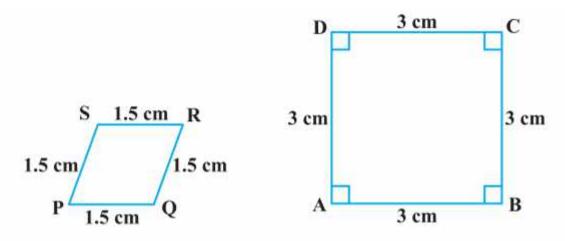


EXERCISE 6.1	PAGE: 122
1. Fill in the blanks using correct word given in the bracke	ets:-
(i) All circles are (congruent, similar)	
Answer: Similar	
(ii) All squares are (similar, congruent)	
Answer: Similar	
(iii) All triangles are similar. (isosceles, equila	teral)
Answer: Equilateral	
(iv) Two polygons of the same number of sides are similar (b) their corresponding sides are (equal, prop	
Answer: (a) Equal	
(b) Proportional	
<ul><li>2. Give two different examples of pair of</li><li>(i) Similar figures</li><li>(ii) Non-similar figures</li></ul>	
Solution:	
(i)Example of two similar figure;  Two Equilateral Triangle	Two Rectangle
(ii) Example of two Non-similar figure;	
Triangle Rhombus	Rectangle Trapezium

3. State whether the following quadrilaterals are similar or not:



# NCERT Solutions for Class 10 Maths Chapter 6 - Triangles



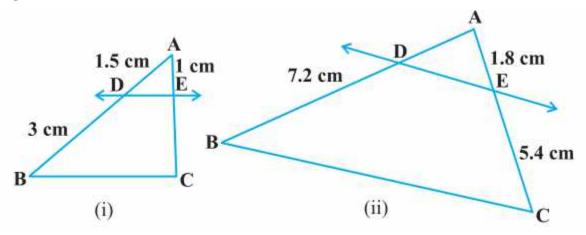
# **Solution:**

From the given two figures, we can see their corresponding angles are different or unequal. Therefore, they are not similar.



EXERCISE 6.2 PAGE: 128

1. In figure. (i) and (ii), DE || BC. Find EC in (i) and AD in (ii).



#### **Solution:**

(i) Given, in  $\triangle$  ABC, DE||BC

: AD/DB = AE/EC [Using Basic proportionality theorem]

 $\Rightarrow$ 1.5/3 = 1/EC

 $\Rightarrow$ EC = 3/1.5

 $EC = 3 \times 10/15 = 2 \text{ cm}$ 

Hence, EC = 2 cm.

(ii) Given, in △ ABC, DE∥BC

: AD/DB = AE/EC [Using Basic proportionality theorem]

 $\Rightarrow$  AD/7.2 = 1.8 / 5.4

 $\Rightarrow$  AD = 1.8 ×7.2/5.4 = (18/10)×(72/10)×(10/54) = 24/10

 $\Rightarrow$  AD = 2.4

Hence, AD = 2.4 cm.

2. E and F are points on the sides PQ and PR, respectively of a  $\Delta$ PQR. For each of the following cases, state whether EF  $\parallel$  QR.

(i) PE = 3.9 cm, EQ = 3 cm, PF = 3.6 cm and FR = 2.4 cm

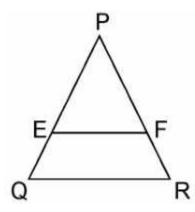
(ii) PE = 4 cm, QE = 4.5 cm, PF = 8 cm and RF = 9 cm

(iii) PQ = 1.28 cm, PR = 2.56 cm, PE = 0.18 cm and PF = 0.63 cm

#### **Solution:**

Given, in  $\triangle PQR$ , E and F are two points on side PQ and PR, respectively. See the figure below;





(i) Given, PE = 3.9 cm, EQ = 3 cm, PF = 3.6 cm and FR = 2.4 cm

Therefore, by using Basic proportionality theorem, we get,

$$PE/EQ = 3.9/3 = 39/30 = 13/10 = 1.3$$

And PF/FR = 
$$3.6/2.4 = 36/24 = 3/2 = 1.5$$

So, we get,  $PE/EQ \neq PF/FR$ 

Hence, EF is not parallel to QR.

(ii) Given, PE = 4 cm, QE = 4.5 cm, PF = 8cm and RF = 9cm

Therefore, by using Basic proportionality theorem, we get,

$$PE/QE = 4/4.5 = 40/45 = 8/9$$

And, PF/RF = 8/9

So, we get here,

PE/QE = PF/RF

Hence, EF is parallel to QR.

(iii) Given, PQ = 1.28 cm, PR = 2.56 cm, PE = 0.18 cm and PF = 0.36 cm

From the figure,

$$EQ = PQ - PE = 1.28 - 0.18 = 1.10 \text{ cm}$$

And, 
$$FR = PR - PF = 2.56 - 0.36 = 2.20$$
 cm

So, 
$$PE/EQ = 0.18/1.10 = 18/110 = 9/55...$$
 (i)

And, 
$$PE/FR = 0.36/2.20 = 36/220 = 9/55...$$
 (ii)

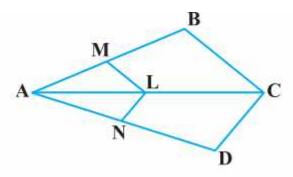
So, we get here,

PE/EQ = PF/FR

Hence, EF is parallel to QR.

3. In the figure, if LM || CB and LN || CD, prove that AM/AB = AN/AD





## **Solution:**

In the given figure, we can see, LM || CB,

By using basic proportionality theorem, we get,

$$AM/AB = AL/AC$$
....(i)

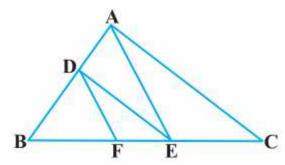
Similarly, given, LN || CD and using basic proportionality theorem,

From equation (i) and (ii), we get,

AM/AB = AN/AD

Hence, proved.

# 4. In the figure, DE||AC| and DF||AE. Prove that BF/FE = BE/EC



#### **Solution:**

In  $\triangle$ ABC, given as, DE || AC

Thus, by using Basic Proportionality Theorem, we get,

$$\therefore$$
BD/DA = BE/EC .....(i)

In  $\triangle BAE$ , given as, DF  $\parallel$  AE

Thus, by using Basic Proportionality Theorem, we get,

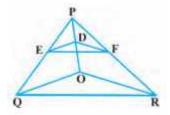
From equation (i) and (ii), we get

BE/EC = BF/FE



Hence, proved.

# 5. In the figure, DE||OQ and DF||OR, show that EF||QR.



## **Solution:**

Given,

In  $\Delta PQO$ , DE  $\parallel OQ$ 

So by using Basic Proportionality Theorem,

PD/DO = PE/EQ.....(i)

Again given, in  $\triangle POR$ , DF || OR,

So by using Basic Proportionality Theorem,

PD/DO = PF/FR.... (ii)

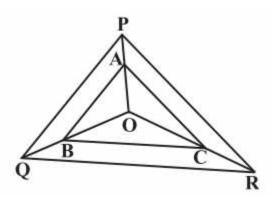
From equation (i) and (ii), we get,

PE/EQ = PF/FR

Therefore, by converse of Basic Proportionality Theorem,

EF  $\parallel$  QR, in  $\triangle$ PQR.

6. In the figure, A, B and C are points on OP, OQ and OR respectively such that AB  $\parallel$  PQ and AC  $\parallel$  PR. Show that BC  $\parallel$  QR.



#### **Solution:**

Given here,

In  $\triangle OPQ$ , AB  $\parallel PQ$ 

By using Basic Proportionality Theorem,

OA/AP = OB/BQ....(i)



Also given,

In ΔOPR, AC || PR

By using Basic Proportionality Theorem

$$\therefore$$
 OA/AP = OC/CR....(ii)

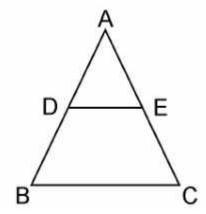
From equation (i) and (ii), we get,

OB/BQ = OC/CR

Therefore, by converse of Basic Proportionality Theorem,

In  $\triangle OQR$ , BC  $\parallel$  QR.

7. Using Basic proportionality theorem, prove that a line drawn through the mid-points of one side of a triangle parallel to another side bisects the third side. (Recall that you have proved it in Class IX).



#### **Solution:**

Given, in  $\triangle ABC$ , D is the midpoint of AB such that AD=DB.

A line parallel to BC intersects AC at E as shown in above figure such that DE || BC.

We have to prove that E is the mid point of AC.

Since, D is the mid-point of AB.

∴ AD=DB

$$\Rightarrow$$
AD/DB = 1 .....(i)

In  $\triangle$ ABC, DE || BC,

By using Basic Proportionality Theorem,

Therefore, AD/DB = AE/EC

From equation (i), we can write,

 $\Rightarrow 1 = AE/EC$ 

 $\therefore$  AE = EC

Hence, proved, E is the midpoint of AC.

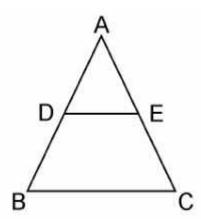
# NCERT Solutions for Class 10 Maths Chapter 6 -Triangles

8. Using Converse of basic proportionality theorem, prove that the line joining the mid-points of any two sides of a triangle is parallel to the third side. (Recall that you have done it in Class IX).

#### **Solution:**

Given, in ΔABC, D and E are the mid points of AB and AC, respectively, such that,

AD=BD and AE=EC.



We have to prove that: DE || BC.

Since, D is the midpoint of AB

∴ AD=DB

$$\Rightarrow$$
AD/BD = 1.....(i)

Also given, E is the mid-point of AC.

∴ AE=EC

 $\Rightarrow$  AE/EC = 1

From equation (i) and (ii), we get,

AD/BD = AE/EC

By converse of Basic Proportionality Theorem,

DE || BC

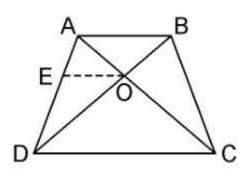
Hence, proved.

9. ABCD is a trapezium in which AB  $\parallel$  DC and its diagonals intersect each other at the point O. Show that AO/BO = CO/DO.

#### **Solution:**

Given, ABCD is a trapezium where AB  $\parallel$  DC and diagonals AC and BD intersect each other at O.





We have to prove, AO/BO = CO/DO

From the point O, draw a line EO touching AD at E, in such a way that,

 $EO \parallel DC \parallel AB$ 

In  $\triangle ADC$ , we have  $OE \parallel DC$ 

Therefore, by using Basic Proportionality Theorem

AE/ED = AO/CO .....(i)

Now, In  $\triangle ABD$ , OE  $\parallel AB$ 

Therefore, by using Basic Proportionality Theorem

DE/EA = DO/BO....(ii)

From equation (i) and (ii), we get,

AO/CO = BO/DO

 $\Rightarrow$ AO/BO = CO/DO

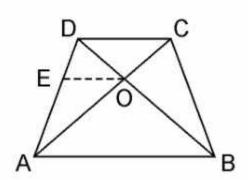
Hence, proved.

10. The diagonals of a quadrilateral ABCD intersect each other at the point O such that AO/BO = CO/DO. Show that ABCD is a trapezium.

#### **Solution:**

Given, Quadrilateral ABCD where AC and BD intersect each other at O such that,

AO/BO = CO/DO.



We have to prove here, ABCD is a trapezium



# NCERT Solutions for Class 10 Maths Chapter 6 - Triangles

From the point O, draw a line EO touching AD at E, in such a way that,

 $EO \parallel DC \parallel AB$ 

In  $\Delta DAB$ , EO  $\parallel AB$ 

Therefore, by using Basic Proportionality Theorem

 $DE/EA = DO/OB \dots (i)$ 

Also, given,

AO/BO = CO/DO

 $\Rightarrow$  AO/CO = BO/DO

 $\Rightarrow$  CO/AO = DO/BO

⇒DO/OB = CO/AO .....(ii)

From equation (i) and (ii), we get

DE/EA = CO/AO

Therefore, by using converse of Basic Proportionality Theorem,

EO || DC also EO || AB

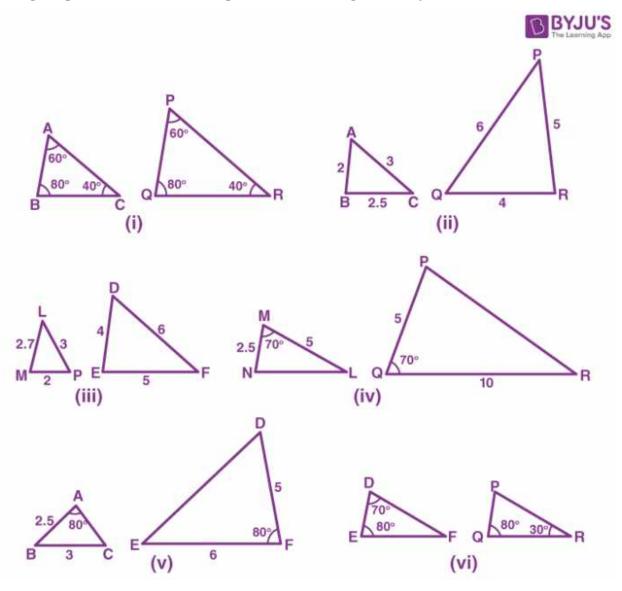
 $\Rightarrow$  AB || DC.

Hence, quadrilateral ABCD is a trapezium with AB || CD.



EXERCISE 6.3 PAGE: 138

1. State which pairs of triangles in the figure are similar. Write the similarity criterion used by you for answering the question and also write the pairs of similar triangles in the symbolic form:



#### **Solution:**

(i) Given, in  $\triangle ABC$  and  $\triangle PQR$ ,

$$\angle A = \angle P = 60^{\circ}$$

$$\angle B = \angle Q = 80^{\circ}$$

$$\angle C = \angle R = 40^{\circ}$$

Therefore, by AAA similarity criterion,



(ii) Given, in  $\triangle ABC$  and  $\triangle PQR$ ,

$$AB/QR = 2/4 = 1/2,$$

$$BC/RP = 2.5/5 = 1/2,$$

$$CA/PA = 3/6 = 1/2$$

By SSS similarity criterion,

$$\Delta ABC \sim \Delta QRP$$

(iii) Given, in  $\Delta$ LMP and  $\Delta$ DEF,

$$LM = 2.7$$
,  $MP = 2$ ,  $LP = 3$ ,  $EF = 5$ ,  $DE = 4$ ,  $DF = 6$ 

$$MP/DE = 2/4 = 1/2$$

$$PL/DF = 3/6 = 1/2$$

$$LM/EF = 2.7/5 = 27/50$$

Here, 
$$MP/DE = PL/DF \neq LM/EF$$

Therefore,  $\Delta$ LMP and  $\Delta$ DEF are not similar.

(iv) In  $\triangle$ MNL and  $\triangle$ QPR, it is given,

$$MN/QP = ML/QR = 1/2$$

$$\angle M = \angle Q = 70^{\circ}$$

Therefore, by SAS similarity criterion

$$\therefore \Delta MNL \sim \Delta QPR$$

(v) In  $\triangle$ ABC and  $\triangle$ DEF, given that,

$$AB = 2.5$$
,  $BC = 3$ ,  $\angle A = 80^{\circ}$ ,  $EF = 6$ ,  $DF = 5$ ,  $\angle F = 80^{\circ}$ 

Here, 
$$AB/DF = 2.5/5 = 1/2$$

And, 
$$BC/EF = 3/6 = 1/2$$

$$\Rightarrow \angle B \neq \angle F$$

Hence,  $\triangle$ ABC and  $\triangle$ DEF are not similar.

(vi) In  $\Delta DEF$ , by sum of angles of triangles, we know that,

$$\angle D + \angle E + \angle F = 180^{\circ}$$

$$\Rightarrow 70^{\circ} + 80^{\circ} + \angle F = 180^{\circ}$$

$$\Rightarrow$$
  $\angle F = 180^{\circ} - 70^{\circ} - 80^{\circ}$ 

$$\Rightarrow \angle F = 30^{\circ}$$

Similarly, In  $\Delta PQR$ ,

$$\angle P + \angle Q + \angle R = 180$$
 (Sum of angles of  $\Delta$ )

$$\Rightarrow \angle P + 80^{\circ} + 30^{\circ} = 180^{\circ}$$



$$\Rightarrow \angle P = 180^{\circ} - 80^{\circ} - 30^{\circ}$$

$$\Rightarrow \angle P = 70^{\circ}$$

Now, comparing both the triangles,  $\Delta DEF$  and  $\Delta PQR$ , we have

$$\angle D = \angle P = 70^{\circ}$$

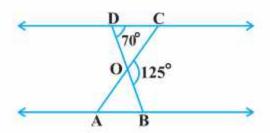
$$\angle F = \angle Q = 80^{\circ}$$

$$\angle F = \angle R = 30^{\circ}$$

Therefore, by AAA similarity criterion,

Hence,  $\Delta DEF \sim \Delta PQR$ 

2. In figure 6.35,  $\triangle$ ODC  $\sim$   $\triangle$ OBA,  $\angle$  BOC = 125° and  $\angle$  CDO = 70°. Find  $\angle$  DOC,  $\angle$  DCO and  $\angle$  OAB.



#### **Solution:**

As we can see from the figure, DOB is a straight line.

Therefore,  $\angle DOC + \angle COB = 180^{\circ}$ 

$$\Rightarrow \angle DOC = 180^{\circ} - 125^{\circ} \text{ (Given, } \angle BOC = 125^{\circ}\text{)}$$

In  $\triangle DOC$ , sum of the measures of the angles of a triangle is  $180^{\circ}$ 

Therefore,  $\angle DCO + \angle CDO + \angle DOC = 180^{\circ}$ 

$$\Rightarrow \angle DCO + 70^{\circ} + 55^{\circ} = 180^{\circ} (Given, \angle CDO = 70^{\circ})$$

$$\Rightarrow \angle DCO = 55^{\circ}$$

It is given that,  $\triangle ODC \sim \triangle OBA$ ,

Therefore,  $\triangle ODC \sim \triangle OBA$ .

Hence, corresponding angles are equal in similar triangles

$$\angle OAB = \angle OCD$$

$$\Rightarrow$$
  $\angle$  OAB = 55°

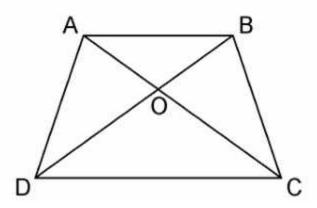
$$\angle OAB = \angle OCD$$

$$\Rightarrow \angle OAB = 55^{\circ}$$

3. Diagonals AC and BD of a trapezium ABCD with AB  $\parallel$  DC intersect each other at the point O. Using a similarity criterion for two triangles, show that AO/OC = OB/OD



#### **Solution:**



In  $\triangle DOC$  and  $\triangle BOA$ ,

AB || CD, thus alternate interior angles will be equal,

∴∠CDO = ∠ABO

Similarly,

 $\angle DCO = \angle BAO$ 

Also, for the two triangles  $\Delta DOC$  and  $\Delta BOA$ , vertically opposite angles will be equal;

∴∠DOC = ∠BOA

Hence, by AAA similarity criterion,

 $\Delta DOC \sim \Delta BOA$ 

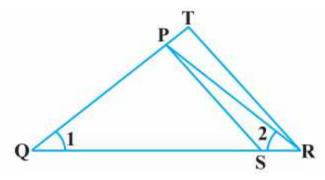
Thus, the corresponding sides are proportional.

DO/BO = OC/OA

 $\Rightarrow$ OA/OC = OB/OD

Hence, proved.

# 4. In the fig.6.36, QR/QS = QT/PR and $\angle 1 = \angle 2$ . Show that $\triangle PQS \sim \triangle TQR$ .



**Solution:** 

In ΔPQR,



 $\angle PQR = \angle PRQ$ 

$$\therefore$$
 PQ = PR .....(i)

Given,

QR/QS = QT/PRUsing equation (i), we get

QR/QS = QT/QP....(ii)

In  $\triangle PQS$  and  $\triangle TQR$ , by equation (ii),

QR/QS = QT/QP

 $\angle Q = \angle Q$ 

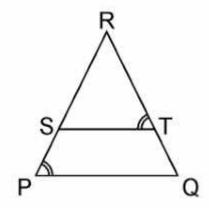
∴ ∆PQS ~ ∆TQR [By SAS similarity criterion]

5. S and T are point on sides PR and QR of  $\triangle$ PQR such that  $\angle$ P =  $\angle$ RTS. Show that  $\triangle$ RPQ ~  $\triangle$ RTS.

# **Solution:**

Given, S and T are point on sides PR and QR of  $\Delta$ PQR

And  $\angle P = \angle RTS$ .



In  $\triangle$ RPQ and  $\triangle$ RTS,

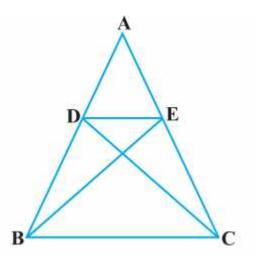
 $\angle RTS = \angle QPS$  (Given)

 $\angle R = \angle R$  (Common angle)

 $\therefore$   $\triangle$ RPQ ~  $\triangle$ RTS (AA similarity criterion)

6. In the figure, if  $\triangle ABE \cong \triangle ACD$ , show that  $\triangle ADE \sim \triangle ABC$ .





# **Solution:**

Given,  $\triangle ABE \cong \triangle ACD$ .

$$\therefore$$
 AB = AC [By CPCT] .....(i)

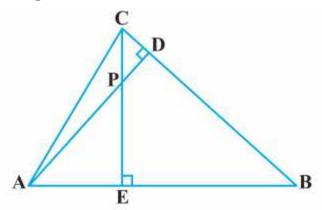
In  $\triangle ADE$  and  $\triangle ABC$ , dividing eq.(ii) by eq(i),

AD/AB = AE/AC

 $\angle A = \angle A$  [Common angle]

 $\therefore \triangle ADE \sim \triangle ABC$  [SAS similarity criterion]

# 7. In the figure, altitudes AD and CE of $\triangle$ ABC intersect each other at the point P. Show that:

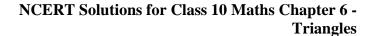


- (i)  $\triangle AEP \sim \triangle CDP$
- (ii)  $\triangle ABD \sim \triangle CBE$
- (iii)  $\triangle AEP \sim \triangle ADB$
- (iv)  $\triangle PDC \sim \triangle BEC$

# **Solution:**

Given, altitudes AD and CE of  $\triangle$ ABC intersect each other at the point P.

(i) In  $\triangle AEP$  and  $\triangle CDP$ ,





 $\angle AEP = \angle CDP (90^{\circ} each)$ 

 $\angle APE = \angle CPD$  (Vertically opposite angles)

Hence, by AA similarity criterion,

 $\triangle AEP \sim \triangle CDP$ 

(ii) In  $\triangle$ ABD and  $\triangle$ CBE,

 $\angle ADB = \angle CEB (90^{\circ} each)$ 

 $\angle ABD = \angle CBE$  (Common Angles)

Hence, by AA similarity criterion,

 $\Delta ABD \sim \Delta CBE$ 

(iii) In  $\triangle$ AEP and  $\triangle$ ADB,

 $\angle AEP = \angle ADB (90^{\circ} each)$ 

 $\angle PAE = \angle DAB$  (Common Angles)

Hence, by AA similarity criterion,

 $\Delta AEP \sim \Delta ADB$ 

(iv) In  $\triangle PDC$  and  $\triangle BEC$ ,

 $\angle PDC = \angle BEC (90^{\circ} \text{ each})$ 

 $\angle PCD = \angle BCE$  (Common angles)

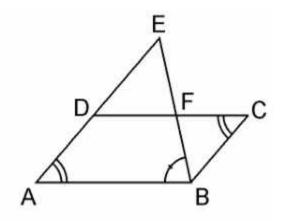
Hence, by AA similarity criterion,

 $\Delta PDC \sim \Delta BEC$ 

# 8. E is a point on the side AD produced of a parallelogram ABCD and BE intersects CD at F. Show that $\Delta ABE \sim \Delta CFB$ .

#### **Solution:**

Given, E is a point on the side AD produced of a parallelogram ABCD and BE intersects CD at F. Consider the figure below,



In  $\triangle ABE$  and  $\triangle CFB$ ,

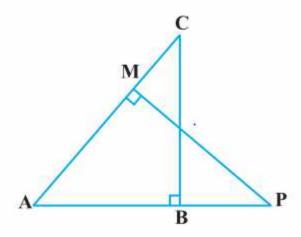


 $\angle A = \angle C$  (Opposite angles of a parallelogram)

 $\angle AEB = \angle CBF$  (Alternate interior angles as  $AE \parallel BC$ )

 $\therefore \triangle ABE \sim \triangle CFB$  (AA similarity criterion)

9. In the figure, ABC and AMP are two right triangles, right angled at B and M, respectively, prove that:



(i)  $\triangle ABC \sim \triangle AMP$ 

(ii) CA/PA = BC/MP

#### **Solution:**

Given, ABC and AMP are two right triangles, right angled at B and M, respectively.

(i) In  $\triangle$ ABC and  $\triangle$ AMP, we have,

 $\angle CAB = \angle MAP$  (common angles)

 $\angle ABC = \angle AMP = 90^{\circ} \text{ (each } 90^{\circ}\text{)}$ 

∴ ΔABC ~ ΔAMP (AA similarity criterion)

(ii) As,  $\triangle$ ABC  $\sim$   $\triangle$ AMP (AA similarity criterion)

If two triangles are similar then the corresponding sides are always equal,

Hence, CA/PA = BC/MP

10. CD and GH are respectively the bisectors of  $\angle ACB$  and  $\angle EGF$  such that D and H lie on sides AB and FE of  $\triangle ABC$  and  $\triangle EFG$  respectively. If  $\triangle ABC \sim \triangle FEG$ , Show that:

(i) CD/GH = AC/FG

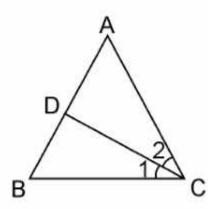
(ii)  $\Delta DCB \sim \Delta HGE$ 

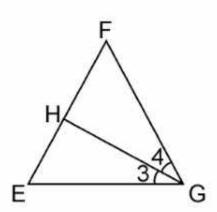
(iii) ΔDCA ~ ΔHGF

#### **Solution:**

Given, CD and GH are respectively the bisectors of  $\angle$ ACB and  $\angle$ EGF such that D and H lie on sides AB and FE of  $\triangle$ ABC and  $\triangle$ EFG, respectively.







(i) From the given condition,

 $\triangle$ ABC ~  $\triangle$ FEG.

 $\therefore \angle A = \angle F, \angle B = \angle E, \text{ and } \angle ACB = \angle FGE$ 

Since,  $\angle ACB = \angle FGE$ 

 $\therefore$   $\angle$ ACD =  $\angle$ FGH (Angle bisector)

And,  $\angle DCB = \angle HGE$  (Angle bisector)

In  $\triangle ACD$  and  $\triangle FGH$ ,

 $\angle A = \angle F$ 

 $\angle ACD = \angle FGH$ 

∴ ΔACD ~ ΔFGH (AA similarity criterion)

 $\Rightarrow$ CD/GH = AC/FG

(ii) In ΔDCB and ΔHGE,

 $\angle DCB = \angle HGE$  (Already proved)

 $\angle B = \angle E$  (Already proved)

∴ ∆DCB ~ ∆HGE (AA similarity criterion)

(iii) In ΔDCA and ΔHGF,

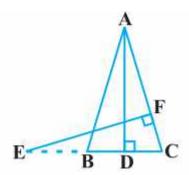
 $\angle$ ACD =  $\angle$ FGH (Already proved)

 $\angle A = \angle F$  (Already proved)

∴ ΔDCA ~ ΔHGF (AA similarity criterion)

11. In the following figure, E is a point on side CB produced of an isosceles triangle ABC with AB = AC. If AD  $\perp$  BC and EF  $\perp$  AC, prove that  $\triangle$ ABD  $\sim$   $\triangle$ ECF.





## **Solution:**

Given, ABC is an isosceles triangle.

$$\therefore$$
 AB = AC

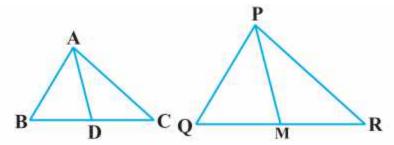
In  $\triangle$ ABD and  $\triangle$ ECF,

$$\angle ADB = \angle EFC \text{ (Each } 90^\circ\text{)}$$

 $\angle BAD = \angle CEF$  (Already proved)

 $\therefore \triangle ABD \sim \triangle ECF$  (using AA similarity criterion)

12. Sides AB and BC and median AD of a triangle ABC are respectively proportional to sides PQ and QR and median PM of  $\Delta$ PQR (see Fig 6.41). Show that  $\Delta$ ABC ~  $\Delta$ PQR.



#### **Solution:**

Given,  $\triangle ABC$  and  $\triangle PQR$ , AB, BC and median AD of  $\triangle ABC$  are proportional to sides PQ, QR and median PM of  $\triangle PQR$ 

i.e. 
$$AB/PQ = BC/QR = AD/PM$$

We have to prove:  $\triangle ABC \sim \triangle PQR$ 

As we know here,

AB/PQ = BC/QR = AD/PM

$$\frac{AB}{PQ} = \frac{\frac{1}{2}BC}{\frac{1}{2}QR} = \frac{AD}{PM}.$$
 (i)

 $\Rightarrow$ AB/PQ = BC/QR = AD/PM (D is the midpoint of BC. M is the midpoint of QR)



 $\Rightarrow \Delta ABD \sim \Delta PQM$  [SSS similarity criterion]

∴ ∠ABD = ∠PQM [Corresponding angles of two similar triangles are equal]

 $\Rightarrow \angle ABC = \angle PQR$ 

In  $\triangle ABC$  and  $\triangle PQR$ 

AB/PQ = BC/QR .....(i)

 $\angle ABC = \angle PQR \dots (ii)$ 

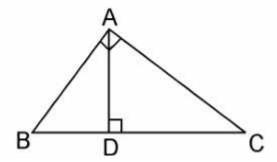
From equation (i) and (ii), we get,

 $\triangle$ ABC ~  $\triangle$ PQR [SAS similarity criterion]

13. D is a point on the side BC of a triangle ABC such that  $\angle$ ADC =  $\angle$ BAC. Show that CA<sup>2</sup> = CB.CD

#### **Solution:**

Given, D is a point on the side BC of a triangle ABC such that  $\angle ADC = \angle BAC$ .



In  $\triangle$ ADC and  $\triangle$ BAC,

 $\angle ADC = \angle BAC$  (Already given)

 $\angle$ ACD =  $\angle$ BCA (Common angles)

∴ ΔADC ~ ΔBAC (AA similarity criterion)

We know that corresponding sides of similar triangles are in proportion.

 $\therefore$  CA/CB = CD/CA

 $\Rightarrow$  CA<sup>2</sup> = CB.CD.

Hence, proved.

14. Sides AB and AC and median AD of a triangle ABC are respectively proportional to sides PQ and PR and median PM of another triangle PQR. Show that  $\Delta ABC \sim \Delta PQR$ .

#### **Solution:**

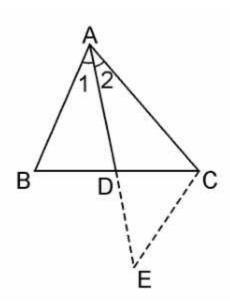
Given: Two triangles  $\triangle$ ABC and  $\triangle$ PQR in which AD and PM are medians such that;

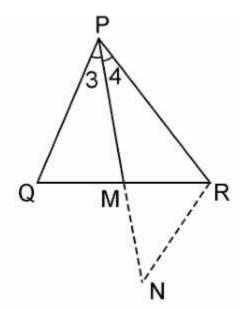
AB/PQ = AC/PR = AD/PM

We have to prove,  $\triangle ABC \sim \triangle PQR$ 



Let us construct first: Produce AD to E so that AD = DE. Join CE, Similarly produce PM to N such that PM = MN, also Join RN.





In  $\triangle$ ABD and  $\triangle$ CDE, we have

AD = DE [By Construction.]

BD = DC [Since, AP is the median]

and,  $\angle ADB = \angle CDE$  [Vertically opposite angles]

 $\therefore \triangle ABD \cong \triangle CDE$  [SAS criterion of congruence]

 $\Rightarrow$  AB = CE [By CPCT] .....(i)

Also, in  $\triangle PQM$  and  $\triangle MNR$ ,

PM = MN [By Construction.]

QM = MR [Since, PM is the median]

and,  $\angle PMQ = \angle NMR$  [Vertically opposite angles]

 $\therefore \Delta PQM = \Delta MNR$  [SAS criterion of congruence]

 $\Rightarrow$  PQ = RN [CPCT] .....(ii)

Now, AB/PQ = AC/PR = AD/PM

From equation (i) and (ii),

 $\Rightarrow$ CE/RN = AC/PR = AD/PM

 $\Rightarrow$  CE/RN = AC/PR = 2AD/2PM

 $\Rightarrow$  CE/RN = AC/PR = AE/PN [Since 2AD = AE and 2PM = PN]

 $\therefore \triangle ACE \sim \triangle PRN$  [SSS similarity criterion]

Therefore,  $\angle 2 = \angle 4$ 



Similarly,  $\angle 1 = \angle 3$ 

$$\therefore$$
  $\angle 1 + \angle 2 = \angle 3 + \angle 4$ 

$$\Rightarrow$$
  $\angle A = \angle P$  ......(iii)

Now, in  $\triangle ABC$  and  $\triangle PQR$ , we have

AB/PQ = AC/PR (Already given)

From equation (iii),

 $\angle A = \angle P$ 

 $\therefore \triangle ABC \sim \triangle PQR$  [ SAS similarity criterion]

15. A vertical pole of a length 6 m casts a shadow 4m long on the ground and at the same time a tower casts a shadow 28 m long. Find the height of the tower.

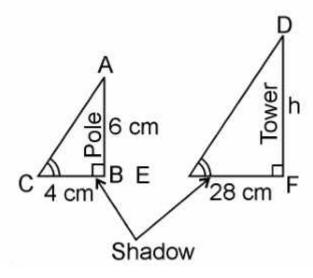
#### **Solution:**

Given, Length of the vertical pole = 6m

Shadow of the pole = 4 m

Let Height of tower = h m

Length of shadow of the tower = 28 m



In  $\triangle$ ABC and  $\triangle$ DEF,

 $\angle C = \angle E$  (angular elevation of sum)

 $\angle B = \angle F = 90^{\circ}$ 

∴ ∆ABC ~ ∆DEF (AA similarity criterion)

: AB/DF = BC/EF (If two triangles are similar corresponding sides are proportional)

∴ 6/h = 4/28

 $\Rightarrow$ h =  $(6 \times 28)/4$ 



$$\Rightarrow h = 6 \times 7$$

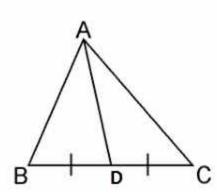
$$\Rightarrow h = 42 \text{ m}$$

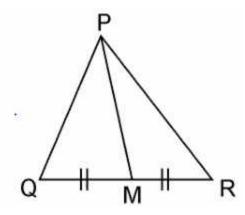
Hence, the height of the tower is 42 m.

16. If AD and PM are medians of triangles ABC and PQR, respectively where  $\Delta ABC \sim \Delta PQR$  prove that AB/PQ = AD/PM.

#### **Solution:**

Given,  $\triangle ABC \sim \triangle PQR$ 





We know that the corresponding sides of similar triangles are in proportion.

$$\therefore$$
AB/PQ = AC/PR = BC/QR....(i)

Also, 
$$\angle A = \angle P$$
,  $\angle B = \angle Q$ ,  $\angle C = \angle R$  .....(ii)

Since AD and PM are medians, they will divide their opposite sides.

$$\therefore$$
 BD = BC/2 and QM = QR/2 .....(iii)

From equations (i) and (iii), we get

$$AB/PQ = BD/QM$$
 .....(iv)

In  $\triangle ABD$  and  $\triangle PQM$ ,

From equation (ii), we have

$$\angle B = \angle Q$$

From equation (iv), we have,

$$AB/PQ = BD/QM$$

$$\therefore \triangle ABD \sim \triangle PQM$$
 (SAS similarity criterion)

$$\Rightarrow$$
AB/PQ = BD/QM = AD/PM



EXERCISE 6.4 PAGE: 143

1. Let  $\triangle$ ABC ~  $\triangle$ DEF and their areas be, respectively, 64 cm<sup>2</sup> and 121 cm<sup>2</sup>. If EF = 15.4 cm, find BC.

**Solution:** Given,  $\triangle ABC \sim \triangle DEF$ ,

Area of  $\triangle ABC = 64 \text{ cm}^2$ 

Area of  $\Delta DEF = 121 \text{ cm}^2$ 

EF = 15.4 cm

$$\therefore \frac{\textit{Area of } \Delta \textit{ABC}}{\textit{Area of } \Delta \textit{DEF}} = \frac{\textit{AB}^2}{\textit{DE}^2}$$

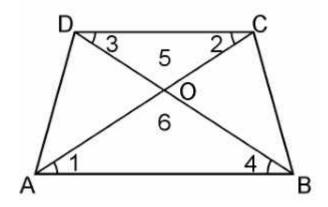
As we know, if two triangles are similar, ratio of their areas are equal to the square of the ratio of their corresponding sides,

- $=AC^2/DF^2=BC^2/EF^2$
- $\therefore 64/121 = BC^2/EF^2$
- $\Rightarrow$  (8/11)<sup>2</sup> = (BC/15.4)<sup>2</sup>
- $\Rightarrow$  8/11 = BC/15.4
- $\Rightarrow$  BC =  $8 \times 15.4/11$
- $\Rightarrow$  BC = 8 × 1.4
- $\Rightarrow$  BC = 11.2 cm

2. Diagonals of a trapezium ABCD with AB  $\parallel$  DC intersect each other at the point O. If AB = 2CD, find the ratio of the areas of triangles AOB and COD.

#### **Solution:**

Given, ABCD is a trapezium with AB || DC. Diagonals AC and BD intersect each other at point O.



In  $\triangle$ AOB and  $\triangle$ COD, we have

 $\angle 1 = \angle 2$  (Alternate angles)

 $\angle 3 = \angle 4$  (Alternate angles)

 $\angle 5 = \angle 6$  (Vertically opposite angle)



# NCERT Solutions for Class 10 Maths Chapter 6 -Triangles

 $\therefore \triangle AOB \sim \triangle COD [AAA similarity criterion]$ 

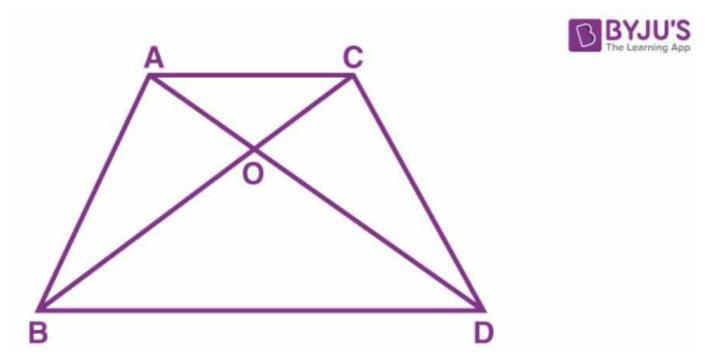
As we know, If two triangles are similar then the ratio of their areas are equal to the square of the ratio of their corresponding sides. Therefore,

Area of  $(\Delta AOB)/A$ rea of  $(\Delta COD) = AB^2/CD^2$ 

- $= (2CD)^2/CD^2$  [: AB = 2CD]
- $\therefore$  Area of ( $\triangle$ AOB)/Area of ( $\triangle$ COD)
- $=4CD^{2}/CD^{2}=4/1$

Hence, the required ratio of the area of  $\triangle AOB$  and  $\triangle COD = 4:1$ 

3. In the figure, ABC and DBC are two triangles on the same base BC. If AD intersects BC at O, show that area  $(\Delta ABC)$ /area  $(\Delta DBC) = AO/DO$ .



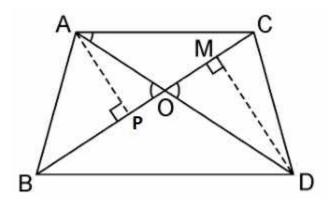
#### **Solution:**

Given, ABC and DBC are two triangles on the same base BC. AD intersects BC at O.

We have to prove: Area  $(\Delta ABC)/A$ rea  $(\Delta DBC) = AO/DO$ 

Let us draw two perpendiculars AP and DM on line BC.





We know that area of a triangle =  $1/2 \times Base \times Height$ 

$$\therefore \frac{\text{ar}(\Delta ABC)}{\text{ar}(\Delta DEF)} = \frac{\frac{1}{2}BC \times AP}{\frac{1}{2}BC \times DM} = \frac{AP}{DM}$$

In  $\triangle$ APO and  $\triangle$ DMO,

 $\angle APO = \angle DMO (Each 90^{\circ})$ 

 $\angle AOP = \angle DOM$  (Vertically opposite angles)

∴ ΔAPO ~ ΔDMO (AA similarity criterion)

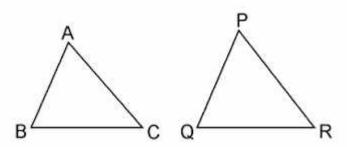
 $\therefore$  AP/DM = AO/DO

 $\Rightarrow$  Area ( $\triangle$ ABC)/Area ( $\triangle$ DBC) = AO/DO.

4. If the areas of two similar triangles are equal, prove that they are congruent.

## **Solution:**

Say  $\triangle$ ABC and  $\triangle$ PQR are two similar triangles and equal in area



Now let us prove  $\triangle ABC \cong \triangle PQR$ .

Since,  $\triangle ABC \sim \triangle PQR$ 

 $\therefore$  Area of ( $\triangle$ ABC)/Area of ( $\triangle$ PQR) = BC<sup>2</sup>/QR<sup>2</sup>

 $\Rightarrow$  BC<sup>2</sup>/QR<sup>2</sup> = 1 [Since, Area( $\triangle$ ABC) = ( $\triangle$ PQR)

 $\Rightarrow$  BC<sup>2</sup>/QR<sup>2</sup>



 $\Rightarrow$  BC = OR

Similarly, we can prove that

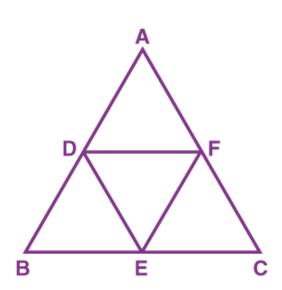
AB = PQ and AC = PR

Thus,  $\triangle ABC \cong \triangle PQR$  [SSS criterion of congruence]

5. D, E and F are respectively the mid-points of sides AB, BC and CA of  $\triangle$ ABC. Find the ratio of the area of  $\triangle$ DEF and  $\triangle$ ABC.

#### **Solution:**





D, E, and F are the mid-points of  $\triangle ABC$ 

∴ DE || AC and

DE = (1/2) AC (Midpoint theorem) .... (1)

In  $\Delta BED$  and  $\Delta BCA$ 

 $\angle BED = \angle BCA$  (Corresponding angles)

 $\angle BDE = \angle BAC$  (Corresponding angles)

 $\angle EBD = \angle CBA$  (Common angles)

∴ΔBED~ΔBCA (AAA similarity criterion)

ar ( $\Delta$ BED) / ar ( $\Delta$ BCA)=(DE/AC)<sup>2</sup>

 $\Rightarrow$ ar ( $\triangle$ BED) / ar ( $\triangle$ BCA) = (1/4) [From (1)]

 $\Rightarrow$ ar ( $\triangle$ BED) = (1/4) ar ( $\triangle$ BCA)

Similarly,

ar ( $\triangle$ CFE) = (1/4) ar (CBA) and ar ( $\triangle$ ADF) = (1/4) ar ( $\triangle$ ADF) = (1/4) ar ( $\triangle$ ABC)

Also,

 $ar(\Delta DEF) = ar(\Delta ABC) - [ar(\Delta BED) + ar(\Delta CFE) + ar(\Delta ADF)]$ 

 $\Rightarrow$ ar ( $\triangle$ DEF) = ar ( $\triangle$ ABC) - (3/4) ar ( $\triangle$ ABC) = (1/4) ar ( $\triangle$ ABC)

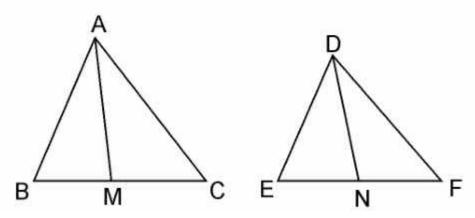
 $\Rightarrow$ ar ( $\triangle$ DEF) / ar ( $\triangle$ ABC) = (1/4)

6. Prove that the ratio of the areas of two similar triangles is equal to the square of the ratio of their corresponding medians.

#### **Solution:**



Given: AM and DN are the medians of triangles ABC and DEF respectively and  $\triangle$ ABC  $\sim$   $\triangle$ DEF.



We have to prove: Area( $\triangle ABC$ )/Area( $\triangle DEF$ ) = AM<sup>2</sup>/DN<sup>2</sup>

Since,  $\triangle ABC \sim \triangle DEF$  (Given)

 $\therefore$  Area( $\triangle$ ABC)/Area( $\triangle$ DEF) = (AB<sup>2</sup>/DE<sup>2</sup>) .....(i)

and, AB/DE = BC/EF = CA/FD .....(ii)

$$\Rightarrow \frac{AB}{DE} = \frac{\frac{1}{2}BC}{\frac{1}{2}EF} = \frac{CD}{FD}$$

In  $\triangle$ ABM and  $\triangle$ DEN,

Since  $\triangle ABC \sim \triangle DEF$ 

 $\therefore \angle B = \angle E$ 

AB/DE = BM/EN [Already Proved in equation (i)]

∴ ∆ABC ~ ∆DEF [SAS similarity criterion]

$$\Rightarrow$$
 AB/DE = AM/DN .....(iii)

∴ ΔABM ~ ΔDEN

As the areas of two similar triangles are proportional to the squares of the corresponding sides.

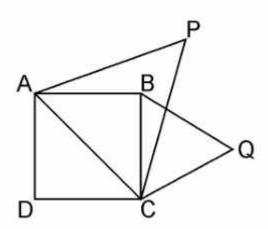
 $\therefore$  area( $\triangle ABC$ )/area( $\triangle DEF$ ) =  $AB^2/DE^2 = AM^2/DN^2$ 

Hence, proved.

7. Prove that the area of an equilateral triangle described on one side of a square is equal to half the area of the equilateral triangle described on one of its diagonals.

**Solution:** 





Given, ABCD is a square whose one diagonal is AC.  $\triangle$ APC and  $\triangle$ BQC are two equilateral triangles described on the diagonals AC and side BC of the square ABCD.

 $Area(\Delta BQC) = \frac{1}{2} Area(\Delta APC)$ 

Since,  $\triangle$ APC and  $\triangle$ BQC are both equilateral triangles, as per given,

∴ ∆APC ~ ∆BQC [AAA similarity criterion]

 $\therefore$  area( $\triangle$ APC)/area( $\triangle$ BQC) = (AC<sup>2</sup>/BC<sup>2</sup>) = AC<sup>2</sup>/BC<sup>2</sup>

Since, Diagonal =  $\sqrt{2}$  side =  $\sqrt{2}$  BC = AC

$$(\frac{\sqrt{2}BC}{BC})^2 = 2$$

 $\Rightarrow$  area( $\triangle$ APC) = 2 × area( $\triangle$ BQC)

 $\Rightarrow$  area( $\triangle$ BQC) = 1/2area( $\triangle$ APC)

Hence, proved.

Tick the correct answer and justify:

8. ABC and BDE are two equilateral triangles such that D is the mid-point of BC. Ratio of the area of triangles ABC and BDE is

(A) 2:1

(B) 1:2

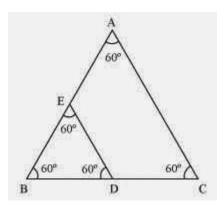
(C) 4:1

(D) 1:4

**Solution:** 

Given,  $\triangle$ ABC and  $\triangle$ BDE are two equilateral triangle. D is the midpoint of BC.





$$\therefore$$
 BD = DC = 1/2BC

Let each side of triangle is 2a.

As,  $\triangle ABC \sim \triangle BDE$ 

: Area(
$$\triangle$$
ABC)/Area( $\triangle$ BDE) = AB<sup>2</sup>/BD<sup>2</sup> = (2a)<sup>2</sup>/(a)<sup>2</sup> = 4a<sup>2</sup>/a<sup>2</sup> = 4/1 = 4:1

Hence, the correct answer is (C).

# 9. Sides of two similar triangles are in the ratio 4:9. Areas of these triangles are in the ratio

(A) 2:3

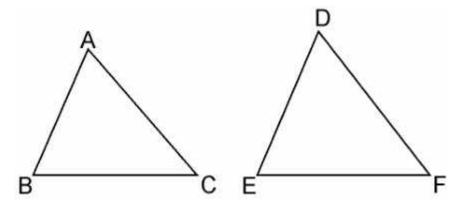
(B) 4:9

(C) 81:16

(D) 16:81

#### **Solution:**

Given, Sides of two similar triangles are in the ratio 4:9.



Let ABC and DEF are two similar triangles, such that,

 $\Delta ABC \sim \Delta DEF$ 

And AB/DE = AC/DF = BC/EF = 4/9

As, the ratio of the areas of these triangles will be equal to the square of the ratio of the corresponding sides,

 $\therefore Area(\Delta ABC)/Area(\Delta DEF) = AB^2/DE^2$ 

: Area( $\triangle$ ABC)/Area( $\triangle$ DEF) =  $(4/9)^2$  = 16/81 = 16:81

Hence, the correct answer is (D).



EXERCISE 6.5 PAGE: 150

- 1. Sides of triangles are given below. Determine which of them are right triangles. In case of a right triangle, write the length of its hypotenuse.
- (i) 7 cm, 24 cm, 25 cm
- (ii) 3 cm, 8 cm, 6 cm
- (iii) 50 cm, 80 cm, 100 cm
- (iv) 13 cm, 12 cm, 5 cm

#### **Solution:**

(i) Given, sides of the triangle are 7 cm, 24 cm, and 25 cm.

Squaring the lengths of the sides of the, we will get 49, 576, and 625.

$$49 + 576 = 625$$

$$(7)^2 + (24)^2 = (25)^2$$

Therefore, the above equation satisfies, Pythagoras theorem. Hence, it is right angled triangle.

Length of Hypotenuse = 25 cm

(ii) Given, sides of the triangle are 3 cm, 8 cm, and 6 cm.

Squaring the lengths of these sides, we will get 9, 64, and 36.

Clearly, 
$$9 + 36 \neq 64$$

Or, 
$$3^2 + 6^2 \neq 8^2$$

Therefore, the sum of the squares of the lengths of two sides is not equal to the square of the length of the hypotenuse.

Hence, the given triangle does not satisfies Pythagoras theorem.

(iii) Given, sides of triangle's are 50 cm, 80 cm, and 100 cm.

Squaring the lengths of these sides, we will get 2500, 6400, and 10000.

However,  $2500 + 6400 \neq 10000$ 

Or, 
$$50^2 + 80^2 \neq 100^2$$

As you can see, the sum of the squares of the lengths of two sides is not equal to the square of the length of the third side.

Therefore, the given triangle does not satisfies Pythagoras theorem.

Hence, it is not a right triangle.

(iv) Given, sides are 13 cm, 12 cm, and 5 cm.

Squaring the lengths of these sides, we will get 169, 144, and 25.

Thus, 
$$144 + 25 = 169$$

Or, 
$$12^2 + 5^2 = 13^2$$

The sides of the given triangle are satisfying Pythagoras theorem.

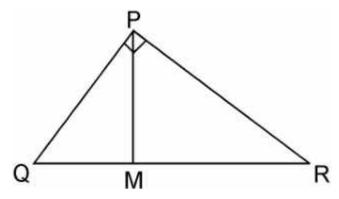


Therefore, it is a right triangle.

Hence, length of the hypotenuse of this triangle is 13 cm.

# 2. PQR is a triangle right angled at P and M is a point on QR such that PM $\perp$ QR. Show that PM<sup>2</sup> = QM $\times$ MR. Solution:

Given,  $\triangle PQR$  is right angled at P is a point on QR such that PM  $\perp QR$ 



We have to prove,  $PM^2 = QM \times MR$ 

In  $\Delta$ PQM, by Pythagoras theorem

$$PQ^2 = PM^2 + QM^2$$

Or, 
$$PM^2 = PQ^2 - QM^2$$
 .....(i)

In  $\triangle PMR$ , by Pythagoras theorem

$$PR^2 = PM^2 + MR^2$$

Or, 
$$PM^2 = PR^2 - MR^2$$
....(ii)

Adding equation, (i) and (ii), we get,

$$2PM^2 = (PQ^2 + PM^2) - (QM^2 + MR^2)$$

$$= QR^2 - QM^2 - MR^2$$
 [:  $QR^2 = PQ^2 + PR^2$ ]

$$= (QM + MR)^2 - QM^2 - MR^2$$

$$= 2QM \times MR$$

$$\therefore PM^2 = QM \times MR$$

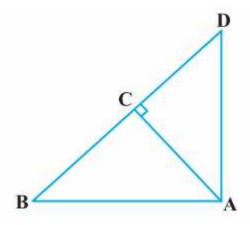
# 3. In Figure, ABD is a triangle right angled at A and AC $\perp$ BD. Show that

(i) 
$$AB^2 = BC \times BD$$

(ii) 
$$AC^2 = BC \times DC$$

(iii) 
$$AD^2 = BD \times CD$$





#### **Solution:**

- (i) In  $\triangle$ ADB and  $\triangle$ CAB,
- $\angle DAB = \angle ACB \text{ (Each } 90^\circ\text{)}$
- $\angle ABD = \angle CBA$  (Common angles)
- ∴ ΔADB ~ ΔCAB [AA similarity criterion]
- $\Rightarrow$  AB/CB = BD/AB
- $\Rightarrow AB^2 = CB \times BD$
- (ii) Let  $\angle CAB = x$

In  $\Delta CBA$ ,

$$\angle CBA = 180^{\circ} - 90^{\circ} - x$$

$$\angle CBA = 90^{\circ} - x$$

Similarly, in  $\Delta CAD$ 

$$\angle CAD = 90^{\circ} - \angle CBA$$

$$= 90^{\circ} - x$$

$$\angle CDA = 180^{\circ} - 90^{\circ} - (90^{\circ} - x)$$

$$\angle CDA = x$$

In  $\triangle$ CBA and  $\triangle$ CAD, we have

$$\angle CBA = \angle CAD$$

$$\angle CAB = \angle CDA$$

$$\angle ACB = \angle DCA \text{ (Each } 90^\circ\text{)}$$

$$\therefore \Delta CBA \sim \Delta CAD$$
 [AAA similarity criterion]

$$\Rightarrow$$
 AC/DC = BC/AC

$$\Rightarrow$$
 AC<sup>2</sup> = DC × BC



(iii) In ΔDCA and ΔDAB,

 $\angle DCA = \angle DAB \text{ (Each } 90^\circ\text{)}$ 

 $\angle$ CDA =  $\angle$ ADB (common angles)

∴ ΔDCA ~ ΔDAB [AA similarity criterion]

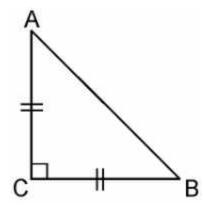
 $\Rightarrow$  DC/DA = DA/DA

 $\Rightarrow$  AD<sup>2</sup> = BD × CD

4. ABC is an isosceles triangle right angled at C. Prove that  $AB^2 = 2AC^2$ .

#### **Solution:**

Given,  $\triangle$ ABC is an isosceles triangle right angled at C.



In  $\triangle ACB$ ,  $\angle C = 90^{\circ}$ 

AC = BC (By isosceles triangle property)

 $AB^2 = AC^2 + BC^2$  [By Pythagoras theorem]

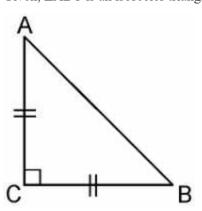
 $= AC^2 + AC^2$  [Since, AC = BC]

 $AB^2 = 2AC^2$ 

5. ABC is an isosceles triangle with AC = BC. If  $AB^2 = 2AC^2$ , prove that ABC is a right triangle.

#### **Solution:**

Given,  $\triangle$ ABC is an isosceles triangle having AC = BC and AB<sup>2</sup> = 2AC<sup>2</sup>





In  $\triangle ACB$ ,

AC = BC

 $AB^2 = 2AC^2$ 

 $AB^2 = AC^2 + AC^2$ 

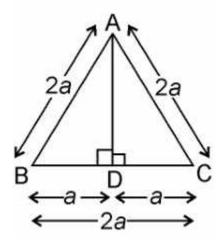
 $= AC^2 + BC^2$  [Since, AC = BC]

Hence, by Pythagoras theorem  $\triangle$ ABC is right angle triangle.

# 6. ABC is an equilateral triangle of side 2a. Find each of its altitudes.

#### **Solution:**

Given, ABC is an equilateral triangle of side 2a.



Draw, AD  $\perp$  BC

In  $\triangle$ ADB and  $\triangle$ ADC,

AB = AC

AD = AD

 $\angle ADB = \angle ADC$  [Both are 90°]

Therefore,  $\triangle ADB \cong \triangle ADC$  by RHS congruence.

Hence, BD = DC [by CPCT]

In right angled  $\triangle ADB$ ,

 $AB^{\scriptscriptstyle 2} = AD^{\scriptscriptstyle 2} + BD^{\scriptscriptstyle 2}$ 

 $(2a)^2 = AD^2 + a^2$ 

 $\Rightarrow$  AD<sup>2=</sup>  $4a^2 - a^2$ 

 $\Rightarrow$  AD<sup>2=</sup> 3 $a^2$ 

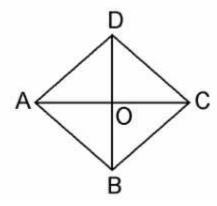
 $\Rightarrow$  AD=  $\sqrt{3}a$ 

7. Prove that the sum of the squares of the sides of rhombus is equal to the sum of the squares of its diagonals.



#### **Solution:**

Given, ABCD is a rhombus whose diagonals AC and BD intersect at O.



We have to prove, as per the question,

$$AB^2 + BC^2 + CD^2 + AD^2 = AC^2 + BD^2$$

Since, the diagonals of a rhombus bisect each other at right angles.

Therefore, AO = CO and BO = DO

In  $\triangle AOB$ ,

$$\angle AOB = 90^{\circ}$$

$$AB^2 = AO^2 + BO^2$$
.....(i) [By Pythagoras theorem]

Similarly,

$$AD^2 = AO^2 + DO^2 \dots (ii)$$

$$DC^2 = DO^2 + CO^2$$
.....(iii)

$$BC^2 = CO^2 + BO^2 \dots (iv)$$

Adding equations (i) + (ii) + (iv), we get,

$$AB^2 + AD^2 + DC^2 + BC^2 = 2(AO^2 + BO^2 + DO^2 + CO^2)$$

$$= 4AO^2 + 4BO^2$$
 [Since, AO = CO and BO = DO]

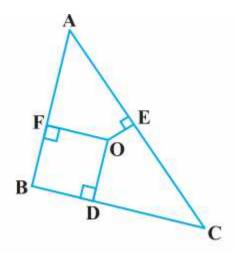
$$= (2AO)^2 + (2BO)^2 = AC^2 + BD^2$$

$$AB^2 + AD^2 + DC^2 + BC^2 = AC^2 + BD^2$$

Hence, proved.

8. In Fig. 6.54, O is a point in the interior of a triangle.





ABC, OD  $\perp$  BC, OE  $\perp$  AC and OF  $\perp$  AB. Show that:

(i)  $OA^2 + OB^2 + OC^2 - OD^2 - OE^2 - OF^2 = AF^2 + BD^2 + CE^2$ ,

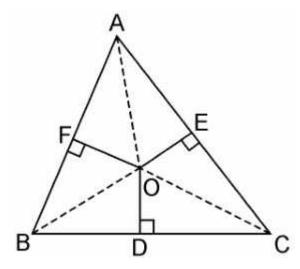
(ii)  $AF^2 + BD^2 + CE^2 = AE^2 + CD^2 + BF^2$ .

## **Solution:**

Given, in  $\triangle ABC$ , O is a point in the interior of a triangle.

And OD  $\perp$  BC, OE  $\perp$  AC and OF  $\perp$  AB.

Join OA, OB and OC



(i) By Pythagoras theorem in  $\triangle AOF$ , we have

 $OA^{\scriptscriptstyle 2} = OF^{\scriptscriptstyle 2} + AF^{\scriptscriptstyle 2}$ 

Similarly, in ΔBOD

 $OB^{\scriptscriptstyle 2} = OD^{\scriptscriptstyle 2} + BD^{\scriptscriptstyle 2}$ 

Similarly, in  $\Delta COE$ 

 $OC^2 = OE^2 + EC^2$ 

Adding these equations,



$$OA^2 + OB^2 + OC^2 = OF^2 + AF^2 + OD^2 + BD^2 + OE^2 + EC^2$$

$$OA^2 + OB^2 + OC^2 - OD^2 - OE^2 - OF^2 = AF^2 + BD^2 + CE^2$$
.

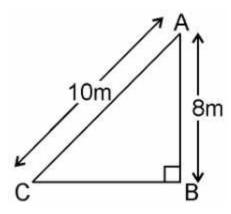
(ii) 
$$AF^2 + BD^2 + EC^2 = (OA^2 - OE^2) + (OC^2 - OD^2) + (OB^2 - OF^2)$$

$$AF^2 + BD^2 + CE^2 = AE^2 + CD^2 + BF^2$$
.

9. A ladder 10 m long reaches a window 8 m above the ground. Find the distance of the foot of the ladder from base of the wall.

#### **Solution:**

Given, a ladder 10 m long reaches a window 8 m above the ground.



Let BA be the wall and AC be the ladder,

Therefore, by Pythagoras theorem,

$$AC^2 = AB^2 + BC^2$$

$$10^2 = 8^2 + BC^2$$

$$BC^2 = 100 - 64$$

$$BC^2 = 36$$

$$BC = 6m$$

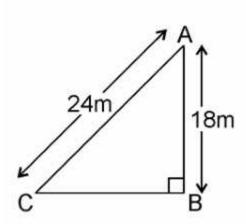
Therefore, the distance of the foot of the ladder from the base of the wall is 6 m.

10. A guy wire attached to a vertical pole of height 18 m is 24 m long and has a stake attached to the other end. How far from the base of the pole should the stake be driven so that the wire will be taut?

#### **Solution:**

Given, a guy wire attached to a vertical pole of height 18 m is 24 m long and has a stake attached to the other end.





Let AB be the pole and AC be the wire.

By Pythagoras theorem,

$$AC^2 = AB^2 + BC^2$$

$$24^2 = 18^2 + BC^2$$

$$BC^2 = 576 - 324$$

$$BC^2 = 252$$

$$BC = 6\sqrt{7}m$$

Therefore, the distance from the base is  $6\sqrt{7}$ m.

11. An aeroplane leaves an airport and flies due north at a speed of 1,000 km per hour. At the same time, another aeroplane leaves the same airport and flies due west at a speed of 1,200 km per hour. How far apart will be the two planes after

$$1\frac{1}{2}$$
 hours?

**Solution:** 

Given,

Speed of first aeroplane = 1000 km/hr

Distance covered by first aeroplane flying due north in

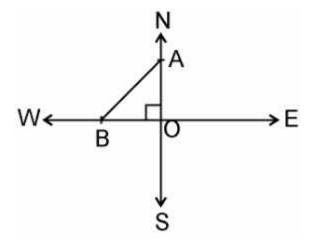
$$1\frac{1}{2}$$
 hours (OA) =  $1000 \times 3/2$  km =  $1500$  km

Speed of second aeroplane = 1200 km/hr

Distance covered by second aeroplane flying due west in

$$1\frac{1}{2}$$
 hours (OB) =  $1200 \times 3/2$  km =  $1800$  km





In right angle  $\Delta AOB$ , by Pythagoras Theorem,

$$AB^2 = AO^2 + OB^2$$

$$\Rightarrow$$
 AB<sup>2</sup> = (1500)<sup>2</sup> + (1800)<sup>2</sup>

$$\Rightarrow$$
 AB =  $\sqrt{(2250000 + 3240000)}$ 

$$=\sqrt{5490000}$$

$$\Rightarrow$$
 AB =  $300\sqrt{61}$  km

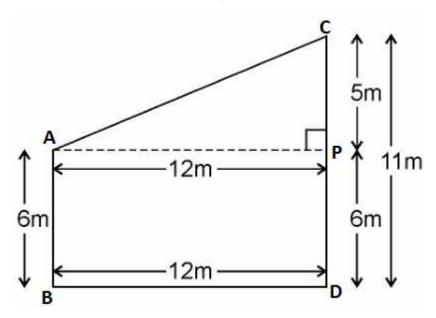
Hence, the distance between two aeroplanes will be  $300\sqrt{61}$  km.

12. Two poles of heights 6 m and 11 m stand on a plane ground. If the distance between the feet of the poles is 12 m, find the distance between their tops.

## **Solution:**

Given, Two poles of heights 6 m and 11 m stand on a plane ground.

And distance between the feet of the poles is 12 m.





Let AB and CD be the poles of height 6m and 11m.

Therefore, CP = 11 - 6 = 5m

From the figure, it can be observed that AP = 12m

By Pythagoras theorem for  $\triangle$ APC, we get,

$$AP^2 = PC^2 + AC^2$$

$$(12m)^2 + (5m)^2 = (AC)^2$$

$$AC^2 = (144+25) \text{ m}^2 = 169 \text{ m}^2$$

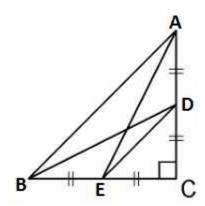
$$AC = 13m$$

Therefore, the distance between their tops is 13 m.

13. D and E are points on the sides CA and CB respectively of a triangle ABC right angled at C. Prove that  $AE^2 + BD^2 = AB^2 + DE^2$ .

# **Solution:**

Given, D and E are points on the sides CA and CB respectively of a triangle ABC right angled at C.



By Pythagoras theorem in  $\triangle$ ACE, we get

$$AC^2 + CE^2 = AE^2$$
 .....(i)

In  $\Delta BCD$ , by Pythagoras theorem, we get

$$BC^2 + CD^2 = BD^2$$
.....(ii)

From equations (i) and (ii), we get,

$$AC^2 + CE^2 + BC^2 + CD^2 = AE^2 + BD^2$$
 .....(iii)

In  $\triangle$ CDE, by Pythagoras theorem, we get

$$DE^2 = CD^2 + CE^2$$

In  $\triangle$ ABC, by Pythagoras theorem, we get

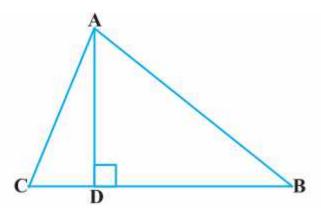
$$AB^2 = AC^2 + CB^2$$

Putting the above two values in equation (iii), we get

$$DE^2 + AB^2 = AE^2 + BD^2.$$



14. The perpendicular from A on side BC of a  $\Delta$  ABC intersects BC at D such that DB = 3CD (see Figure). Prove that  $2AB^2 = 2AC^2 + BC^2$ .



#### **Solution:**

Given, the perpendicular from A on side BC of a  $\Delta$  ABC intersects BC at D such that;

DB = 3CD.

In  $\triangle$  ABC,

AD  $\perp$ BC and BD = 3CD

In right angle triangle, ADB and ADC, by Pythagoras theorem,

$$AB^2 = AD^2 + BD^2 \dots (i)$$

$$AC^2 = AD^2 + DC^2$$
 .....(ii)

Subtracting equation (ii) from equation (i), we get

$$AB^2 - AC^2 = BD^2 - DC^2$$

$$= 9CD^2 - CD^2$$
 [Since, BD = 3CD]

 $= 8CD^2$ 

$$= 8(BC/4)^{2}[Since, BC = DB + CD = 3CD + CD = 4CD]$$

Therefore,  $AB^2 - AC^2 = BC^2/2$ 

$$\Rightarrow 2(AB^2 - AC^2) = BC^2$$

$$\Rightarrow 2AB^2 - 2AC^2 = BC^2$$

$$\therefore 2AB^2 = 2AC^2 + BC^2.$$

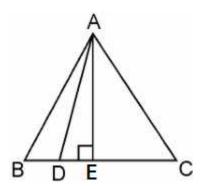
15. In an equilateral triangle ABC, D is a point on side BC such that BD = 1/3BC. Prove that 9AD<sup>2</sup> = 7AB<sup>2</sup>.

## **Solution:**

Given, ABC is an equilateral triangle.

And D is a point on side BC such that BD = 1/3BC





Let the side of the equilateral triangle be a, and AE be the altitude of  $\triangle$ ABC.

$$\therefore BE = EC = BC/2 = a/2$$

And, AE = 
$$a\sqrt{3/2}$$

Given, 
$$BD = 1/3BC$$

$$\therefore$$
 BD = a/3

$$DE = BE - BD = a/2 - a/3 = a/6$$

In  $\triangle$ ADE, by Pythagoras theorem,

$$AD^2 = AE^2 + DE^2$$

$$AD^{2} = \left(\frac{a\sqrt{3}}{2}\right)^{2} + \left(\frac{a}{6}\right)^{2}$$
$$= \left(\frac{3a^{2}}{4}\right) + \left(\frac{a^{2}}{36}\right)$$
$$= \frac{28a^{2}}{36}$$
$$= \frac{7}{9}AB^{2}$$

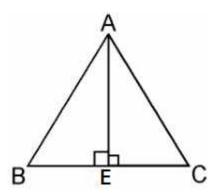
$$\Rightarrow$$
 9 AD<sup>2</sup> = 7 AB<sup>2</sup>

16. In an equilateral triangle, prove that three times the square of one side is equal to four times the square of one of its altitudes.

## **Solution:**

Given, an equilateral triangle say ABC,





Let the sides of the equilateral triangle be of length a, and AE be the altitude of  $\triangle ABC$ .

$$\therefore BE = EC = BC/2 = a/2$$

In  $\triangle ABE$ , by Pythagoras Theorem, we get

$$AB^2 = AE^2 + BE^2$$

$$a^2 = AE^2 + \left(\frac{a}{2}\right)^2$$

$$AE^2 = a^2 - \frac{a^2}{4}$$

$$AE^2 = \frac{3a^2}{4}$$

$$4AE^2 = 3a^2$$

 $\Rightarrow$  4 × (Square of altitude) = 3 × (Square of one side)

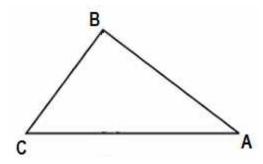
Hence, proved.

17. Tick the correct answer and justify: In  $\Delta ABC$ ,  $AB=6\sqrt{3}$  cm, AC=12 cm and BC=6 cm. The angle B is:

- (A)  $120^{\circ}$
- **(B)** 60°
- (C) 90°
- **(D)**  $45^{\circ}$

**Solution:** 

Given, in  $\triangle ABC$ ,  $AB = 6\sqrt{3}$  cm, AC = 12 cm and BC = 6 cm.





# NCERT Solutions for Class 10 Maths Chapter 6 - Triangles

We can observe that,

 $AB^2 = 108$ 

 $AC^2 = 144$ 

And,  $BC^2 = 36$ 

 $AB^{\scriptscriptstyle 2} + BC^{\scriptscriptstyle 2} = AC^{\scriptscriptstyle 2}$ 

The given triangle,  $\triangle ABC$ , is satisfying Pythagoras theorem.

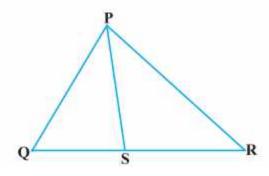
Therefore, the triangle is a right triangle, right-angled at B.

Hence, the correct answer is (C).



EXERCISE 6.6 PAGE: 152

1. In Figure, PS is the bisector of  $\angle$  QPR of  $\triangle$  PQR. Prove that QS/PQ = SR/PR

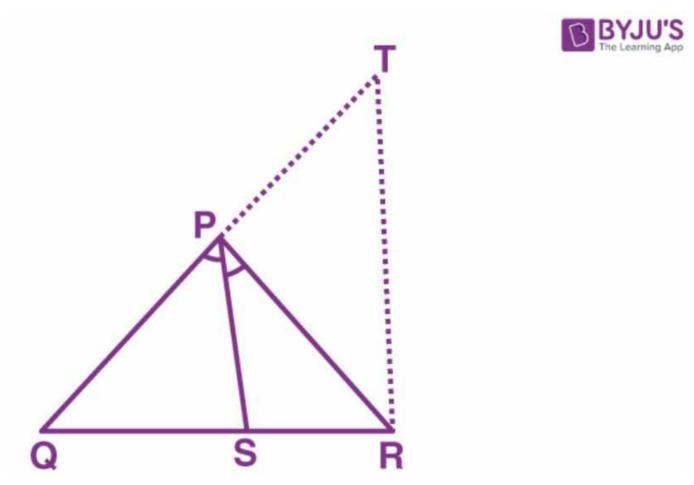


# **Solution:**

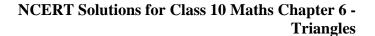
Let us draw a line segment RT parallel to SP which intersects extended line segment QP at point T.

Given, PS is the angle bisector of ∠QPR. Therefore,

$$\angle QPS = \angle SPR....(i)$$



As per the constructed figure,





CDD DDTCC	DOUTED	···
$\angle SPR = \angle PRT(Since.$	PS   I K ).	 (11)

 $\angle QPS = \angle QRT(Since, PS||TR) \dots (iii)$ 

From the above equations, we get,

 $\angle PRT = \angle QTR$ 

Therefore,

PT=PR

In  $\triangle$ QTR, by basic proportionality theorem,

QS/SR = QP/PT

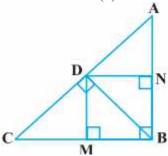
Since, PT=TR

Therefore,

QS/SR = PQ/PR

Hence, proved.

2. In Fig. 6.57, D is a point on hypotenuse AC of  $\triangle$ ABC, such that BD  $\bot$ AC, DM  $\bot$  BC and DN  $\bot$  AB. Prove that: (i) DM<sup>2</sup> = DN . MC (ii) DN<sup>2</sup> = DM . AN.

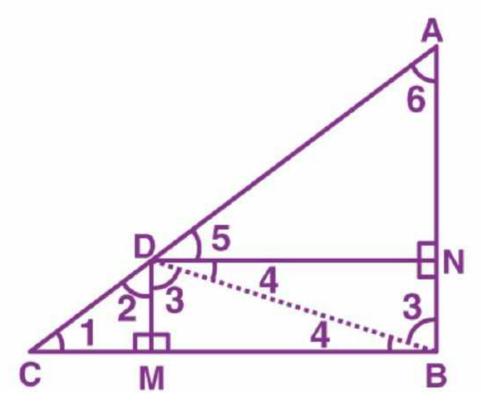


# **Solution:**

1. Let us join Point D and B.







Given,

BD  $\perp$ AC, DM  $\perp$  BC and DN  $\perp$  AB

Now from the figure we have,

DN || CB, DM || AB and  $\angle$ B = 90 °

Therefore, DMBN is a rectangle.

So, DN = MB and DM = NB

The given condition which we have to prove, is when D is the foot of the perpendicular drawn from B to AC.

$$\therefore \angle CDB = 90^{\circ} \Rightarrow \angle 2 + \angle 3 = 90^{\circ} \dots (i)$$

In  $\triangle$ CDM,  $\angle 1 + \angle 2 + \angle$ DMC =  $180^{\circ}$ 

$$\Rightarrow \angle 1 + \angle 2 = 90^{\circ}$$
 ..... (ii)

In  $\triangle DMB$ ,  $\angle 3 + \angle DMB + \angle 4 = 180^{\circ}$ 

$$\Rightarrow$$
  $\angle 3 + \angle 4 = 90^{\circ}$  ......(iii)

From equation (i) and (ii), we get

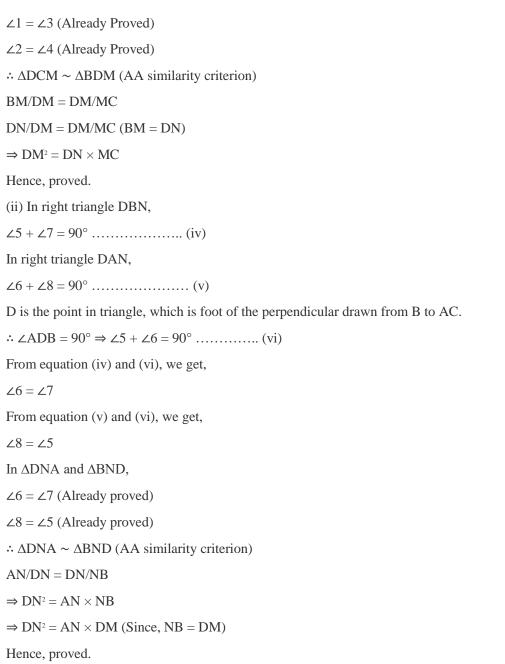
$$\angle 1 = \angle 3$$

From equation (i) and (iii), we get

$$\angle 2 = \angle 4$$

In  $\Delta$ DCM and  $\Delta$ BDM,

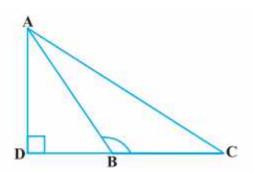




3. In Figure, ABC is a triangle in which  $\angle ABC > 90^{\circ}$  and AD  $\perp$  CB produced. Prove that

 $AC^2 = AB^2 + BC^2 + 2 BC.BD.$ 





## **Solution:**

By applying Pythagoras Theorem in  $\triangle$ ADB, we get,

$$AB^2 = AD^2 + DB^2$$
 ..... (i)

Again, by applying Pythagoras Theorem in  $\Delta ACD$ , we get,

$$AC^2 = AD^2 + DC^2$$

$$AC^2 = AD^2 + (DB + BC)^2$$

$$AC^2 = AD^2 + DB^2 + BC^2 + 2DB \times BC$$

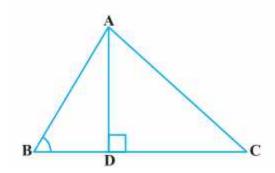
From equation (i), we can write,

$$AC^2 = AB^2 + BC^2 + 2DB \times BC$$

Hence, proved.

4. In Figure, ABC is a triangle in which  $\angle$  ABC < 90° and AD  $\bot$  BC. Prove that

$$AC^2 = AB^2 + BC^2 - 2 BC.BD.$$



#### **Solution:**

By applying Pythagoras Theorem in ΔADB, we get,

$$AB^2 = AD^2 + DB^2$$

We can write it as;

$$\Rightarrow$$
 AD<sup>2</sup> = AB<sup>2</sup> - DB<sup>2</sup> .....(i)

By applying Pythagoras Theorem in  $\triangle$ ADC, we get,

$$AD^2 + DC^2 = AC^2$$



From equation (i),

$$AB^2 - BD^2 + DC^2 = AC^2$$

$$AB^{2} - BD^{2} + (BC - BD)^{2} = AC^{2}$$

$$AC^2 = AB^2 - BD^2 + BC^2 + BD^2 - 2BC \times BD$$

$$AC^2 = AB^2 + BC^2 - 2BC \times BD$$

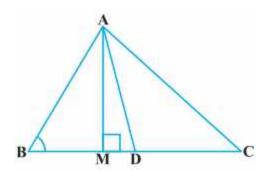
Hence, proved.

# 5. In Figure, AD is a median of a triangle ABC and AM $\perp$ BC. Prove that :

(i) 
$$AC^2 = AD^2 + BC.DM + 2 (BC/2)^2$$

(ii) 
$$AB^2 = AD^2 - BC.DM + 2 (BC/2)^2$$

(iii) 
$$AC^2 + AB^2 = 2 AD^2 + \frac{1}{2} BC^2$$



# **Solution:**

(i) By applying Pythagoras Theorem in  $\triangle$ AMD, we get,

$$AM^2 + MD^2 = AD^2$$
 ..... (i)

Again, by applying Pythagoras Theorem in  $\triangle$ AMC, we get,

$$AM^2 + MC^2 = AC^2$$

$$AM^2 + (MD + DC)^2 = AC^2$$

$$(AM^2 + MD^2) + DC^2 + 2MD.DC = AC^2$$

From equation(i), we get,

$$AD^2 + DC^2 + 2MD.DC = AC^2$$

Since, DC=BC/2, thus, we get,

$$AD^2 + (BC/2)^2 + 2MD.(BC/2)^2 = AC^2$$

$$AD^2 + (BC/2)^2 + 2MD \times BC = AC^2$$

Hence, proved.

(ii) By applying Pythagoras Theorem in ΔABM, we get;

$$AB^2 = AM^2 + MB^2$$

$$= (AD^2 - DM^2) + MB^2$$

# NCERT Solutions for Class 10 Maths Chapter 6 -Triangles

$$= (AD^2 - DM^2) + (BD - MD)^2$$

$$=AD^2-DM^2+BD^2+MD^2-2BD\times MD$$

$$= AD^2 + BD^2 - 2BD \times MD$$

$$= AD^2 + (BC/2)^2 - 2(BC/2) MD$$

$$= AD^2 + (BC/2)^2 - BC MD$$

Hence, proved.

(iii) By applying Pythagoras Theorem in ΔABM, we get,

$$AM^2 + MB^2 = AB^2$$
 ..... (i)

By applying Pythagoras Theorem in  $\triangle$ AMC, we get,

$$AM^2 + MC^2 = AC^2$$
 (ii)

Adding both the equations (i) and (ii), we get,

$$2AM^2 + MB^2 + MC^2 = AB^2 + AC^2$$

$$2AM^2 + (BD - DM)^2 + (MD + DC)^2 = AB^2 + AC^2$$

$$2AM^2 + BD^2 + DM^2 - 2BD.DM + MD^2 + DC^2 + 2MD.DC = AB^2 + AC^2$$

$$2AM^2 + 2MD^2 + BD^2 + DC^2 + 2MD (-BD + DC) = AB^2 + AC^2$$

$$2(AM^2 + MD^2) + (BC/2)^2 + (BC/2)^2 + 2MD(-BC/2 + BC/2)^2 = AB^2 + AC^2$$

$$2AD^2 + BC^2/2 = AB^2 + AC^2$$

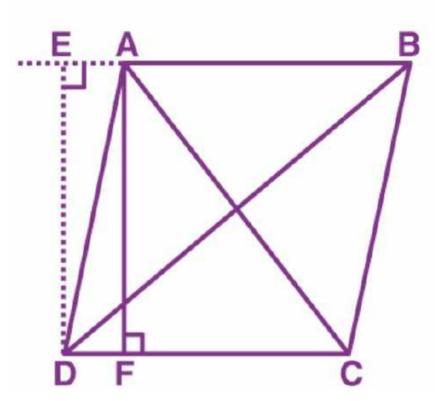
6. Prove that the sum of the squares of the diagonals of parallelogram is equal to the sum of the squares of its sides.

## **Solution:**

Let us consider, ABCD be a parallelogram. Now, draw perpendicular DE on extended side of AB, and draw a perpendicular AF meeting DC at point F.







By applying Pythagoras Theorem in ΔDEA, we get,

$$DE^2 + EA^2 = DA^2$$
 ..... (i)

By applying Pythagoras Theorem in ΔDEB, we get,

$$DE^2 + EB^2 = DB^2$$

$$DE^2 + (EA + AB)^2 = DB^2$$

$$(DE^2 + EA^2) + AB^2 + 2EA \times AB = DB^2$$

$$DA^{2} + AB^{2} + 2EA \times AB = DB^{2}$$
 ..... (ii)

By applying Pythagoras Theorem in  $\triangle ADF$ , we get,

$$AD^2 = AF^2 + FD^2$$

Again, applying Pythagoras theorem in  $\triangle$ AFC, we get,

$$AC^2 = AF^2 + FC^2 = AF^2 + (DC - FD)^2$$

$$= AF^2 + DC^2 + FD^2 - 2DC \times FD$$

$$= (AF^2 + FD^2) + DC^2 - 2DC \times FD AC^2$$

$$AC^2 = AD^2 + DC^2 - 2DC \times FD$$
 ......(iii)

Since ABCD is a parallelogram,

$$AB = CD \dots (iv)$$

And 
$$BC = AD \dots (v)$$



In  $\triangle DEA$  and  $\triangle ADF$ ,

 $\angle DEA = \angle AFD (Each 90^{\circ})$ 

 $\angle EAD = \angle ADF (EA \parallel DF)$ 

AD = AD (Common Angles)

 $\therefore \Delta EAD \cong \Delta FDA$  (AAS congruence criterion)

$$\Rightarrow$$
 EA = DF .....(vi)

Adding equations (i) and (iii), we get,

$$DA^{2} + AB^{2} + 2EA \times AB + AD^{2} + DC^{2} - 2DC \times FD = DB^{2} + AC^{2}$$

$$DA^{2} + AB^{2} + AD^{2} + DC^{2} + 2EA \times AB - 2DC \times FD = DB^{2} + AC^{2}$$

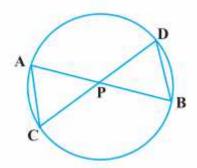
From equation (iv) and (vi),

$$BC^2 + AB^2 + AD^2 + DC^2 + 2EA \times AB - 2AB \times EA = DB^2 + AC^2$$

$$AB^2 + BC^2 + CD^2 + DA^2 = AC^2 + BD^2$$

# 7. In Figure, two chords AB and CD intersect each other at the point P. Prove that:

- (i)  $\triangle APC \sim \triangle DPB$
- (ii)  $AP \cdot PB = CP \cdot DP$



## **Solution:**

Firstly, let us join CB, in the given figure.

(i) In  $\triangle$ APC and  $\triangle$ DPB,

 $\angle$ APC =  $\angle$ DPB (Vertically opposite angles)

 $\angle CAP = \angle BDP$  (Angles in the same segment for chord CB)

Therefore,

 $\triangle$ APC ~  $\triangle$ DPB (AA similarity criterion)

(ii) In the above, we have proved that  $\triangle APC \sim \triangle DPB$ 

We know that the corresponding sides of similar triangles are proportional.

$$\therefore$$
 AP/DP = PC/PB = CA/BD

$$\Rightarrow$$
AP/DP = PC/PB

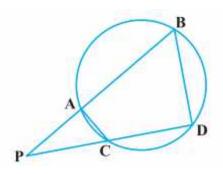


 $\therefore$ AP. PB = PC. DP

Hence, proved.

8. In Fig. 6.62, two chords AB and CD of a circle intersect each other at the point P (when produced) outside the circle. Prove that:

- (i)  $\triangle$  PAC  $\sim$   $\triangle$  PDB
- (ii)  $PA \cdot PB = PC \cdot PD$ .



# **Solution:**

(i) In  $\triangle PAC$  and  $\triangle PDB$ ,

 $\angle P = \angle P$  (Common Angles)

As we know, exterior angle of a cyclic quadrilateral is  $\angle PCA$  and  $\angle PBD$  is opposite interior angle, which are both equal.

 $\angle PAC = \angle PDB$ 

Thus,  $\triangle PAC \sim \triangle PDB(AA \text{ similarity criterion})$ 

(ii) We have already proved above,

 $\triangle APC \sim \triangle DPB$ 

We know that the corresponding sides of similar triangles are proportional.

Therefore,

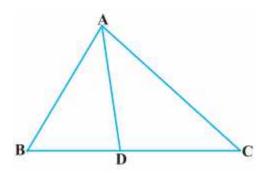
AP/DP = PC/PB = CA/BD

AP/DP = PC/PB

 $\therefore$  AP. PB = PC. DP

9. In Figure, D is a point on side BC of  $\triangle$  ABC such that BD/CD = AB/AC. Prove that AD is the bisector of  $\angle$  BAC.



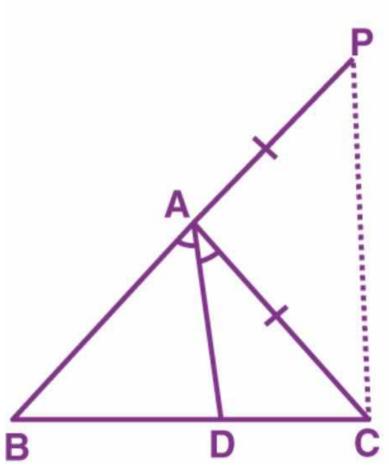


# **Solution:**

In the given figure, let us extend BA to P such that;

AP = AC.

Now join PC.





Given, BD/CD = AB/AC

 $\Rightarrow$  BD/CD = AP/AC

By using the converse of basic proportionality theorem, we get,

 $AD \parallel PC$ 

# NCERT Solutions for Class 10 Maths Chapter 6 -Triangles

$\angle BAD =$	ZAPC (Co	orresponding	angles)	 (i)

And, 
$$\angle DAC = \angle ACP$$
 (Alternate interior angles) ...... (ii)

By the new figure, we have;

$$AP = AC$$

$$\Rightarrow \angle APC = \angle ACP \dots (iii)$$

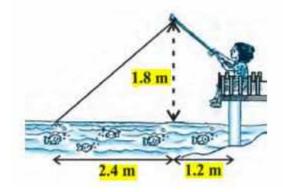
On comparing equations (i), (ii), and (iii), we get,

 $\angle BAD = \angle APC$ 

Therefore, AD is the bisector of the angle BAC.

Hence, proved.

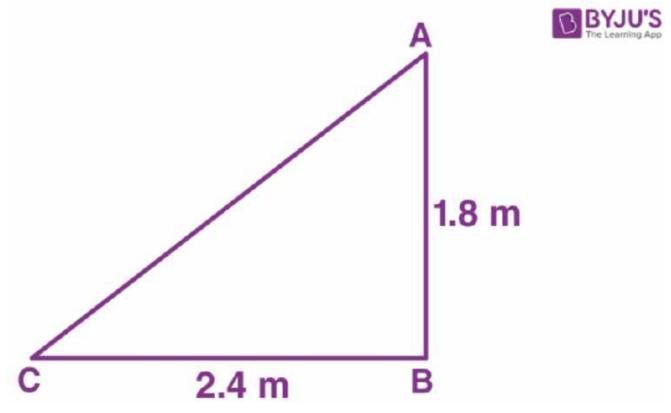
10. Nazima is fly fishing in a stream. The tip of her fishing rod is 1.8 m above the surface of the water and the fly at the end of the string rests on the water 3.6 m away and 2.4 m from a point directly under the tip of the rod. Assuming that her string (from the tip of her rod to the fly) is taut, how much string does she have out (see Figure)? If she pulls in the string at the rate of 5 cm per second, what will be the horizontal distance of the fly from her after 12 seconds?



#### **Solution:**

Let us consider, AB is the height of the tip of the fishing rod from the water surface and BC is the horizontal distance of the fly from the tip of the fishing rod. Therefore, AC is now the length of the string.





To find AC, we have to use Pythagoras theorem in  $\triangle$ ABC, is such way;

$$AC^2 = AB^2 + BC^2$$

$$AB^2 = (1.8 \text{ m})^2 + (2.4 \text{ m})^2$$

$$AB^2 = (3.24 + 5.76) \text{ m}^2$$

$$AB^2 = 9.00 \text{ m}^2$$

$$\implies$$
 AB =  $\sqrt{9}$  m = 3m

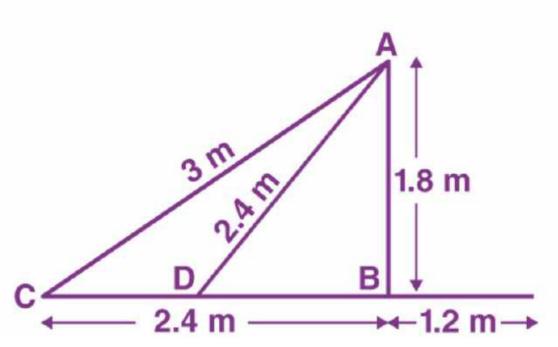
Thus, the length of the string out is 3 m.

As its given, she pulls the string at the rate of 5 cm per second.

Therefore, string pulled in 12 seconds =  $12 \times 5 = 60 \text{ cm} = 0.6 \text{ m}$ 







Let us say now, the fly is at point D after 12 seconds.

Length of string out after 12 seconds is AD.

AD = AC - String pulled by Nazima in 12 seconds

$$= (3.00 - 0.6) \text{ m}$$

= 2.4 m

In ΔADB, by Pythagoras Theorem,

$$AB^2 + BD^2 = AD^2$$

$$(1.8 \text{ m})^2 + \text{BD}^2 = (2.4 \text{ m})^2$$

$$BD^2 = (5.76 - 3.24) \text{ m}^2 = 2.52 \text{ m}^2$$

$$BD = 1.587 \text{ m}$$

Horizontal distance of fly = BD + 1.2 m

$$= (1.587 + 1.2) \text{ m} = 2.787 \text{ m}$$

$$= 2.79 \text{ m}$$