition of secondary minima

$$\sin N\beta = 0, \quad R = 0$$

Then $\beta = n\pi$ ($n \in \mathbb{Z}$) $\Rightarrow \frac{\pi}{q_b} = n\pi$

or $\pi(e+d) \sin \alpha = n\pi$

$$(e+d) \sin \alpha = n\pi \quad \text{--- (4)}$$

And, $\lambda = \frac{(e+d) \sin \alpha}{n} \quad \text{--- (5)}$

Given no. ⑤ is required relation for wavelength of light called for diffraction at a grating.

where, $(e+d)$ \rightarrow grating element
and, $e =$ thickness of transparent part
 $d \rightarrow$ thickness of opaque.

$\alpha =$ angle of diffraction

$n =$ order of spectrum

(c) condition for secondary maxima

$$\frac{dI}{d\beta} = 0$$

$$I = \left[\frac{A \sin \alpha}{d} \cdot \frac{\sin N\beta}{\sin \beta} \right]^2$$

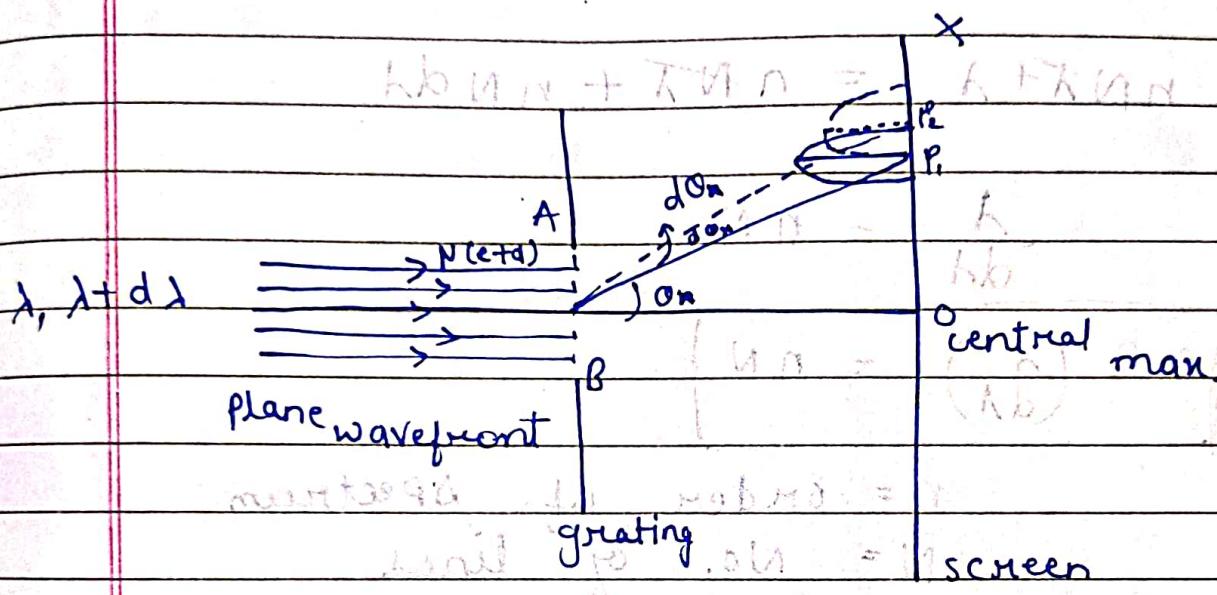
$$\frac{dI}{d\beta} = \left(\frac{A \sin \alpha}{d} \right)^2 \cdot \frac{d}{d\beta} \left[\frac{\sin N\beta}{\sin \beta} \right]^2$$

$$\frac{dI}{d\beta} = \left(\frac{A \sin \alpha}{d} \right)^2 \cdot \frac{N^2 \sin N\beta}{\sin^2 \beta} \times \cos N\beta$$

$$N^2 \sin N\beta = 0 \Rightarrow N^2 (b+2) = 0$$

$$N^2 (b+2) = d$$

→ Resolving power of a grating
 An ability of diffraction grating to separate or reduce two different closer or very closer wavelength λ and $\lambda + d\lambda$: $\frac{\sin \theta}{\sin (\theta - d\theta)} = 1 + \frac{d\lambda}{\lambda}$



If it consist of N lines, then

Equation for grating maxima

$$N(e+d) \sin \theta = nN\lambda \quad - \text{minima}$$

$$n(e+d) \sin \theta = (nN+1)\lambda \quad - \text{maxima}$$

According to Rayleigh criteria.

P_2 , max. for λ in direction onto

Similarly, P_1 , min. for $\lambda + d\lambda$

$$N(e+d) \sin \theta = (nN+1)\lambda \quad (1)$$

$$N(e+d) \sin\theta = n N_0 (\lambda + d\lambda) - ① \quad (1800)$$

from eqn ① & ②

$$(nN+1)_1 = nN(\lambda+d\lambda)$$

$$nN\lambda + \lambda = nN\lambda + nNd\lambda$$

$$\frac{d\lambda}{d\lambda} = nN$$

$$\text{R.P. } \left(\frac{d\lambda}{d\lambda} \right) = nN$$

n = order of Spectrum

N = No. of lines.

Q.1) A grating having 18000 LPIT, finds maximum order of spectrum if $\lambda = 6000 \text{ \AA}$

Solve =

$$(e+d) \sin\theta = n\lambda \quad , \quad n_{\max}, \quad \theta = 90^\circ$$

$$\text{and here } e + d = \lambda (1 + N_0) = 6000 \times (1 + 18000)$$

$$\frac{2.54 \text{ cm}}{18000} \sin 90^\circ = n \times 6000 \times 10^{-8} \text{ cm}$$

$$n = \frac{2.54 \text{ cm}}{18000} \times \frac{1 \text{ cm}}{6 \times 10^{-5} \text{ cm}}$$

$$n = 2.35$$

2nd order of Spectrum

SemiconductorSemiconductor

Material - Ge, Si

Types:- ① Intrinsic Semiconductor

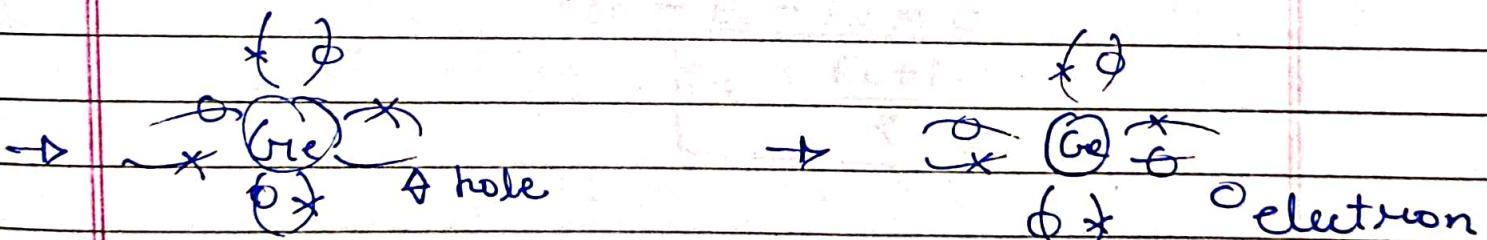
- pure material
- $n = p$
- as insulator at 0 K

② Extrinsic (doping)

P-type

N-type

→ Trivalent = Al, B → Pentavalent = N, Ph process



→ holes are majority charge carriers

→ electrons are majority charge carriers

→ $P \rightarrow$ excess

→ $N \rightarrow$ excess

Date: / / Page no: _____

type P = holes
type n = electrons

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- Fermilevel is in intrinsic semiconductor
- Fermilevel is in intrinsic semiconductor.
- Intrinsic semiconductor is also pure material

$$n = p$$

$$N_c e^{-(E_c - E_F)/kT} = N_v e^{-(E_F - E_v)/kT}$$

taking log on both sides

$$\frac{-(E_c - E_F)}{kT} = \log \frac{N_v}{N_c} - \frac{(E_F + E_v)}{kT}$$

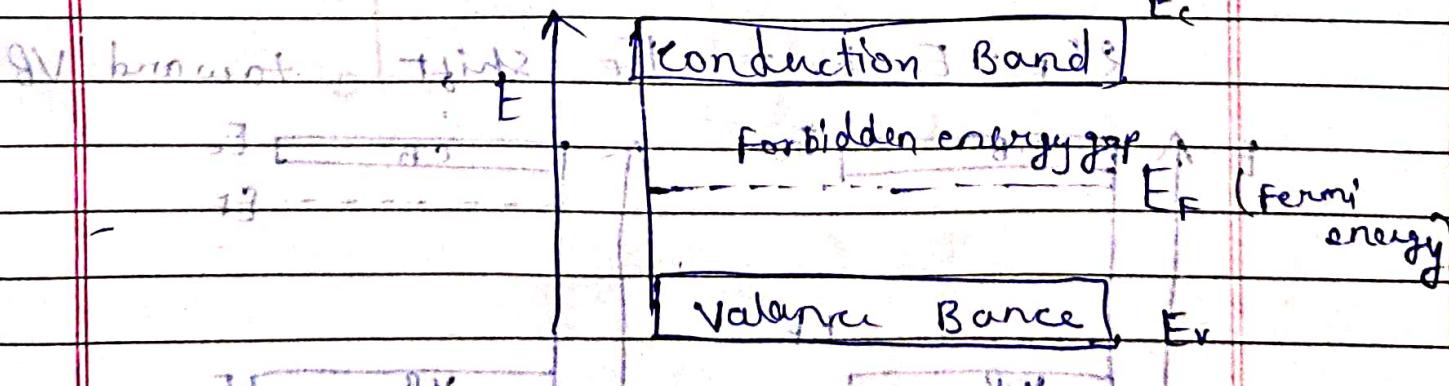
$$\text{or } -E_c + E_F = kT \log \frac{N_v}{N_c} - E_F + E_v$$

$$E_c + E_F + (E_F - E_v) = kT \log \left(\frac{N_v}{N_c} \right)$$

$$\rho E_F = E_c - E_v = 0$$

$$\text{with } \boxed{\rho E_F = E_c + E_v}$$

$\rho < 0$, $E_c > E_F > E_v$



Fermilevel lies in middle of CB & VB

sopt-11

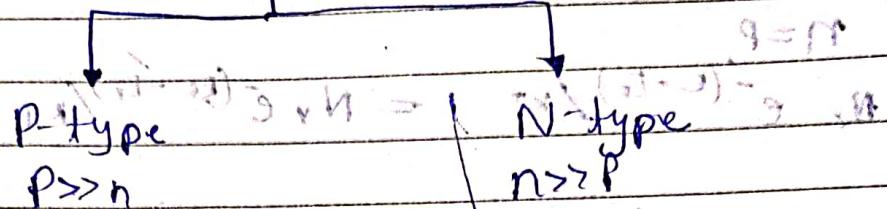
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Fermi levels in Extrinsic Semiconductors

Population distribution of electrons in extrinsic semiconductor

Level



P-type Semiconductor

$$\frac{n}{N_c} e^{-(E_c - E_F)/kT} = \frac{N_v}{N_c} e^{-(E_F - E_v)/kT}$$

Taking log of both sides $\Rightarrow T = 300K$

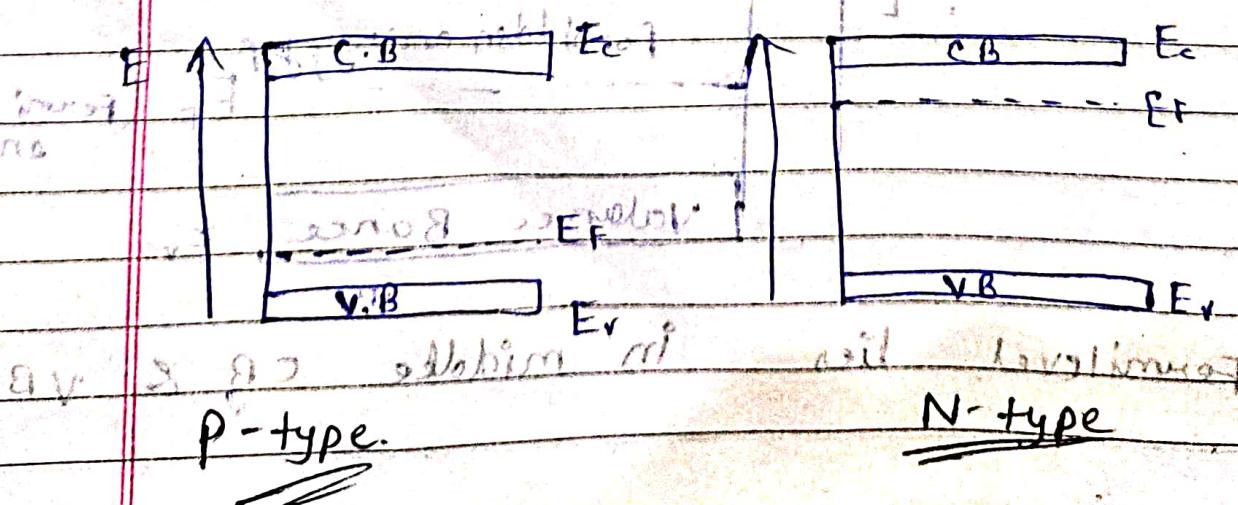
$$\frac{(n/N_c) e^{-(E_c - E_F)/kT}}{(N_v/N_c) e^{-(E_F - E_v)/kT}} \ll \log \frac{N_v}{N_c} + E_F - E_v$$

$$\text{or } 0 = \nu_3 - \nu_2 \rightarrow \nu_2$$

$$-E_c + E_F + E_F - E_v \ll kT \left[\log \frac{N_v}{N_c} \right] - E_F + E_v$$

$$-E_c + E_F + E_F - E_v \ll kT \left[\log \frac{N_v}{N_c} \right], \quad p \gg n$$

E_F or $E_F = E_F$ shift toward VB



Fermi Dirac Distribution function.

$$F(E) = \frac{1}{e^{(E-E_F)/kT} + 1}$$

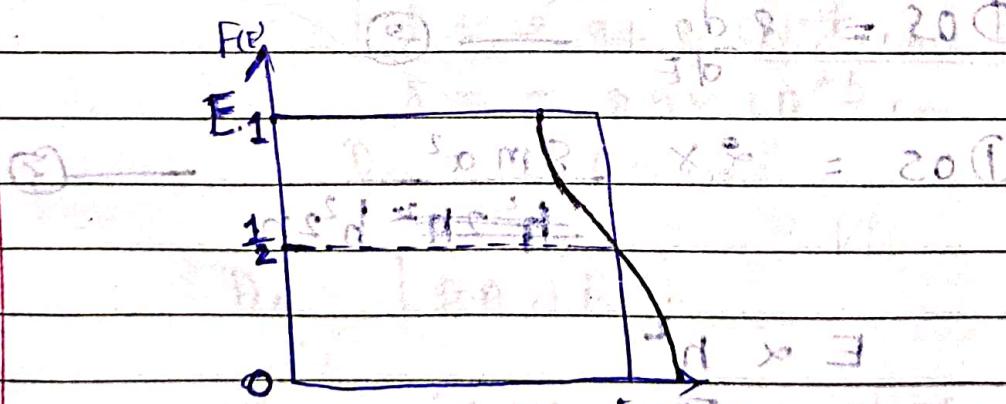
$T > 0K$, $E = E_F$ \rightarrow most of the atoms are in ground state.

$$F(E=E_F) = \frac{1}{e^0 + 1} = \frac{1}{2} \text{ most}$$

$T = 0K$, $E > E_F$: All electrons are in ground state.

$$F(E) = \frac{1}{e^0 + 1} = \frac{1}{e^0 + 1} = 0$$

$$E < E_F \Rightarrow F(E) = 1 \text{ and } 1 - F(E) = 0$$



$(E-E_F) = 0.2 \text{ eV} \Rightarrow T = 200K$

$kT = 0.0256 \text{ eV}$

$2.56 \times 10^{-2} \text{ eV}$

* Density of states - It is defined as

$$\frac{dn}{dE} \quad E < T$$

no. of atoms / energy $E < T$

$$\text{from } E_n = \frac{1}{2} \frac{n^2 h^2}{8ma^2} \quad (1) \quad E_n \rightarrow E$$

$$dE = \frac{h^2}{8ma^2} dn$$

$$\frac{dn}{dE} = \frac{8ma^2}{h^2 n}$$

Alc to Polres perin

Electron has 2 spins ($\frac{1}{2}, -\frac{1}{2}$)

$$DOS = 2 \cdot \frac{dn}{dE} \quad (2)$$

$$DOS = 2 \times \frac{8ma^2}{h^2 n} \quad (3)$$

$$E \propto n^2$$

$$\text{or } n \propto \sqrt{E}$$

$$DOS \propto \frac{1}{\sqrt{E}}$$

Problems

Q1 Newton's ring are observed normally in reflected light of wavelength 5.89×10^{-5} cm. The diameter of 10th dark ring is 0.50 cm. Find the radius of curvature of lens & thickness of film.

$$2.0 \times 2.0 = 12$$

$$11.201 \times 10^{-5}$$

Solve:-

Q2 The moveable mirror of Michelson's Interferometer is moved through a distance of 0.02603 mm. Find the number of fringes shifted across the cross-wire of eye piece of telescope, if a wavelength of 52060 Å is used.

$$N^F = \lambda$$

Solve:- 1) Given, $R = 10.611$ cm Ans
 $m = 1 \times 0.02603 \times 10^3 = 2.603 \times 10^{-4}$ cm

$$n = 5.89 \times 10^{-5}$$
 cm

$$D_{10} = 0.50$$
 cm

$$2.603 \times 10^{-4} = n$$

$$D_h = \sqrt{4 \pi R \times \frac{\lambda}{\delta}}$$

$$D_{10} = \sqrt{4 \times 10 \times 5.89 \times 10^{-5} \times R}$$

$$(0.50)^2 = 4 \times 5.89 \times 10^{-4} \times R$$

$$0.25$$

~~$$0.25 \times 10^{-4} = 2.356 \times 10^{-3} \times R$$~~

$$1.0611 = R$$

$$R = 106.11 \text{ cm}$$

similalry

$\therefore \text{if } \frac{2t}{\lambda} = \frac{\pi^2}{4R}$ then t will be minimum
 $\text{so } t = \frac{\lambda}{2} = \frac{\pi R}{2}$ for first beat

$\therefore \text{if } \frac{2t}{\lambda} = \frac{\pi^2}{4R}$ not in minimum then
 minimum to either end beat. so $t = \frac{\lambda}{2}$

$$2t = \frac{0.5 \times 0.5}{4 \times 106.11}$$

Distance in centimetre

$$\therefore \text{distance} = 2.94 \times 10^{-4} \text{ cm}$$

Solver-2 Given, $\lambda = ?$ to find

$$\text{so } \lambda = 0.02603 \times 10^{-3} \text{ m}$$

$$\text{A base to } \lambda = 52060 \times 10^{-8} \text{ m}$$

$$\lambda = ?$$

$$52060 \times 10^{-8} \text{ m} = 2 \times 0.02603 \times 10^{-3} \text{ m}$$

$$2.01 \times 10^{-8} = \lambda \text{ N}$$

$$N = \frac{52060 \times 10^{-8}}{2 \times 0.02603 \times 10^{-3}}$$

$$2.01 \times 10^{-8} [N = 1.001 \times 10^{-1}] = 0.01$$

$$2.01 \times 10^{-8} \times 10^{-1} = 0.01$$

$$2.01 \times 10^{-8} \times 10^{-1} = 0.01$$

$$0.01 = 1.001 \times 10^{-1}$$

$$1 = 1.001 \times 10^{-1}$$