Class -VI Mathematics (Ex. 3.1) Questions

	(a) 2 ⁴	4	(b) 15	(c) 21	(d) 27
	(e) 12	2	(f) 20	(g) 18	(h) 23
	(i) 36)			
2.	Write	e first five n	nultiples of:		
	(a) 5		(b) 8	(c) 9	
3.	Matcl	h the items	in column 1 with th	e items in column 2:	
	Colur	nn 1		Column 2	
	(i)	35	(a) M	ultiple of 8	
	(ii)	15	(b) M	ultiple of 7	
	(iii)	16	(c) Mı	ultiple of 70	
	(iv)	20	(d) Fa	ctor of 30	
	(v)	20	(e) Fa	ctor of 50	
4.	Find	all the mult	ciples of 9 up to 100		

Write all the factors of the following numbers:

Class -VI Mathematics (Ex. 3.1) Answers

1. (a)
$$24 = 1 \times 24 = 2 \times 12 = 3 \times 8 = 4 \times 6 = 6 \times 4$$

$$\therefore$$
 Factors of 24 = 1, 2, 3, 4, 6, 12, 24

(b)
$$15 = 1 \times 15 = 3 \times 5 = 5 \times 3$$

$$\therefore$$
 Factors of 15 = 1, 3, 5, 15

(c)
$$21 = 1 \times 21 = 3 \times 7 = 7 \times 3$$

$$\therefore$$
 Factors of 21 = 1, 3, 7, 21

(d)
$$27 = 1 \times 27 = 3 \times 9 = 9 \times 3$$

$$\therefore$$
 Factors of 27 = 1, 3, 9, 27

(e)
$$12 = 1 \times 12 = 2 \times 6 = 3 \times 4 = 4 \times 3$$

$$\therefore$$
 Factors of 12 = 1, 2, 3, 4, 6, 12

(f)
$$20 = 1 \times 20 = 2 \times 10 = 4 \times 5 = 5 \times 4$$

$$\therefore$$
 Factors of 20 = 1, 2, 4, 5, 10, 20

(g)
$$18 = 1 \times 18 = 2 \times 9 = 3 \times 6$$

$$\therefore$$
 Factors of 18 = 1, 2, 3, 6, 9, 18

(h)
$$23 = 1 \times 23$$

$$\therefore$$
 Factors of 23 = 1, 23

(i)
$$36 = 1 \times 36 = 2 \times 18 = 3 \times 12 = 4 \times 9 = 6 \times 6$$

$$\therefore$$
 Factors of 36 = 1, 2, 3, 4, 6, 9, 12, 18, 36

2. (a)
$$5 \times 1 = 5$$
, $5 \times 2 = 10$, $5 \times 3 = 15$, $5 \times 4 = 20$, $5 \times 5 = 25$

$$\therefore$$
 First five multiples of 5 are 5, 10, 15, 20, 25.

(b)
$$8 \times 1 = 8$$
, $8 \times 2 = 16$, $8 \times 3 = 24$, $8 \times 4 = 32$, $8 \times 5 = 40$

(c)
$$9 \times 1 = 9$$
, $9 \times 2 = 18$, $9 \times 3 = 27$, $9 \times 4 = 36$, $9 \times 5 = 45$

3. (i)
$$\rightarrow$$
 (b), (ii) \rightarrow (d), (iii) \rightarrow (a), (iv) \rightarrow (f), (v) \rightarrow (e)

Class -VI Mathematics (Ex. 3.2) Questions

1.										
	(a) Odd numbers.									
2.	(b) Even numbers.	State whether the following statements are true or false:								
۷.	(a) The sum of three odd numbers is even.									
	(b) The sum of two o			ar ic ayan						
	(c) The product of th			ci is even.						
	(d) If an even numbe			always odd						
	(e) All prime number		z, the quotient is t	iiways ouu.						
	(f) Prime numbers d		, factors							
	(g) Sum of two prime	_								
	(h) 2 is the only even		-							
	(i) All even numbers									
	(j) The product of tw	_								
	(),									
3.	The numbers 13 and	d 31 are prim	e numbers. Both t	hese numbers have same	digits 1 and 3.					
	Find such pairs of pr	ime numbers ι	ıp to 100.							
4.	Write down separate	=	_							
5.	What is the greatest	=								
6.	Express the following	g as the sum of	two odd numbers	:						
	(a) 44	(b) 36	(c) 24	(d) 18						
7.	Give three pairs of pi	ime numbers	whose difference i	s 2.						
				re called twin primes.]						
8.	Which of the following			, , , , , , , , , , , , , , , , , , ,						
	(a) 23	(b) 51	(c) 37	(d) 26						
9.	Write seven consecu	. ,	. ,	an 100 so that there is no	prime number					
	between them.	-								
10.	Express each of the f	ollowing numb	ers as the sum of t	three odd primes:						
	(a) 21	(b) 31	(c) 53	(d) 61						
11.	Write five pairs of pr	ime numbers l	ess than 20 whose	sum is divisible by 5.						
	[Hint: $3 + 7 = 10$]									
12.	Fill in the blanks:									
	(a) A number which	has only two fa	actors is called a	'						
	(b) A number which	has more than	two factors is calle	ed a						
	(c) 1 neither	nor	·							
	(d) The smallest prin	ne number is _	·							
	(e) The smallest com	posite number	r is							
	(f) The smallest ever	(f) The smallest even number is								

Class -VI Mathematics (Ex. 3.2) Answers

1. (a) The sum of any two odd numbers is an even number.

Example: 1 + 3 = 4, 3 + 5 = 8

(b) The sum of any two even numbers is an even number.

Example: 2 + 4 = 6, 6 + 8 = 14

2. (a) False

(b) True

(c) True

(d) False

(e) False

(f) False

(g) False

(h) True

(i) False

(j) True

3. 17 and 71; 37 and 73; 79 and 97

4. Prime numbers:

2, 3, 5, 7, 11, 13, 17, 19

Composite numbers: 4, 6, 8, 9, 10, 12, 14, 15, 16, 18

5. The greatest prime number between 1 and 10 is '7'.

6. (a) 3 + 41 = 44

(b) 5 + 31 = 36

(c) 7 + 17 = 24

(d) 7 + 11 = 18

7. 3 and 5;

5 and 7;

11 and 13

8. (a) 23 and (c) 37 are prime numbers.

9. 90, 91, 92, 93, 94, 95, 96

10. (a) 21 = 3 + 7 + 11

(b) 31 = 3 + 11 + 17

(c) 53 = 13 + 17 + 23

(d) 61 = 19 + 29 + 13

11. 2 + 3 = 5;

7 + 13 = 20;

3 + 17 = 20;

2 + 13 = 15;

5 + 5 = 10

12. (a) Prime number

(b) Composite number

(c) Prime number and composite number

(d) 2

(e) 4

(f) 2

Class -VI Mathematics (Ex. 3.3) Questions

1. Using divisibility test, determine which of the following numbers are divisible by 2; by 3; by 4; by 5; by 8; by 9; by 10; by 11. (say yes or no)

Number				D	ivisible b	ру			
128	Yes	No	Yes	No	No	Yes	No	No	No
990									
1586									
275									
6686									
639210									
429714									
2856									
3060									
406839									

	3060 406839									
2.	Using divisi (a) 572 (e) 12159 (i) 1700	-	(b) 726	352 60	(c) 5	owing nu 500 1084	(d)	6000		8:
3.	Using divisi (a) 297144 (e) 901352 (i) 639210	·	(b) 125	8 750	(c) 4	335	(d)	61233	e by 6:	
4.	Using divisi (a) 5445 (e) 100000	,	(b) 108	24		owing nu 138965			-	
5.	Write the snumbers so (a)	that the	number fo	ormed is	divisibly b	y 3:	nks spac	e of each	of the f	ollowing
6.	Write the snumbers so (a) 92	that the	number fo	ormed is	divisibly l	y 11:	inks spac	e of each	of the f	ollowing

Class -VI Mathematics (Ex. 3.3) Answers

1. Sol.

Number		Divisible by							
	2	3	4	5	6	8	9	10	11
128	Yes	No	Yes	No	No	Yes	No	No	No
990	Yes	Yes	No	Yes	Yes	No	Yes	Yes	Yes
1586	Yes	No	No	No	No	No	No	No	No
275	No	No	No	Yes	No	No	No	No	Yes
6686	Yes	No	No	No	No	No	No	No	No
639210	Yes	Yes	No	Yes	Yes	No	No	Yes	Yes
429714	Yes	Yes	No	No	Yes	No	Yes	No	No
2856	Yes	Yes	Yes	No	Yes	Yes	No	No	No
3060	Yes	Yes	Yes	Yes	Yes	No	Yes	Yes	No
406839	No	Yes	No						

- 2. (a) 572 \rightarrow Divisible by 4 as its last two digits are divisible by 4.
 - \rightarrow Not divisible by 8 as its last three digits are not divisible by 8.
 - (b) $726352 \rightarrow$ Divisible by 4 as its last two digits are divisible by 4.
 - \rightarrow Divisible by 8 as its last three digits are divisible by 8.
 - (c) 5500 \rightarrow Divisible by 4 as its last two digits are divisible by 4.
 - \rightarrow Not divisible by 8 as its last three digits are not divisible by 8.
 - (d) $6000 \rightarrow \text{Divisible by 4 as its last two digits are 0}$.
 - \rightarrow Divisible by 8 as its last three digits are 0.
 - (e) 12159 \rightarrow Not divisible by 4 and 8 as it is an odd number.
 - (f) 14560 \rightarrow Divisible by 4 as its last two digits are divisible by 4.
 - \rightarrow Divisible by 8 as its last three digits are divisible by 8.
 - (g) 21084 \rightarrow Divisible by 4 as its last two digits are divisible by 4.
 - \rightarrow Not divisible by 8 as its last three digits are not divisible by 8.
 - (h) 31795072 \rightarrow Divisible by 4 as its last two digits are divisible by 4.
 - \rightarrow Divisible by 8 as its last three digits are divisible by 8.
 - (i) 1700 \rightarrow Divisible by 4 as its last two digits are 0.
 - \rightarrow Not divisible by 8 as its last three digits are not divisible by 8.
 - (j) 5500 \rightarrow Not divisible by 4 as its last two digits are not divisible by 4.
 - \rightarrow Not divisible by 8 as its last three digits are not divisible by 8.
- 3. (a) 297144 \rightarrow Divisible by 2 as its units place is an even number.
 - \rightarrow Divisible by 3 as sum of its digits (= 27) is divisible by 3.

Since the number is divisible by both 2 and 3, therefore, it is also divisible by 6.

```
(b) 1258
                  \rightarrow Divisible by 2 as its units place is an even number.
                  \rightarrow Not divisible by 3 as sum of its digits (= 16) is not divisible by 3.
    Since the number is not divisible by both 2 and 3, therefore, it is not divisible by 6.
(c) 4335
                  \rightarrow Not divisible by 2 as its units place is not an even number.
                  \rightarrow Divisible by 3 as sum of its digits (= 15) is divisible by 3.
    Since the number is not divisible by both 2 and 3, therefore, it is not divisible by 6.
(d) 61233
                  \rightarrow Not divisible by 2 as its units place is not an even number.
                  \rightarrow Divisible by 3 as sum of its digits (= 15) is divisible by 3.
    Since the number is not divisible by both 2 and 3, therefore, it is not divisible by 6.
(e) 901352
                  \rightarrow Divisible by 2 as its units place is an even number.
                  \rightarrow Not divisible by 3 as sum of its digits (= 20) is not divisible by 3.
    Since the number is not divisible by both 2 and 3, therefore, it is not divisible by 6.
                  \rightarrow Divisible by 2 as its units place is an even number.
(f) 438750
                  \rightarrow Divisible by 3 as sum of its digits (= 27) is not divisible by 3.
    Since the number is divisible by both 2 and 3, therefore, it is divisible by 6.
(g) 1790184
                  \rightarrow Divisible by 2 as its units place is an even number.
                  \rightarrow Divisible by 3 as sum of its digits (= 30) is not divisible by 3.
    Since the number is divisible by both 2 and 3, therefore, it is divisible by 6.
(h) 12583
                  \rightarrow Not divisible by 2 as its units place is not an even number.
                  \rightarrow Not divisible by 3 as sum of its digits (= 19) is not divisible by 3.
    Since the number is not divisible by both 2 and 3, therefore, it is not divisible by 6.
                  \rightarrow Divisible by 2 as its units place is an even number.
(i) 639210
                  \rightarrow Divisible by 3 as sum of its digits (= 21) is not divisible by 3.
    Since the number is divisible by both 2 and 3, therefore, it is divisible by 6.
(j) 17852
                  \rightarrow Divisible by 2 as its units place is an even number.
                  \rightarrow Not divisible by 3 as sum of its digits (= 23) is not divisible by 3.
    Since the number is not divisible by both 2 and 3, therefore, it is not divisible by 6.
(a) 5445
                  \rightarrow Sum of the digits at odd places = 4 + 5 = 9
                  \rightarrow Sum of the digits at even places = 4 + 5 = 9
                  \rightarrow Difference of both sums = 9 - 9 = 0
    Since the difference is 0, therefore, the number is divisible by 11.
(b) 10824
                  \rightarrow Sum of the digits at odd places = 4 + 8 + 1 = 13
                  \rightarrow Sum of the digits at even places = 2 + 0 = 2
                  \rightarrow Difference of both sums = 13 - 2 = 11
    Since the difference is 11, therefore, the number is divisible by 11.
                  \rightarrow Sum of the digits at odd places = 5 + 9 + 3 + 7 = 24
(c) 7138965
                  \rightarrow Sum of the digits at even places = 6 + 8 + 1 = 15
                  \rightarrow Difference of both sums = 24 - 15 = 9
    Since the difference is neither 0 nor 11, therefore, the number is not divisible by 11.
(d) 70169308 \rightarrow \text{Sum of the digits at odd places} = 8 + 3 + 6 + 0 = 17
```

4.

 \rightarrow Sum of the digits at even places = 0 + 9 + 1 + 7 = 17

$$\rightarrow$$
 Difference of both sums = 17 - 17 = 0

Since the difference is 0, therefore, the number is divisible by 11.

(e) $10000001 \rightarrow \text{Sum of the digits at odd places} = 1 + 0 + 0 + 0 = 1$

 \rightarrow Sum of the digits at even places = 0 + 0 + 0 + 1 = 1

 \rightarrow Difference of both sums = 1 - 1 = 0

Since the difference is 0, therefore, the number is divisible by 11.

(f) 901153 \rightarrow Sum of the digits at odd places = 3 + 1 + 0 = 4

 \rightarrow Sum of the digits at even places = 5 + 1 + 9 = 15

 \rightarrow Difference of both sums = 15 - 4 = 11

Since the difference is 11, therefore, the number is divisible by 11.

5. (a) We know that a number is divisible by 3 if the sum of all digits is divisible by 3.

Therefore, Smallest digit: 2 \rightarrow <u>26724 = 2 + 6 + 7 + 2 + 4 = 21</u>

Largest digit: 8 \rightarrow 86724 = 8 + 6 + 7 + 2 + 4 = 27

(b) We know that a number is divisible by 3 if the sum of all digits is divisible by 3.

Therefore, Smallest digit: $0 \rightarrow 4765\underline{0}2 = 4 + 7 + 6 + 5 + 0 + 2 = 24$

Largest digit: 9 \rightarrow 476592 = 4 + 7 + 6 + 5 + 0 + 2 = 33

6. (a) We know that a number is divisible by 11 if the difference of the sum of the digits at odd places and that of even places should be either 0 or 11.

Therefore, $92\underline{8}389 \rightarrow 0dd \ places = 9 + 8 + 8 = 25$

Even places = 2 + 3 + 9 = 14

Difference = 25 - 14 = 11

(b) We know that a number is divisible by 11 if the difference of the sum of the digits at odd places and that of even places should be either 0 or 11.

Therefore, $8\underline{6}9484 \rightarrow 0dd \text{ places} = 8 + 9 + 8 = 25$

Even places = 6 + 4 + 4 = 14

Difference = 25 - 14 = 11

Class -VI Mathematics (Ex. 3.4) Questions

1. Find the common factors of:

(a) 20 and 28

(b) 15 and 25

(c) 35 and 50

(d) 56 and 120

2. Find the common factors of:

(a) 4, 8 and 12

(b) 5, 15 and 25

3. Find the first three common multiples of:

(a) 6 and 8

(b) 12 and 18

4. Write all the numbers less than 100 which are common multiples of 3 and 4.

5. Which of the following numbers are co-prime:

(a) 18 and 35

(b) 15 and 37

(c) 30 and 415

(d) 17 and 68

(e) 216 and 215

(f) 81 and 16

6. A number is divisible by both 5 and 12. By which other number will that number be always divisible?

7. A number is divisible by 12. By what other numbers will that number be divisible?

Class -VI Mathematics (Ex. 3.4) Answers

- 1. (a) Factors of 20 = 1, 2, 4, 5, 10, 20 Factors of 28 = 1, 2, 4, 7, 14, 28 Common factors = 1, 2, 4
 - (b) Factors of 15 = 1, 3, 5, 15 Factors of 25 = 1, 5, 25 Common factors = 1, 5
 - (c) Factors of 35 = 1, 5, 7, 35 Factors of 50 = 1, 2, 5, 10, 25, 50 Common factors = 1, 5
 - (d) Factors of 56 = 1, 2, 4, 7, 8, 14, 28, 56 Factors of 120 = 1, 2, 3, 4, 5, 6, 8, 10, 12, 15, 20, 24, 30, 60, 120 Common factors = 1, 2, 4, 8
- 2. (a) Factors of 4 = 1, 2, 4
 Factors of 8 = 1, 2, 4, 8
 Factors of 12 = 1, 2, 3, 4, 6, 12
 Common factors of 4, 8 and 12 = 1, 2, 4
 - (b) Factors of 5 = 1, 5 Factors of 15 = 1, 3, 5, 15 Factors of 25 = 1, 5, 25 Common factors of 5, 15 and 25 = 1, 5
- 4. Multiple of 3 = 3, 6, 9, 12, 15, 18, 21, 24, 27, 30, 33, 36, 39, 42, 45, 48, 51, 54, 57, 60, 63, 66, 69, 72, 75, 78, 81, 84, 87, 90, 93, 96, 99

 Multiple of 4 = 4, 8, 12, 16, 20, 24, 28, 32, 36, 40, 44, 48, 52, 56, 60, 64, 68, 72, 76, 80, 84, 88, 92, 96, 100

 Common multiples of 3 and 4 = 12, 24, 36, 48, 60, 72, 84, 96
- 5. (a) Factors of 18 = 1, 2, 3, 6, 9, 18 Factors of 35 = 1, 5, 7, 35

Common factor = 1

Since, both have only one common factor, i.e., 1, therefore, they are co-prime numbers.

(b) Factors of 15 = 1, 3, 5, 15

Factors of 37 = 1,37

Common factor = 1

Since, both have only one common factor, i.e., 1, therefore, they are co-prime numbers.

(c) Factors of 30 = 1, 2, 3, 5, 6, 15, 30

Factors of 415 = 1, 5,, 83, 415

Common factor = 1, 5

Since, both have more than one common factor, therefore, they are not co-prime numbers.

(d) Factors of 17 = 1, 17

Factors of 68 = 1, 2, 4, 17, 34, 86

Common factor = 1, 17

Since, both have more than one common factor, therefore, they are not co-prime numbers.

(e) Factors of 216 = 1, 2, 3, 4, 6, 8, 36, 72, 108, 216

Factors of 215 = 1, 5, 43, 215

Common factor = 1

Since, both have only one common factor, i.e., 1, therefore, they are co-prime numbers.

(f) Factors of 81 = 1, 3, 9, 27, 81

Factors of 16 = 1, 2, 4, 8, 16

Common factor = 1

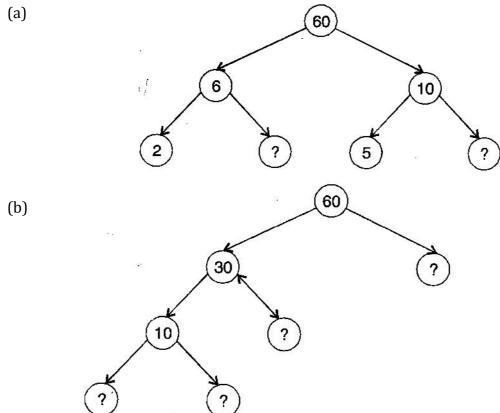
Since, both have only one common factor, i.e., 1, therefore, they are co-prime numbers.

- 6. $5 \times 12 = 60$. The number must be divisible by 60.
- 7. Factors of 12 are 1, 2, 3, 4, 6, 12.

Therefore, the number also be divisible by 1,2,3 4 and 6.

Class -VI Mathematics (Ex. 3.5) Questions

- 1. Which of the following statements are true:
 - (a) If a number is divisible by 3, it must be divisible by 9.
 - (b) If a number is divisible by 9, it must be divisible by 3.
 - (c) If a number is divisible by 18, it must be divisible by both 3 and 6.
 - (d) If a number is divisible by 9 and 10 both, then it must be divisible by 90.
 - (e) If two numbers are co-primes, at least one of them must be prime.
 - (f) All numbers which are divisible by 4 must also by divisible by 8.
 - (g) All numbers which are divisible by 8 must also by divisible by 4.
 - (h) If a number is exactly divides two numbers separately, it must exactly divide their sum.
 - (i) If a number is exactly divides the sum of two numbers, it must exactly divide the two numbers separately.
- 2. Here are two different factor trees for 60. Write the missing numbers.



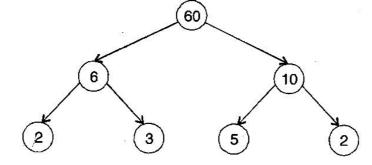
- 3. Which factors are not included in the prime factorization of a composite number?
- 4. Write the greatest 4-digit number and express it in terms of its prime factors.
- 5. Write the smallest 5-digit number and express it in terms of its prime factors.

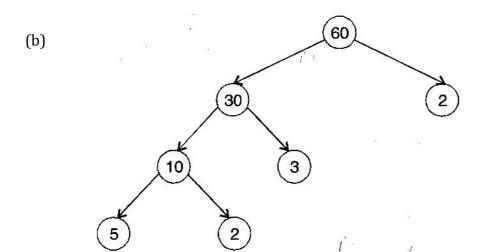
- 6. Find all the prime factors of 1729 and arrange them in ascending order. Now state the relation, if any, between, two consecutive prime numbers.
- 7. The product of three consecutive numbers is always divisible by 6. Verify this statement with the help of some examples.
- 8. The sum of three consecutive numbers is always divisible by 4. Verify this statement with the help of some examples.
- 9. In which of the following expressions, prime factorization has been done:
 - (a) $24 = 2 \times 3 \times 4$
 - (b) $56 = 7 \times 2 \times 2 \times 2$
 - (c) $70 = 2 \times 5 \times 7$
 - (d) $54 = 2 \times 3 \times 9$
- 10. Determine if 25110 is divisible by 45. [Hint: 5 and 9 are co-prime numbers. Test the divisibility of the number by 5 and 9.]
- 11. 18 is divisible by both 2 and 3. It is also divisible by $2 \times 3 = 6$. Similarly, a number is divisible by 4 and 6. Can we say that the number must be divisible by $4 \times 6 = 24$? If not, give an example to justify your answer.
- 12. I am the smallest number, having four different prime factors. Can you find me?

Class -VI Mathematics (Ex. 3.5) Answers

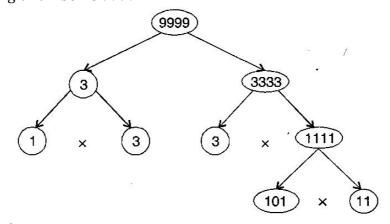
- 1. Statements (b), (c), (d), (g) and (h) are true.
- 2. Sol.

(a)



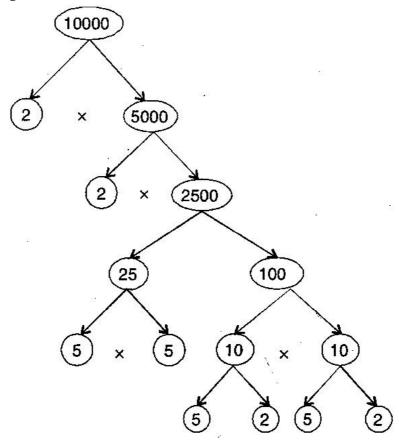


- 3. 1
- 4. The greatest four digit number is 9999.



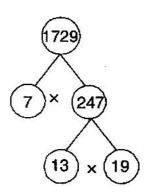
The prime factors of 9999 are $3 \times 3 \times 11 \times 101$.

5. The smallest five digit number is 10000.



The prime factors of 10000 are 2 x 2 x 2 x 2 x 5 x 5 x 5 x 5.

6. Sol.



Prime factors of 1729 are $7 \times 13 \times 19$.

The difference of two consecutive prime factors is 6.

7. Among the three consecutive numbers, there must be one even number and one multiple of 3. Thus, the product must be multiple of 6.

Example:

(i)
$$2 \times 3 \times 4 = 24$$

(ii)
$$4 \times 5 \times 6 = 120$$

- 8. 3 + 5 = 8 and 8 is divisible by 4.
 - 5 + 7 = 12 and 12 is divisible by 4.
 - 7 + 9 = 16 and 16 is divisible by 4.
 - 9 + 11 = 20 and 20 is divisible by 4.
- 9. In expressions (b) and (c), prime factorization has been done.
- 10. The prime factorization of $45 = 5 \times 9$
 - 25110 is divisible by 5 as '0' is at its unit place.
 - 25110 is divisible by 9 as sum of digits is divisible by 9.
 - Therefore, the number must be divisible by $5 \times 9 = 45$
- 11. No. Number 12 is divisible by both 6 and 4 but 12 is not divisible by 24.
- 12. $2 \times 3 \times 5 \times 7 = 210$

Class -VI Mathematics (Ex. 3.6) Questions

1. Find the H.C.F. of the following numbers:

(a) 18, 48

(b) 30, 42

(c) 18, 60

(d) 27, 63

(e) 36, 84

(f) 34, 102

(g) 70, 105, 175

(h) 91, 112, 49

(i) 18, 54, 81

(j) 12, 45, 75

- 2. What is the H.C.F. of two consecutive:
 - (a) numbers?
 - (b) even numbers?
 - (c) odd numbers?
- 3. H.C.F. of co-prime numbers 4 and 15 was found as follows by factorization:

 $4 = 2 \times 2$ and $15 = 3 \times 5$ since there is no common prime factor, so H.C.F. of 4 and 15 is 0. Is the answer correct? If not, what is the correct H.C.F.?

Class -VI Mathematics (Ex. 3.6) Answers

- 1. (a) Factors of 18 = 2 x 3 x 3 Factors of 48 = 2 x 2 x 2 x 2 x 3 H.C.F. (18, 48) = 2 x 3 = 6
 - (c) Factors of $18 = 2 \times 3 \times 3$ Factors of $60 = 2 \times 2 \times 3 \times 5$ H.C.F. $(18, 60) = 2 \times 3 = 6$
 - (e) Factors of 36 = 2 x 2 x 3 x 3 Factors of 84 = 2 x 2 x 3 x 7 H.C.F. (36, 84) = 2 x 2 x 3 = 12
 - (g) Factors of 70 = 2 x 5 x 7 Factors of 105 = 3 x 5 x 7 Factors of 175 = 5 x 5 x 7 H.C.F. = 5 x 7 = 35
 - (i) Factors of 18 = 2 x 3 x 3 Factors of 54 = 2 x 3 x 3 x 3 Factors of 81 = 3 x 3 x 3 x 3 H.C.F. = 3 x 3 = 9

- (b) Factors of $30 = 2 \times 3 \times 5$ Factors of $42 = 2 \times 3 \times 7$ H.C.F. $(30, 42) = 2 \times 3 = 6$
- (d) Factors of 27 = 3 x 3 x 3 Factors of 63 = 3 x 3 x 7 H.C.F. (27, 63) = 3 x 3 = 9
- (f) Factors of 34 = 2 x 17 Factors of 102 = 2 x 3 x 17 H.C.F. (34, 102) = 2 x 17 = 34
- (h) Factors of 91 = 7 x 13 Factors of 112 = 2 x 2 x 2 x 2 x 7 Factors of 49 = 7 x 7 H.C.F. = 1 x 7 = 7
- (j) Factors of 12 = 2 x 2 x 3 Factors of 45 = 3 x 3 x 5 Factors of 75 = 3 x 5 x 5 H.C.F. = 1 x 3 = 3
- 2. (a) H.C.F. of two consecutive numbers be 1.
 - (b) H.C.F. of two consecutive even numbers be 2.
 - (c) H.C.F. of two consecutive odd numbers be 1.
- 3. No. The correct H.C.F. is 1.

Class -VI Mathematics (Ex. 3.7) Questions

- 1. Renu purchases two bags of fertilizer of weights 75 kg and 69 kg. Find the maximum value of weight which can measure the weight of the fertilizer exact number of times.
- 2. Three boys step off together from the same spot. Their steps measure 63 cm, 70 cm and 77 cm respectively. What is the maximum distance each should cover so that all can cover the distance in complete steps?
- 3. The length, breadth and height of a room are 825 cm, 675 cm and 450 cm respectively. Find the longest tape which can measure the three dimensions of the room exactly.
- 4. Determine the smallest 3-digit number which is exactly divisible by 6, 8 and 12.
- 5. Determine the largest 3-digit number which is exactly divisible by 8, 10 and 12.
- 6. The traffic lights at three different road crossings change after every 48 seconds, 72 seconds and 108 seconds respectively. If they change simultaneously at 7 a.m. at what time will they change simultaneously again?
- 7. Three tankers contain 403 liters and 465 liters of diesel respectively. Find the maximum capacity of a container that can measure the diesel of three containers exact number of times.
- 8. Find the least number which when divided by 6, 15 and 18, leave remainder 5 in each case.
- 9. Find the smallest 4-digit number which is divisible by 18, 24 and 32.
- 10. Find the L.C.M. of the following numbers:(a) 9 and 4 (b) 12 and 5 (c) 6 and 5 (d) 15 and 4Observe a common property in the obtained L.C.Ms. Is L.C.M. the product of two numbers in each case?

11.	Find the L.C.M. of the f	ollowing numbers in	which one number is	the factor of other
	(a) 5, 20	(b) 6, 18	(c) 12, 48	(d) 9, 45
	What do you observe i	n the result obtained	7	

Class -VI Mathematics (Ex. 3.7) Answers

1. For finding maximum weight, we have to find H.C.F. of 75 and 69.

Factors of $75 = 3 \times 5 \times 5$

Factors of $69 = 3 \times 69$

H.C.F. = 3

Therefore the required weight is 3 kg.

2. For finding minimum distance, we have to find L.C.M of 63, 70, 77.

L.C.M. of 63, 70 and $77 = 7 \times 9 \times 10 \times 11 = 6930 \text{ cm}$.

Therefore, the minimum distance is 6930 cm.

_ 7	63, 70, 77
9	9, 10, 11
10	1, 10, 11
11	1, 1, 11
	1, 1, 1

3. The measurement of longest tape = H.C.F. of 825 cm, 675 cm and 450 cm.

Factors of $825 = 3 \times 5 \times 5 \times 11$

Factors of $675 = 3 \times 5 \times 5 \times 3 \times 3$

Factors of $450 = 2 \times 3 \times 3 \times 5 \times 5$

H.C.F. = $3 \times 5 \times 5 = 75 \text{ cm}$

Therefore, the longest tape is 75 cm.

4. L.C.M. of 6, 8 and $12 = 2 \times 2 \times 2 \times 3 = 24$

The smallest 3-digit number = 100

To find the number, we have to divide 100 by 24

	4
24)	24
-	<u>-24</u>
	4

Therefore, the required number = 100 + (24 - 4) = 120.

5. L.C.M. of 8, 10, $12 = 2 \times 2 \times 2 \times 3 \times 5 = 120$

The largest three digit number = 999

Now,
$$120) 999$$
 -960

Therefore, the required number = 999 - 39 = 960

2	8, 10, 12
2	4, 5, 6
2	2, 5, 3
3	1, 5, 3
5	1, 5, 1
	1, 1, 1

6, 8, 12

3, 4, 6 3, 2, 3

3, 1, 3 1, 1, 1

2

2

3

6. L.C.M. of 48, 72, $108 = 2 \times 2 \times 2 \times 2 \times 3 \times 3 \times 3 = 432$ sec.

After 432 seconds, the lights change simultaneously.

432 second = 7 minutes 12 seconds

Therefore the time = 7 a.m. + 7 minutes 12 seconds

7. The maximum capacity of container = H.C.F. (403, 434, 465)

Factors of $403 = 13 \times 31$

Factors of $434 = 2 \times 7 \times 31$

Factors of $465 = 3 \times 5 \times 31$

H.C.F. = 31

Therefore, 31 liters of container is required to measure the quantity.

8. L.C.M. of 6, 15 and $18 = 2 \times 3 \times 3 \times 5 = 90$

Therefore the required number = 90 + 5 = 95

2	6, 15, 18		
3	3, 15,	9	
3	1, 5,	3	
5	1, 5,	1	
· · · · ·	1, 1,	1	

2

2

2

3

5

8, 10, 12

2, 5, 3

6

4, 5,

1, 5,

1, 1,

9. L.C.M. of 18, 24 and $32 = 2 \times 2 \times 2 \times 2 \times 2 \times 3 \times 3 = 288$

The smallest four-digit number = 1000

Now,
$$288) 1000 \\ -864 \\ 136$$

Therefore, the required number is 1000 + (288 - 136) = 1152.

10. (a) L.C.M. of 9 and 4

$$= 2 \times 2 \times 3 \times 3 = 36$$

(b) L.C.M. of 12 and 5 = $2 \times 2 \times 3 \times 5 = 60$

18,	24, 3	32
9, 1	12,	16
9,	6,	8
9,	3,	4
9,	3,	2
9,	3,	1
3,	1,	1
1,	1,	1
	9, 1 9, 9, 9, 9,	9, 3, 9, 3, 9, 3, 3, 1,

_	1
2	9, 4
2	9, 2
3	9, 1
3	3, 1
	1, 1
2	12, 5

2	12, 5
2	6, 5
3	3, 5
5	1, 5
	1, 1

(c) L.C.M. of 6 and 5		
$= 2 \times 3 \times 5 = 30$	2	6, 5
	3	3, 5
	5	1, 5
		1, 1
(d) L.C.M. of 15 and 4		
$= 2 \times 2 \times 3 \times 5 = 60$		15, 4
	2	15, 2
Yes, the L.C.M. is equal to the product of two numbers in each case.		15, 1
And L.C.M. is also the multiple of 3.		5, 1
r		1, 1
11. (a) L.C.M. of 5 and 20		
$= 2 \times 2 \times 5 = 20$	2	5, 20
	2	5, 10
	5	
	-	5, 5 1, 1
(b) L.C.M. of 6 and 18		
$2 \times 3 \times 3 = 18$		6, 18
	3	3, 9
	3	1, 3
		1, 1
(c) L.C.M. of 12 and 48		,
$2 \times 2 \times 2 \times 2 \times 3 = 48$	2	12, 48
	2	6, 24
	2	3, 12
	2	3, 6
	3	3, 3
		1, 1
(d) L.C.M. of 9 and 45		
$= 3 \times 3 \times 5 = 45$	3	9, 45
	3	3, 15
	5	1, 5
		1, 1

From these all cases, we can conclude that if the smallest number if the factor of largest number, then the L.C.M. of these two numbers is equal to that of larger number.