
Linear Equations in Two Variables

Exercise 4.1

Write the correct answer in each of the following:

1. **The linear equation $2x - 5y = 7$ has**

(A) A unique solution
(B) Two solutions
(C) Infinitely many solutions
(D) No solution

Sol. $2x - 5y = 7$ is a linear equation in two variables. A linear equation in two variables has infinitely many solution.
Hence, (c) is the correct answer.

2. **The equation $2x + 5y = 7$ has a unique solution, if x, y are:**

(A) Natural numbers
(B) Positive real numbers
(C) Real numbers
(D) Rational numbers

Sol. The equation $2x + 5y = 7$ has a unique solution if x, y are natural numbers.
Hence, (a) is the correct answer.

3. **If $(2, 0)$ is a solution of the linear equation $2x + 3y = k$, then the value of k is**

(A) 4
(B) 6
(C) 5
(D) 2

Sol. Substituting $x = 2$ and $y = 0$ in the given equation $2x + 3y = k$, we get
 $2(2) + 3(0) = k \Rightarrow k = 4$
Therefore, the value of k is 4.
Hence, (a) is the correct answer.

4. **Any solution of the linear equation $2x + 0y + 9 = 0$ in two variables is of the form:**

(a) $\left(-\frac{9}{2}, m\right)$
(b) $\left(n, -\frac{9}{2}\right)$
(c) $\left(0, -\frac{9}{2}\right)$
(d) $(-9, 0)$

Sol. The given linear equation is $2x + 0y + 9 = 0 \Rightarrow 2x = -9$
 $\therefore x = -\frac{9}{2}$

Since the coefficient of y is 0 in the given equation, the solution can be given as $\left(-\frac{9}{2}, m\right)$.

Hence, (a) is the correct answer.

5. The graph of the linear equation $2x + 3y = 6$ cuts the y -axis at the point

- (A) (2, 0)
- (B) (0, 3)
- (C) (3, 0)
- (D) (0, 2)

Sol. The graph of the linear equation $2x + 3y = 6$ cuts the y -axis at the point where x -coordinate is zero.

Putting $x = 0$ in $2x + 3y = 6$, we get

$$2(0) + 3y = 6 \Rightarrow 3y = 6 \Rightarrow y = 6 \div 3 = 2$$

So, (0, 2) is the required point.

Hence, (d) is the correct answer.

6. The equation $x = 7$, in two variables, can be written as

- (A) $1.x + 1.y = 7$
- (B) $1.x + 0.y = 7$
- (C) $0.x + 1.y = 7$
- (D) $0.x + 0.y = 7$

Sol. The equation $x = 7$ in two variables can be expressed as $1.x + 0.y = 7$.

Hence, (b) is the correct answer.

7. Any point on the x -axis is of the form

- (A) (x, y)
- (B) (0, y)
- (C) (x, 0)
- (D) (x, x)

Sol. Any point on the x -axis has its ordinate 0.

So, any point on the x -axis is of the form (x, 0).

Hence, (c) is the correct answer.

8. Any point on the line $y = x$ is of the form

- (A) (a, a)
- (B) (0, a)
- (C) (a, 0)
- (D) (a, -a)

Sol. Any point on the line $y = x$ will have x and y coordinate same.

So, any point on the line $y = x$ is of the form (a, a).

Hence, (a) is the correct answer.

9. The equation of x -axis is of the form

- (A) $x = 0$
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- (B) $y = 0$
(C) $x + y = 0$
(D) $x = y$

Sol. $y = 0$ is the equation of x-axis.
Hence, (b) is the correct answer.

10. The graph of $y = 6$ is a line

- (A) parallel to x-axis at a distance 6 units from the origin
(B) parallel to y-axis at a distance 6 units from the origin
(C) making an intercept 6 on the x-axis.
(D) making an intercept 6 on both the axes.

Sol. The given equation $y = 6$ does not contain x. Its graph is a line parallel to x-axis.
So, the graph of $y = 6$ is a line parallel to x-axis at a distance 6 units from the origin.
Hence, (a) is the correct answer.

11. $x = 5, y = 2$ is a solution of the linear equation

- (A) $x + 2y = 7$
(B) $5x + 2y = 7$
(C) $x + y = 7$
(D) $5x + y = 7$

Sol. $x = 5, y = 2$ is a solution of the linear equation $x + y = 7$, as $5 + 2 = 7$.
Hence, (c) is a correct answer.

12. If a linear equation has solutions $(-2, 2)$, $(0, 0)$ and $(2, -2)$, then it is of the form

- (A) $y - x = 0$
(B) $x + y = 0$
(C) $-2x + y = 0$
(D) $-x + 2y = 0$

Sol. The points $(-2, 2)$ and $(2, -2)$ have x and y coordinates of opposite signs.
Also, any point on the graph of $x + y = 0$
i.e., $y = -x$ will have x and y coordinate of opposite signs. The Point $(0, 0)$ also satisfies $x + y = 0$.
Hence, (b) is the correct answer.

13. The positive solutions of the equation $ax + by + c = 0$ always lie in the

- (A) 1st quadrant
(B) 2nd quadrant
(C) 3rd quadrant
(D) 4th quadrant

Sol. Quadrant I consist of all points (x, y) for which the x and y are positive.
So, the positive solution of the equation $ax + by + c = 0$ always lie in the 1st quadrant.
Hence, (a) is the correct answer.

14. The graph of the linear equation $2x + 3y = 6$ is a line which meets the x-axis at the point

(A) (0, 2)

(B) (2, 0)

(C) (3, 0)

(D) (0, 3)

Sol. The graph of the linear equation $2x + 3y = 6$ is a line which meets the x-axis at the point where $y = 0$.

Now putting $y = 0$ in $2x + 3y = 6$, we get

$$2x + 3(0) = 6 \Rightarrow 2x = 6 \Rightarrow x = 6 \div 2 = 3$$

So, (3, 0) is a point on the line $2x + 3y = 6$.

Hence, (c) is the correct answer.

15. The graph of the linear equation $y = x$ passes through the point.

(a) $\left(\frac{3}{2}, \frac{-3}{2}\right)$

(b) $\left(0, \frac{3}{2}\right)$

(c) (1, 1)

(d) $\left(\frac{-1}{2}, \frac{1}{2}\right)$

Sol. We know that any point on the line $y = x$ will have x and y coordinates same.

So, the graph of the linear equation $y = x$ passes through the point (1, 1).

Hence, (c) is the correct answer.

16. If we multiply or divide both sides of a linear equation with a non-zero number, then the solution of the linear equation:

(A) Changes

(B) Remains the same

(C) Changes in case of multiplication only

(D) Changes in case of division only

Sol. If we multiply or divide both sides of a linear equation with a non-zero number, then the solution of the linear equation remains the same.

Hence, (b) is the correct answer.

17. How many linear equations in x and y can be satisfied by $x = 1$ and $y = 2$?

(A) Only one

(B) Two

(C) Infinitely many

(D) Three

Sol. There are infinitely many linear equations which are satisfied by $x = 1$ and $y = 2$.

For example, a linear equation $x + y = 3$ is satisfied by $x = 1$ and $y = 2$.

Others are $y = 2x$, $y - x = 1$, $2y - x = 3$ etc.

Hence, (c) is the correct answer.

18. The point of the form (a, a) always lies on:

- (A) x-axis
- (B) y-axis
- (C) On the line $y = x$
- (D) On the line $x + y = 0$

Sol. The points of the form (a, a) have x and y coordinates same. So, the point of the form (a, a) always lies on the line $y = x$.
Hence, (c) is the correct answer.

19. The point of the form $(a, -a)$ always lies on the line

- (A) $x = a$
- (B) $y = -a$
- (C) $y = x$
- (D) $x + y = 0$

Sol. The point of the $(a, -a)$ have x and y coordinate of opposite signs.
So, the points of the form $(a, -a)$ always lie on the line $y = -x$, i.e., $x + y = 0$.
Hence, (d) is the correct answer.

Linear Equations in Two Variables

Exercise 4.2

Write whether the following statements are true or false. Justify your answer.

1. The point $(0, 3)$ lies on the graph of the linear equation $3x + 4y = 12$.

Sol. Substituting $x = 0$ and $y = 3$ in the equation

$$3(0) + 4(3) = 12 \Rightarrow 12 = 12, \text{ which is true.}$$

The point $(0, 3)$ satisfies the equation $3x + 4y = 12$.

Hence, the given statement is true.

2. The graph of the linear equation $x + 2y = 7$ passes through the point $(0, 7)$.

Sol. Substituting $x = 0$ and $y = 7$ in the given equation $x + 2y = 7$, we get

$$0 + 2(7) = 7 \Rightarrow 14 = 7, \text{ which is false.}$$

The point $(0, 7)$ does not satisfy the equation.

Hence, the given statement is false.

3. The graph given below represents the linear equation $x + y = 0$.

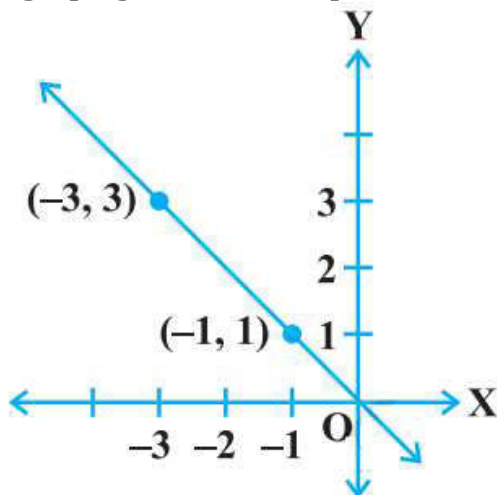


Fig. 4.1

Sol. The given equation is $x + y = 0$, i.e., $y = -x$.

Any point on the graph of $y = -x$, will have x and y coordinates of opposite signs.

As the points $(-1, 1)$ and $(-3, 3)$ have x and y coordinates of opposite signs, so these points satisfy the given equation and the two points determine a unique line, hence the given statement is true.

4. The graph given below represents the linear equation $x = 3$ (see Fig. 4.2).
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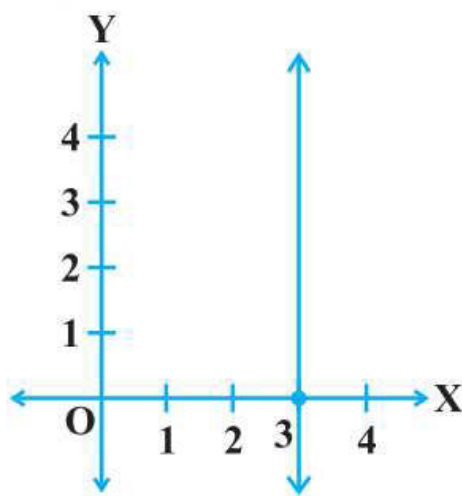


Fig. 4.2

- Sol.** We know that the graph of the equation $x = a$ is a line parallel to the y-axis and to the right of y-axis, if $a > 0$.
The given statement is true, since the graph is a line parallel to y-axis at a distance of 3 units to the right of it.

5. The coordinates of points in the table:

X	0	1	2	3	4
y	2	3	4	-5	6

Represent some of the solution of the equation $x - y + 2 = 0$.

- Sol.** The points (0, 2), (1, 3), (2, 4) and (4, 6) satisfy the given equation $x - y + 2 = 0$. Each of these points is the solution of the equation $x - y + 2 = 0$. But, they do not satisfy the given equation as $3 - (-5) + 2 = 0$, i.e., $3 + 5 + 2 = 0$ or $10 = 0$, which is false.
Hence, the given statement is false, since the point (3, -5) does not satisfy the given equation.

6. Every point on the graph of a linear equation in two variables does not represent a solution of the linear equation.

- Sol.** As every point on the graph of linear equation in two variables represents a solution of the equation, so the given statement is false.

7. The graph of every linear equation in two variables need not be a line.

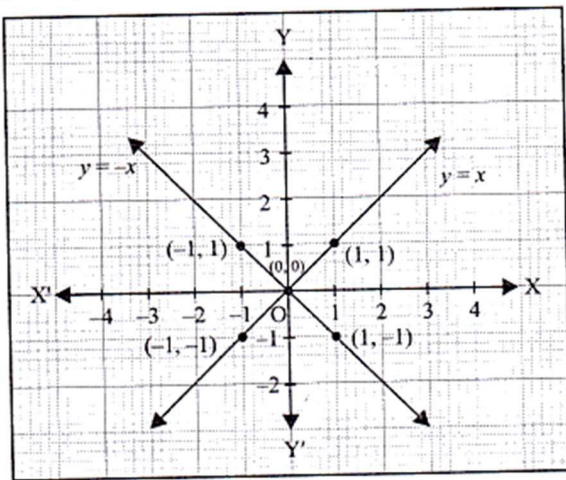
- Sol.** As the graph of a linear equation in two variables is always a line, so the given statement is false.

Linear Equations in Two Variables

Exercise 4.3

1. Draw the graphs of linear equations $y = x$ and $y = -x$ on the same Cartesian plane. What do you observe?

Sol. Any point on the graph of $y = x$ will have x and y coordinates same. The line passes through the points $(0, 0)$, $(1, 1)$ and $(-1, -1)$.
Again, any point on the graph of $y = -x$ will have x and y coordinates of opposite signs. The line passes through the points $(1, -1)$ and $(-1, 1)$.
Also, $(0, 0)$ satisfy $y = -x$.
The graph of linear equation $y = x$ and $y = -x$ on the same Cartesian plane is shown in the figure given below.



We observe that the graph of these equation passes through $(0, 0)$.

2. Determine the point on the graph of the linear equation $2x + 5y = 19$, whose ordinate is $1\frac{1}{2}$ times its abscissa.

Sol. Let the coordinate of the point be $(2, 3)$.

Now, for $x = 2$ and $y = 3$.

$$2x + 5y = 2(2) + 5(3) = 4 + 15 = 19$$

Therefore, the point $(2, 3)$ is a solution of the equation $2x + 5y = 19$.

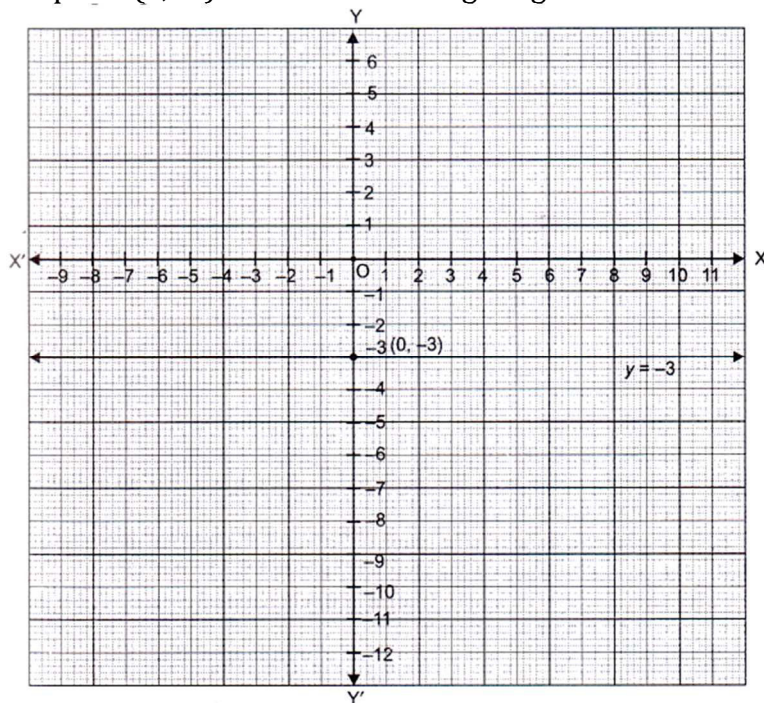
Abcissa of the point is 2 and ordinate is 3.

$$\text{Now, } 2 \times 1\frac{1}{2} = 2 \times \frac{3}{2} = 3$$

So, ordinate of the point $(2, 3)$ is $1\frac{1}{2}$ times its abscissa.

3. Draw the graph of the equation represented by a straight line which is parallel to the x -axis and at a distance 3 units below it.
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Sol. The graph of the equation $y = -3$ is a line parallel to the axis and at a distance 3 units below it. So, graph of the equation $y = -3$ is a line parallel to x-axis and passing through the point $(0, -3)$ as shown in the figure given below:



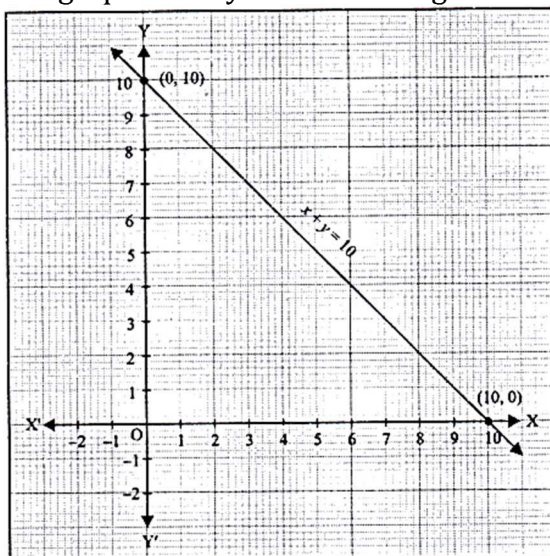
4. Draw the graph of the linear equation whose solutions are represented by the points having the sum of coordinates as 10 units.

Sol. A linear equation whose solutions are represented by the points having the sum of coordinates as 10 units is $x + y = 10$.

When $x = 0$, $y = 10$ and when $x = 10$, $y = 0$.

Now, plot these two points $(0, 10)$ and $(10, 0)$ on a graph paper and join them to obtain a straight line.

The graph of $x + y = 10$ is a straight line as shown in the figure given below.



5. Write the linear equation such that each point on its graph has an ordinate 3 times its abscissa.

Sol. A linear equation such that each point on its graph has an ordinate 3 times its abscissa is $y = 3x$.

6. If the point (3, 4) lies on the graph of $3y = ax + 7$, then find the value of a.

Sol. The point (3, 4) lies on the graph of $3y = ax + 7$.

Substituting $x = 3$ and $y = 4$ in the given equation $3y = ax + 7$, we get

$$\therefore 3 \times 4 = a \times 3 + 7$$

$$\Rightarrow 12 = 3a + 7 \Rightarrow 3a = 5 \Rightarrow a = \frac{5}{3}$$

7. How many solution(s) of the equation $2x + 1 = x - 3$ are there on the:

(i) Number line

(ii) Cartesian plane?

Sol. (i) The number of solution(s) of the equation $2x + 1 = x - 3$ which are on the number line is one.

$$2x + 1 = x - 3 \Rightarrow 2x - x = -3 - 1 \Rightarrow x = -4$$

$\therefore x = -4$ is the solution of the given equation.

(ii) The number of solution(s) of the equation $2x + 1 = x - 3$ which are on the Cartesian plane are infinitely many solutions.

8. Find the solution of the linear equation $x + 2y = 8$ which represents a point on

(i) x-axis (ii) y-axis

Sol. We know that the point which lies on x-axis has its ordinate 0.

Putting $y = 0$ in the equation $x + 2y = 8$, we get

$$x + 2(0) = 8 \Rightarrow x = 8$$

A point which lies on y-axis has its abscissa 0.

Putting $x = 0$ in the equation $x + 2y = 8$, we get

$$0 + 2y = 8 \Rightarrow y = 4$$

9. For what value of c, the linear equation $2x + cy = 8$ has equal values of x and y for its solution.

Sol. The value of c for which the linear equation $2x + cy = 8$ has equal values of x and y

i.e., $x = y$ for its solution is

$$2x + cy = 8 \Rightarrow 2x + cx = 8 \quad [\because y = x]$$

$$\Rightarrow cx = 8 - 2x$$

$$\therefore c = \frac{8 - 2x}{x}, x \neq 0$$

10. Let y varies directly as x. If y = 12 when x = 4, then write a linear equation. What is the value of y when x = 5?

Sol. y varies directly as x.

$$\Rightarrow y \propto x,$$

$$\therefore y = kx$$

Substituting $y = 12$ when $x = 4$, we get

$$12 = k \times 4 \Rightarrow k = 12 \div 4 = 3$$

Hence, the required equation is $y = 3x$.

The value of y when $x = 5$ is $y = 3 \times 5 = 15$.

Linear Equations in Two Variables

Exercise 4.4

1. Show that the points A (1, 2), B (-1, -16) and C (0, -7) lie on the graph of the linear equation $y = 9x - 7$.

Sol. For A (1, 2), we have $2 = 9(1) - 7 = 9 - 7 = 2$

For B (-1, -16), we have $-16 = 9(-1) - 7 = -9 - 7 = -16$

For C (0, -7), we have $-7 = 9(0) - 7 = 0 - 7 = -7$

We see that the line $y = 9x - 7$ is satisfied by the points A (1, 2), B (-1, -16) and C (0, -7).

Therefore, A (1, 2), B (-1, -16) and C (0, -7) are solutions of the linear equation $y = 9x - 7$ and therefore, lie on the graph of the linear equation $y = 9x - 7$.

2. The following observed values of x and y are thought to satisfy a linear equation.

x	6	-6
y	-2	6

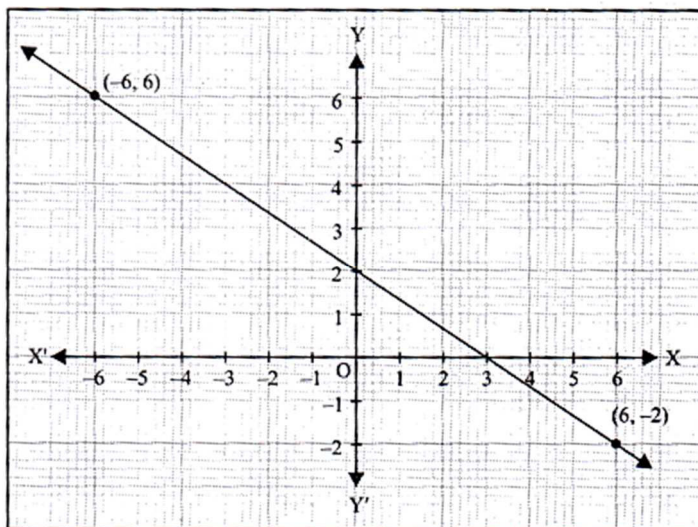
Write the linear equation.

Draw the graph using the values of x, y given in the above table. At what points the graph of the linear equation

(i) cuts the x-axis (ii) cuts the y-axis

Sol. The linear equation is $2x + 3y = 6$. Both the points (6, -2) and (-6, 6) satisfy the given linear equation.

Plot the points (-6, 6) and (6, -2) on a graph paper. Now join these two points and obtain a line. We see that the graph cuts the x-axis at (3, 0) and y-axis at (0, 2).



3. Draw the graph of the linear equation $3x + 4y = 6$. At what points, the graph cuts the x-axis and the y-axis.

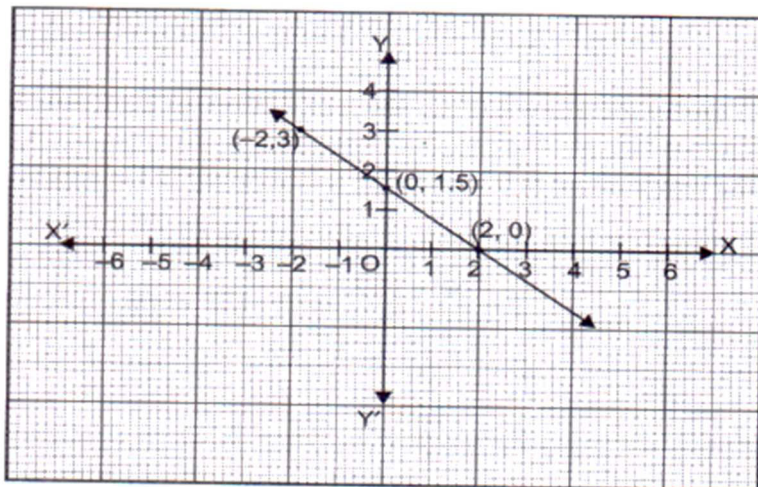
Sol. The solutions of the linear equation

$$3x + 4y = 6$$

Can be expressed in the form of a table as follows by writing the values of y below the corresponding value of x:

X	2	-2	0
y	0	3	1.5

Now plot the points (2, 0), (-2, 3) and (0, 1.5) on a graph paper. Now, join the points and obtain a line.



We see that the graph cuts the x-axis at (2, 0) and y-axis at (0, 1.5).

4. **The linear equation that converts Fahrenheit (F) to Celsius ($^{\circ}\text{C}$) is given by the relation:**

$$C = \frac{5F - 160}{9}$$

- (i) If the temperature is 86°F , what is the temperature in Celsius?
(ii) If the temperature is 35°C , what is the temperature in Fahrenheit?
(iii) If the temperature is 0°C what is the temperature in Fahrenheit and if the temperature is 0°F , what is the temperature in Celsius?
(iv) What is the numerical value of the temperature which is same in both the scales?

Sol. $C = \frac{5F - 160}{9}$

(i) Putting $F = 86^{\circ}$, we get $C = \frac{5(86) - 160}{9} = \frac{430 - 160}{9} = \frac{270}{9} = 30^{\circ}$

Hence, the temperature in Celsius is 30°C .

(ii) Putting $C = 35^{\circ}$, we get $35^{\circ} = \frac{5(F) - 160}{9} \Rightarrow 315^{\circ} = 5F - 160$

$$\Rightarrow 5F = 315 + 160 = 475$$

$$\therefore F = \frac{475}{5} = 95^{\circ}$$

Hence, the temperature in Fahrenheit is 95°F .

(iii) Putting $C = 0^\circ$, we get

$$0 = \frac{5F - 160}{9} \Rightarrow 0 = 5F - 160$$

$$\Rightarrow 5F = 160$$

$$\therefore F = \frac{160}{5} = 32^\circ$$

Now, putting $F = 0^\circ$, we get

$$C = \frac{5F - 160}{9} \Rightarrow C = \frac{5(0) - 160}{9} = \left(-\frac{160}{9}\right)^\circ$$

If the temperature is 0° C, the temperature in Fahrenheit is 32° and if the temperature is 0° F, then the temperature in Celsius is $\left(-\frac{160}{9}\right)^\circ$ C.

(iv) Putting $C = F$, in the given relation, we get

$$F = \frac{5F - 160}{9} \Rightarrow 9F = 5F - 160$$

$$\Rightarrow 4F = -160$$

$$\therefore F = \frac{-160}{4} = -40^\circ$$

Hence, the numerical value of the temperature which is same in both the scales is -40 .
The linear equation that converts Kelvin (x) to Fahrenheit (y) is given by the relation:

$$y = \frac{9}{5}(x - 273) + 32$$

- 5. If the temperature of a liquid can be measured in Kelvin units as x° K or in Fahrenheit units as y° F, the relation between the two systems of measurement of temperature is given by the linear equation**

$$y = \frac{9}{5}(x - 273) + 32$$

(i) Find the temperature of the liquid in Fahrenheit if the temperature of the liquid is 313° K.

(ii) If the temperature is 158° F, then find the temperature in Kelvin.

Sol. $y = \frac{9}{5}(x - 273) + 32$

(i) When the temperature of the liquid is $x = 313^\circ$ K

$$y = \frac{9}{5}(313 - 273) + 32 = \frac{9}{5} \times 40 + 32 = 72^\circ + 32^\circ = 104^\circ \text{ F}$$

(ii) When the temperature of the liquid is $y = 158^\circ$ F

$$158 = \frac{9}{5}(x - 273) + 32 \Rightarrow \frac{9}{5}(x - 273) = 158 - 32$$

$$\Rightarrow x - 273 = 126 \times \frac{5}{6} = 70$$

$$\Rightarrow x - 273 = 70 = 273 + 70 = 343^0 K$$

6. The force exerted to pull a cart is directly proportional to the acceleration produced in the body. Express the statement as a linear equation in two variables and draw the graph of the same by taking the constant mass equal to 6 kg. Read from the graph, the force required when the acceleration produced is (i) 5 m/sec², (ii) 6 m/sec².

Sol. We have $y \propto x \Rightarrow y = mx$

Where y denotes the force, x denotes the acceleration and m denotes the constant mass.

Taking $m = 6\text{kg}$, we get $y = 6x$

Now, we form a table as follows by writing the value of y below the corresponding value of x.

X	0	1	2
y	0	6	12

Plot the points (0, 0), (1, 6) and (2, 12) on a graph paper and join any two points and obtain a line.

