

Theory of Computation

Basics/DFA

Lecture 2

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Symbol : anything $\{ \text{a, b, } \alpha, \beta, \text{a, b, } 2, @, \epsilon, +, -, \dots \}$ Ex $\{ \underline{a}, \underline{b} \}$

Alphabet

Σ, Δ, T

Ex $\sum^2, \sum^3, \sum^* \{ \text{Power} \}$
Length 2

String : $\in \text{or } \lambda, \frac{a, b}{1}, \underbrace{aa, ab, ba, bb}_2, \dots \dots \dots$
Epsilon
0 length String

Language :

$L_1: aba$

$L_2: \overbrace{a^* b^*}$

$\{ \epsilon, a, b, ab, \cancel{ba}, \dots \}$

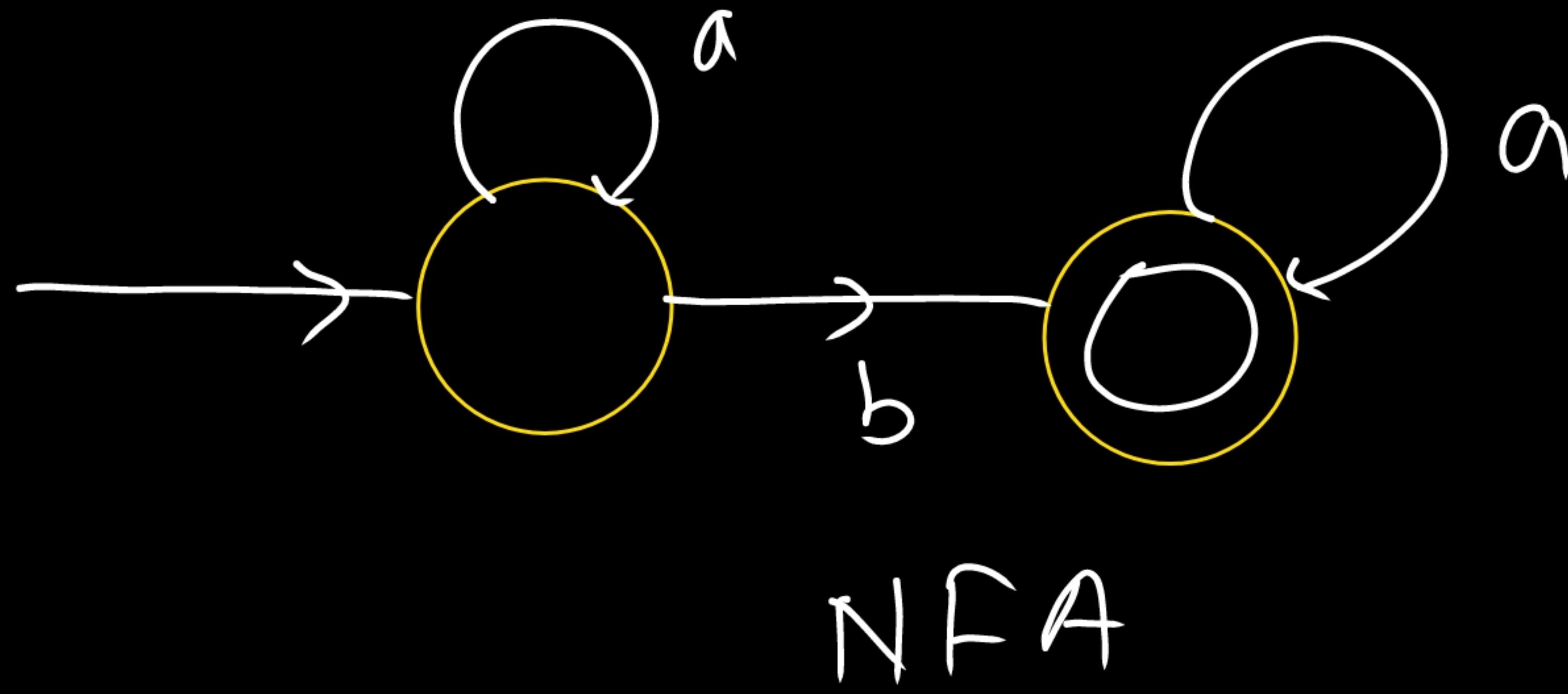
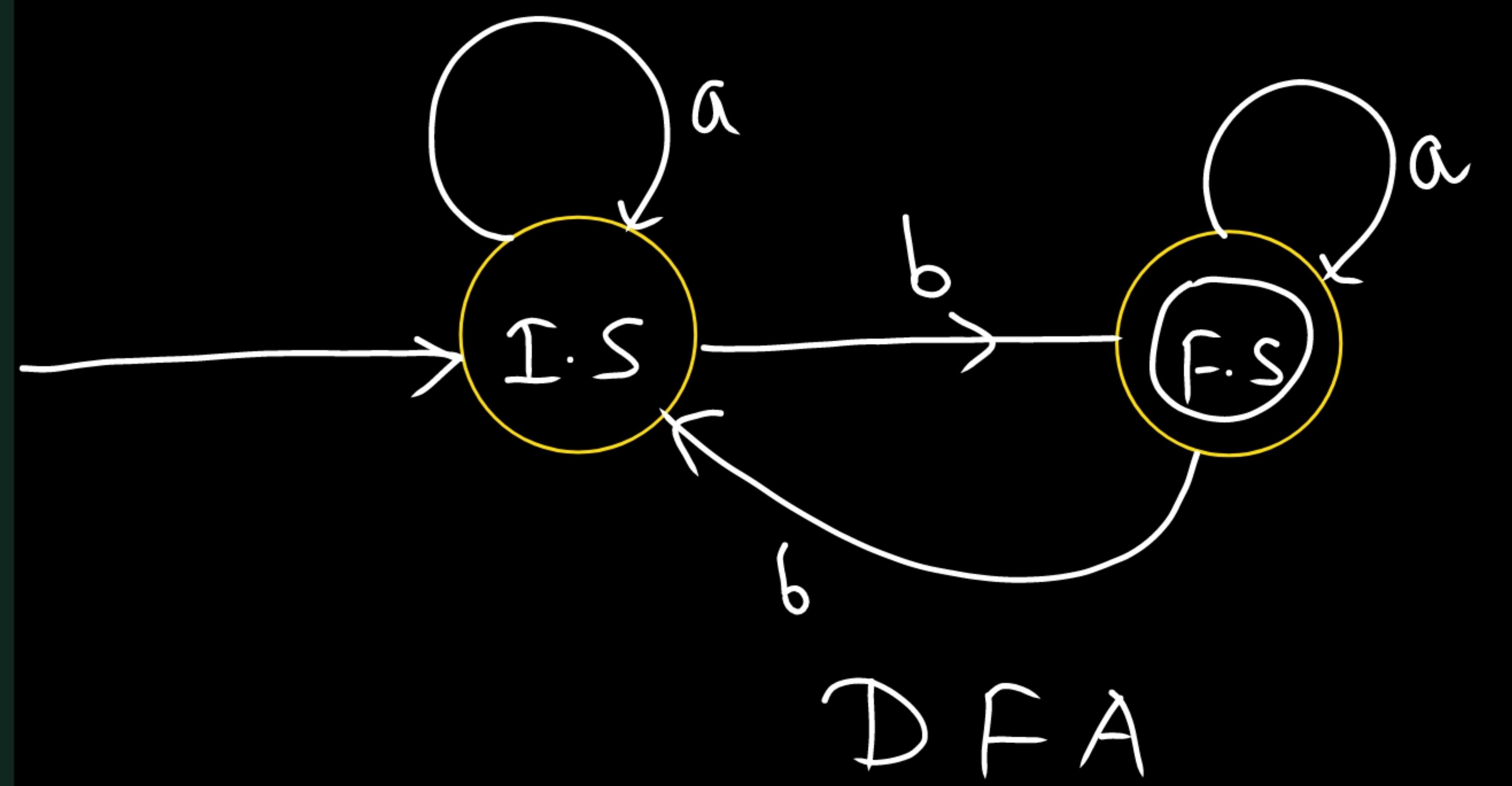
$a^*: \{ \epsilon, a, aa, \dots, a^{n+1} \}$

	Language	Machine	Grammar	
FA	Regular	$DFA \equiv NFA$	Reg Grammar	Type-3
FA + 1 Stack	Context free lang	$NPDA > DPDA$	CFG	Type-2
FA + 2 Stack	Context Sensitive lang	Linear Bounded Automata	CSL	Compiler
FA + 2 Stack	Recursive Enumerable	$NTM \asymp DTM$	free G	Type-1
		...		Type-0

Power

$$\Sigma = \{a, b\}$$

DFA vs NFA : Transition Table



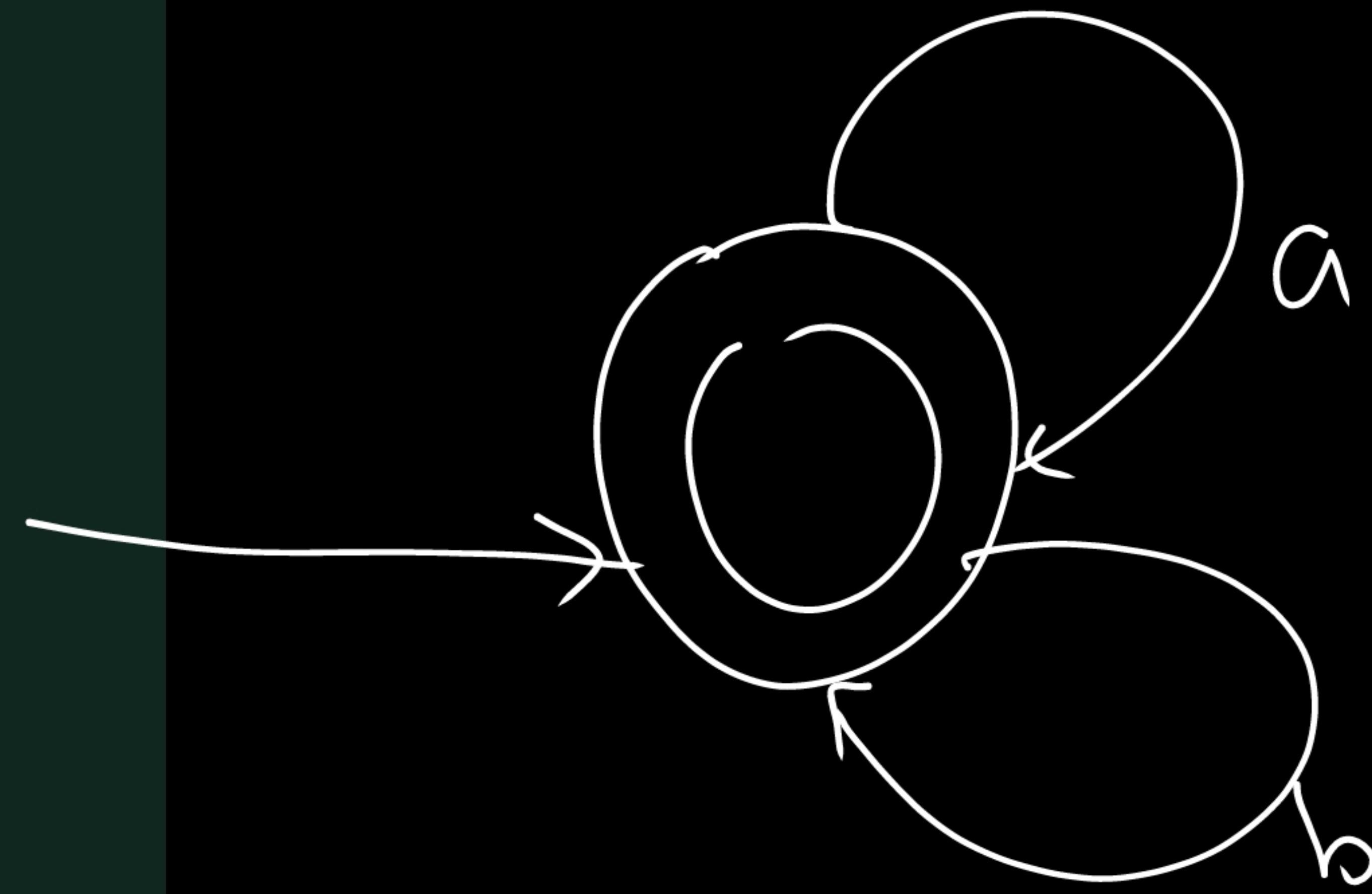
Transition
Table

	a	b
I.S	I.S	F.S
F.S	F.S	I.S

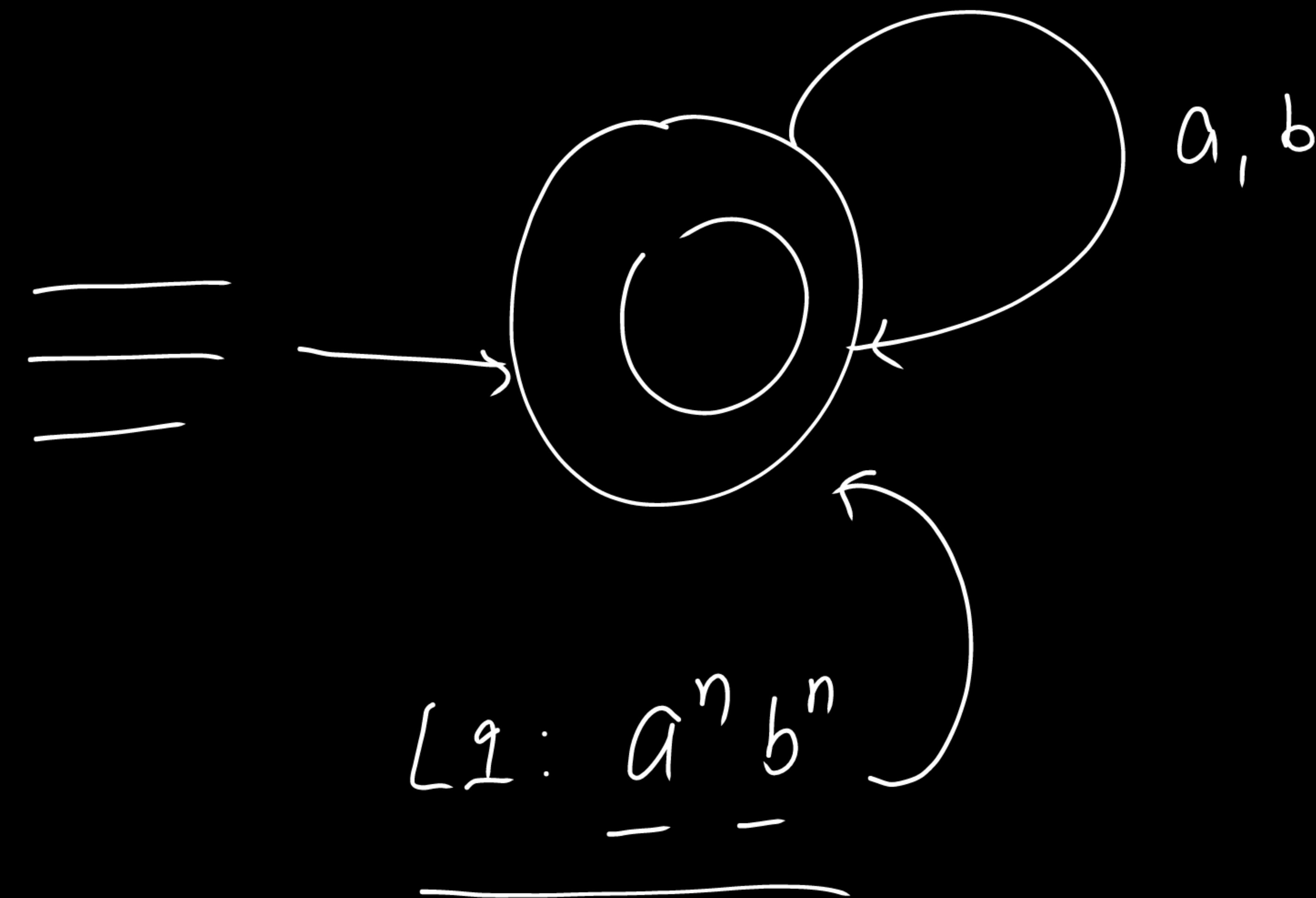
	a	b
I.S	I.S	F.S
F.S	F.S	-

1. Construct minimal Finite Automata that accepts all strings of a's and b's including ϵ

$$L_1: \{ \epsilon,$$

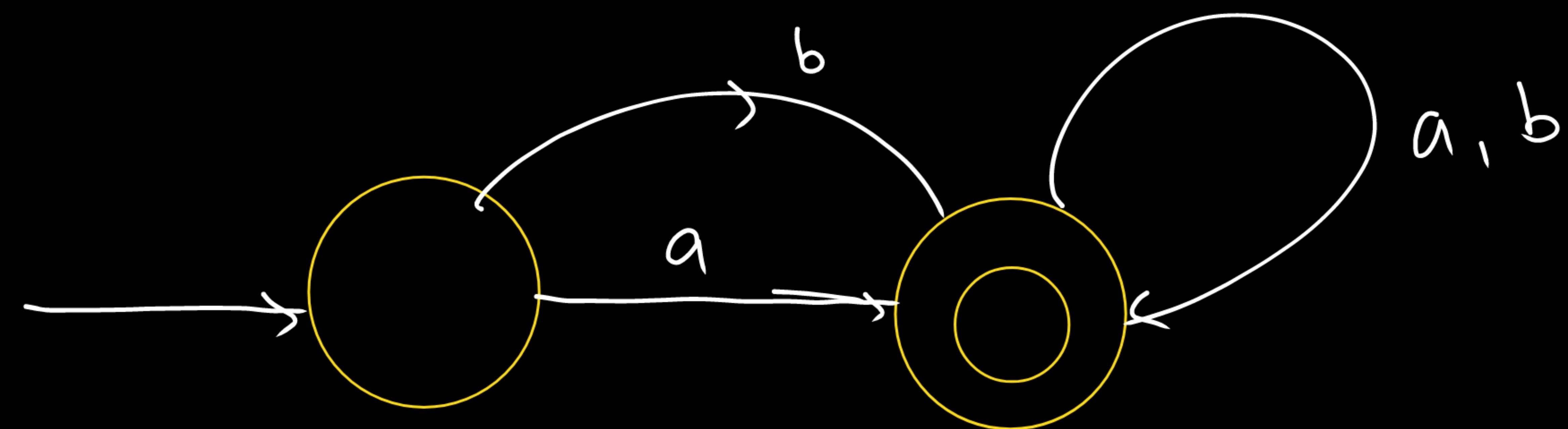


Universal
Lang.



$$L_2: \underline{\underline{a^n b^n}}$$

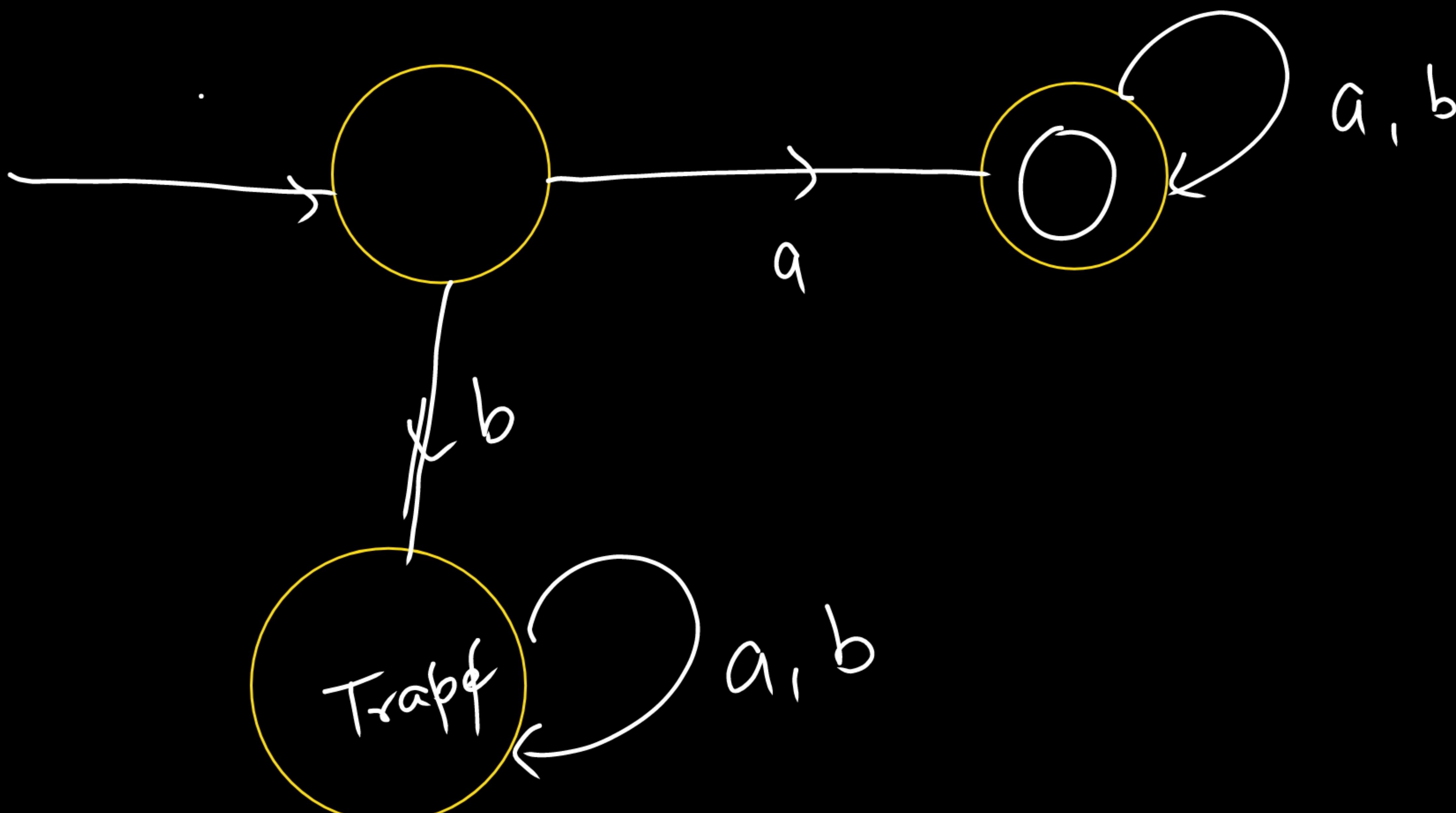
2. Construct minimal Finite Automata that accepts all strings of a's and b's excluding ϵ



L1: $\{ \underline{a}, \underline{b}, \underline{ab}, \underline{ba}, \underline{aa}, \underline{bb} \dots \}$

3. Construct minimal Finite Automata that accepts all strings of a's and b's, where each string starts with a.

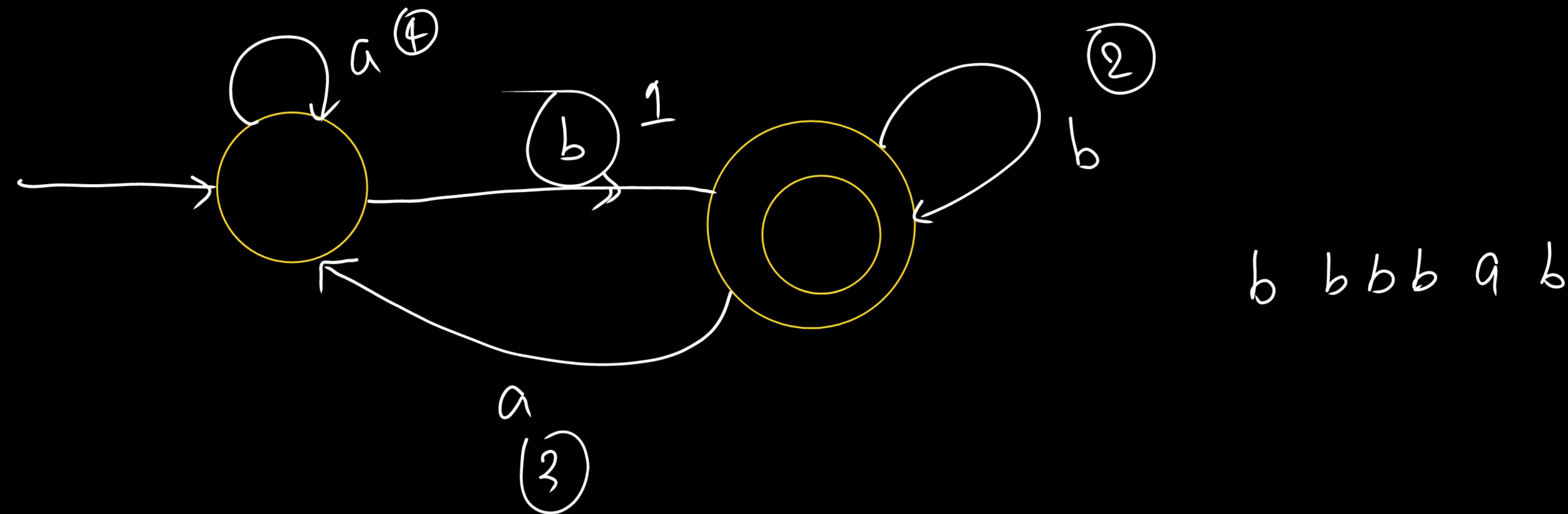
$$L_1: \left\{ a, b, \underset{x}{aa}, \underset{x}{ab}, \underset{x}{ba}, \underset{x}{bb}, \dots \right\}$$



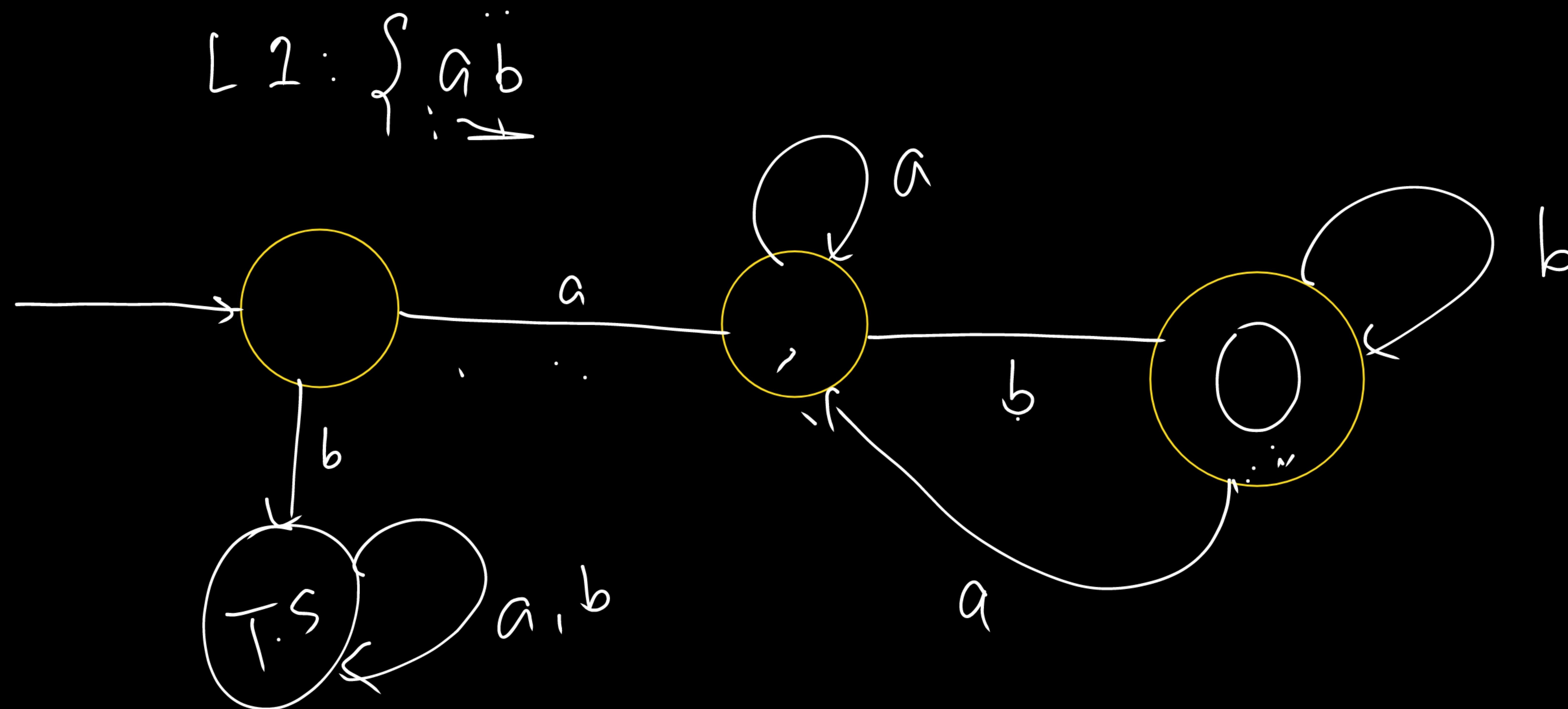
	a	b
I.S	F.S	T.S
F.S	F.S	F.S
T.S	T.S	T.S

4. Construct minimal Finite Automata that accepts all strings of a's and b's, where each string ends with b.

$$L_1: \left\{ \begin{array}{l} a, b, ab, ba, bb, \dots, aaaaaaaab \\ \text{X } \checkmark \text{ X } \checkmark \text{ X } \end{array} \right. \text{ infinite } \right\}$$



5. Construct minimal Finite Automata that accepts all strings of a's and b's, where each string starts with a and ends with b.



6. Construct minimal Finite Automata that accepts all strings of a's and b's, where each string contain **ab** as substring.

7. Construct minimal Finite Automata that accepts all strings of a's and b's, where each string starts with the substring ab.



Thank You

