

References:

1. <https://www.cs.purdue.edu/homes/ayg/CS251/slides/chap13c.pdf>
2. Introduction to Algorithms 3rd Edition by Clifford Stein, Thomas H. Cormen, Charles E. Leiserson, Ronald L. Rivest

Algorithm 1 INSERT,DELETE,SEARCH INTERVAL TREES

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1: procedure SEARCH(root,interval)                                ▷ interval to be searched has attributes low and high
2:   if root = NULL then return NULL
3:   if Interval[root].low ≤ interval.high and interval.low ≤ Interval[root].high then                                ▷ Checking for
   overlaps return Interval[root]
4:   if left[root] ≠ NULL and max[left[root]] ≥ interval.low then return SEARCH(left[root],interval) ▷
   interval may overlap with an interval in left subtree
   return SEARCH(right[root],interval)                                ▷ Otherwise recur for right subtree
5:
6: procedure LEFT-ROTATE(T,x)
7:   y ← right[x]
8:   right[x] ← left[y]
9:   if left[y] ≠ NIL then
10:    parent[left[y]] ← x
11:    parent[y] ← parent[x]
12:    if parent[x] ← NIL then
13:      root[T] ← y
14:    else if x = left[parent[x]] then
15:      left[parent[x]] ← y
16:    else
17:      right[parent[x]] ← y
18:    left[y] ← x
19:    parent[x] ← y
20:    max[x] = MAX(max[left[x]], max[right[x]], high[x])                                ▷ reconfiguring the augmented values
21:    max[y] = MAX(max[left[y]], max[right[y]], high[y])
22:    max[parent[y]] = MAX(max[left[parent[y]]], max[right[parent[y]]], high[parent[y]])
23:
24: procedure RIGHT-ROTATE(T,y)                                ▷ analogous to LEFT-ROTATE
25:   x ← left[y]
26:   left[y] ← right[x]
27:   if right[x] ≠ NIL then
28:    parent[right[x]] ← y
29:    parent[x] ← parent[y]
30:    if parent[y] ← NIL then
31:      root[T] ← x
32:    else if y = right[parent[y]] then
33:      right[parent[y]] ← x
34:    else
35:      left[parent[y]] ← x
36:    right[x] ← y
37:    parent[y] ← x
38:    max[x] = MAX(max[left[x]], max[right[x]], high[x])
39:    max[y] = MAX(max[left[y]], max[right[y]], high[y])
40:    max[parent[x]] = MAX(max[left[parent[x]]], max[right[parent[x]]], high[parent[x]])
41:

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42: procedure BST-INSERT( $T, z$ )
43:    $y \leftarrow NIL$ 
44:    $x \leftarrow root[T]$ 
45:   while  $x \neq NIL$  do
46:      $y \leftarrow x$ 
47:     if  $low[z] < low[x]$  then
48:        $x \leftarrow left[x]$ 
49:     else
50:        $x \leftarrow right[x]$ 
51:    $parent[z] \leftarrow y$ 
52:   if  $y = NIL$  then
53:      $root[T] \leftarrow z$  ▷  $z$  is the only node
54:   else if  $low[z] < low[y]$  then ▷ setting up the pointers to  $z$ 
55:      $left[y] \leftarrow z$ 
56:   else
57:      $right[y] \leftarrow z$ 
58:    $max[z] = high[z]$  ▷ setting up augmented value of inserted node
59:
60: procedure RB-INSERT( $T, x$ ) ▷ inserting a node in interval(Red Black) tree
61:    $BST-INSERT(T, x)$  ▷ First insert  $x$  as normally inserted into BST and color it red
62:    $color[x] \leftarrow RED$ 
63:   while  $x \neq root[T]$  and  $color[parent[x]] = RED$  do
64:     if  $parent[x] = left[parent[parent[x]]]$  then
65:        $y \leftarrow right[parent[parent[x]]]$  ▷ uncle
66:       if  $color[y] = RED$  then ▷ Case a
67:          $color[parent[x]] \leftarrow BLACK$ 
68:          $color[y] \leftarrow BLACK$ 
69:          $color[parent[parent[x]]] \leftarrow RED$ 
70:          $x \leftarrow parent[parent[x]]$  ▷ Change  $x$  to grandparent
71:       else if  $x = right[parent[x]]$  then ▷ Case b: Left Right Case
72:          $x \leftarrow parent[x]$ 
73:          $LEFT-ROTATE(T, x)$ 
74:          $color[parent[x]] \leftarrow BLACK$  ▷ Follow Case b: Left Left Case
75:          $color[parent[parent[x]]] \leftarrow RED$ 
76:          $RIGHT-ROTATE(T, parent[parent[x]])$ 
77:       else ▷ Case b: Left Left Case
78:          $color[parent[x]] \leftarrow BLACK$ 
79:          $color[parent[parent[x]]] \leftarrow RED$ 
80:          $RIGHT-ROTATE(T, parent[parent[x]])$ 
81:     else
82:       (do the same thing in then in line 64 clause with "right" and "left" swapped) ▷ Case b: Right
      Left and Right Right Case
83:    $color[root[T]] \leftarrow BLACK$  ▷ Since root is always black
84:

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85: procedure RB-DELETE( $T, z$ )                                ▷ Deleting a node in RB-Tree
86:   if  $left[z] = nil[T]$  or  $right[z] = nil[T]$  then           ▷ z has no or 1 child
87:      $y \leftarrow z$ 
88:   else
89:      $y \leftarrow RB - SUCCESSOR(z)$                         ▷ z has 2 children
90:   if  $left[y] \neq nil[T]$  then
91:      $x \leftarrow left[y]$ 
92:   else
93:      $x \leftarrow right[y]$ 
94:    $parent[x] \leftarrow parent[y]$                             ▷ y gets removed
95:    $max[parent[x]] = MAX(high[x], high[parent[x]])$           ▷ changed the augmented value
96:   if  $parent[y] = nil[T]$  then
97:      $root[T] \leftarrow x$ 
98:   else if  $y = left[parent[y]]$  then                        ▷ reconfiguring the pointers to x
99:      $left[parent[y]] \leftarrow x$ 
100:  else
101:     $right[parent[y]] \leftarrow x$ 
102:  if  $y \neq z$  then                                          ▷ z had 2 children
103:     $low[z] \leftarrow low[y]$                                 ▷ changed the augmented and key values
104:     $high[z] \leftarrow high[y]$ 
105:     $max[z] \leftarrow MAX(high[z], max[left[z]], max[right[z]])$ 
106:  if  $color[y] = BLACK$  then                                ▷ no change in black height for deleting red
107:     $RB - DELETE - CORRECTION(T, x)$                         ▷ if deleted black, need to check for violations
  return  $y$ 
108:
109: procedure RB-SUCCESSOR( $x$ )                                ▷ helper for finding successor for a node in tree
110:   if  $right[x] \neq NIL$  then return  $RB - MINIMUM(right[x])$ 
111:    $y \leftarrow parent[x]$ 
112:   while  $y \neq NIL$  and  $x = right[y]$  do
113:      $x \leftarrow y$ 
114:    $y \leftarrow parent[y]$ 
  return  $y$ 
115:
116: procedure RB-MINIMUM( $x$ )                                    ▷ helper for finding minimum in tree
117:   while  $left[x] \neq NIL$  do
118:      $x \leftarrow left[x]$ 
  return  $x$ 
119:

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120: procedure RB-DELETE-CORRECTION( $T, x$ )
121:   while  $x \neq \text{root}[T]$  and  $\text{color}[x] = \text{BLACK}$  do
122:     if  $x = \text{left}[\text{parent}[x]]$  then                                 $\triangleright$  assume  $x$  has double black
123:        $w \leftarrow \text{right}[\text{parent}[x]]$                                  $\triangleright$  Old Sibling
124:       if  $\text{color}[w] = \text{RED}$  then
125:          $\text{color}[w] \leftarrow \text{BLACK}$                                  $\triangleright$  Recolour old sibling and parent
126:          $\text{color}[\text{parent}[x]] \leftarrow \text{RED}$ 
127:          $\text{LEFT-ROTATE}(T, \text{parent}[x])$ 
128:          $w \leftarrow \text{right}[\text{parent}[x]]$ 
129:         if  $\text{color}[\text{left}[w]] = \text{BLACK}$  and  $\text{color}[\text{right}[w]] = \text{BLACK}$  then  $\triangleright$  both the children of siblings
are black
130:            $\text{color}[w] \leftarrow \text{RED}$ 
131:            $x \leftarrow \text{parent}[x]$                                  $\triangleright$  will recur for parent
132:         else if  $\text{color}[\text{right}[w]] = \text{BLACK}$  then                     $\triangleright$  one of the children of sibling is red
133:            $\text{color}[\text{left}[w]] \leftarrow \text{BLACK}$                          $\triangleright$  Right Left Case
134:            $\text{color}[w] \leftarrow \text{RED}$ 
135:            $\text{RIGHT-ROTATE}(T, w)$ 
136:            $w \leftarrow \text{right}[\text{parent}[x]]$ 
137:            $\text{color}[w] \leftarrow \text{color}[\text{parent}[x]]$ 
138:            $\text{color}[\text{parent}[x]] \leftarrow \text{BLACK}$ 
139:            $\text{color}[\text{right}[w]] \leftarrow \text{BLACK}$ 
140:            $\text{LEFT-ROTATE}(T, \text{parent}[x])$ 
141:            $x \leftarrow \text{root}(T)$ 
142:         else                                                     $\triangleright$  Right Right Case
143:            $\text{color}[w] \leftarrow \text{color}[\text{parent}[x]]$ 
144:            $\text{color}[\text{parent}[x]] \leftarrow \text{BLACK}$ 
145:            $\text{color}[\text{right}[w]] \leftarrow \text{BLACK}$ 
146:            $\text{LEFT-ROTATE}(T, \text{parent}[x])$ 
147:            $x \leftarrow \text{root}(T)$ 
148:       else
149:         (do the same thing in then in line 122 clause with "right" and "left" swapped)  $\triangleright$  Case b: Left
Left and Left Right Case
150:        $\text{color}[x] \leftarrow \text{BLACK}$ 
151:

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