(i) 
$$\frac{9\pi}{5}$$

We have,

$$1^c = \left\{\frac{180}{\pi}\right\}^0$$

Now,

$$\left(\frac{9\pi}{5} \times \frac{180}{\pi}\right)^0$$
$$= 324^\circ$$

(ii) 
$$\frac{-5\pi}{6}$$

We have,

$$1^c = \left(\frac{180}{\pi}\right)^0$$

Now,

$$\left(\frac{-5\pi}{6}\right)^c = \left(\frac{-5\pi}{6} \times \frac{180}{\pi}\right)^0 = -150^\circ$$

(iii) 
$$\left(\frac{18\pi}{5}\right)^c$$

We have,

$$1^c = \left(\frac{180}{\pi}\right)^0$$

Now,

$$\left(\frac{18\pi}{5}\right)^c = \left(\frac{18\pi}{5} \times \frac{180}{\pi}\right)^0$$
$$= 648^\circ$$

(iv) We have,

$$1^c = \left(\frac{180}{\pi}\right)^0$$

Now,

$$(-3)^{c} = \left(-3 \times \frac{180}{\pi}\right)^{0}$$

$$= \left(\frac{180}{22} \times 7 \times -3\right)^{0}$$

$$= \left(-171 \frac{9}{11}\right)^{0}$$

$$= -171^{0} \left(\frac{9}{11} \times 60\right)^{1}$$

$$= -171^{0}49^{1}5^{11}$$

(v) We have,

$$\pi$$
 radians =  $180^{\circ}$ 

$$1^c = \left(\frac{180}{\pi}\right)^0$$

Now,

$$(11)^c = \left(11 \times \frac{180}{\pi}\right)^0$$
$$= \left(11 \times 180 \times \frac{7}{22}\right)^0$$
$$= 630^0$$

(vi) We have,

$$\pi$$
 radians = 180 $^{0}$ 

$$1^e = \left(\frac{180}{\pi}\right)^0$$

Now,

$$1^{e} = \left(1 \times \frac{180}{\pi}\right)^{0}$$

$$= 1 \times \frac{180 \times 7}{22}$$

$$= 57^{0} \left(\frac{3}{11} \times 60\right)$$

$$= 57^{0} 16^{1} \left(\frac{4}{11} \times 60\right)^{11}$$

$$= 57^{0} 16^{1} 21^{11}$$

We have,

$$1^{\circ} = \left(\frac{\pi}{180}\right)^{c}$$

Nοw,

$$300^{\circ} = 300 \times \frac{\pi}{180} = \frac{5\pi}{3}$$

We have,

$$1^{\circ} = \left(\frac{\pi}{180}\right)^{\circ}$$

Now,

$$35^{\circ} = 35 \times \frac{\pi}{180} = \frac{7\pi}{36}$$

We have,

$$180^\circ = \pi^c$$

$$1^{\circ} = \left(\frac{\pi}{100}\right)^{\circ}$$

Now,

$$-56^{\circ} = -56 \times \frac{\pi}{180} = \frac{-14\pi}{45}$$

We have,

$$1^\circ = \left(\frac{\pi}{180}\right)^c$$

Now,

$$135^{\circ} = 135 \times \frac{\pi}{180} = \frac{3\pi}{4}$$

We have,

$$180^\circ=\pi^c$$

$$1^{\circ} = \left(\frac{\pi}{180}\right)^{c}$$

New,

$$-300^{\circ} = -300 \times \frac{\pi}{180} = \frac{-5\pi}{3}$$

(vi)  $7^{\circ}30^{1}$ 

We have,

$$180^{\circ} = x^{c}$$

$$1^{\circ} = \left(\frac{\pi}{180}\right)^{\circ}$$

$$7^{\circ} 30^{1} = \left(7 \times \frac{\pi}{180}\right)^{\circ} \times \left(\frac{30}{60}\right)^{0}$$

$$= \left(7\frac{1}{2}\right)^{0} \times \left(\frac{\pi}{180}\right)^{\circ}$$

$$= \left(\frac{15}{2} \times \frac{\pi}{180}\right)^{\circ}$$

(vii) 125°00<sup>1</sup>

We have,

$$\therefore 1^{\circ} = \left(\frac{\pi}{180}\right)^{c}$$

$$125^{\circ}30^{1} = 125^{\circ} \left(\frac{30}{60}\right)^{0}$$

$$= \left(125\frac{1}{2}\right)^{0}$$

$$= \left(\frac{251}{2} \times \frac{\pi}{180}\right)^{c} = \frac{251\pi}{360}$$

$$(viii) = 47°30^1$$

We have,

$$1^{\circ} = \left(\frac{\pi}{180}\right)^{\circ}$$

$$-47^{\circ}30^{\circ} = -47^{\circ}\left(\frac{30}{60}\right)^{\circ}$$

$$= \left(-47\frac{1}{2}\right)^{\circ}$$

$$= \left(\frac{-95}{2}\right)^{\circ}$$

$$= \left(\frac{-95}{2} \times \frac{\pi}{180}\right)^{c}$$
$$= \frac{-19\pi}{72}$$

Let  $\theta_1$  and  $\theta_2$  be two acute angles of a right angled triangle.

difference of acute angles

$$\theta_1 - \theta_2 = \frac{2\pi}{5}$$
 radians

in a right angled triangle, 100

$$\theta_1 + \theta_2 = \frac{\pi}{2}$$

$$\theta_1 - \theta_2 = \frac{2\pi}{5}$$

$$\theta_1 + \theta_2 = \frac{\pi}{2}$$

On solving

$$2\theta_1 = \frac{2\pi}{5} + \frac{\pi}{2}$$

$$\theta_1 = \frac{9\pi}{20}$$

From equation (ii)

$$\theta_2 = \frac{\pi}{20}$$

So angles in degrees

$$\theta_1 = \frac{9\pi}{20} \times \frac{180}{\pi} = 81^\circ$$

and 
$$\theta_2 = \frac{\pi}{20} \times \frac{180}{\pi} = 9^\circ$$

Let  $\theta_1$  and  $\theta_2$  and  $\theta_3$  be the angle or triangle.

$$\theta_1 = \frac{2}{3}x$$
 gradiants

$$\theta_2 = \frac{3}{2}x$$
 degrees and

$$\theta_3 = \frac{\pi x}{75} x$$
 radians

Now,

we have to express all the angles in degrees

$$\theta_1 = \left(\frac{3}{2} \times \times \frac{90}{100}\right)^0$$
$$= \frac{3}{5} \times$$

$$\left[1g = \frac{90}{100} \text{ degree}\right]$$

$$\theta_2 = \frac{3}{2}x^0$$

$$\theta_2 = \frac{\pi \times}{75} \times \frac{180}{\pi} = \frac{12 \times}{5}$$

By angleslam property,

$$\theta_1 + \theta_2 + \theta_3 = 180^\circ$$

$$\therefore \frac{3}{5}x^{\circ} + \frac{3}{2}x^{0} + \frac{12x}{5} = 180^{\circ}$$

$$\Rightarrow \frac{9}{2}x^0 = 180^0$$

$$\therefore \ \theta_1 = 24^0, \ \theta_2 = 60^0, \ \theta_3 = 96^0$$

General formula for interior angles of polygon with n side

$$= \left(\frac{2n-4}{n}\right) \times 90^{\circ}$$

(i) Pentagon has 5 sides

: magnitude of the interior angle

$$= \frac{2 \times 5 - 4}{5} \times 90^{\circ}$$
$$= \frac{6}{5} \times 90 = 180^{\circ}$$

Now,

 $1^c = \frac{180}{s}$  And each angle of Pentagon

$$= \frac{2 \times 5 - 4}{5} \times \frac{\pi}{2}$$
$$= \left(\frac{3\pi}{5}\right)^{c}$$

108°, 
$$\left(\frac{3\pi}{5}\right)^c$$

(ii) Octagon

: each angle = 
$$\frac{2 \times 8 - 4}{8} \times 90^{\circ}$$
  
= 135°

Again,

each angle = 
$$\frac{2 \times 8 - 4}{8} \times \frac{\pi}{2}$$
  
=  $\left(\frac{3\pi}{4}\right)^{c}$ 

1350 
$$\left(\frac{3\pi}{4}\right)$$

(iii) Heptagon

$$n = 7$$

: each angle = 
$$\frac{2 \times 7 - 4}{7} \times 90^{\circ}$$
  
=  $\frac{10}{7} \times 90^{\circ}$   
=  $\frac{900^{\circ}}{7}$ 

Again,

each angle = 
$$\frac{2 \times 7 - 4}{7} \times \frac{\pi}{2}$$
  
=  $\frac{10}{7} \times \frac{\pi}{2}$   
=  $\left(\frac{5\pi}{7}\right)^{c}$ 

$$128^{0}34^{1}17^{11}, \left(\frac{5\pi}{7}\right)^{c}$$

### (iv) Duodecagon

$$n = 12$$

each angle = 
$$\frac{2 \times 12 - 4}{12} \times 90^{\circ}$$
  
=  $\frac{20}{12} \times 90^{\circ}$   
=  $150^{\circ}$ 

Agian,

each angle = 
$$\frac{2 \times 12 - 4}{12} \times \frac{\pi}{2}$$
  
=  $\frac{20}{12} \times \frac{\pi}{2}$   
=  $\left(\frac{5\pi}{6}\right)^{c}$ 

$$150^{\circ}$$
,  $\left(\frac{5\pi}{6}\right)^{\circ}$ 

Let the angles in degrees be a-3d, a-d, a+d, a+3dThen,

sum of the angles = 3600

$$a = 90^{\circ}$$

Also,

greatest angle = 1200

$$a + 3d = 120^{\circ}$$

$$\Rightarrow$$
 90° + 3d = 120°

$$\Rightarrow$$
 3d = 30<sup>0</sup>

$$\Rightarrow$$
  $d = 10^{\circ}$ 

Hence, angles in degrees

and in radians, we know that

$$1^0 = \left(\frac{\pi}{180}\right)^c$$

$$\therefore \qquad 60 \times \frac{\pi}{180} = \frac{\pi}{3} \,, \ 80 \times \frac{\pi}{180} = \frac{4\pi}{9} \,,$$

$$100 \times \frac{\pi}{180} = \frac{5\pi}{9}$$
 and  $120 \times \frac{\pi}{180} = \frac{2\pi}{3}$ 

$$\frac{\pi}{3}$$
,  $\frac{4\pi}{9}$ ,  $\frac{5\pi}{9}$ ,  $\frac{2\pi}{3}$ 

Let A, B & C be the angles of triangle ABC. We are given that A, B & C are in A.P.

$$\therefore$$
 Let  $A = a - d$ ,  $B = a$  and  $C = a + d$ 

According to the question,

$$A + B + C = 180^{0}$$

[By angle sum property]

$$a-d+a+a+d=180^0$$

$$\Rightarrow 3a = 180^{\circ} \Rightarrow a = 60^{\circ}$$

---

Again,

$$\frac{\text{least angle}}{\text{mean angle}} = \frac{1}{120^0}$$

$$\Rightarrow \frac{a-d}{a} = \frac{1}{120}$$

$$\Rightarrow \qquad d = \frac{119a}{120}$$

$$\Rightarrow d = \frac{119}{120} \times 60^{0}$$

$$= \left(\frac{119}{2}\right)^{0}$$

$$= \frac{119}{2} \times \frac{\pi}{180} = \frac{119\pi}{360} \text{ radians}$$

Now,

$$1^0 = \frac{\pi}{180} \text{ radians}$$

$$B = a = 60^0 = \frac{\pi}{3} \text{ radians}$$

$$A = a - d = \frac{\pi}{3} - \frac{119\pi}{360} = \frac{\pi}{360}$$
 radians

$$C = a + d = \frac{\pi}{3} + \frac{119\pi}{360} = \frac{239\pi}{360}$$
 radians.

Let n & m be the number of sides in two regular polygon respectively.

We know that each angle of n-sided regular polygon is  $\frac{(2n-4)}{n}$  right angles.

Now,

According to the question,

$$\frac{\left(\frac{2n-4}{n}\right) \times 90^{0}}{\left(\frac{2m-4}{m}\right) \times 90^{0}} = \frac{3}{2}$$

$$\frac{(2n-4)m}{(2m-4)n} = \frac{3}{2}$$
---(

Also,

$$n = 2m$$
 ——(ii) [given]

Put(ii)in(i), we get

$$\frac{(4m-4)m}{(2m-4)2m} = \frac{3}{2}$$

$$\Rightarrow 4m-4=6m-12$$

$$\Rightarrow 2m=8$$

$$\therefore m=4$$

From (ii)

$$n = 2m$$
$$= 2 \times 4 = 8$$

$$n = 8, m = 4$$

According to the question,

So, 
$$A + B + C = 180^{\circ}$$

$$\Rightarrow a-d+a+a+d=180^0$$

$$\Rightarrow 3a = 180^{\circ} \Rightarrow a = 60^{\circ}$$

Also,

greatest angle in 5 times the least

$$a+d=5(a-d)$$

$$\Rightarrow d = \frac{2}{3}a$$

$$\Rightarrow d = \frac{2}{3} \times 60 = 40^{\circ}$$

$$A = a - d = 20^{\circ}$$

$$B = a = 60^{\circ}$$

$$C = a + d = 100^{0}$$

$$1^0 = \left(\frac{\pi}{180^0}\right) \text{ radians}$$

$$A = 20 \times \frac{\pi}{180} = \frac{\pi}{9}$$

$$\beta=60\times\frac{\pi}{180}=\frac{\pi}{3}$$

$$C=100\times\frac{\pi}{180}=\frac{5\pi}{9}$$

Thus,

$$A = \frac{\pi}{9}$$
,  $B = \frac{\pi}{3}$ ,  $C = \frac{5\pi}{9}$ 

Let n and m be the number of sides in two regular polygon respectively.

We know that each angle of n-sided regular polygon is

$$\left(\frac{2n-4}{n}\right)$$
 right angles.

Now,

According to the question

$$\frac{n}{m} = \frac{5}{4} \Rightarrow \frac{5m}{4} = n \qquad ---(i)$$

Also,

$$\left(\frac{2n-4}{n}\right)90^{0} - \left(\frac{2m-4}{m}\right)90^{0} = 9^{0}$$

$$\Rightarrow \frac{(2n-4)m - (2m-4)n}{mn} = \left(\frac{1}{10}\right)^{0} ---(ii)$$

From (i) and (ii), we get

$$\frac{\left(2 \times \frac{5}{4}m - 4\right)m - \left(2m - 4\right)\frac{5}{4}m}{\frac{5}{4}m^2} = \frac{1}{10}$$

$$\Rightarrow \frac{\left(10m - 16\right) - \left(10m - 20\right)}{5m} = \frac{1}{10}$$

$$\Rightarrow \frac{4}{m} = \frac{1}{2} \Rightarrow m = 8$$

$$n = \frac{5}{4}m = 10$$

Thus,

$$n = 10, m = 8$$

Let AB be the rail road

$$\angle AOB = 25^{\circ} = 25 \times \frac{\pi}{180} = \left(\frac{5\pi}{36}\right)^{\circ}$$

$$10 = \left(\frac{\pi}{180}\right)^{C}$$

We know that

$$\theta = \frac{\text{arc}}{\text{radius}}$$

$$\Rightarrow \qquad \angle AOB = \frac{AB}{OA}$$

$$\Rightarrow \frac{5\pi}{36} = \frac{40}{r}$$

$$\Rightarrow r = \frac{40 \times 36}{5\pi}$$

$$\Rightarrow r = \frac{288}{\pi} \text{ meter}$$

$$\pi = \frac{22}{7}$$

## Q12

Let, 
$$\angle AOB = \theta = 1$$

$$AB = \operatorname{arc} AB = I$$

$$OA = OB = r = 5280m$$

$$\Rightarrow 1' = \left(\frac{1}{60}\right)^0 = \left(\frac{1}{60} \times \frac{\pi}{180}\right)^0$$

$$\left[ \because \mathbf{1}^0 = \left( \frac{\pi}{180} \right)^c \right]$$

Now,

We know that

$$\theta = \frac{\text{arc}}{\text{radius}}$$

$$\Rightarrow \qquad \left(\frac{\pi}{180 \times 60}\right)^c = \frac{1}{5280}$$

$$\Rightarrow$$
  $I = \frac{5280\pi}{180 \times 60} = 1.5365 \text{ m}$ 

$$\pi = \frac{22}{7}$$

Since A wheel makes 360 revoulation in 1 minutes

 $\therefore$  Wheel will make  $\frac{360}{60}$  revolution in 1 secons

That is, 6 revoultin in1 second

Now,

In one revolutin the wheel makes  $360^{0}$  angle ... In 6 revolution the wheel will make  $360^{0} \times 6$  angles

$$=2160^{\circ}$$

$$1^0 = \left(\frac{\pi}{180}\right)^c$$

$$2160^{0} = \left(\frac{2160}{180} \times \pi\right)^{c}$$
$$= 12\pi$$

(i) We have,

$$= 0.75 \, \text{m}$$

---(i)

$$AB = \text{arc } AB = 10 \text{ cm}$$
  
= 0.1 m

Also,

$$\theta = \frac{\text{arc}}{\text{radius}}$$

$$\Rightarrow \theta = \frac{0.1}{0.75} = \left(\frac{2}{15}\right)^{c}$$

$$\theta = \frac{2}{15} \text{ radian}$$

$$OA = 75 \text{ cm} = 0.75 \text{ m}$$

From (A)

$$\theta = \frac{0.15}{0.75} = \frac{1}{5} \text{ radian}$$

$$\theta = \frac{1}{5}$$
 radian

$$AB = 21 \text{ cm} = 0.21 \text{ m}$$

From (A)

$$\theta = \frac{0.21}{0.75} = \frac{7}{25}$$

$$\theta = \frac{0.21}{0.75} = \frac{7}{25}$$

$$\theta = \frac{7}{25} \text{ radian}$$

We have,

$$OA = OB = \text{radius of circle} = 30 \text{ cm} = 0.3 \text{ m}$$
  
 $AB = \text{chord } AB = 30 \text{ cm} = 0.3 \text{ m}$   
 $Arc AB = \widehat{AB} = I \text{ (say)}$ 

Now,

ΔAOB is equilateral triangle as OA = OB = AB = 30 cm

$$\therefore \angle AOB = 60^{\circ} = \frac{\pi}{3} \text{ radian.}$$

$$\theta = \frac{\text{arc}}{\text{radius}}$$

$$\Rightarrow \frac{\pi}{3} = \frac{1}{0.3}$$

$$\Rightarrow I = \frac{0.3}{3}\pi = 0.1\pi \text{ m}$$

. / = arc AB = 10π cm.

#### **Q16**

We have,

In circular track,

$$OA = OB = r = 150 \text{ m}$$

 $\angle AOB = \theta$  = angle the train turns in 10 seconds

Speed of train = 66 km/hr

= 
$$\frac{66 \times 1000}{60 \times 60}$$
 m/sec  
=  $\frac{110}{6}$  m/sec

.. Train will travel in 10 sec =  $\frac{110}{6} \times 10 = \frac{1100}{6}$  m

$$arc AB = \frac{1100}{6} m$$

Thus,

$$\theta = \frac{\text{arc}}{\text{radius}} = \frac{1100}{6 \times 1500} = \frac{11}{90} \text{ radian}$$

.. The train will turn by  $\left(\frac{11}{90}\right)^c$  angle in 10 sec.

Let, r be the distance, at which poin in placed. So that it completely conceals the full moon.

Let, E be the eye of the observer.

Now,

$$\theta = 31' = \left(\frac{31}{60}\right)^0 \qquad \left[\because 60' = 1^0\right]$$
$$= \frac{31}{60} \times \left(\frac{\pi}{180}\right)^c \qquad \left[\because 1^0 = \left(\frac{\pi}{180}\right)^c\right]$$

Also,

Now,

by 
$$\theta = \frac{\text{arc}}{\text{radius}}$$

$$\frac{31\pi}{60 \times 180} = \frac{0.02}{r}$$

$$\Rightarrow r = \frac{0.02 \times 60 \times 180}{31\pi}$$

$$- 2.217 \text{ m}$$

$$\boxed{\because x - \frac{22}{7}}$$

Thus,

The coin should be placed at a distance of 2.217 m from the eye.

#### **Q18**

Let, E be the eye of the observer and S be the sum.

Now,

$$\angle ACB = \theta = 32^{\circ}$$

$$= \left(\frac{32}{60}\right)^{\circ}$$

$$= \left(\frac{32}{60} \times \frac{\pi}{180}\right)^{\circ}$$

$$\theta = \frac{\text{arc}}{\text{radius}}$$

$$\Rightarrow \frac{32}{60} \times \frac{\pi}{180} = \frac{AB}{91 \times 10^6} \text{ km}$$

$$\Rightarrow AB = \frac{91 \times 10^6 \times 32 \times \pi}{60 \times 180}$$
= 8.474074 \times 10<sup>5</sup> km
= 847407.4 km

.. Distance of sun is 847407.4 km.

Let,  $C_1 \otimes C_2$  are two circles with same Arc length /. That is AB = CD = I

Let,  $\theta_1$  adn  $\theta_2$  are two angles subtended by arc AB and CD on respective ordes.

Let, 
$$OA = OB = r$$
 [radius of  $C_1$ ]  
and  $OC = O\Delta = R$  [radius of  $C_2$ ]

Also,

$$\theta_1 = 65^0 = \left(\frac{65\pi}{180}\right)^c$$

and 
$$\theta_2 = 110^0 = \left(\frac{110\pi}{180}\right)^c$$

We know

$$\theta = \frac{\text{arc}}{\text{radius}}$$

: For Ct

$$S_1 = \frac{AB}{AB}$$

$$\Rightarrow$$
  $\theta_1 = \frac{1}{2}$ 

$$r = \frac{1}{\theta_0}$$

For C<sub>2</sub>

$$\theta_2 = \frac{CO}{R}$$

$$\Rightarrow$$
  $\theta_2 = \frac{1}{6}$ 

$$\Rightarrow$$
  $R = \frac{I}{\theta}$ 

From (i) and (ii)

$$\frac{r}{R} = \frac{\frac{f}{\theta_1}}{\frac{f}{\theta_2}} = \frac{\theta_2}{\theta_1} = \frac{\frac{110\pi}{180}}{\frac{65\pi}{180}} = \frac{22}{13}$$

r:R = 22:13

Let, 
$$AB = \operatorname{arc} AB = 22 \text{ cm}$$
  
 $OA = OB = r = 100 \text{ cm}$ 

Let  $\theta$  bet the angle subtanded by arc AB at centre O.

$$\Rightarrow \qquad \theta = \frac{\text{arc}}{\text{radius}}$$

$$\Rightarrow \qquad \theta = \frac{22}{100} \text{ radian}$$

$$\Rightarrow \qquad \theta = \left(\frac{22}{100} \times \frac{180}{\pi}\right)^0 \qquad \qquad \left[ \because 1 \text{ radian} = \left(\frac{180}{\pi}\right)^0 \right]$$

$$= 12.6^0$$

$$= 12^0 36^1 \qquad \left[ \because 1^0 = 60^1 \right]$$

$$\theta = 12^{0}36^{\circ}$$