

AI1103: Assignment 2

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Download all python codes from

need

and latex-tikz codes from

<https://github.com/tanmaygar/AI-Course/blob/main/Assignment3/Assignment3.tex>

On converting to r and θ form, we get:

$$\Pr(Y > |X|) = \frac{1}{\pi} \int_{\pi/4}^{3\pi/4} \int_0^1 r dr d\theta \quad (0.0.7)$$

$$= \frac{1}{\pi} \int_{\pi/4}^{3\pi/4} \left(\frac{1}{2} r^2 \right) \Big|_0^1 d\theta \quad (0.0.8)$$

$$= \frac{1}{\pi} \int_{\pi/4}^{3\pi/4} \frac{1}{2} d\theta \quad (0.0.9)$$

$$= \frac{1}{2\pi} \left(\frac{3\pi}{4} - \frac{\pi}{4} \right) \quad (0.0.10)$$

$$= \frac{1}{2\pi} \cdot \frac{\pi}{2} \quad (0.0.11)$$

$$= \frac{1}{4} \quad (0.0.12)$$

PROBLEM GATE 2007 (MA), Q. 14:

Let X and Y be jointly distributed random variables having the joint probability density function

$$f(x, y) = \begin{cases} \frac{1}{\pi}, & \text{if } x^2 + y^2 \leq 1 \\ 0, & \text{otherwise} \end{cases}$$

Then $P(Y > \max(X, -X))$ is

SOLUTION:

Since we require $Y > \max(X, -X)$

$$\max(X, -X) = |X| \quad (0.0.1)$$

We need to find

$$\Pr(Y > |X|) \quad (0.0.2)$$

Integrating the probability distribution function on our domain

$$\Pr(Y > |X|) = \iint_{\{y > |x|\}} f(x, y) dx dy \quad (0.0.3)$$

$$= \iint_{\{y > |x|, x^2 + y^2 \leq 1\}} \frac{1}{\pi} dx dy \quad (0.0.4)$$

$$+ \iint_{\{y > |x|, x^2 + y^2 > 1\}} 0 dx dy \quad (0.0.5)$$

$$= \frac{1}{\pi} \iint_{\{y > |x|, x^2 + y^2 \leq 1\}} dx dy \quad (0.0.6)$$