

AI1103: Assignment 1

Tanmay Garg
CS20BTECH11063 EE20BTECH11048

13 March 2021

Problem Statement:

An urn contains 25 balls of which 10 balls bear a mark 'X' and the remaining 15 bear a mark 'Y'. A ball is drawn at random from the urn, its mark is noted down and it is replaced. If 6 balls are drawn in this way, find the probability that:

1. all will bear 'X' mark.
2. not more than 2 will bear 'Y' mark.
3. at least one ball will bear 'Y' mark.
4. the number of balls with 'X' mark and 'Y' mark will be equal.

Solution:

Let X be the number of balls which have 'X' mark on them
Using the expression of binomial distribution

$$P(X = r) = \binom{n}{r} p^r q^{n-r}$$

We have

$$\begin{aligned} n &= 6 \\ p &= \frac{2}{5} = 0.4 \\ q &= \frac{3}{5} = 0.6 \end{aligned}$$

For (i) we need to find $P(X = 6)$

$$P(X = 6) = \binom{6}{6} p^6 q^0 = \left(\frac{2}{5}\right)^6 = 0.004096$$

For (ii) we need to find $P(X \geq 4)$

$$P(X \geq 4) = \sum_{r=4}^6 \binom{6}{r} p^r q^{n-r} = 0.1792$$

For (iii) we need to find $P(X \leq 5)$

$$P(X \leq 5) = \sum_{r=0}^5 \binom{6}{r} p^r q^{n-r} = 0.995904$$

For (iv) we need to find $P(X = 3)$

$$P(X = 3) = \binom{6}{3} p^3 q^3 = 0.27648$$