Class -VI Mathematics (Ex. 3.1) Questions

1.	Write	e all the fact	tors of the following	numbers:				
	(a) 2 ⁴	4	(b) 15	(c) 21	(d) 27			
	(e) 12	2	(f) 20	(g) 18	(h) 23			
	(i) 36	,)						
2.	Write	e first five n	nultiples of:					
	(a) 5		(b) 8	(c) 9				
3.	Match the items in column 1 with the items in column 2:							
	Column 1			Column 2				
	(i)	35	(a) Mı	ıltiple of 8				
	(ii)	15	(b) M	ultiple of 7				
	(iii)	16	(c) Mı	ıltiple of 70				
	(iv)	20	(d) Fa	ctor of 30				
	(v)	20	(e) Fa	ctor of 50				
4.	Find	all the mult	iples of 9 up to 100.					

Class -VI Mathematics (Ex. 3.1) Answers

1. (a)
$$24 = 1 \times 24 = 2 \times 12 = 3 \times 8 = 4 \times 6 = 6 \times 4$$

$$\therefore$$
 Factors of 24 = 1, 2, 3, 4, 6, 12, 24

(b)
$$15 = 1 \times 15 = 3 \times 5 = 5 \times 3$$

$$\therefore$$
 Factors of 15 = 1, 3, 5, 15

(c)
$$21 = 1 \times 21 = 3 \times 7 = 7 \times 3$$

$$\therefore$$
 Factors of 21 = 1, 3, 7, 21

(d)
$$27 = 1 \times 27 = 3 \times 9 = 9 \times 3$$

$$\therefore$$
 Factors of 27 = 1, 3, 9, 27

(e)
$$12 = 1 \times 12 = 2 \times 6 = 3 \times 4 = 4 \times 3$$

$$\therefore$$
 Factors of 12 = 1, 2, 3, 4, 6, 12

(f)
$$20 = 1 \times 20 = 2 \times 10 = 4 \times 5 = 5 \times 4$$

$$\therefore$$
 Factors of 20 = 1, 2, 4, 5, 10, 20

(g)
$$18 = 1 \times 18 = 2 \times 9 = 3 \times 6$$

$$\therefore$$
 Factors of 18 = 1, 2, 3, 6, 9, 18

(h)
$$23 = 1 \times 23$$

$$\therefore$$
 Factors of 23 = 1, 23

(i)
$$36 = 1 \times 36 = 2 \times 18 = 3 \times 12 = 4 \times 9 = 6 \times 6$$

$$\therefore$$
 Factors of 36 = 1, 2, 3, 4, 6, 9, 12, 18, 36

2. (a)
$$5 \times 1 = 5$$
, $5 \times 2 = 10$, $5 \times 3 = 15$, $5 \times 4 = 20$, $5 \times 5 = 25$

(b)
$$8 \times 1 = 8$$
, $8 \times 2 = 16$, $8 \times 3 = 24$, $8 \times 4 = 32$, $8 \times 5 = 40$

(c)
$$9 \times 1 = 9$$
, $9 \times 2 = 18$, $9 \times 3 = 27$, $9 \times 4 = 36$, $9 \times 5 = 45$

$$\therefore$$
 First five multiples of 9 are 9, 18, 27, 36, 45.

3. (i)
$$\rightarrow$$
 (b), (ii) \rightarrow (d), (iii) \rightarrow (a), (iv) \rightarrow (f), (v) \rightarrow (e)

Class -VI Mathematics (Ex. 3.2) Questions

1.	What is the sun							
	(a) Odd numbe							
2	(b) Even number							
2.		the following stateme						
		three odd numbers is						
	. ,	two odd numbers and t of three odd numbe		s even.				
				ave odd				
		umber is divided by 2 ımbers are odd.	z, the quotient is always	lys ouu.				
		pers do not have any	factors					
		prime numbers is alv						
	107	even prime number.	•					
		nbers are composite						
		t of two even number						
	() The product	cor two even mamber	s is arways even.					
3.	The numbers 1	3 and 31 are prime	numbers. Both thes	e numbers have same digits 1	and 3.			
	Find such pairs	of prime numbers up	o to 100.					
4.	Write down sep	parately the prime an	d composite number	s less than 20.				
5.	What is the gre	atest prime number l	etween 1 and 10?					
6.	Express the foll	owing as the sum of t	two odd numbers:					
	(a) 44	(b) 36	(c) 24	(d) 18				
7.	Give three pairs	s of prime numbers w	vhose difference is 2.					
		prime numbers whos		called twin primes.l				
8.	_	llowing numbers are		,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,				
	(a) 23	(b) 51	(c) 37	(d) 26				
9.		,		100 so that there is no prime r	number			
	between them.	•		•				
10.	Express each of	f the following numbe	ers as the sum of thre	e odd primes:				
	(a) 21	(b) 31	(c) 53	(d) 61				
11.	Write five pairs	s of prime numbers le	ss than 20 whose su	n is divisible by 5.				
	[Hint: $3 + 7 = 10$	0]						
12.	Fill in the blank	s:						
	(a) A number which has only two factors is called a							
	(b) A number w	hich has more than t	wo factors is called a	·•				
	(c) 1 neither	nor	-					
	• •	t prime number is						
		t composite number	is					
	(f) The smallest even number is .							

Class -VI Mathematics (Ex. 3.2) Answers

(a) The sum of any two odd numbers is an even number.

Example: 1 + 3 = 4, 3 + 5 = 8

(b) The sum of any two even numbers is an even number.

Example: 2 + 4 = 6, 6 + 8 = 14

- 2. (a) False
- (b) True
- (c) True
- (d) False
- (e) False
- (f) False

- (g) False
- (h) True
- (i) False
- (j) True
- 3. 17 and 71; 37 and 73; 79 and 97
- Prime numbers: 2, 3, 5, 7, 11, 13, 17, 19

Composite numbers: 4, 6, 8, 9, 10, 12, 14, 15, 16, 18

- 5. The greatest prime number between 1 and 10 is '7'.
- 6. (a) 3 + 41 = 44
- (b) 5 + 31 = 36
- (c) 7 + 17 = 24 (d) 7 + 11 = 18

- 7. 3 and 5;
- 5 and 7;
- 11 and 13
- 8. (a) 23 and (c) 37 are prime numbers.
- 90, 91, 92, 93, 94, 95, 96
- 10. (a) 21 = 3 + 7 + 11

(b) 31 = 3 + 11 + 17

(c) 53 = 13 + 17 + 23

(d) 61 = 19 + 29 + 13

- 11. 2 + 3 = 5;
- 7 + 13 = 20;
- 3 + 17 = 20;
- 2 + 13 = 15;
- 5 + 5 = 10

- 12. (a) Prime number
 - (b) Composite number
 - (c) Prime number and composite number
 - (d) 2
 - (e) 4
 - (f) 2

Class -VI Mathematics (Ex. 3.3) Questions

1. Using divisibility test, determine which of the following numbers are divisible by 2; by 3; by 4; by 5; by 8; by 9; by 10; by 11. (say yes or no)

Number		Divisible by							
128	Yes	No	Yes	No	No	Yes	No	No	No
990									
1586									
275									
6686									
639210									
429714									
2856									
3060									
406839									

	429714 2856					
	3060 406839					
2.	Using divisibility t	est, determine which	n of the following num	bers are divisibl	y by 4; by	8:
	(a) 572	(b) 726352	(c) 5500	(d) 6000		
	(e) 12159	(f) 14560	(g) 21084	(h) 317950	72	
	(i) 1700	(j) 2150				
3.	Using divisibility t	est, determine which	of the following num	bers are divisibl	e by 6:	
	(a) 297144	(b) 1258	(c) 4335	(d) 61233		
	(e) 901352	(f) 438750	(g) 1790184	(h) 12583		
	(i) 639210	(j) 17852				
4.	Using divisibility t	est, determine which	of the following num	bers are divisibl	e by 11:	
	(a) 5445	(b) 10824	(c) 7138965	(d) 701693	808	
	(e) 10000001	(f) 901153				
5.		et digit and the larg	est digit in the blanl divisibly by 3:	ks space of eac	h of the f	ollowing
	(a) 6724	(b) 4765	2			
6.	Write the smalles	t digit and the larg	est digit in the blanl	ks space of eac	h of the f	ollowing
	numbers so that th	ne number formed is	divisibly by 11:			
	(a) 92 38	9 (b) 8	9484			

Class -VI Mathematics (Ex. 3.3) Answers

1. Sol.

Number		Divisible by							
	2	3	4	5	6	8	9	10	11
128	Yes	No	Yes	No	No	Yes	No	No	No
990	Yes	Yes	No	Yes	Yes	No	Yes	Yes	Yes
1586	Yes	No	No	No	No	No	No	No	No
275	No	No	No	Yes	No	No	No	No	Yes
6686	Yes	No	No	No	No	No	No	No	No
639210	Yes	Yes	No	Yes	Yes	No	No	Yes	Yes
429714	Yes	Yes	No	No	Yes	No	Yes	No	No
2856	Yes	Yes	Yes	No	Yes	Yes	No	No	No
3060	Yes	Yes	Yes	Yes	Yes	No	Yes	Yes	No
406839	No	Yes	No						

2	(a) E72	Divisible by A as its last true disite and divisible by A	
Ζ.	1315/2	\rightarrow Divisible by 4 as its last two digits are divisible by 4.	

 \rightarrow Not divisible by 8 as its last three digits are not divisible by 8.

(b) $726352 \rightarrow$ Divisible by 4 as its last two digits are divisible by 4.

 \rightarrow Divisible by 8 as its last three digits are divisible by 8.

(c) 5500 \rightarrow Divisible by 4 as its last two digits are divisible by 4.

 \rightarrow Not divisible by 8 as its last three digits are not divisible by 8.

(d) $6000 \rightarrow \text{Divisible by 4 as its last two digits are 0}.$

 \rightarrow Divisible by 8 as its last three digits are 0.

(e) 12159 \rightarrow Not divisible by 4 and 8 as it is an odd number.

(f) 14560 \rightarrow Divisible by 4 as its last two digits are divisible by 4.

 \rightarrow Divisible by 8 as its last three digits are divisible by 8.

(g) 21084 \rightarrow Divisible by 4 as its last two digits are divisible by 4.

 \rightarrow Not divisible by 8 as its last three digits are not divisible by 8.

(h) 31795072 \rightarrow Divisible by 4 as its last two digits are divisible by 4.

 \rightarrow Divisible by 8 as its last three digits are divisible by 8.

(i) 1700 \rightarrow Divisible by 4 as its last two digits are 0.

 \rightarrow Not divisible by 8 as its last three digits are not divisible by 8.

(j) 5500 \rightarrow Not divisible by 4 as its last two digits are not divisible by 4.

 \rightarrow Not divisible by 8 as its last three digits are not divisible by 8.

3. (a) 297144 \rightarrow Divisible by 2 as its units place is an even number.

 \rightarrow Divisible by 3 as sum of its digits (= 27) is divisible by 3.

Since the number is divisible by both 2 and 3, therefore, it is also divisible by 6.

 \rightarrow Divisible by 3 as sum of its digits (= 15) is divisible by 3. Since the number is not divisible by both 2 and 3, therefore, it is not divisible by 6. (d) 61233 \rightarrow Not divisible by 2 as its units place is not an even number. \rightarrow Divisible by 3 as sum of its digits (= 15) is divisible by 3. Since the number is not divisible by both 2 and 3, therefore, it is not divisible by 6. (e) 901352 \rightarrow Divisible by 2 as its units place is an even number. \rightarrow Not divisible by 3 as sum of its digits (= 20) is not divisible by 3. Since the number is not divisible by both 2 and 3, therefore, it is not divisible by 6. \rightarrow Divisible by 2 as its units place is an even number. (f) 438750 \rightarrow Divisible by 3 as sum of its digits (= 27) is not divisible by 3. Since the number is divisible by both 2 and 3, therefore, it is divisible by 6. (g) 1790184 \rightarrow Divisible by 2 as its units place is an even number. \rightarrow Divisible by 3 as sum of its digits (= 30) is not divisible by 3. Since the number is divisible by both 2 and 3, therefore, it is divisible by 6. (h) 12583 \rightarrow Not divisible by 2 as its units place is not an even number. \rightarrow Not divisible by 3 as sum of its digits (= 19) is not divisible by 3. Since the number is not divisible by both 2 and 3, therefore, it is not divisible by 6. \rightarrow Divisible by 2 as its units place is an even number. (i) 639210 \rightarrow Divisible by 3 as sum of its digits (= 21) is not divisible by 3. Since the number is divisible by both 2 and 3, therefore, it is divisible by 6. (j) 17852 \rightarrow Divisible by 2 as its units place is an even number. \rightarrow Not divisible by 3 as sum of its digits (= 23) is not divisible by 3. Since the number is not divisible by both 2 and 3, therefore, it is not divisible by 6. (a) 5445 \rightarrow Sum of the digits at odd places = 4 + 5 = 9 4. \rightarrow Sum of the digits at even places = 4 + 5 = 9 \rightarrow Difference of both sums = 9 - 9 = 0 Since the difference is 0, therefore, the number is divisible by 11. (b) 10824 \rightarrow Sum of the digits at odd places = 4 + 8 + 1 = 13 \rightarrow Sum of the digits at even places = 2 + 0 = 2 \rightarrow Difference of both sums = 13 - 2 = 11 Since the difference is 11, therefore, the number is divisible by 11. \rightarrow Sum of the digits at odd places = 5 + 9 + 3 + 7 = 24 (c) 7138965 \rightarrow Sum of the digits at even places = 6 + 8 + 1 = 15 \rightarrow Difference of both sums = 24 - 15 = 9 Since the difference is neither 0 nor 11, therefore, the number is not divisible by 11. (d) $70169308 \rightarrow \text{Sum of the digits at odd places} = 8 + 3 + 6 + 0 = 17$

 \rightarrow Divisible by 2 as its units place is an even number.

Since the number is not divisible by both 2 and 3, therefore, it is not divisible by 6.

 \rightarrow Not divisible by 2 as its units place is not an even number.

 \rightarrow Not divisible by 3 as sum of its digits (= 16) is not divisible by 3.

(b) 1258

(c) 4335

- \rightarrow Sum of the digits at even places = 0 + 9 + 1 + 7 = 17
- \rightarrow Difference of both sums = 17 17 = 0

Since the difference is 0, therefore, the number is divisible by 11.

- (e) $10000001 \rightarrow \text{Sum of the digits at odd places} = 1 + 0 + 0 + 0 = 1$
 - \rightarrow Sum of the digits at even places = 0 + 0 + 0 + 1 = 1
 - \rightarrow Difference of both sums = 1 1 = 0

Since the difference is 0, therefore, the number is divisible by 11.

- (f) 901153 \rightarrow Sum of the digits at odd places = 3 + 1 + 0 = 4
 - \rightarrow Sum of the digits at even places = 5 + 1 + 9 = 15
 - \rightarrow Difference of both sums = 15 4 = 11

Since the difference is 11, therefore, the number is divisible by 11.

5. (a) We know that a number is divisible by 3 if the sum of all digits is divisible by 3.

Therefore, Smallest digit: 2

 \rightarrow <u>26724 = 2 + 6 + 7 + 2 + 4 = 21</u>

Largest digit: 8

- \rightarrow 86724 = 8 + 6 + 7 + 2 + 4 = 27
- (b) We know that a number is divisible by 3 if the sum of all digits is divisible by 3.

Therefore, Smallest digit: 0

 \rightarrow 4765<u>0</u>2 = 4 + 7 + 6 + 5 + 0 + 2 = 24

Largest digit: 9

- \rightarrow 476592 = 4 + 7 + 6 + 5 + 0 + 2 = 33
- 6. (a) We know that a number is divisible by 11 if the difference of the sum of the digits at odd places and that of even places should be either 0 or 11.

Therefore, 92<u>8</u>389

- \rightarrow Odd places = 9 + 8 + 8 = 25
 - Even places = 2 + 3 + 9 = 14
 - Difference = 25 14 = 11
- (b) We know that a number is divisible by 11 if the difference of the sum of the digits at odd places and that of even places should be either 0 or 11.

Therefore, 8<u>6</u>9484

- \rightarrow Odd places = 8 + 9 + 8 = 25
 - Even places = 6 + 4 + 4 = 14
 - Difference = 25 14 = 11

Class -VI Mathematics (Ex. 3.4) Questions

1. Find the common factors of:

(a) 20 and 28

(b) 15 and 25

(c) 35 and 50

(d) 56 and 120

2. Find the common factors of:

(a) 4, 8 and 12

(b) 5, 15 and 25

3. Find the first three common multiples of:

(a) 6 and 8

(b) 12 and 18

4. Write all the numbers less than 100 which are common multiples of 3 and 4.

5. Which of the following numbers are co-prime:

(a) 18 and 35

(b) 15 and 37

(c) 30 and 415

(d) 17 and 68

(e) 216 and 215

(f) 81 and 16

6. A number is divisible by both 5 and 12. By which other number will that number be always divisible?

7. A number is divisible by 12. By what other numbers will that number be divisible?

Class -VI Mathematics (Ex. 3.4) Answers

- 1. (a) Factors of 20 = 1, 2, 4, 5, 10, 20 Factors of 28 = 1, 2, 4, 7, 14, 28 Common factors = 1, 2, 4
 - (b) Factors of 15 = 1, 3, 5, 15 Factors of 25 = 1, 5, 25 Common factors = 1, 5
 - (c) Factors of 35 = 1, 5, 7, 35 Factors of 50 = 1, 2, 5, 10, 25, 50 Common factors = 1, 5
 - (d) Factors of 56 = 1, 2, 4, 7, 8, 14, 28, 56 Factors of 120 = 1, 2, 3, 4, 5, 6, 8, 10, 12, 15, 20, 24, 30, 60, 120 Common factors = 1, 2, 4, 8
- 2. (a) Factors of 4 = 1, 2, 4
 Factors of 8 = 1, 2, 4, 8
 Factors of 12 = 1, 2, 3, 4, 6, 12
 Common factors of 4, 8 and 12 = 1, 2, 4
 - (b) Factors of 5 = 1, 5 Factors of 15 = 1, 3, 5, 15 Factors of 25 = 1, 5, 25 Common factors of 5, 15 and 25 = 1, 5
- 4. Multiple of 3 = 3, 6, 9, 12, 15, 18, 21, 24, 27, 30, 33, 36, 39, 42, 45, 48, 51, 54, 57, 60, 63, 66, 69, 72, 75, 78, 81, 84, 87, 90, 93, 96, 99

 Multiple of 4 = 4, 8, 12, 16, 20, 24, 28, 32, 36, 40, 44, 48, 52, 56, 60, 64, 68, 72, 76, 80, 84, 88, 92, 96, 100

 Common multiples of 3 and 4 = 12, 24, 36, 48, 60, 72, 84, 96
- 5. (a) Factors of 18 = 1, 2, 3, 6, 9, 18 Factors of 35 = 1, 5, 7, 35

Common factor = 1

Since, both have only one common factor, i.e., 1, therefore, they are co-prime numbers.

(b) Factors of 15 = 1, 3, 5, 15

Factors of 37 = 1,37

Common factor = 1

Since, both have only one common factor, i.e., 1, therefore, they are co-prime numbers.

(c) Factors of 30 = 1, 2, 3, 5, 6, 15, 30

Factors of 415 = 1, 5,, 83, 415

Common factor = 1, 5

Since, both have more than one common factor, therefore, they are not co-prime numbers.

(d) Factors of 17 = 1, 17

Factors of 68 = 1, 2, 4, 17, 34, 86

Common factor = 1, 17

Since, both have more than one common factor, therefore, they are not co-prime numbers.

(e) Factors of 216 = 1, 2, 3, 4, 6, 8, 36, 72, 108, 216

Factors of 215 = 1, 5, 43, 215

Common factor = 1

Since, both have only one common factor, i.e., 1, therefore, they are co-prime numbers.

(f) Factors of 81 = 1, 3, 9, 27, 81

Factors of 16 = 1, 2, 4, 8, 16

Common factor = 1

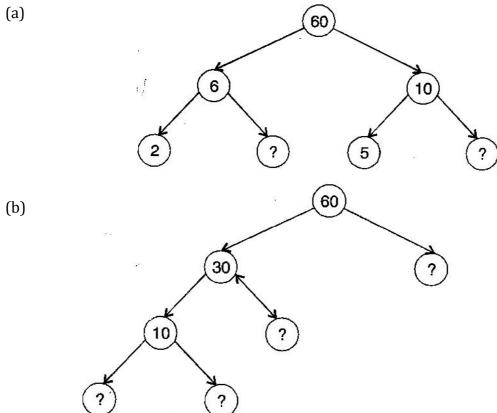
Since, both have only one common factor, i.e., 1, therefore, they are co-prime numbers.

- 6. $5 \times 12 = 60$. The number must be divisible by 60.
- 7. Factors of 12 are 1, 2, 3, 4, 6, 12.

Therefore, the number also be divisible by 1,2,3 4 and 6.

Class -VI Mathematics (Ex. 3.5) Questions

- 1. Which of the following statements are true:
 - (a) If a number is divisible by 3, it must be divisible by 9.
 - (b) If a number is divisible by 9, it must be divisible by 3.
 - (c) If a number is divisible by 18, it must be divisible by both 3 and 6.
 - (d) If a number is divisible by 9 and 10 both, then it must be divisible by 90.
 - (e) If two numbers are co-primes, at least one of them must be prime.
 - (f) All numbers which are divisible by 4 must also by divisible by 8.
 - (g) All numbers which are divisible by 8 must also by divisible by 4.
 - (h) If a number is exactly divides two numbers separately, it must exactly divide their sum.
 - (i) If a number is exactly divides the sum of two numbers, it must exactly divide the two numbers separately.
- 2. Here are two different factor trees for 60. Write the missing numbers.



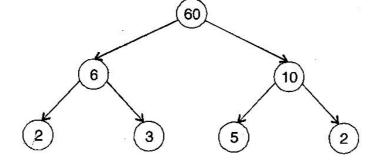
- 3. Which factors are not included in the prime factorization of a composite number?
- 4. Write the greatest 4-digit number and express it in terms of its prime factors.
- 5. Write the smallest 5-digit number and express it in terms of its prime factors.

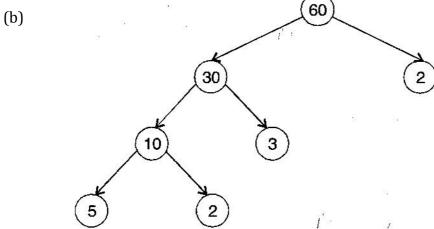
- 6. Find all the prime factors of 1729 and arrange them in ascending order. Now state the relation, if any, between, two consecutive prime numbers.
- 7. The product of three consecutive numbers is always divisible by 6. Verify this statement with the help of some examples.
- 8. The sum of three consecutive numbers is always divisible by 4. Verify this statement with the help of some examples.
- 9. In which of the following expressions, prime factorization has been done:
 - (a) $24 = 2 \times 3 \times 4$
 - (b) $56 = 7 \times 2 \times 2 \times 2$
 - (c) $70 = 2 \times 5 \times 7$
 - (d) $54 = 2 \times 3 \times 9$
- 10. Determine if 25110 is divisible by 45. [Hint: 5 and 9 are co-prime numbers. Test the divisibility of the number by 5 and 9.]
- 11. 18 is divisible by both 2 and 3. It is also divisible by $2 \times 3 = 6$. Similarly, a number is divisible by 4 and 6. Can we say that the number must be divisible by $4 \times 6 = 24$? If not, give an example to justify your answer.
- 12. I am the smallest number, having four different prime factors. Can you find me?

Class -VI Mathematics (Ex. 3.5) **Answers**

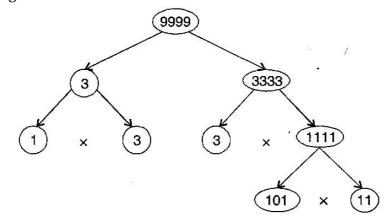
- Statements (b), (c), (d), (g) and (h) are true. 1.
- 2. Sol.

(a)



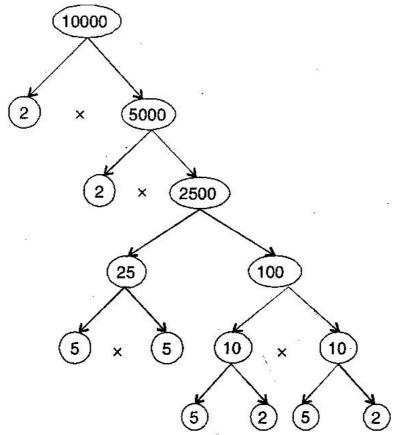


- 3. 1
- The greatest four digit number is 9999.



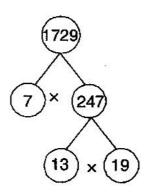
The prime factors of 9999 are $3 \times 3 \times 11 \times 101$.

5. The smallest five digit number is 10000.



The prime factors of 10000 are 2 x 2 x 2 x 2 x 5 x 5 x 5 x 5.

6. Sol.



Prime factors of 1729 are $7 \times 13 \times 19$.

The difference of two consecutive prime factors is 6.

7. Among the three consecutive numbers, there must be one even number and one multiple of 3. Thus, the product must be multiple of 6.

Example:

- (i) $2 \times 3 \times 4 = 24$
- (ii) $4 \times 5 \times 6 = 120$

8. 3 + 5 = 8 and 8 is divisible by 4.

5 + 7 = 12 and 12 is divisible by 4.

7 + 9 = 16 and 16 is divisible by 4.

9 + 11 = 20 and 20 is divisible by 4.

- 9. In expressions (b) and (c), prime factorization has been done.
- 10. The prime factorization of $45 = 5 \times 9$

25110 is divisible by 5 as '0' is at its unit place.

25110 is divisible by 9 as sum of digits is divisible by 9.

Therefore, the number must be divisible by $5 \times 9 = 45$

- 11. No. Number 12 is divisible by both 6 and 4 but 12 is not divisible by 24.
- 12. $2 \times 3 \times 5 \times 7 = 210$

Class -VI Mathematics (Ex. 3.6) Questions

- 1. Find the H.C.F. of the following numbers:
 - (a) 18, 48

- (c) 18, 60
- (e) 36, 84
- (g) 70, 105, 175
- (i) 18, 54, 81

- (b) 30, 42
- (d) 27, 63
- (f) 34, 102
- (h) 91, 112, 49
- (j) 12, 45, 75
- 2. What is the H.C.F. of two consecutive:
 - (a) numbers?
 - (b) even numbers?
 - (c) odd numbers?
- 3. H.C.F. of co-prime numbers 4 and 15 was found as follows by factorization: $4 = 2 \times 2$ and $15 = 3 \times 5$ since there is no common prime factor, so H.C.F. of 4 and 15 is 0. Is the answer correct? If not, what is the correct H.C.F.?

Class -VI Mathematics (Ex. 3.6) Answers

- 1. (a) Factors of $18 = 2 \times 3 \times 3$ Factors of $48 = 2 \times 2 \times 2 \times 2 \times 3$ H.C.F. $(18, 48) = 2 \times 3 = 6$
 - (c) Factors of $18 = 2 \times 3 \times 3$ Factors of $60 = 2 \times 2 \times 3 \times 5$ H.C.F. $(18, 60) = 2 \times 3 = 6$
 - (e) Factors of 36 = 2 x 2 x 3 x 3 Factors of 84 = 2 x 2 x 3 x 7 H.C.F. (36, 84) = 2 x 2 x 3 = 12
 - (g) Factors of 70 = 2 x 5 x 7 Factors of 105 = 3 x 5 x 7 Factors of 175 = 5 x 5 x 7 H.C.F. = 5 x 7 = 35
 - (i) Factors of 18 = 2 x 3 x 3 Factors of 54 = 2 x 3 x 3 x 3 Factors of 81 = 3 x 3 x 3 x 3 H.C.F. = 3 x 3 = 9

- (b) Factors of $30 = 2 \times 3 \times 5$ Factors of $42 = 2 \times 3 \times 7$ H.C.F. $(30, 42) = 2 \times 3 = 6$
- (d) Factors of $27 = 3 \times 3 \times 3$ Factors of $63 = 3 \times 3 \times 7$ H.C.F. $(27, 63) = 3 \times 3 = 9$
- (f) Factors of 34 = 2 x 17 Factors of 102 = 2 x 3 x 17 H.C.F. (34, 102) = 2 x 17 = 34
- (h) Factors of 91 = 7 x 13 Factors of 112 = 2 x 2 x 2 x 2 x 7 Factors of 49 = 7 x 7 H.C.F. = 1 x 7 = 7
- (j) Factors of 12 = 2 x 2 x 3 Factors of 45 = 3 x 3 x 5 Factors of 75 = 3 x 5 x 5 H.C.F. = 1 x 3 = 3
- 2. (a) H.C.F. of two consecutive numbers be 1.
 - (b) H.C.F. of two consecutive even numbers be 2.
 - (c) H.C.F. of two consecutive odd numbers be 1.
- 3. No. The correct H.C.F. is 1.

Class -VI Mathematics (Ex. 3.7) Questions

- 1. Renu purchases two bags of fertilizer of weights 75 kg and 69 kg. Find the maximum value of weight which can measure the weight of the fertilizer exact number of times.
- 2. Three boys step off together from the same spot. Their steps measure 63 cm, 70 cm and 77 cm respectively. What is the maximum distance each should cover so that all can cover the distance in complete steps?
- 3. The length, breadth and height of a room are 825 cm, 675 cm and 450 cm respectively. Find the longest tape which can measure the three dimensions of the room exactly.
- 4. Determine the smallest 3-digit number which is exactly divisible by 6, 8 and 12.
- 5. Determine the largest 3-digit number which is exactly divisible by 8, 10 and 12.
- 6. The traffic lights at three different road crossings change after every 48 seconds, 72 seconds and 108 seconds respectively. If they change simultaneously at 7 a.m. at what time will they change simultaneously again?
- 7. Three tankers contain 403 liters and 465 liters of diesel respectively. Find the maximum capacity of a container that can measure the diesel of three containers exact number of times.
- 8. Find the least number which when divided by 6, 15 and 18, leave remainder 5 in each case.
- 9. Find the smallest 4-digit number which is divisible by 18, 24 and 32.
- 10. Find the L.C.M. of the following numbers:(a) 9 and 4 (b) 12 and 5 (c) 6 and 5 (d) 15 and 4Observe a common property in the obtained L.C.Ms. Is L.C.M. the product of two numbers in each case?

11.	Find the L.C.M. of the f	ollowing numbers in	which one number is	the factor of other:
	(a) 5, 20	(b) 6, 18	(c) 12, 48	(d) 9, 45
	What do vou observe i	n the result obtained	?	

Class -VI Mathematics (Ex. 3.7) Answers

For finding maximum weight, we have to find H.C.F. of 75 and 69.

Factors of $75 = 3 \times 5 \times 5$

Factors of $69 = 3 \times 69$

H.C.F. = 3

Therefore the required weight is 3 kg.

2. For finding minimum distance, we have to find L.C.M of 63, 70, 77.

L.C.M. of 63, 70 and $77 = 7 \times 9 \times 10 \times 11 = 6930 \text{ cm}$.

Therefore, the minimum distance is 6930 cm.

_ 7	63, 70, 77
9	9, 10, 11
10	1, 10, 11
11	1, 1, 11
	1, 1, 1

The measurement of longest tape = H.C.F. of 825 cm, 675 cm and 450 cm.

Factors of $825 = 3 \times 5 \times 5 \times 11$

Factors of $675 = 3 \times 5 \times 5 \times 3 \times 3$

Factors of $450 = 2 \times 3 \times 3 \times 5 \times 5$

H.C.F. = $3 \times 5 \times 5 = 75 \text{ cm}$

Therefore, the longest tape is 75 cm.

4. L.C.M. of 6, 8 and $12 = 2 \times 2 \times 2 \times 3 = 24$

The smallest 3-digit number = 100

To find the number, we have to divide 100 by 24

	4
24)	24
:	<u>-24</u>
	4

24) 24	 3	3, .
_24		1, 1
<u>-24</u>		
4		

Therefore, the required number = 100 + (24 - 4) = 120.

5. L.C.M. of 8, 10, $12 = 2 \times 2 \times 2 \times 3 \times 5 = 120$

The largest three digit number = 999

Now,
$$120) 999$$
 -960 39

Therefore, the required number = 999 - 39 = 960

8, 10, 12					
4, 5,	6				
2, 5,	3				
1, 5,	3				
1, 5,	1				
1, 1,	1				
	4, 5, 2, 5,				

6, 8, 12

6. L.C.M. of 48, 72, $108 = 2 \times 2 \times 2 \times 2 \times 3 \times 3 \times 3 = 432$ sec.

After 432 seconds, the lights change simultaneously.

432 second = 7 minutes 12 seconds

Therefore the time = 7 a.m. + 7 minutes 12 seconds

7. The maximum capacity of container = H.C.F. (403, 434, 465)

Factors of $403 = 13 \times 31$

Factors of $434 = 2 \times 7 \times 31$

Factors of $465 = 3 \times 5 \times 31$

H.C.F. = 31

Therefore, 31 liters of container is required to measure the quantity.

8. L.C.M. of 6, 15 and $18 = 2 \times 3 \times 3 \times 5 = 90$

Therefore the required number = 90 + 5 = 95

2	6, 15, 1	18
3	3, 15,	9
3	1, 5,	3
5	1, 5,	1
	1, 1,	1

2

2

2

3

5

8, 10, 12

6

3

4, 5,

2, 5,

1, 5,

1, 1,

9. L.C.M. of 18, 24 and $32 = 2 \times 2 \times 2 \times 2 \times 2 \times 3 \times 3 = 288$

The smallest four-digit number = 1000

Now,
$$288) 1000 \\ -864 \\ \hline 136$$

Therefore, the required number is 1000 + (288 - 136) = 1152.

2 18, 24, 32 2 9, 12, 16 2 9, 6, 8 2 2 9, 3, 2 3 3, 1 3 3, 1, 1, 1

2

10. (a) L.C.M. of 9 and 4

$$= 2 \times 2 \times 3 \times 3 = 36$$

(b) L.C.M. of 12 and 5 = $2 \times 2 \times 3 \times 5 = 60$

2	9, 2
3	9, 1
3	3, 1
	1, 1
2	12, 5
2	6, 5
3	3, 5
5	1, 5
	1, 1

9, 4

(c) L.C.M. of 6 and 5		
$= 2 \times 3 \times 5 = 30$	2	6, 5
	3	6, 5 3, 5
	5	1, 5
		1, 5 1, 1
(d) L.C.M. of 15 and 4		
$= 2 \times 2 \times 3 \times 5 = 60$		15, 4
	2	15, 2
Yes, the L.C.M. is equal to the product of two numbers in each case.		15, 1
And L.C.M. is also the multiple of 3.		5, 1
		5, 1 1, 1
11. (a) L.C.M. of 5 and 20		
$= 2 \times 2 \times 5 = 20$	2	5, 20
	2	5, 10
	5	5, 5
		1, 1
(b) L.C.M. of 6 and 18	<u> </u>	
$2 \times 3 \times 3 = 18$	2	6, 18
	3	3, 9
	3	1, 3
		1, 3 1, 1
(c) L.C.M. of 12 and 48		
2 x 2 x 2 x 2 x 3 = 48	2	12, 48
	2	6, 24
	2	3, 12
	2	3, 6
	3	3, 3
		1, 1
(d) L.C.M. of 9 and 45		
$= 3 \times 3 \times 5 = 45$	3	9, 45
	3	3, 15
	5	1, 5
		1, 1

From these all cases, we can conclude that if the smallest number if the factor of largest number, then the L.C.M. of these two numbers is equal to that of larger number.