EXERCISE 11.1

PAGE NO: 120

Choose the correct answer from the given four options:

- 1. If the sum of the areas of two circles with radii R1 and R2 is equal to the area of a circle of radius R, then
 - $(\mathbf{A}) \mathbf{R}_1 + \mathbf{R}_2 = \mathbf{R}$
- (B) $R_1^2 + R_2^2 = R^2$
- (C) $R_1 + R_2 < R$
- (D) $R_1^2 + R_2^2 < R^2$

Solution:

(B)
$$R_1^2 + R_2^2 = R^2$$

Explanation:

According to the question,

Area of circle = Area of first circle + Area of second circle

$$\therefore \pi R^2 = \pi R_1^2 + \pi R_2^2$$

$$\Rightarrow R^2 = R_1^2 + R_2^2$$

- : Option B is correct.
- 2. If the sum of the circumferences of two circles with radii R1 and R2 is equal to the circumference of a circle of radius R, then
 - $(\mathbf{A}) \mathbf{R}_1 + \mathbf{R}_2 = \mathbf{R}$
- (B) $R_1 + R_2 > R$
- (C) $R_1 + R_2 < R$
- (D) Nothing definite can be said about the relation among R₁, R₂ & R.

Solution:

$$(\mathbf{A}) \mathbf{R}_1 + \mathbf{R}_2 = \mathbf{R}$$

Explanation:

According to the question,

Circumference of circle with radius R = Circumference of first circle with radius $R_1 + \text{Circumference}$ of second circle with radius R_2

$$\therefore 2\pi R = 2\pi R_1 + 2\pi R_2$$

$$\Rightarrow$$
 R = R₁+ R₂

- : Option A is correct.
- 3. If the circumference of a circle and the perimeter of a square are equal, then
 - (A) Area of the circle = Area of the square
 - (B) Area of the circle > Area of the square
 - (C) Area of the circle < Area of the square
 - (D) Nothing definite can be said about the relation between the areas of the circle & square.

Solution:

(B) Area of the circle > Area of the square

Explanation:

According to the question,

Circumference of a circle = Perimeter of square

Let r be the radius of the circle and a be the side of square.

: From the given condition, we have $2\pi r = 4a$

$$(22/7)r = 2a$$

$$\Rightarrow 11r = 7a$$

$$\Rightarrow$$
 a = (11/7)a

$$\Rightarrow$$
 r = (7/11)a(i)

Now, area of circle = $A_1 = \pi r^2$ and area of square = $A_2 = a^2$

From equation (i), we have

$$A_1 = \pi \times (7/11)^2$$

$$=(22/7)\times(49/121)a^2$$



$$= (14/11)a^2$$
 and $A_2 = a^2$

$$A_1 = (14/11) A_2$$

$$\Rightarrow A_1 > A_2$$

Hence, Area of the circle > Area of the square.

∴ Option B is correct.

4. Area of the largest triangle that can be inscribed in a semi-circle of radius r units is

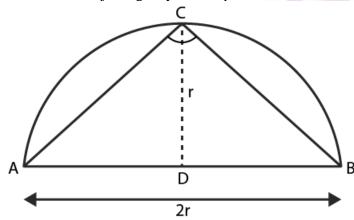
- (A) r^2 sq. units
- (B) $\frac{1}{2}r^2$ sq. units
- (C) $2 r^2$ sq. units
- (D) $\sqrt{2} r^2$ sq. units

Solution:

(A) r^2 sq. units

Explanation:

The largest triangle that can be inscribed in a semi-circle of radius r units is the triangle having its base as the diameter of the semi-circle and the two other sides are taken by considering a point C on the circumference of the semi-circle and joining it by the end points of diameter A and B.



 \therefore \angle C = 90° (by the properties of circle)

So, $\triangle ABC$ is right angled triangle with base as diameter AB of the circle and height be CD.

Height of the triangle = r

- ∴ Area of largest $\triangle ABC = (1/2) \times Base \times Height = (1/2) \times AB \times CD$
- $= (1/2) \times 2r \times r = r^2$ sq. units
- : Option A is correct.

5. If the perimeter of a circle is equal to that of a square, then the ratio of their areas is

- (A) 22:7
- (B) 14:11
- (C) 7 : 22
- (D) 11: 14

Solution:

(B) 14:11

Explanation:

Let r be the radius of the circle and a be the side of the square.

According to the question,

Perimeter of a circle = Perimeter of a square

 $\Rightarrow 2\pi r = 4a$

 \Rightarrow a = $\pi r/2$

Area of the circle = r^2 and Area of the square = a^2

Now, Ratio of their areas = (Area of circle)/(Area of square)



$$= \frac{\pi r^2}{a^2} = \frac{\pi r^2}{\left(\frac{\pi r^2}{2}\right)^2} = \frac{\pi r^2}{\frac{\pi^2 r^2}{4}}$$

 $=4/\pi$

= [4/(22/7)]

= 14/11

: Option B is correct.





EXERCISE 11.2

PAGE NO: 122

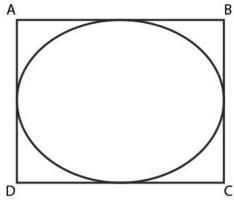
1. Is the area of the circle inscribed in a square of side a cm, a^2 cm²? Give reasons for your answer. Solution:

False

Explanation:

Let a be the side of square.

We are given that the circle is inscribed in the square.



Diameter of circle = Side of square = a

Radius of the circle = a/2

Area of the circle = $\pi r^2 = \pi (a/2)^2 = (\pi a^2)/4 \text{ cm}^2$

Hence, area of the circle is $(\pi a^2)/4$ cm²

Thus the area of the circle inscribed in a square of side a cm is not a² cm²

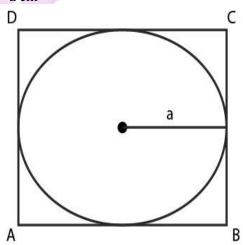
2. Will it be true to say that the perimeter of a square circumscribing a circle of radius a cm is 8a cm? Give reasons for your answer.

Solution:

True

Explanation:

Let r be the radius of circle = a cm



 \therefore Diameter of the circle = d = 2 × Radius = 2a cm As the circle is inscribed in the square, therefore, Side of a square = Diameter of circle = 2a cm

Hence, Perimeter of a square = $4 \times (\text{side}) = 4 \times 2a = 8a \text{ cm}$

Thus, it will be true to say that the perimeter of a square circumscribing a circle of radius a cm is 8a cm.

3. In Fig 11.3, a square is inscribed in a circle of diameter d and another square is circumscribing the circle. Is the area of the outer square four times the area of the inner square? Give reasons for your answer.

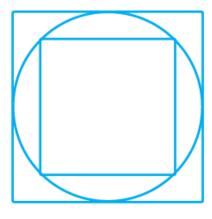


Fig.11.3

Solution:

False

Explanation:

Diameter of the circle = d

Therefore,

Diagonal of inner square EFGH = Side of the outer square ABCD = Diameter of circle = d

Let side of inner square EFGH be a

Now in right angled triangle EFG,

$$(EG)^2 = (EF)^2 + (FG)^2$$

By Pythagoras theorem)

$$\Rightarrow$$
 d² = a² +a²

$$\Rightarrow$$
 d² = 2a²

$$\Rightarrow$$
 $a^2 = d^2/2$

 \therefore Area of inner circle = $a^2 = d^2/2$

Also, Area of outer square $= d^2$

: the area of the outer circle is only two times the area of the inner circle.

Thus, area of outer square is not equal to four times the area of the inner square.

4. Is it true to say that area of a segment of a circle is less than the area of its corresponding sector? Why? Solution:

False

Explanation:

It is not true because in case of major segment, area is always greater than the area of its corresponding sector. It is true only in the case of minor segment.

Thus, we can conclude that it is not true to say that area of a segment of a circle is less than the area of its corresponding sector.

5. Is it true that the distance travelled by a circular wheel of diameter d cm in one revolution is 2 d cm? Why?



Solution:

False

Explanation:

Distance travelled by a circular wheel of radius r in one revolution equals the circumference of the circle.

We know that,

Circumference of the circle = $2\pi d$; where d is the diameter of the circle.

Thus, it is not true that the distance travelled by a circular wheel of diameter d cm in one revolution is 2 d cm.

6. In covering a distance s metres, a circular wheel of radius r metres makes $s/2\pi r$ revolutions. Is this statement true? Why?

Solution:

True

Explanation:

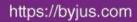
The distance travelled by a circular wheel of radius r m in one revolution is equal to the circumference of the circle = $2\pi r$

No. of revolutions completed in $2\pi r$ m distance = 1

No. of revolutions completed in 1 m distance = $(1/2\pi r)$

No. of revolutions completed in s m distance = $(1/2\pi r) \times s = s/2\pi r$

Thus, the statement "in covering a distance s metres, a circular wheel of radius r metres makes $s/2\pi r$ revolutions" is true.



EXERCISE 11.3

PAGE NO: 125

1. Find the radius of a circle whose circumference is equal to the sum of the circumferences of two circles of radii 15 cm and 18 cm.

Solution:

Radius of first circle = r_1 = 15 cm

Radius of second circle = $r_2 = 18$ cm

 \therefore Circumference of first circle = $2\pi r_1 = 30\pi$ cm

Circumference of second circle = $2\pi r_2 = 36\pi$ cm

Let the radius of the circle = R

According to the question,

Circumference of circle = Circumference of first circle + Circumference of second circle

 $2\pi R = 2\pi r_1 + 2\pi r_2$

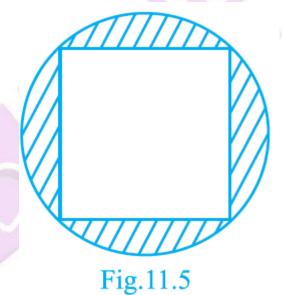
 $\Rightarrow 2\pi R = 30\pi + 36\pi$

 $\Rightarrow 66\pi \Rightarrow R = 33$

 \Rightarrow Radius = 33 cm

Hence, required radius of a circle is 33 cm.

2. In Fig. 11.5, a square of diagonal 8 cm is inscribed in a circle. Find the area of the shaded region.



Solution:

Let a be the side of square.

∴ Diameter of a circle = Diagonal of the square = 8 cm

In right angled triangle ABC,

Using Pythagoras theorem,

$$(AC)^2 = (AB)^2 + (BC)^2$$

$$(8)^2 = a^2 + a^2$$

$$\Rightarrow$$
 64= 2a²

$$\Rightarrow$$
 a²= 32

Hence,

area of square = a^2 = 32 cm²

 \therefore Radius of the circle = Diameter/2 = 4 cm

 \therefore Area of the circle = $\pi r^2 = \pi (4)^2 = 16 \text{ cm}^2$

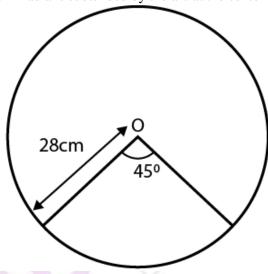
Therefore, the area of the shaded region = Area of circle – Area of square

The area of the shaded region = $16\pi - 32$

- $= 16 \times (22/7) 32$
- = 128/7
- $= 18.286 \text{ cm}^2$
- 3. Find the area of a sector of a circle of radius 28 cm and central angle 45°. **Solution:**

Area of a sector of a circle = $(1/2)r^2\theta$,

(Here r = radius and $\theta = angle$ in radians subtended by the arc at the center of the circle)



Here, Radius of circle = 28 cm

Angle subtended at the center = 45°

Angle subtended at the center (in radians) = $\theta 45\pi/180 = \pi/4$

: Area of a sector of a circle = $\frac{1}{2}$ r² θ

$$= \frac{1}{2} \times (28)^{2} \times (\pi/4)$$

$$= 28 \times 28 \times (22/8 \times 7)$$

$$= 308 \text{ cm}^{2}$$

Hence, the required area of a sector of a circle is 308 cm².

4. The wheel of a motor cycle is of radius 35 cm. How many revolutions per minute must the wheel make so as to keep a speed of 66 km/h?

Solution:

Radius of wheel = r = 35 cm

1 revolution of the wheel = Circumference of the wheel

=
$$2\pi r$$

= $2 \times (22/7) \times 35$
= 220 cm

But, given that,

Speed of the wheel = 66 km/hr

$$= (66 \times 1000 \times 100)/60$$
 cm/min

- = 110000 cm/min
- \therefore Number of revolutions in 1 min = 110000/220 = 500

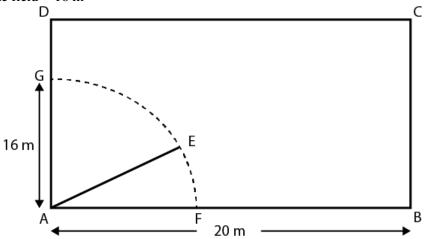
Hence, required number of revolutions per minute is 500.

5. A cow is tied with a rope of length 14 m at the corner of a rectangular field of dimensions $20m \times 16m$. Find the area of the field in which the cow can graze. Solution:

Let ABCD be a rectangular field.

Length of field = 20 m

Breadth of the field = 16 m



According to the question,

A cow is tied at a point A.

Let length of rope be AE = 14 m = l.

Angle subtended at the center of the sector = 90°

Angle subtended at the center (in radians) $\theta = 90\pi/180 = \pi/2$

: Area of a sector of a circle = $\frac{1}{2}$ $r^2\theta$

$$= \frac{1}{2} \times (14)^2 \times (\pi/2)$$

 $= 154 \text{ m}^2$

Hence, the required area of a sector of a circle is 154 m².

6. Find the area of the flower bed (with semi-circular ends) shown in Fig. 11.6.

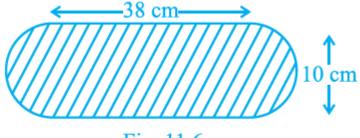


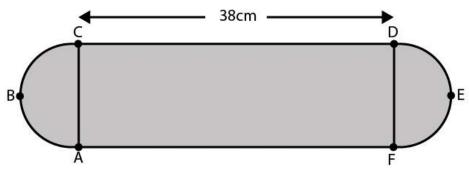
Fig. 11.6

Solution:

According to the given figure,

Length and breadth of the rectangular portion AFDC of the flower bed are 38 cm and 10 cm respectively. We know that,

Area of the flower bed = Area of the rectangular portion + Area of the two semi-circles.



- \therefore Area of rectangle AFDC = Length \times Breadth
- $= 38 \times 10 = 380 \text{ cm}^2$

Both ends of flower bed are semi-circle in shape.

- : Diameter of the semi-circle = Breadth of the rectangle AFDC = 10 cm
- \therefore Radius of the semi circle = 10/2 = 5 cm

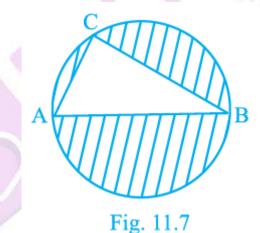
Area of the semi-circle = $\pi r^2/2 = 25\pi/2 \text{ cm}^2$

Since there are two semi-circles in the flower bed,

∴ Area of two semi-circles = $2 \times (\pi r^2/2) = 25\pi$ cm²

Total area of flower bed = $(380 + 25\pi)$ cm²

7. In Fig. 11.7, AB is a diameter of the circle, AC = 6 cm and BC = 8 cm. Find the area of the shaded region (Use $\pi = 3.14$).



Solution:

According to the question,

AC = 6cm and BC = 8 cm

A triangle in a semi-circle with hypotenuse as diameter is right angled triangle.

Using Pythagoras theorem in right angled triangle ACB,

$$(AB)^2 = (AC)^2 + (CB)^2$$

$$(AB)^2 = (6)^2 + (8)^2$$

$$\Rightarrow (AB)^2 = 36 + 64$$

$$\Rightarrow$$
(AB)² = 100 \Rightarrow (AB)= 10

∴ Diameter of the circle = 10 cm

Thus, Radius of the circle = 5 cm

Area of circle = πr^2

$$=\pi(5)^2$$

$$=25\pi$$
 cm²



 $= 25 \times 3.14 \text{ cm}^2$

 $= 78.5 \text{ cm}^2$

We know that,

Area of the right angled triangle = ($\frac{1}{2}$) × Base × Height

 $= (1/2) \times AC \times CB$

 $= (\frac{1}{2}) \times 6 \times 8$

 $= 24 \text{ cm}^2$

Now, Area of the shaded region = Area of the circle – Area of the triangle

 $= (78.5-24) \text{cm}^2$

 $= 54.5 \text{cm}^2$



EXERCISE 11.4

PAGE NO: 132

1. The area of a circular playground is 22176 m^2 . Find the cost of fencing this ground at the rate of Rs 50 per metre.

Solution:

Cost of fencing 1 meter of ground = Rs 50

- \therefore Cost of fencing the total ground = Rs 528×50 = Rs 26,400
- 2. The diameters of front and rear wheels of a tractor are 80 cm and 2 m respectively. Find the number of revolutions that rear wheel will make in covering a distance in which the front wheel makes 1400 revolutions.

Solution:

According to the question,

Diameter of front wheels = $d_1 = 80$ cm

Diameter of rear wheels = $d_2 = 2 \text{ m} = 200 \text{ cm}$

Let r_1 be the radius of the front wheels = 80/2 = 40 cm

Let r_2 be the radius of the rear wheels = 200/2 = 100 cm

Now, Circumference of the front wheels = $2\pi r$

$$= 2 \times (22/7) \times 40$$

= 1760/7 cm

Circumference of the rear wheels = $2\pi r = 2 \times (22/7) \times 100 = 4400/7$ cm

No. of revolutions made by the front wheel = 1400

: Distance covered by the front wheel = $1400 \times (1760/7) = 352000$ cm

Number of revolutions made by rear wheel in covering a distance in which the front wheel makes 1400 revolutions.

Distance covered by front wheel

= Circumference of the rear wheel

$$= \frac{\frac{352000}{4400}}{7}$$

$$= \frac{\frac{352000 \times 7}{4400}}{6400}$$
= 560 revolutions.

3. Sides of a triangular field are 15 m, 16 m and 17 m. With the three corners of the field a cow, a buffalo and a horse are tied separately with ropes of length 7 m each to graze in the field. Find the area of the field which cannot be grazed by the three animals.

Solution:

According to the question,

Sides of the triangle are 15 m, 16 m, and 17 m.

Now, perimeter of the triangle = (15+16+17) m = 48 m

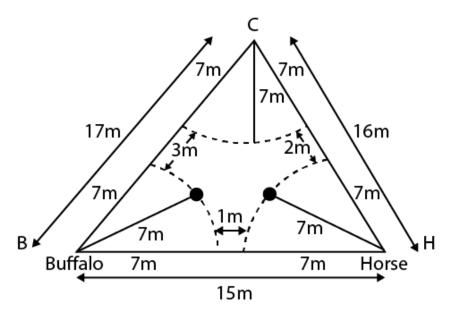
 \therefore Semi-perimeter of the triangle = s = 48/2 = 24 m

By Heron's formula,

Area of the triangle = $\sqrt{(s(s-a)(s-b)(s-c))}$, here a, b and c are the sides of triangle

 $= \sqrt{(24(24-15)(24-16)(24-17))}$

 $= 109.982 \text{ m}^2$



Let B, C and H be the corners of the triangle on which buffalo, cow and horse are tied respectively with ropes of 7 m each.

So, the area grazed by each animal will be in the form of a sector.

 \therefore Radius of each sector = r = 7 m

Let x, y, z be the angles at corners B, C, H respectively.

 \therefore Area of sector with central angle x,

$$= \frac{1}{2} (x/180) \times \pi r^2 = (x/360) \times \pi (7)^2$$

Area of sector with central angle y,

$$= \frac{1}{2} (y/180) \times \pi r^2 = (y/360) \times \pi (7)^2$$

Area of sector with central angle z,

Area of sector with central angle z,
=
$$\frac{1}{2} (z/180) \times \pi r^2 = (z/360) \times \pi (7)^2$$

Area of field not grazed by the animals = Area of triangle - (area of the three sectors)

$$= (109.982) - \left(\left(\frac{x}{360} \right) \times \pi(7)^2 + \left(\frac{y}{360} \right) \times \pi(7)^2 + \left(\frac{z}{360} \right) \times \pi(7)^2 \right)$$

$$= 109.982 - \left(\left(\frac{x+y+z}{360} \right) \times \pi(7)^2 \right)$$

$$= 109.982 - \left(\left(\frac{180}{360} \right) \times \left(\frac{22}{7} \right) \times 49 \right)$$

$$= 109.892 - 77$$

$$= 32.982 \text{ cm}^2$$

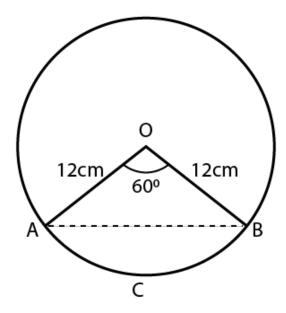
4. Find the area of the segment of a circle of radius 12 cm whose corresponding sector has a central angle of 60° (Use $\pi = 3.14$).

Solution:

According to the question, Radius of the circle = r = 12 cm

$$\therefore$$
 OA = OB = 12 cm

$$\angle AOB = 60^{\circ} \text{ (given)}$$



Since triangle OAB is an isosceles triangle, $\therefore \angle OAB = \angle OBA = \theta$ (say)

Also, Sum of interior angles of a triangle is 180°,

$$\therefore \theta + \theta + 60^{\circ} = 180^{\circ}$$

$$\Rightarrow 2\theta = 120^{\circ} \Rightarrow \theta = 60^{\circ}$$

Thus, the triangle AOB is an equilateral triangle.

$$\therefore$$
 AB = OA = OB = 12 cm

Area of the triangle AOB = $(\sqrt{3}/4)\times a^2$, where a is the side of the triangle.

$$=(\sqrt{3}/4)\times(12)^2$$

$$= (\sqrt{3}/4) \times 144$$

$$= 36\sqrt{3} \text{ cm}^2$$

$$= 62.354 \text{ cm}^2$$

Now, Central angle of the sector AOBCA = $\emptyset = 60^{\circ} = (60\pi / 180) = (\pi/3)$ radians

Thus, area of the sector AOBCA = $\frac{1}{2}$ r² \emptyset

$$= \frac{1}{2} \times 12^2 \times \frac{\pi}{3}$$

$$= 12^2 \times (22 / (7 \times 6))$$

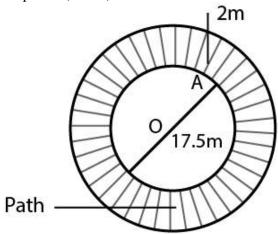
$$= 75.36 \text{ cm}^2$$

Now, Area of the segment ABCA = Area of the sector AOBCA - Area of the triangle AOB $= (75.36 - 62.354) \text{ cm}^2 = 13.006 \text{ cm}^2$

5. A circular pond is 17.5 m is of diameter. It is surrounded by a 2 m wide path. Find the cost of constructing the path at the rate of Rs 25 per m² **Solution:**

Diameter of the circular pond = 17.5 m

Let r be the radius of the park = (17.5/2) m = 8.75 m



According to the question,

The circular pond is surrounded by a path of width 2 m.

So, Radius of the outer circle = R = (8.75+2) m = 10.75 m

Area of the road = Area of the outer circular path - Area of the circular pond

$$= \pi r^2 - \pi R^2$$

$$= 3.14 \times (10.75)^2 - 3.14 \times (8.75)^2$$

$$=3.14\times((10.75)^2-(8.75)^2)$$

$$= 3.14 \times ((10.75 + 8.75) \times (10.75 - 8.75))$$

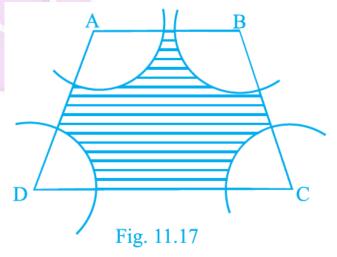
$$= 3.14 \times 19.5 \times 2 = 122.46 \text{ m}^2$$

Hence, the area of the path is 122.46 m².

Now, Cost of constructing the path per $m^2 = Rs. 25$

 \therefore cost of constructing 122.46m² of the path = Rs. 25 × 122.46 = Rs. 3061.50

6. In Fig. 11.17, ABCD is a trapezium with AB \parallel DC, AB = 18 cm, DC = 32 cm and distance between AB and DC = 14 cm. If arcs of equal radii 7 cm with centres A, B, C and D have been drawn, then find the area of the shaded region of the figure.



Solution:

AB = 18 cm, DC = 32 cm

Distance between AB and DC = Height = 14 cm

Now, Area of the trapezium = $(1/2) \times (Sum \text{ of parallel sides}) \times Height$

$$= (\frac{1}{2}) \times (18+32) \times 14 = 350 \text{cm}^2$$

As AB \parallel DC, \therefore \angle A + \angle D = 180°

And $\angle B + \angle C = 180^{\circ}$

Also, radius of each arc = 7 cm

Therefore,

Area of the sector with central angle $A = (\frac{1}{2}) \times (\angle A/180) \times \pi \times r^2$

Area of the sector with central angle D = $(\frac{1}{2}) \times (\angle D/180) \times \pi \times r^2$

Area of the sector with central angle $B = (\frac{1}{2}) \times (\angle B/180) \times \pi \times r^2$

Area of the sector with central angle $C = (\frac{1}{2}) \times (\angle C/180) \times \pi \times r^2$

Total area of the sectors,

$$\begin{split} & = \frac{\angle A}{360} \times \pi \times r^2 + \frac{\angle D}{360} \times \pi \times r^2 + \frac{\angle B}{360} \times \pi \times r^2 + \frac{\angle C}{360} \times \pi \times r^2 \\ & = \left(\frac{\angle A + \angle D}{360} \times \pi \times r^2\right) + \left(\frac{\angle B + \angle C}{360} \times \pi \times r^2\right) \\ & = \left(\frac{180}{360} \times \frac{22}{7} \times 49\right) + \left(\frac{180}{360} \times \frac{22}{7} \times 49\right) \end{split}$$

= 77 + 77

= 154

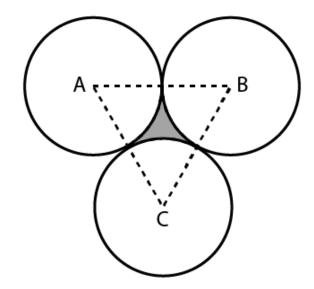
∴ Area of shaded region = Area of trapezium – (Total area of sectors)

 $= 350 - 154 = 196 \text{ cm}^2$

Hence, the required area of shaded region is 196 cm².

7. Three circles each of radius 3.5 cm are drawn in such a way that each of them touches the other two. Find the area enclosed between these circles. Solution:

The three circles are drawn such that each of them touches the other two.



By joining the centers of the three circles,

We get,

AB = BC = CA = 2(radius) = 7 cm

Therefore, triangle ABC is an equilateral triangle with each side 7 cm.

- : Area of the triangle = $(\sqrt{3}/4) \times a^2$, where a is the side of the triangle.
- $=(\sqrt{3}/4)\times 7^2$
- $= (49/4) \sqrt{3} \text{ cm}^2$
- $= 21.2176 \text{ cm}^2$

Now, Central angle of each sector = $\emptyset = 60^{\circ} (60\pi/180)$

 $= \pi/3$ radians

Thus, area of each sector = $(1/2) r^2 \theta$

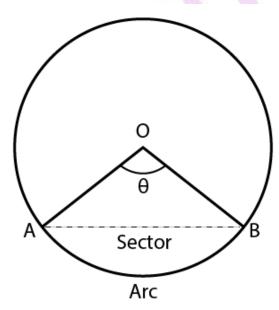
- $= (1/2) \times (3.5)^2 \times (\pi/3)$
- $= 12.25 \times (22/(7 \times 6))$
- $= 6.4167 \text{ cm}^2$

Total area of three sectors = $3 \times 6.4167 = 19.25 \text{ cm}^2$

- : Area enclosed between three circles = Area of triangle ABC Area of the three sectors
- =21.2176-19.25
- $= 1.9676 \text{ cm}^2$

Hence, the required area enclosed between these circles is 1.967 cm² (approx.).

8. Find the area of the sector of a circle of radius 5 cm, if the corresponding arc length is 3.5 cm. Solution:



Radius of the circle = r = 5 cm

Arc length of the sector = 1 = 3.5 cm

Let the central angle (in radians) be θ .

As, Arc length = Radius \times Central angle (in radians)

: Central angle (θ) = Arc length / Radius = 1 / r = 3.5/5 = 0.7 radians

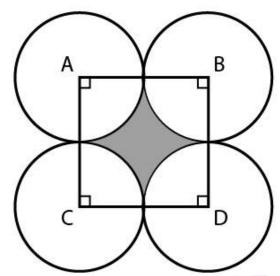
Now, Area of the sector = $(\frac{1}{2}) \times r^2\theta = (\frac{1}{2}) \times 25 \times 0.7 = 8.75 \text{ cm}^2$

Hence, required area of the sector of a circle is 8.75 cm².

9. Four circular cardboard pieces of radii 7 cm are placed on a paper in such a way that each piece touches other two pieces. Find the area of the portion enclosed between these pieces. Solution:

According to the question,

The four circles are placed such that each piece touches the other two pieces.



By joining the centers of the circles by a line segment, we get a square ABDC with sides,

$$AB = BD = DC = CA = 2(Radius) = 2(7) cm = 14 cm$$

Now, Area of the square = $(\text{Side})^2 = (14)^2 = 196 \text{ cm}^2$

ABDC is a square,

Therefore, each angle has a measure of 90°.

i.e.,
$$\angle A = \angle B = \angle D = \angle C = 90^{\circ} = \pi/2 \text{ radians} = \theta \text{ (say)}$$

Given that.

Radius of each sector = 7 cm

Area of the sector with central angle $A = (\frac{1}{2})r^2\theta$

=
$$\frac{1}{2}$$
 r² θ
= $\frac{1}{2}$ × 49 × π /2
= $\frac{1}{2}$ × 49 × (22/(2×7))
= (77/2) cm²

Since the central angles and the radius of each sector are same, area of each sector is 77/2 cm²

 \therefore Area of the shaded portion = Area of square – Area of the four sectors

$$= 196 - (4 \times (77/2))$$

= 196 - 154
= 42 cm²

Therefore, required area of the portion enclosed between these pieces is 42 cm².

10. On a square cardboard sheet of area 784 cm², four congruent circular plates of maximum size are placed such that each circular plate touches the other two plates and each side of the square sheet is tangent to two circular plates. Find the area of the square sheet not covered by the circular plates. Solution:

According to the question,

Area of the square $= 784 \text{ cm}^2$

∴ Side of the square = $\sqrt{\text{Area}} = \sqrt{784} = 28 \text{ cm}$

The four circular plates are congruent,

Then diameter of each circular plate = 28/2 = 14 cm

 \therefore Radius of each circular plate = 7 cm

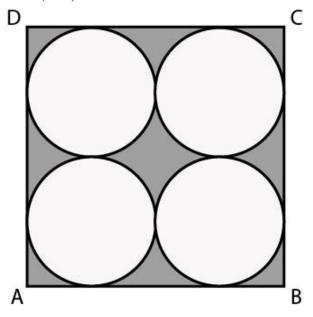
We know that,

Area of the sheet not covered by plates = Area of the square – Area of the four circular plates As all four circular plates are congruent,

We have, area of all four plates equal.



∴ Area of one circular plate = $\pi r^2 = (22/7) \times 7^2 = 154 \text{ cm}^2$



Then,

Area of four plates = $4 \times 154 = 616 \text{ cm}^2$

Area of the sheet not covered by plates = $784 - 616 = 168 \text{ cm}^2$