

Theory of Computation

RegLang_EpsilonNFAtoNFA

Lecture 17

Gaurav Raj

$$1. (a + b)^+ + (abba)^* = (a + b)^*$$

True

$$2. \underbrace{a(a + \varepsilon)^+ + b(a + \varepsilon)^+}_{\varepsilon} = (a + b)^*$$

False

$$3. (a(ba)^* + b(ab)^*)^* = (a + b)^*$$

True

$$4. (b^*a)^* + (a^*b)^* = (a + b)^*$$

True

$$5. a(a+b)^* + b(a+b)^* = (a + b)^*$$

True

$\varphi \cdot a = \varphi$

$a \cdot \varphi = \varphi$

$\varphi \cdot R = \varphi$

$R \cdot \varphi = \varphi$

Φ is dominator

Regular Language vs Regular Language

1. $L = \{\}$ over $\Sigma = \{a, b\}$

$R = \varphi.ab = \varphi_aa = \varphi^+$

$$\varphi^+ = \{ \}^*$$

2. $L = \{\}$ over $\Sigma = \underline{\{a, b, c\}}$

$R = \varphi.c$

$$\Sigma^0 = \varepsilon$$

3. $L = \underline{\{\varepsilon\}}$ over $\Sigma = \{a\}$

$R = \varphi^* = \varepsilon = \varepsilon^+ = \varepsilon^* = (a)^0$

→ 4. $L = \{w \mid w \in \{a, b\}^*, w > 0\}$.

$R = (a+b)^+, \Sigma^+$

5. $L = \{w \mid w \in \{a, b\}^*, w \text{ starts with } a\}$.

$R = a(a+b)^*, a \Sigma^*$

6. $L = \{aw \mid w \in \{a, b\}^*\}$.

$R =))$

7. $L = \{awb \mid w \in \{a, b\}^*\}$.

$R = a\Sigma^*b$

Regular Language vs Regular Language

1. $L = \{wx \mid w \in \underline{\{aa,bb\}}, x \in (a+b)^*\}.$

$$R = (aa+bb)(a+b)^*$$

2. $L = \{wx \mid w \in (a+b)^*, x \in \{aa,bb\}\}.$

$$R = (a+b)^*(aa+bb)$$

3. $L = \{w \mid w \in \{a,b\}^*, |w|=2\}.$

$$R = \sum^2, aa+ab+ba+bb$$

4. $L = \{w \mid w \in \{a,b\}^*, |w|=3\}.$

$$R = \sum^3$$

5. $L = \{w \mid \underline{w \in a^*b^*}, |w|=2\}.$

$$R = aa + bb + ab$$

Regular Language vs Regular Language

1. $L = \{w \mid w \in a^*, |w|=2\}$.

$$R = aa, \Sigma^2$$

2. $L = \{w \mid w \in b^*, |w|=2\}$.

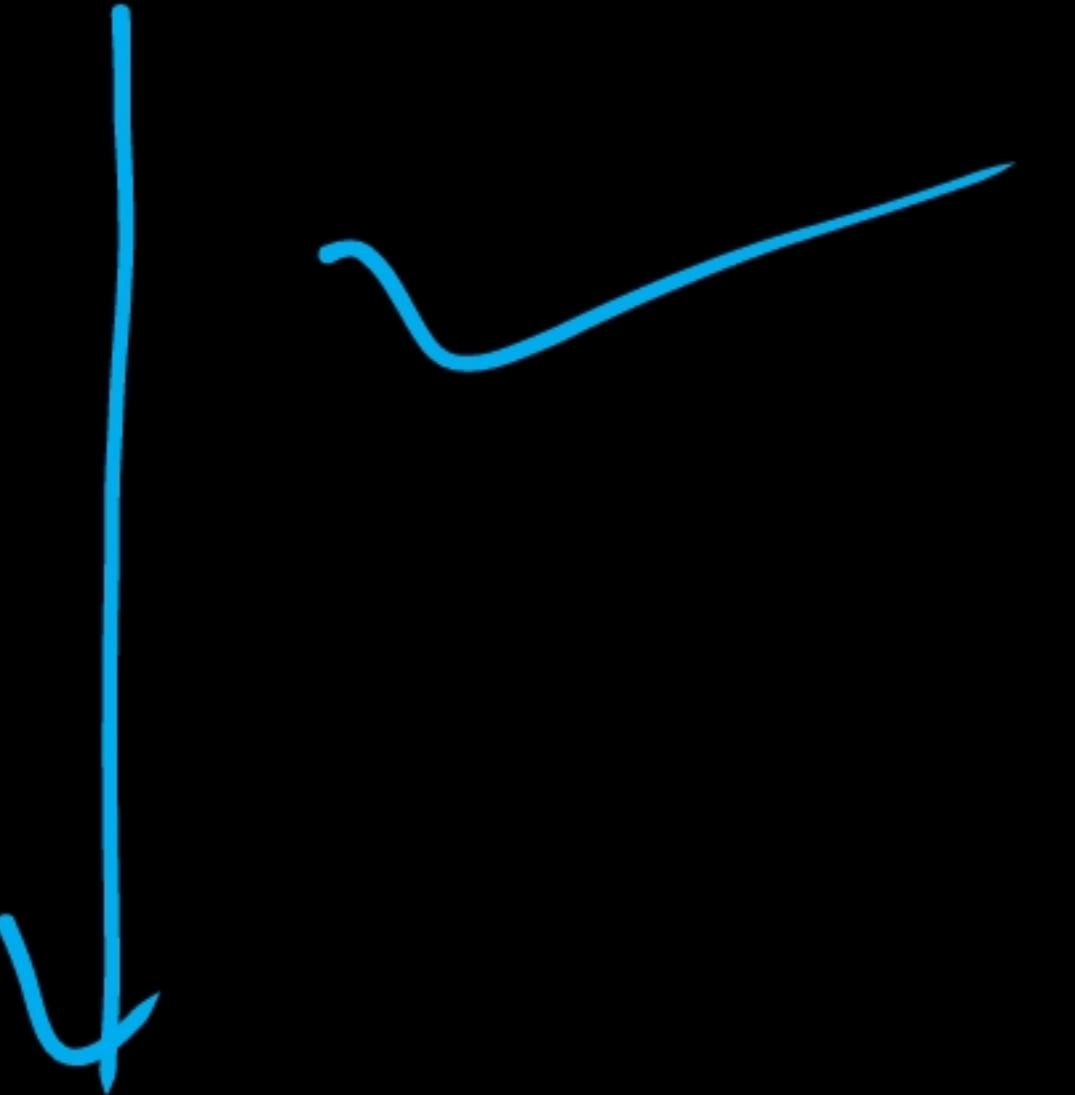
$$R = bb$$

3. $L = \{w \mid w \in \{a,b\}^*, \underline{|w| \leq 2}\}$.

$$(\underline{\epsilon+a+b})^2$$

$$R = \epsilon + a + b + \dots = \epsilon + \Sigma + \Sigma^2$$

4. $L = \{w \mid w \in \{a,b\}^*, |w| \leq 100\}$.



$$R = \epsilon + \dots$$

5. $L = \{w \mid w \in \{a,b\}^*, |w| \geq 2\}$.

$$R = \Sigma^2 \cdot (a+b)^*$$

~~aa + ab~~

$$(\underline{\epsilon+a+b}) \cdot (\underline{\epsilon+a+b})$$

$$\epsilon + a + b + aa + ab + ba + bb$$

Regular Language vs Regular Language

1. $L = \{w \mid w \in \underline{(a+b)^*}, \underline{|w|} = \text{even}\}$.

2. $L = \{w \mid w \in (a+b)^*, |w| = \text{odd}\}$.

3. $L = \{w \mid w \in \underline{a^*}, |w| = \text{even}\}$.

4. $L = \{w \mid w \in \underline{b^*}, |w| = \text{odd}\}$.

5. $L = \{w \mid w \in \underline{a^*b^*}, \underline{|w|} = \text{even}\}$.

6. $L = \{w \mid w \in a^*b^*, |w| = \text{odd}\}$.

7. $L = \{w \mid w \in (aa)^*, |w| = \text{odd}\}$.

$$a(\Sigma^2)^* + b(\Sigma^2)^*$$

$$\underbrace{(aa)^*}_{\text{even}} \cdot \underbrace{b(bb)^*}_{\text{odd}} +$$

$$a(aa)^* \cdot (bb)^*$$

$$\cancel{a(aa)^*} \neq$$

$$R = (\Sigma^2)^*, [(a+b)^2]^*$$

$$R = (a+b)(\Sigma^2)^*$$

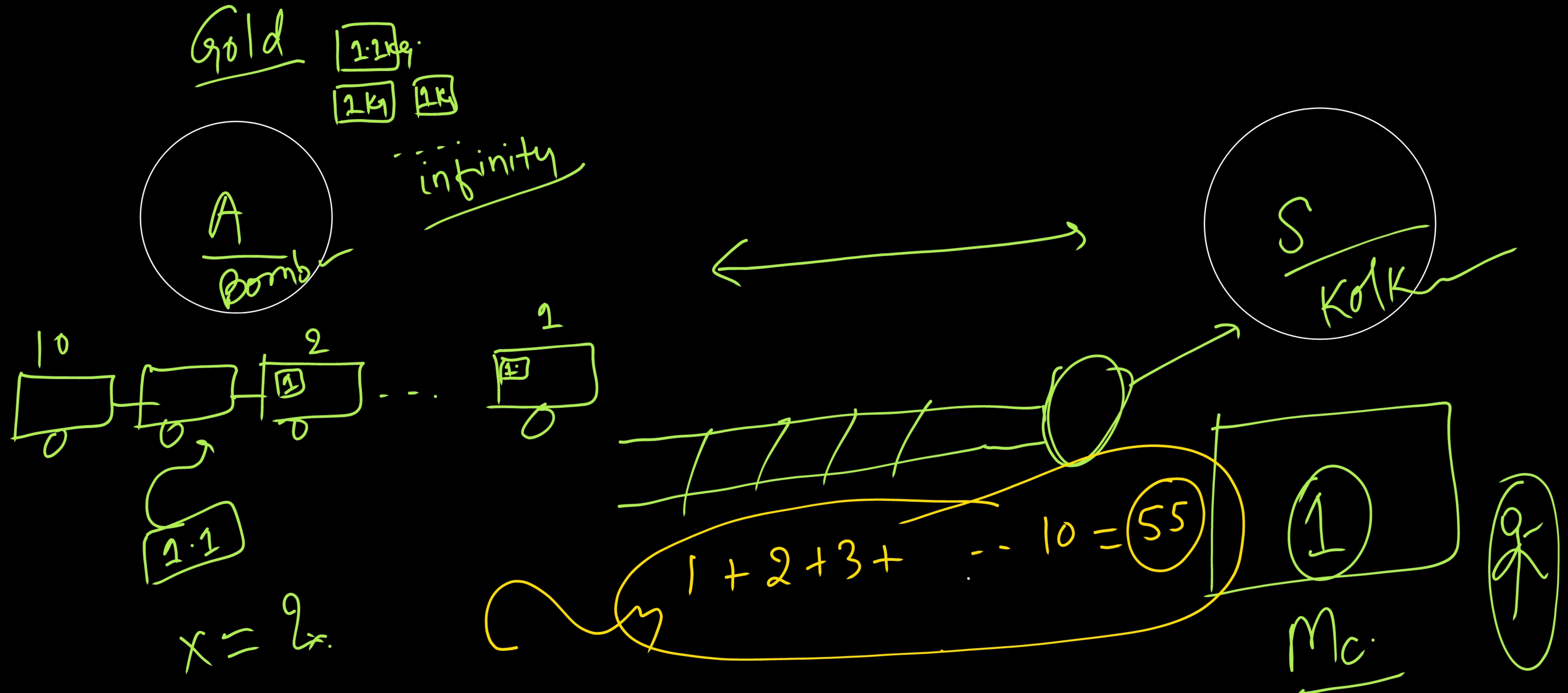
$$R = (aa)^*$$

$$R = b(bb)^*$$

$$R = \underbrace{(aa)^*}_{\text{even}} \cdot \underbrace{(bb)^*}_{\text{even}} +$$

$$R = \underbrace{a(aa)^*}_{\text{odd}} \cdot \underbrace{b(bb)^*}_{\text{odd}}$$

Regular Language vs Regular Language





Thank You

