

## Exercise - 13A

1. Draw a line segment AB of length 7 cm. Using ruler and compasses, find a point P on AB such that  $\frac{AP}{AB} = \frac{3}{5}$ .

**Sol:**

Steps of Construction:

Step 1: Draw a line segment  $AB = 7\text{ cm}$

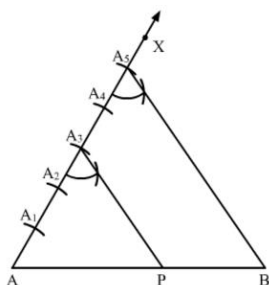
Step 2: Draw a ray AX, making an acute angle  $\angle BAX$ .

Step 3: Along AX, mark 5 points (greater of 3 and 5)  $A_1, A_2, A_3, A_4$  and  $A_5$  such that

$$AA_1 = A_1A_2 = A_2A_3 = A_3A_4 = A_4A_5$$

Step 4: Join  $A_5B$ .

Step 5: From  $A_3$ , draw  $A_3P$  parallel to  $A_5B$  (draw an angle equal to  $\angle AA_5B$ ), meeting AB in P.



Here, P is the point on AB such that  $\frac{AP}{PB} = \frac{3}{2}$  or  $\frac{AP}{AB} = \frac{3}{5}$ .

2. Draw a line segment of length 7.6 cm and divide it in the ratio 5:8. Measure the two parts.

**Sol:**

Steps of Construction:

Step 1: Draw a line segment  $AB = 7.6\text{ cm}$

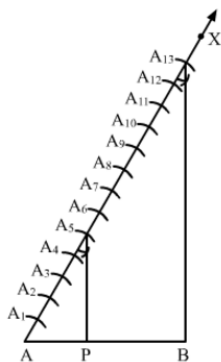
Step 2: Draw a ray AX, making an acute angle  $\angle BAX$ .

Step 3: Along AX, mark  $(5+8=)13$  points  $A_1, A_2, A_3, A_4, A_5, A_6, A_7, A_8, A_9, A_{10}, A_{11}, A_{12}$  and  $A_{13}$  such that

$$AA_1 = A_1A_2 = A_2A_3 = A_3A_4 = A_4A_5 = A_5A_6 = A_6A_7 = A_7A_8 = A_8A_9 = A_9A_{10} = A_{10}A_{11} = A_{11}A_{12} = A_{12}A_{13}.$$

Step 4: Join  $A_{13}B$ .

Step 5: From  $A_5$ , draw  $A_5P$  parallel to  $A_{13}B$  (draw an angle equal to  $\angle AA_{13}B$ ), meeting AB in P.



Here,  $P$  is the point on  $AB$  which divides it in the ratio  $5 : 8$ .

$\therefore$  Length of  $AP = 2.9 \text{ cm}$  (Approx)

Length of  $BP = 4.7 \text{ cm}$  (Approx)

3. Construct a  $\Delta PQR$ , in which  $PQ = 6 \text{ cm}$ ,  $QR = 7 \text{ cm}$  and  $PR = 8 \text{ cm}$ . Then, construct another triangle whose sides are  $\frac{4}{5}$  times the corresponding sides of  $\Delta PQR$

**Sol:**

Steps of Construction

Step 1: Draw a line segment  $QR = 7 \text{ cm}$ .

Step 2: With  $Q$  as center and radius  $6 \text{ cm}$ , draw an arc.

Step 3: With  $R$  as center and radius  $8 \text{ cm}$ , draw an arc cutting the previous arc at  $P$ .

Step 4: Join  $PQ$  and  $PR$ . Thus,  $\Delta PQR$  is the required triangle.

Step 5: Below  $QR$ , draw an acute angle  $\angle RQX$ .

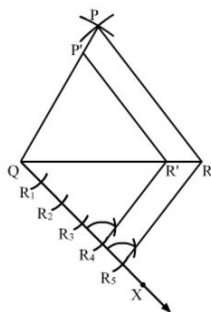
Step 6: Along  $OX$ , mark five points  $R_1, R_2, R_3, R_4$  and  $R_5$  such that

$$QR_1 = R_1R_2 = R_2R_3 = R_3R_4 = R_4R_5.$$

Step 7: Join  $RR_5$ .

Step 8: From  $R_4$ , draw  $R_4R' \parallel RR_5$  meeting  $QR$  at  $R'$ .

Step 9: From  $R'$ , draw  $P'R' \parallel PR$  meeting  $PQ$  in  $P'$ .



Here,  $\Delta P'QR'$  is the required triangle, each of whose sides are  $\frac{4}{5}$  times the corresponding sides of  $\Delta PQR$ .

4. Construct a triangle with sides 5 cm, 6 cm, and 7 cm and then another triangle whose sides are  $\frac{7}{5}$  of the corresponding sides of the first triangle.

**Sol:**

Steps of Construction :

Step 1: Draw a line segment  $BC = 4\text{ cm}$ .

Step 2: With B as center, draw an angle of  $90^\circ$ .

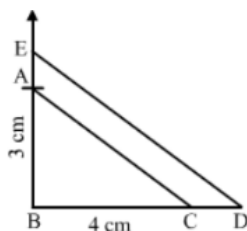
Step 3: With B as center and radius equal to 3 cm, cut an arc at the right angle and name it A.

Step 4: Join AB and AC.

Thus,  $\Delta ABC$  is obtained.

Step 5: Extend BC to D, such that  $BD = \frac{7}{5}BC = 75(4)\text{ cm} = 5.6\text{ cm}$ .

Step 6: Draw  $DE \parallel CA$ , cutting AB produced to E.



Thus,  $\Delta EBD$  is the required triangle, each of whose sides is  $\frac{7}{5}$  the corresponding sides of  $\Delta ABC$ .

5. Construct a  $\Delta ABC$  with  $BC = 7\text{ cm}$ ,  $\angle B = 60^\circ$  and  $AB = 6\text{ cm}$ . Construct another triangle whose sides are  $\frac{3}{4}$  times the corresponding sides of  $\Delta ABC$ .

**Sol:**

Steps of Construction

Step 1: Draw a line segment  $BC = 7\text{ cm}$ .

Step 2: At B, draw  $\angle XBC = 60^\circ$ .

Step 3: With B as center and radius 6 cm, draw an arc cutting the ray BX at A.

Step 4: Join AC. Thus,  $\Delta ABC$  is the required triangle.

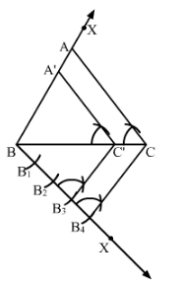
Step 5: Below BC, draw an acute angle  $\angle YBC$ .

Step 6: Along BY, mark four points  $B_1, B_2, B_3$  and  $B_4$  such that  $BB_1 = B_1B_2 = B_2B_3 = B_3B_4$ .

Step 7: Join  $CB_4$ .

Step 8: From  $B_3$ , draw  $B_3C' \parallel CB_4$  meeting  $BC$  at  $C'$ .

Step 9: From  $C'$ , Draw  $A'C' \parallel AC$  meeting  $AB$  in  $A'$ .



Here,  $\triangle A'BC'$  is the required triangle whose sides are  $\frac{3}{4}$  times the corresponding sides of  $\triangle ABC$ .

6. Construct a  $\triangle ABC$  in which  $AB = 6$  cm,  $\angle A = 30^\circ$  and  $\angle B = 60^\circ$ . Construct another  $\triangle AB'C'$  similar to  $\triangle ABC$  with base  $AB' = 8$  cm.

**Sol:**

Steps of Construction

Step 1: Draw a line segment  $AB = 6$  cm.

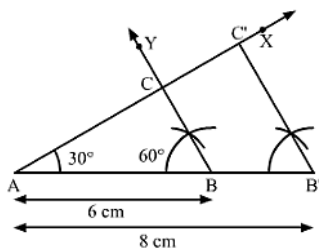
Step 2: At A, draw  $\angle XAB = 30^\circ$ .

Step 3: At B, draw  $\angle YBA = 60^\circ$ . Suppose AX and BY intersect at C.

Thus,  $\triangle ABC$  is the required triangle.

Step 4: Produce AB to  $B'$  such that  $AB' = 8$  cm.

Step 5: From  $B'$ , draw  $B'C' \parallel BC$  meeting AX at  $C'$ .



Here,  $\triangle AB'C'$  is the required triangle similar to  $\triangle ABC$ .

7. Construct a  $\triangle ABC$  in which  $BC = 8$  cm,  $\angle B = 45^\circ$  and  $\angle C = 60^\circ$ . Construct another triangle similar to  $\triangle ABC$  such that its sides are  $\frac{3}{5}$  of the corresponding sides of  $\triangle ABC$ .

**Sol:**

Steps of Construction

Step 1: Draw a line segment  $BC = 8$  cm.

Step 2: At B, draw  $\angle XBC = 45^\circ$ .

Step 3: At  $C$ , draw  $\angle YCB = 60^\circ$ . Suppose  $BX$  and  $CY$  intersect at  $A$ .

Thus,  $\triangle ABC$  is the required triangle

Step 4: Below  $BC$ , draw an acute angle  $\angle ZBC$ .

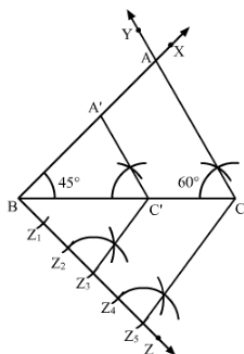
Step 5: Along  $BZ$ , mark five points  $Z_1, Z_2, Z_3, Z_4$  and  $Z_5$  such that

$$BZ_1 = Z_1Z_2 = Z_2Z_3 = Z_3Z_4 = Z_4Z_5.$$

Step 6: Join  $CZ_5$ .

Step 7: From  $Z_3$ , draw  $Z_3C' \parallel CZ_5$  meeting  $BC$  at  $C'$ .

Step 8: From  $C'$ , draw  $A'C' \parallel AC$  meeting  $AB$  in  $A'$ .



Here,  $\triangle A'BC'$  is the required triangle whose sides are  $\frac{3}{5}$  of the corresponding sides of  $\triangle ABC$ .

8. To construct a triangle similar to  $\triangle ABC$  in which  $BC = 4.5$  cm,  $\angle B = 45^\circ$  and  $\angle C = 60^\circ$ , using a scale factor of  $\frac{3}{7}$ ,  $BC$  will be divided in the ratio

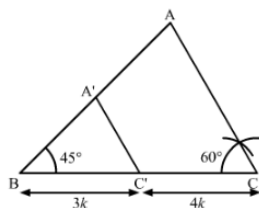
(a) 3 : 4 (b) 4 : 7 (c) 3 : 10 (d) 3 : 7

**Answer: (a) 3 : 4**

**Sol:**

To construct a triangle similar to  $\triangle ABC$  in which  $BC = 4.5$  cm,  $\angle B = 45^\circ$  and  $\angle C = 60^\circ$ ,

using a scale factor of  $\frac{3}{7}$ ,  $BC$  will be divided in the ratio 3 : 4.



Here,  $\triangle ABC \sim \triangle A'BC'$

$$BC' : C'C = 3 : 4$$

$$\text{or } BC' : BC = 3 : 7$$

Hence, the correct answer is option A.

9. Construct an isosceles triangles whose base is 8 cm and altitude 4 cm and then another triangle whose sides are  $1\frac{1}{2}$  times the corresponding sides of the isosceles triangle.

**Sol:**

Steps of Construction

Step 1: Draw a line segment  $BC = 8\text{cm}$ .

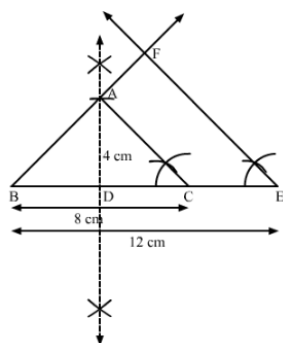
Step 2: Draw the perpendicular bisector  $XY$  of  $BC$ , cutting  $BC$  at  $D$ .

Step 3: With  $D$  as center and radius 4 cm, draw an arc cutting  $XY$  at  $A$ .

Step 4: Join  $AB$  and  $AC$ . Thus, an isosceles  $\triangle ABC$  whose base is 8 cm and altitude 4 cm is obtained.

Step 5: Extend  $BC$  to  $E$  such that  $BE = \frac{3}{2}BC = \frac{3}{2} \times 8\text{cm} = 12\text{cm}$ .

Step 6: Draw  $EF \parallel CA$ , cutting  $BA$  produced in  $F$ .



Here,  $\triangle BEF$  is the required triangle similar to  $\triangle ABC$  such that each side of  $\triangle BEF$  is  $1\frac{1}{2}$  (or  $\frac{3}{2}$ ) times the corresponding side of  $\triangle ABC$ .

10. Draw a right triangle in which the sides (other than hypotenuse) are of lengths 4 cm and 3 cm. Then, construct another triangle whose sides are  $\frac{5}{3}$  times the corresponding sides of the given triangle.

**Sol:**

Steps of Construction

Step 1: Draw a line segment  $BC = 3\text{cm}$ .

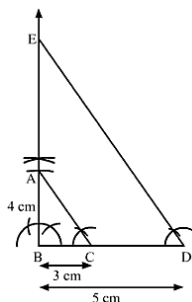
Step 2: At  $B$ , draw  $\angle XBC = 90^\circ$ .

Step 3: With  $B$  as center and radius 4 cm, draw an arc cutting  $BX$  at  $A$ .

Step 4: Join  $AC$ . Thus, a right  $\triangle ABC$  is obtained.

Step 5: Extend  $BC$  to  $D$  such that  $BD = \frac{5}{3}BC = \frac{5}{3} \times 3\text{cm} = 5\text{cm}$ .

Step 6: Draw  $DE \parallel CA$ , cutting  $BX$  in  $E$ .



Here,  $\triangle BDE$  is the required triangle similar to  $\triangle ABC$  such that each side of  $\triangle BDE$  is  $\frac{5}{3}$  times the corresponding side of  $\triangle ABC$ .

### Exercise – 13B

1. Draw a circle of radius 3 cm. Form a point P, 7 cm away from the centre of the circle, draw two tangents to the circle. Also, measure the lengths of the tangents.

**Sol:**

Steps of Construction

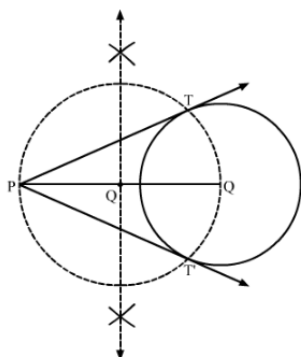
Step 1: Draw a circle with O as center and radius 3 cm.

Step 2: Mark a point P outside the circle such that  $OP = 7\text{ cm}$ .

Step 3: Join OP. Draw the perpendicular bisector XY of OP, cutting OP at Q.

Step 4: Draw a circle with Q as center and radius PQ (or OQ), to intersect the given circle at the points T and T'.

Step 5: Join PT and PT'.



Here, PT and PT' are the required tangents.

$$PT = PT' = 6.3\text{ cm (Approx)}$$

2. Draw two tangents to a circle of radius 3.5 cm from a point P at a distance of 6.2 cm from its centre.

**Sol:**

Steps of Construction

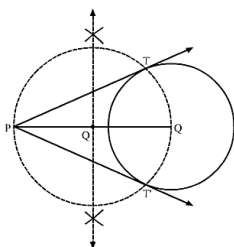
Step 1: Draw a circle with O as center and radius 3.5 cm.

Step 2: Mark a point  $P$  outside the circle such that  $OP = 6.2\text{ cm}$ .

Step 3: Join  $OP$ . Draw the perpendicular bisector  $XY$  of  $OP$ , cutting  $OP$  at  $Q$ .

Step 4: Draw a circle with  $Q$  as center and radius  $PQ$  (or  $OQ$ ), to intersect the given circle at the points  $T$  and  $T'$ .

Step 5: Join  $PT$  and  $PT'$ .



Here,  $PT$  and  $PT'$  are the required tangents.

3. Draw a circle of radius 3.5 cm. Take two points  $A$  and  $B$  on one of its extended diameter, each at a distance of 5 cm from its center. Draw tangents to the circle from each of these points  $A$  and  $B$ .

**Sol:**

Steps of Construction

Step 1: Draw a circle with center  $O$  and radius 3.5 cm.

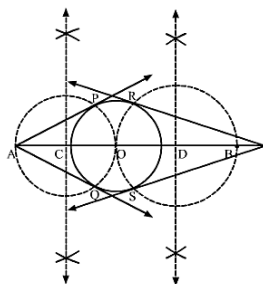
Step 2: Extends its diameter on both sides and mark two points  $A$  and  $B$  on it such that  $OA = OB = 5\text{ cm}$ .

Step 3: Draw the perpendicular bisectors of  $OA$  and  $OB$ . Let  $C$  and  $D$  be the mid-points of  $OA$  and  $OB$ , respectively.

Step 4: Draw a circle with  $C$  as center and radius  $OC$  (or  $AC$ ), to intersect the circle with center  $O$ , at the points  $P$  and  $Q$ .

Step 5: Draw another circle with  $D$  as center and radius  $OD$  (or  $BD$ ), to intersect the circle with center  $O$  at the points  $R$  and  $S$ .

Step 6: Join  $AP$  and  $AQ$ , Also, join  $BR$  and  $BS$ .



Here,  $AP$  and  $AQ$  are the tangents to the circle from  $A$ , Also,  $BR$  and  $BS$  are the tangents to the circle from  $B$ .



4. Draw a circle with center  $O$  and radius 4 cm. Draw any diameter  $AB$  of this circle. Construct tangents to the circle at each of the two end points of the diameter  $AB$ .

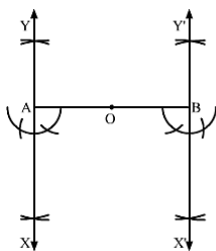
**Sol:**

Step 1: Draw a circle with center  $O$  and radius 4 cm.

Step 2: Draw any diameter  $AOB$  of the circle.

Step 3: At  $A$ , draw  $\angle OAX = 90^\circ$ . Produce  $XA = Y$ .

Step 4: At  $B$ , draw  $\angle OBX' = 90^\circ$ . Produce  $X'B$  to  $Y'$ .



Here,  $XAY$  and  $X'BY'$  are the tangents to the circle at the end points of the diameter  $AB$ .

5. Draw a circle with the help of a bangle. Take any point  $P$  outside the circle. Construct the pair of tangents from the point  $P$  to the circle.

**Sol:**

Steps of Construction

Step 1: Draw a circle with the help of a bangle.

Step 2: Mark a point  $P$  outside the circle.

Step 3: Through  $P$ , draw a secant  $PAB$  to intersect the circle at  $A$  and  $B$ .

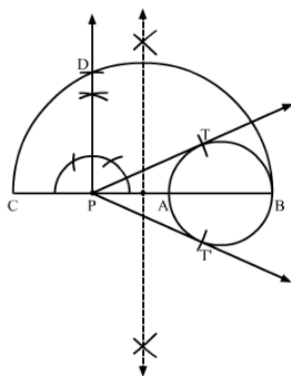
Step 4: Produce  $AP$  to  $C$  such that  $PA = PC$ .

Step 5: Draw a semicircle with  $CB$  as diameter.

Step 6: Draw  $PD \perp BC$ , intersecting the semicircle at  $D$ .

Step 7: With  $P$  as center and  $PD$  as radius, draw arcs to intersect the circle at  $T$  and  $T'$ .

Step 8: Join  $PT$  and  $PT'$ .



Here,  $PT$  and  $PT'$  are the required pair of tangents.

6. Draw a line segment  $AB$  of length 8 cm. Taking  $A$  as centre, draw a circle of radius 4 cm and taking  $B$  as centre, draw another circle of radius 3 cm. Construct tangents to each circle from the centre of the other circle.

**Sol:**

Steps of Construction

Step 1: Draw a line segment  $AB = 8$  cm.

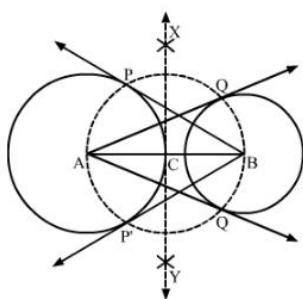
Step 2: With  $A$  as center and radius 4 cm, draw a circle.

Step 3: With  $B$  as center and radius 3 cm, draw another circle.

Step 4: Draw the perpendicular bisector  $XY$  of  $AB$ , cutting  $AB$  at  $C$ .

Step 5: With  $C$  as center and radius  $AC$  (or  $BC$ ), draw a circle intersecting the circle with center  $A$  at  $P$  and  $P'$  and the circle with center  $B$  at  $Q$  and  $Q'$ .

Step 6: Join  $BP$  and  $BP'$ . Also, join  $AQ$  and  $AQ'$ .



Here,  $AQ$  and  $AQ'$  are the tangents from  $A$  to the circle with center  $B$ . Also,  $BP$  and  $BP'$  are the tangents from  $B$  to the circle with center  $A$ .

7. Draw a circle of radius 4.2. Draw a pair of tangents to this circle inclined to each other at an angle of  $45^\circ$

**Sol:**

Steps of Construction:

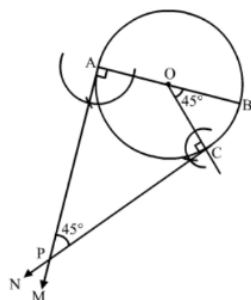
Step 1: Draw a circle with center  $O$  and radius = 4.2 cm.

Step 2: Draw any diameter  $AOB$  of this circle.

Step 3: Construct  $\angle BOC = 45^\circ$ , such that the radius  $OC$  meets the circle at  $C$ .

Step 4: Draw  $AM \perp AB$  and  $CN \perp OC$ .

$AM$  and  $CN$  intersect at  $P$ .



Thus,  $PA$  and  $PC$  are the required tangents to the given circle inclined at an angle of  $45^\circ$ .

8. Write the steps of construction for drawing a pair of tangents to a circle of radius 3 cm, which are inclined to each other at an angle of  $60^\circ$ .

**Sol:**

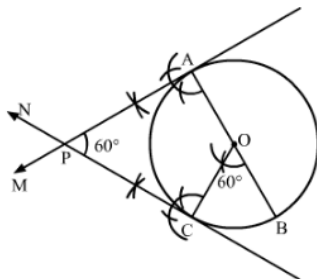
Steps of Construction

Step 1: Draw a circle with center  $O$  and radius 3 cm.

Step 2: Draw any diameter  $AOB$  of the circle.

Step 3: Construct  $\angle BOC = 60^\circ$  such that radius  $OC$  cuts the circle at  $C$ .

Step 4: Draw  $AM \perp AB$  and  $CN \perp OC$ . Suppose  $AM$  and  $CN$  intersect each other at  $P$ .



Here,  $AP$  and  $CP$  are the pair of tangents to the circle inclined to each other at an angle of  $60^\circ$ .

9. Draw a circle of radius 3 cm. Draw a tangent to the circle making an angle  $30^\circ$  with a line passing through the centre.

**Sol:**

Steps Of construction:

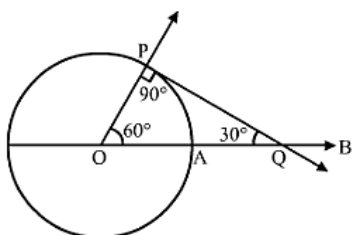
Step 1: Draw a circle with center  $O$  and radius 3 cm.

Step 2: Draw radius  $OA$  and produce it to  $B$ .

Step 3: Make  $\angle AOP = 60^\circ$

Step 4: Draw  $PQ \perp OP$ , meeting  $OB$  at  $Q$ .

Step 5: Then,  $PQ$  is the desired tangent, such that  $\angle OQP = 30^\circ$



10. Construct a tangent to a circle of radius 4 cm from a point on the concentric circle of radius 6 cm and measure its length. Also, verify the measurement by actual calculation.

**Sol:**

Steps of Construction

Step 1: Mark a point  $O$  on the paper

Step 2: With  $O$  as center and radii 4 cm and 6 cm, draw two concentric circles.

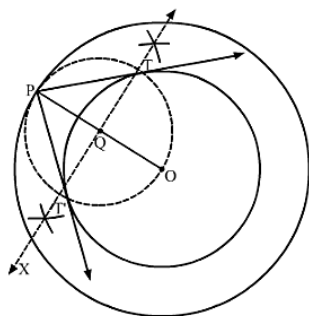
Step 3: Mark a point P on the outer circle.

Step 4: Join OP.

Step 5: Draw the perpendicular bisector  $XY$  of  $OP$ , cutting  $OP$  at  $Q$ .

Step 6: Draw a circle with  $Q$  as center and radius  $OQ$  (or  $PQ$ ), to intersect the inner circle in points T and T'.

Step 7: Join PT and PT'.



Here, PT and PT' are the required tangents.

$PT = PT' \approx 4.5 \text{ cm}$  (Approx)

Verification by actual calculation

Join OT to form a right  $\triangle OTP$  (Radius is perpendicular to the tangent at the point of contact)

In right  $\triangle OTP$ ,

$$OP^2 = OT^2 + PT^2 \quad (\text{Pythagoras Theorem})$$

$$\Rightarrow PT = \sqrt{OP^2 - OT^2}$$

$$\Rightarrow PT = \sqrt{6^2 - 4^2} = \sqrt{36 - 16} = \sqrt{20} \approx 4.5 \text{ cm}$$

$$(OP = 6 \text{ cm and } OT = 4 \text{ cm})$$

### Exercise - Formative Assessment

11. Draw a line segment AB of length 5.4 cm. Divide it into six equal parts. Write the steps of construction.

**Sol:**

Steps of Construction:

Step 1: Draw a line segment  $AB = 5.4 \text{ cm}$ .

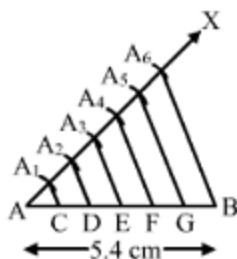
Step 2: Draw a ray AX, making an acute angle,  $\angle BAX$ .

Step 3: Along AX, mark 6 points  $A_1, A_2, A_3, A_4, A_5$  such that,

$$AA_1 = A_1A_2 = A_2A_3 = A_3A_4 = A_4A_5 = A_5A_6.$$

Step 4: Join  $A_6B$ .

Step 5: Draw  $A_1C, A_2D, A_3D, A_4F$  and  $A_5A_6$ .



Thus, AB is divided into six equal parts.

12. Draw a line segment AB of length 6.5 cm and divided it in the ratio 4 : 7. Measure each of the two parts.

**Sol:**

Steps of Construction:

Step 1: Draw a line segment  $AB = 6.5\text{ cm}$ .

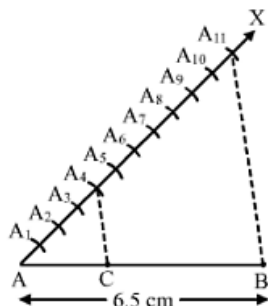
Step 2: Draw a ray AX, making an acute angle  $\angle BAX$ .

Step 3: Along AX, mark  $(4 + 7) = 11$  points  $A_1, A_2, A_3, A_4, A_5, A_6, A_7, A_8, A_9, A_{10}, A_{11}$  such that  $AA_1 = A_1A_2 = A_2A_3 = A_3A_4 = A_4A_5 = A_5A_6 = A_6A_7 = A_7A_8 = A_8A_9 = A_9A_{10} = A_{10}A_{11}$

Step 4: Join  $A_{11}B$ .

Step 5: From  $A_4$ , draw  $A_4C \parallel A_{11}B$ , meeting AB at C.

Thus, C is the point on AB, which divides it in the ratio 4 : 7.



Thus,  $AC : CB = 4 : 7$

From the figure,

$$AC = 2.36\text{ cm}$$

$$CB = 4.14\text{ cm}$$

13. Construct a  $\triangle ABC$  in which  $BC = 6.5\text{ cm}$ ,  $AB = 4.5\text{ cm}$  and  $\angle ABC = 60^\circ$

**Sol:**

Steps of Construction:

Step 1: Draw a line segment  $BC = 6.5\text{ cm}$ .

Step 2: With B as center, draw an angle of  $60^\circ$ .

Step 3: With B as center and radius equal to 4.5 cm, draw an arc, cutting the angle at A

Step 4: Join AB and AC.

Thus,  $\triangle ABC$  is obtained.

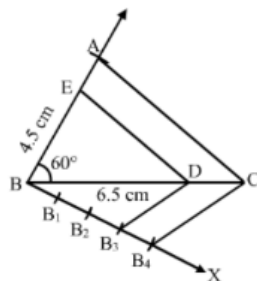
Step 5: Below  $BC$ , draw an acute  $\angle CBX$ .

Step 6: Along  $BX$ , mark off four points  $B_1, B_2, B_3, B_4$  such that  $BB_1 = B_1B_2 = B_2B_3 = B_3B_4$ .

Step 7: Join  $B_4C$ .

Step 8: From  $B_3$ , draw  $B_3D \parallel B_4C$ , meeting  $BC$  at  $D$ .

Step 9: From  $D$ , draw  $DE \parallel CA$ , meeting  $AB$  at  $E$ .



Thus,  $\triangle EBD$  is the required triangle, each of whose sides is  $\frac{3}{4}$  the corresponding sides of  $\triangle ABC$ .

14. Construct a  $\triangle ABC$  in which  $BC = 5\text{cm}$ ,  $\angle C = 60^\circ$  and altitude from A equal to 3 cm. Construct a  $\triangle ADE$  similar to  $\triangle ABC$  such that each side of  $\triangle ADE$  is  $\frac{3}{2}$  times the corresponding side of  $\triangle ABC$ . Write the steps of construction.

**Sol:**

Steps of Construction:

Step 1: Draw a line  $l$ .

Step 2: Draw an angle of  $90^\circ$  at  $M$  on  $l$

Step 3: Cut an arc of radius 3 cm on the perpendicular. Mark the point as A

Step 4: With A as center, make an angle of  $30^\circ$  and let it cut  $l$  at C. We get  $\angle ACB = 60^\circ$ .

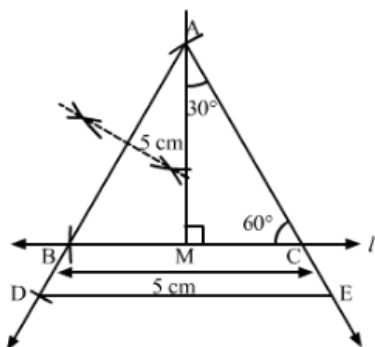
Step 5: Cut an arc of 5 cm from C on  $l$  and mark the point as B.

Step 6: Join AB.

Thus,  $\triangle ABC$  is obtained

Step 7: Extend AB to D, such that  $BD = BC$ .

Step 8: Draw  $DE \parallel BC$ , cutting AC produced to E.



Then,  $\triangle ADE$  is the required triangle, each of whose sides is of the corresponding sides of  $\triangle ABC$ .

15. Construct an isosceles triangle whose base is 9 cm and altitude 5 cm. Construct another triangle whose sides are  $\frac{3}{4}$  of the corresponding sides of the first isosceles triangle.

**Sol:**

Steps of Construction:

Step 1: Draw a line segment  $BC = 9\text{ cm}$

Step 2: With B as center, draw an arc each above and below BC.

Step 3: With C as center, draw an arc each above and below BC.

Step 4: Join their points of intersection to obtain the perpendicular bisector of BC. Let it intersect BC at D

Step 5: From D, cut an arc of radius 5 cm and mark the point as A

Step 6: Join AB and AC

Thus  $\triangle ABC$  is obtained

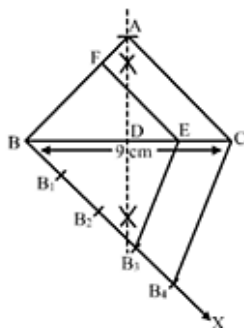
Step 5: Below BC, make an acute  $\angle CBX$ .

Step 6: Along BX, mark off four points  $B_1, B_2, B_3, B_4$  such that  $BB_1 = B_1B_2 = B_2B_3 = B_3B_4$

Step 7: Join  $B_4C$ .

Step 8: From  $B_3$ , draw  $B_2E \parallel B_4C$  meeting BC at E.

Step 9: From E, draw  $EF \parallel CA$  meeting AB at F.



Thus,  $\triangle FBE$  is the required triangle, each of whose sides is  $\frac{3}{4}$  the corresponding sides of the first triangle.

16. Draw a  $\triangle ABC$ , right-angled at B such that  $AB = 3$  cm and  $BC = 4$  cm. Now, Construct a triangle similar to  $\triangle ABC$ , each whose sides is  $\frac{7}{5}$  times the corresponding side of  $\triangle ABC$ .

**Sol:**

Steps of Construction

Sept 1: Draw a line segment  $BC = 4$  cm

Sept 2: With B as center draw an angle of  $90^\circ$

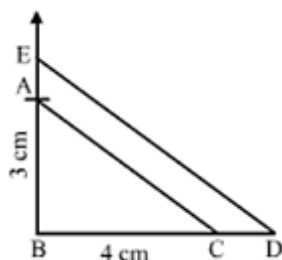
Step 3: With B as center and radius equal to 3cm cat an arc at the night angle and name it A

Step 4: Join AB and AC

Thus,  $\triangle ABC$  is obtained

Step 5: Extend BC to D, such that  $BD = \frac{7}{5} BC = \frac{7}{5}(4) \text{ cm} = 5.6 \text{ cm}$

Step 6: Draw  $DE \parallel CA$  cutting AB produced to E



Thus,  $\triangle EBD$  is the required triangle, each of whose sides is  $\frac{7}{5}$  the corresponding sides of  $\triangle ABC$ .

17. Draw a circle of radius 4.8 cm. Take a point P on it. Without using the centre of the circle, construct a tangent at the point P. Write the steps of construction.

**Sol:**

Steps of Construction:

Step 1: Draw a circle of radius 4.8 cm.

Step 2: Mark a point P on it.

Step 3: Draw any chord PQ.

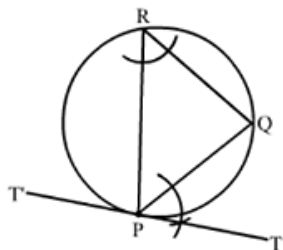
Step 4: Take a point R on the major arc QP

Step 5: Join PR and RQ.

Step6: Draw  $\angle QPT = \angle PRQ$

Step 7: Produce  $TP$  to  $T'$ , as shown in the figure.





TPT is the required tangent.

18. Draw a circle of radius 3.5 cm. Draw a pair of tangents to this circle which are inclined to each other at an angle of  $60^\circ$ . Write the steps of construction.

**Sol:**

Steps of Construction:

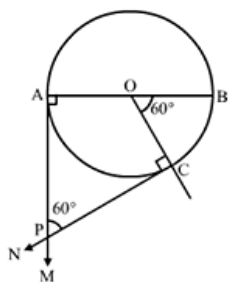
Step 1: Draw a circle with center  $O$  and radius = 3.5cm

Step 2: Draw any diameter  $AOB$  of this circle

Step 3: Construct  $\angle BOC = 60^\circ$ , such that the radius  $OC$  meets the circle at  $C$ .

Step 4: Draw  $MA \perp AB$  and  $NC \perp OC$ .

Let  $AM$  and  $CN$  intersect at  $P$ .



Then,  $PA$  and  $PC$  are the required tangents to the given circle that are inclined at an angle of  $60^\circ$

19. Draw a circle of radius 4 cm. Draw tangent to the circle making an angle of  $60^\circ$  with a line passing through the centre.

**Sol:**

Steps of construction

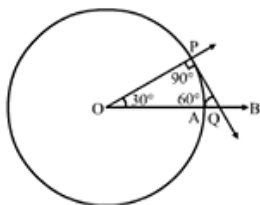
Step 1: Draw a circle with center  $O$  and radius 4cm

Step 2: Draw radius  $OA$  and produce it to  $B$ .

Step 3: Make  $\angle AOP = 30^\circ$

Step 4: Draw  $PQ \perp OP$ , meeting  $OB$  at  $Q$ .

Step 5: Then,  $PQ$  is the desired tangent, such that  $\angle OQP = 60^\circ$



20. Draw two concentric circles of radii 4 cm and 6 cm. Construct a tangent to the smaller circle from a point on the larger circle. Measure the length of this tangent.

**Sol:**

Step of Construction:

Step 1: Draw a circle with  $O$  as center and radius 6 cm

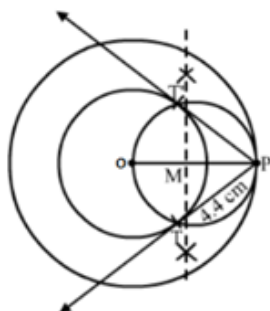
Step 2: Draw another circle with  $O$  as center and radius 4 cm

Step 2: Mark a point  $P$  on the circle with radius 6 cm

Step 3: Join  $OP$  and bisect it at  $M$ .

Step 4: Draw a circle with  $M$  as center and radius equal to  $MP$  to intersect the given circle with radius 4 cm at points  $T$  and  $T'$ .

Step 5: Join  $PT$  and  $PT'$ .



Thus,  $PT$  or  $PT'$  the required tangents and measure 4.4 cm each.