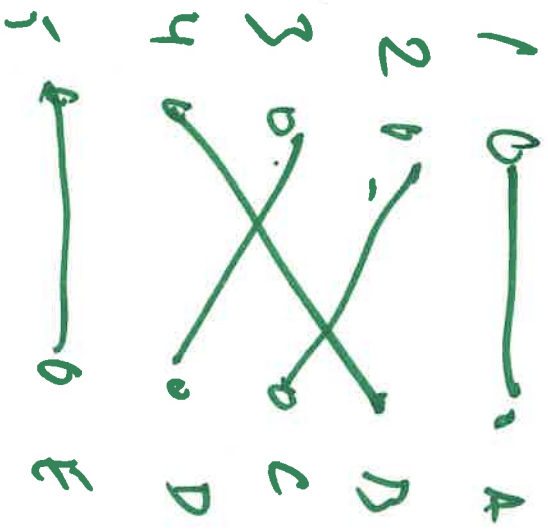
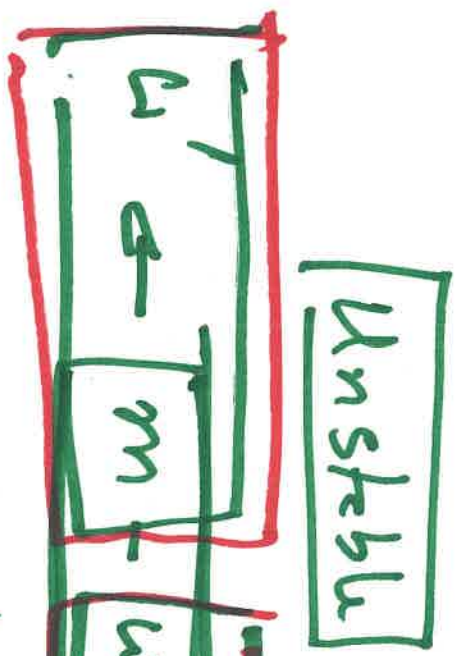


Set 5: Stable Matching



Perfect Matching

(Stable?)



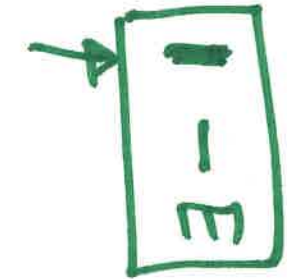
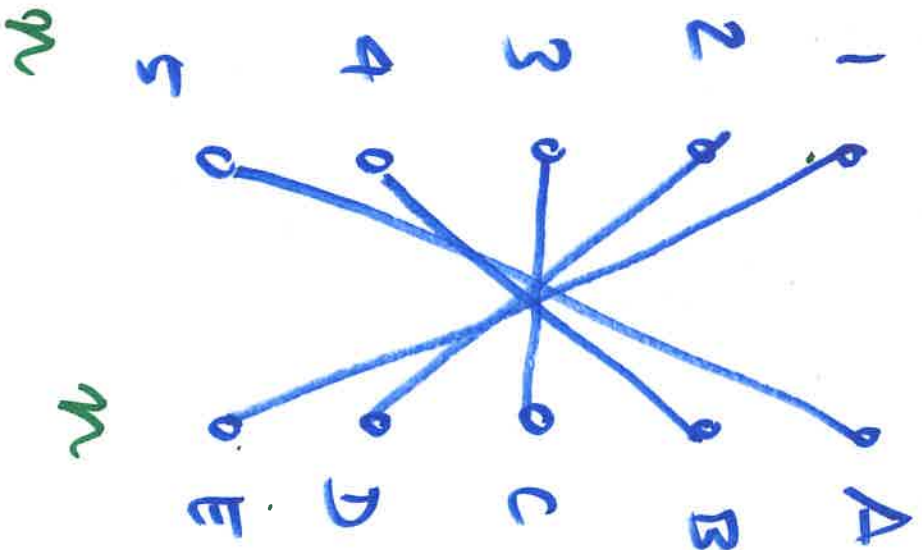
one unstable pair

unstable.

m has not been paired up with ω

$m : \omega > \omega' \Rightarrow \times$
 $\omega : m > m' \Rightarrow \times$

$\omega \rightarrow m'' > m$
 $\omega \rightarrow m' > m''$

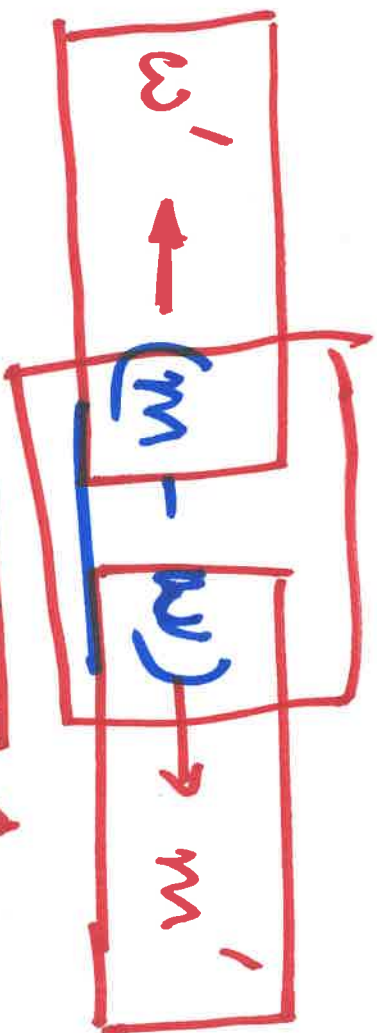


1 - A > B > C > D > E
 2
 3
 4
 5

5 > 4 > 3 > 2 > 1

A
 B
 C
 D
 E

$O(n^2)$



unstable

$\omega : \omega$

$\omega > \omega' > m$

$\omega' > m$

$\omega' > m$

$\omega \rightarrow m''$

$\omega : m'' > m''$

$\omega - m''$

$m' > m$

$m' > m$

$\omega - m'$

$\omega : m' > m''$

$$\begin{array}{l}
 m_1 : w_1 > w_2 \\
 m_2 : w_1 > w_2 \\
 w_1 : m_1 > m_2 \\
 w_2 : m_1 > m_2
 \end{array}$$

$$\begin{array}{l}
 m_1 - w_1 \\
 m_2 - w_2
 \end{array}$$

$$\begin{array}{l}
 m_1 : w_1 > w_2 \\
 m_2 : w_2 > w_1 \\
 w_1 : m_2 > m_1 \\
 w_2 : m_1 > m_2
 \end{array}$$

$$\begin{array}{l}
 m_1 - w_1 \\
 m_2 - w_2
 \end{array}
 \left. \vphantom{\begin{array}{l} m_1 - w_1 \\ m_2 - w_2 \end{array}} \right\} \text{S.M}$$

$$\begin{array}{l}
 m_1 - w_2 \\
 m_2 - w_1
 \end{array}
 \left. \vphantom{\begin{array}{l} m_1 - w_2 \\ m_2 - w_1 \end{array}} \right\} \text{S.M}$$

x: App ; Y: Hospital

x prefers Y to its assigned hospital Z

Y " x to it admitted she W

~~x~~ \rightarrow ~~Z~~ Y

x: Y > Z

Y \leftarrow ~~X~~ X

Y: ~~X > W~~ W > X

X	\rightarrow	Z
Y	\rightarrow	W

X	\rightarrow	Z	x: Y > Z
Y	\rightarrow	W	Y: X > W

unstable

matching