## ELECTROMAGNETIC WAVES CHAPTER - 40

$$\begin{split} 1. \quad & \frac{\in_0}{dt} \frac{d\varphi_E}{dt} = \frac{\in_0}{dt} \frac{EA}{4\pi \; \epsilon_0 r^2} \\ & = \frac{M^{-1}L^{-3}T^4A^2}{M^{-1}L^{-3}A^2} \times \frac{A^1T^1}{L^2} \times \frac{L^2}{T} = A^1 \\ & = (Current) \qquad (proved). \end{split}$$

2. 
$$E = \frac{Kq}{x^2}$$
, [from coulomb's law]

$$\begin{split} \varphi_E &= EA = \frac{KqA}{x^2} \\ I_d &= \in_0 \frac{d\varphi E}{dt} = \in_0 \frac{d}{dt} \frac{kqA}{x^2} = \in_0 KqA = \frac{d}{dt} x^{-2} \\ &= \in_0 \times \frac{1}{4\pi \in_0} \times q \times A \times -2 \times x^{-3} \times \frac{dx}{dt} = \frac{qAv}{2\pi x^3} \,. \end{split}$$

3. 
$$E = \frac{Q}{\epsilon_0 A}$$
 (Electric field)

$$\begin{split} \varphi &= E.A. = \frac{Q}{\epsilon_0} \frac{A}{A} \frac{A}{2} = \frac{Q}{\epsilon_0} 2 \\ i_0 &= \epsilon_0 \frac{d\varphi_E}{dt} = \epsilon_0 \frac{d}{dt} \left(\frac{Q}{\epsilon_0} 2\right) = \frac{1}{2} \left(\frac{dQ}{dt}\right) \\ &= \frac{1}{2} \frac{d}{dt} (EC e^{-t/RC}) = \frac{1}{2} EC - \frac{1}{RC} e^{-t/RC} = \frac{-E}{2R} e^{\frac{-td}{RE_0 \lambda}} \end{split}$$

4. 
$$E = \frac{Q}{\epsilon_0 A}$$
 (Electric field)

$$\begin{split} \varphi &= E.A. = \frac{Q}{\in_0} \frac{A}{A} \frac{A}{2} = \frac{Q}{\in_0} \frac{1}{2} \\ i_0 &= \in_0 \frac{d\varphi_E}{dt} = \in_0 \frac{d}{dt} \left(\frac{Q}{\in_0} \frac{1}{2}\right) = \frac{1}{2} \left(\frac{dQ}{dt}\right) \end{split}$$

5. 
$$B = \mu_0 H$$

$$\Rightarrow H = \frac{B}{\mu_0}$$

$$\frac{E_0}{H_0} = \frac{B_0 / (\mu_0 \in_0 C)}{B_0 / \mu_0} = \frac{1}{\epsilon_0 C}$$
$$= \frac{1}{8.85 \times 10^{-12} \times 3 \times 10^8} = 376.6 \Omega = 377 \Omega.$$

Dimension 
$$\frac{1}{\epsilon_0} = \frac{1}{[LT^{-1}][M^{-1}L^{-3}T^4A^2]} = \frac{1}{M^{-1}L^{-2}T^3A^2} = M^1L^2T^{-3}A^{-2} = [R].$$

6. 
$$E_0 = 810 \text{ V/m}, B_0 = ?$$

We know, 
$$B_0$$
 =  $\mu_0 \in_0 C \; E_0$ 

Putting the values,

$$B_0 = 4\pi \times 10^{-7} \times 8.85 \times 10^{-12} \times 3 \times 10^8 \times 810$$
  
= 27010.9 × 10<sup>-10</sup> = 2.7 × 10<sup>-6</sup> T = 2.7 μT.

7. B = 
$$(200 \mu T) \sin [(4 \times 10^{15} 5^{-1}) (t - x/C)]$$

a) 
$$B_0 = 200 \mu T$$

$$E_0 = C \times B_0 = 200 \times 10^{-6} \times 3 \times 10^8 = 6 \times 10^4$$

b) Average energy density = 
$$\frac{1}{2\mu_0}B_0^2 = \frac{(200\times 10^{-6})^2}{2\times 4\pi\times 10^{-7}} = \frac{4\times 10^{-8}}{8\pi\times 10^{-7}} = \frac{1}{20\pi} = 0.0159 = 0.016.$$

8. 
$$I = 2.5 \times 10^{14} \text{ W/m}^2$$

We know, 
$$I = \frac{1}{2} \in_0 E_0^2 C$$

$$\Rightarrow E_0^2 = \frac{2I}{\in_0 C} \qquad \text{or } E_0 = \sqrt{\frac{2I}{\in_0 C}}$$

$$E_0 = \sqrt{\frac{2 \times 2.5 \times 10^{14}}{8.85 \times 10^{-12} \times 3 \times 10^8}} = 0.4339 \times 10^9 = 4.33 \times 10^8 \text{ N/c}.$$

$$B_0 = \mu_0 \in_0 C E_0$$

$$= 4 \times 3.14 \times 10^{-7} \times 8.854 \times 10^{-12} \times 3 \times 10^{8} \times 4.33 \times 10^{8} = 1.44 \text{ T}.$$

9. Intensity of wave = 
$$\frac{1}{2} \in_0 E_0^2 C$$

$$\in_0$$
 = 8.85  $\times$   $10^{-12}$  ;  $E_0$  = ? ;  $C$  = 3  $\times$   $10^8$  ,  $I$  = 1380 W/m²

$$1380 = 1/2 \times 8.85 \times 10^{-12} \times E_0^2 \times 3 \times 10^8$$

$$\Rightarrow E_0^2 = \frac{2 \times 1380}{8.85 \times 3 \times 10^{-4}} = 103.95 \times 10^4$$

$$\Rightarrow$$
 E<sub>0</sub> = 10.195 × 10<sup>2</sup> = 1.02 × 10<sup>3</sup>

$$E_0 = B_0C$$

$$\Rightarrow \ B_0 = E_0/C = \frac{1.02 \times 10^3}{3 \times 10^8} = 3.398 \times 10^{-5} = 3.4 \times 10^{-5} \, T.$$

