- **1.** (i) {2}
- (ii) {0, 1}
- (iii)  $\{1, p\}$

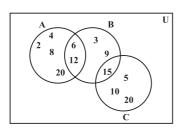
- 2. (i)  $\{0, -1, 1\}$
- (ii)  $\left\{\frac{-11}{3}\right\}$
- (iii)  $\left\{-\sqrt{3}, -\sqrt{2}, \sqrt{2}, \sqrt{3}\right\}$
- 3.  $\{1, 2, 2^2, 2^3, \dots 2^{p-1}, (2^p-1)\}$
- 4. (i) True (ii) False
- (iii) True (iv) True

- **7.** (i) {2, 4, 6, 8, ..., 98} (ii) (1,4, 9, 16, 25, 36, 49, 64, 81,}

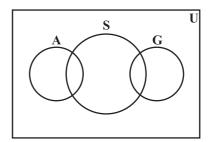
- **8.** (i)  $\{4, 8, 12\}$  (ii)  $\{7, 8, 9\}$  (iii)  $\left\{\frac{1}{2}, 1, \frac{3}{2}\right\}$  (iv)  $\{0, 1, 2\}$

- **9.** (i) {4, 5, 6, ....10} (ii) {5}
- (iii)  $\{1, 2, 3, 4, 5\}$

**10.** 



11.



- **13.** True
- 14. False
- **15.** True

- **16.** True
- **17.** True
- **22.**  $T = \{10\}$
- 24. (i) 2 (ii) 3 (iii) 3 (iv) 9
- **25.** 25
- **26.** 20
- **27.** (a) 3300 (b) 4000
- **28.** (i) 6, (ii) 3, (iii) 9, (iv) 1, (v) 2, (vi) 6, (vii) 30, (viii) 20 **29.** C
- **30.** В
- **31.** B
- **32.** D
- **33.** C

- **34.** D
- **35.** B
- **36.** B
- **37.** C

38. C **39.** C

**40.** A

**41.** B

**42.** В **43.** C

**44.** [1,2]

**45.** 1

**46.** *n* (B)

47.  $A \cap B'$ 

**48.** {\phi, {1}, {2}, {1, 2}

**49.** 

{0, 1, 2, 3, 4, 5, 6, 8} **50.**(i) {1,5, 9, 10} (ii) {1, 2,3, 5, 6, 7, 9, 10}

**51.**  $A \cup B'$ 

True

**52.** (i)  $\leftrightarrow$  (b) (ii)  $\leftrightarrow$  (c) (iii)  $\leftrightarrow$  (a) (iv)  $\leftrightarrow$  (f) (v)  $\leftrightarrow$  (d) (vi)  $\leftrightarrow$  (e) **54.** False

55. False

**56.** True

**57.** True

**53.** 

58. False

## 2.3 EXERCISE

(i)  $\{(-1, 1), (-1, 3), (2, 1), (2, 3), (3, 1), (3, 3)\}$ 

(ii)  $\{(1,-1), (1,2), (1,3), (3,-1), (3,2), (3,3)\}$ 

(iii)  $\{(1, 1), (1, 3), (3, 1), (3, 3)\}$ 

(iv)  $\{(-1,-1),(-1,2),(-1,3),(2,-1),(2,2),(2,3),(3,-1),(3,2),(3,3)\}$ 

**2.** {(0, 1), (0, 2), (1, 1), (1, 2), (2, 1), (2, 2)}

3. (i)  $\{(0,3),(1,3)\}$ 

(ii)  $\{(0,2), (0,3), (0,4), (0,5), (1,2), (1,3), (1,4), (1,5)\}$ 

4. (i)  $a = \frac{11}{3}$  and  $b = \frac{2}{3}$  (ii) a = 0 and b = -2

**5.** (i) {(1, 4), (2, 3), (3, 2), (4, 1)}

(ii)  $\{(1, 1), (1, 2), (1, 3), (2, 1), (2, 2), (3, 1)\}$ 

(iii)  $\{(4,5),(5,4),(5,5)\}$ 

**6.** Domain of  $R = \{0, 3, 4, 5\} = Range of R$ 

7. Domain of  $R_1 = [-5, 5]$  and Range of  $R_1 = [-3, 17]$ 

8.  $R_2 = \{(0, 8), (8, 0), (0, -8), (-8, 0)\}$ 

9. Domain of  $R_3 = \mathbf{R}$  and range of  $R_3 = \mathbf{R}^+ \cup \{0\}$ 

10. (i) h is not a function (ii) f is a function (iii) g is a function (iv) s is a function(v) t is a constant function

**11.** (a) 6

(b)  $\frac{1364}{4}$  (c) 13 (d)  $t^2-4$  (e) t+5

**12.** (a) x = 4 (b) x > 4

**13.** (i)  $(f+g) x = x^2 + 2x + 2$ 

(ii) (f - g)  $x = 2x - x^2$ 

(iii) 
$$(fg) x = 2x^3 + x^3 + 2x + 1$$
 (iv)  $\left(\frac{f}{g}\right) x = \frac{2x+1}{x^2+1}$ 

**14.** (i) 
$$f = \{(-1, 0), (0, 1), (3, 28), (7, 344), (9, 730)\}$$

**15.** 
$$x = -1$$
,  $\frac{4}{3}$ 

**16.** Yes, 
$$\alpha = 2$$
,  $\beta = -1$ 

17. (i) 
$$R - \{2n\pi : n \in Z\}$$

$$(iv)R - \{-1, 1\}$$

(v) 
$$R - \{4\}$$

**18.** (i) 
$$[\frac{3}{2}, \infty)$$
 (ii)  $(-\infty, 1]$  (iii)  $[0, \infty)$  (iv)  $[-2, 4]$ 

(iv) 
$$[-2, 4]$$

19. 
$$f(x) = \begin{cases} -2x, -3 \le x < -2 \\ 4, -2 \le x < 2 \\ 2, 2 \le x \le 3 \end{cases}$$

**21.** (i) 
$$(f+g) x = \sqrt{x} + x$$

(ii) 
$$(f-g) x = \sqrt{x} - x$$

(iii) 
$$(fg) x = \frac{3}{x^2}$$

(iv) 
$$\left(\frac{f}{g}\right)x = \frac{1}{\sqrt{x}}$$

22. Domain of 
$$f = (5, \infty)$$
 and Range of  $f = R^+$ 

- **24.** D
- **25.** D
- **26.** B
- **27.** C

- **28.** B
- **29.** B
- **30.** A
- **31.** C

- **32.** C
- **33.** A
- **34.** B
- **35.** A

- **36.** {2, 3, 4, 5}
- 37. (a)  $\leftrightarrow$  (iii) (b)  $\leftrightarrow$  (iv) (c)  $\leftrightarrow$  (ii) (d)  $\leftrightarrow$  (i)

- 38. False
- 39. False
- **40.** True
- 41. False

**42.** True.

4. 
$$\frac{56}{33}$$

$$5. \ \frac{2\cos x}{\sqrt{\cos 2x}}$$

8. 
$$\frac{1}{\sqrt{2}+1}$$

**15.** 
$$\theta = n\pi + (-1)^n \frac{\pi}{4} - \frac{\pi}{4}$$

$$16. \quad \theta = 2n\pi + \frac{7\pi}{4}$$

**17.** 
$$\theta = 2n\pi \pm \frac{\pi}{3}$$

**18.** 
$$\theta = \frac{\pi}{3}, \frac{5\pi}{3}$$

**19.** 
$$x = \frac{\pi}{6}, \frac{\pi}{4}, \frac{\pi}{2}$$

**25.** 
$$\frac{23}{17} \left( \frac{\sqrt{3} - 1}{2} + \frac{1}{\sqrt{2}} \right)$$

**26.** 
$$\frac{3}{2}$$

27. 
$$n\pi \pm \frac{\pi}{4}$$

28. 
$$\frac{n\pi}{2} \pm \frac{\pi}{8}$$

**29.** 
$$\theta = 2n\pi \pm \frac{\pi}{4} + \frac{\pi}{12}$$

61. 
$$\frac{1}{8}$$

**63.** 
$$\frac{1}{4} [4 - 3(a^2 - 1)^2], \sqrt{2 - a^2}$$

**64.** 
$$x^2 - \frac{2}{\sin 2A}x + 1$$
 **65.** 13

64. 
$$x - \frac{1}{\sin 2A}$$

**76.** (a) 
$$\leftrightarrow$$
 (iv) (b)  $\leftrightarrow$  (i) (c)  $\leftrightarrow$  (ii) (d)  $\leftrightarrow$  (iii)

**1.** 
$$P(n): 2n < \angle n$$

2. 
$$P(n): 1+2+3+...+n = \frac{n(n+1)}{2}$$

**26.** A

**27.** B

**28.** A

**29.** 4

30. False

#### 5.3 EXERCISE

 $2^n$ 1.

2. -1+i 3. (0,-2) 4.  $\frac{2}{5}$ 

(1,0) 6.  $i\cot \frac{\theta}{2}$  11.  $\frac{3}{2}-2i$  12.  $\frac{1}{2}-2i$ 

**13.** 1:3

**14.**  $\left(\frac{10}{3}, 0\right), \frac{2}{3}$  **15.** 1 **18.** 0

**21.**  $\sqrt{2} \pm i\sqrt{2}, -\sqrt{2} \pm i\sqrt{2}$ 

**22.** -2-i

23.  $\sqrt{2} \left( \cos \frac{5\pi}{12} + i \sin \frac{5\pi}{12} \right)$ 

**25.** (i)  $(a^2 + b^2)(|z_1|^2 + |z_2|^2)$ 

(ii) -15

(iii) -2 (iv) 0 (v)  $\frac{1}{2} - \frac{i}{2}$ 

(vi)  $\overline{z}_1$  (vii) 0

(viii) 6 and 0 (ix) a circle

 $(x) - 2\sqrt{3} + 2i$ 

**26.** (i) F

(ii) F

(iii) T

(iv) T

(v) T

(vi) T

(vii) F

(viii) F

**27.** (a)  $\leftrightarrow$  (v),

(b)  $\leftrightarrow$  (iii),

(c)  $\leftrightarrow$  (i),

(d)  $\leftrightarrow$  (iv),

(e)  $\leftrightarrow$  (ii),

(f)  $\leftrightarrow$  (vi),

 $(g) \leftrightarrow (viii)$  and

(h)  $\leftrightarrow$  (vii)

28. 
$$\frac{-2}{25} - i\frac{11}{25}$$
 29. No

30. 
$$\frac{(a^2+1)^4}{4a^2+1}$$

**30.** 
$$\frac{(a^2+1)^4}{4a^2+1}$$
 **31.**  $-2\sqrt{3}+2i$ 

33. 
$$\frac{2\pi}{3}$$

1. 
$$\frac{1}{3} \le x \le 1$$

1. 
$$\frac{1}{3} \le x \le 1$$
 2.  $[0,1] \cup [3,4]$  3.  $(-\infty, -5) \cup (-3, 3) \cup [5, \infty)$ 

4. 
$$[-4,-2] \cup [2,6]$$
 5.  $\left[\frac{-34}{3},\frac{22}{3}\right]$  6. No Solution

- 7. More than 2000.
- **8.** Between 7.77 and 8.77.
- More than 230 litres but less than 920 litres.
- 10. Between 104 °F and 113 °F
- 11. 41 cm.
- 12. Between 8 km and 10 km
- 13. No Solution
- **14.**  $x + y \le 20$ ,  $3x + 2y \le 48$ ,  $x \ge 0$ ,  $y \ge 0$
- **15.**  $x + y \le 8$ ,  $x + y \ge 4$ ,  $x \le 5$ ,  $y \le 5$ ,  $x \ge 0$ ,  $y \ge 0$
- 17. No Solution.
- **19.** C
- **20.** C
- **21.** A
- **22.** B

- **23.** D
- **24.** C
- **25.** B
- **26.** A

- **28.** B
- **29.** A
- **30.** B

- **27.** D **31.** (i) F
- (ii) F
- (iii) T
- (iv) F

- (v) T
- (vi) F
- (vii) T
- (viii) F

(xii) F

(xiii)F (xiv) T (xv) T. 32. (i)  $\leq$ (ii) ≥ (iii) >(iv) > (v) > (vi) >(vii) < , >  $(viii) \leq .$ 7.3 EXERCISE **4.** 144 **1.** 1440 **2.** 481 **3.** 780 **6.** 3960 **5.** 22 **7.** 4,68000 **8.** 200 9.  $^{n-3}C_{r-3}(r-2)!3!$  10. 14400 **11.** 112 **15.** r = 3**17.** 190 **16.** 192 **18.** 8400 **19.** 3 **20.** 11 **22.** (a)  $11C_4$  (b)  $6C_2 \times 5C_2$  (c)  $6C_4 + 5C_4$ **23.** (i) 14C<sub>9</sub> (ii) 14C<sub>11</sub> **24.**  $2(20C_5 \times 20C_6)$ **25.** (i) 21, (ii) 441 (iii) 91 **26.** A **27.** B **28.** C **29.** B **30.** C **31.** A **32.** B **33.** D **34.** B **35.** C **36.** D **37.** A 38. C **39.** B **42.** 0 **40.** B **41.** n = 7**43.**  $n^r$ **46.** 5<sup>6</sup> **44.** 1,51,200 **45.** 80 **47.** 18 **48.** 35 **49.** 7800 **50.** 64 **51.** False **52.** False **53.** False **54.** True 55. True **56.** True **57.** True 58. False **59.** False **60.** (a)  $\leftrightarrow$  (ii) (b)  $\leftrightarrow$  (iii) and  $(c) \leftrightarrow (i)$ **61.** (a)  $\leftrightarrow$  (iii) (b)  $\leftrightarrow$  (i)  $(c) \leftrightarrow (iv),$  $(d) \leftrightarrow (ii)$ **62.** (a)  $\leftrightarrow$  (iv) (b)  $\leftrightarrow$  (iii)  $(d) \leftrightarrow (i)$  $(c) \leftrightarrow (ii),$ **63.** (a)  $\leftrightarrow$  (i) (b)  $\leftrightarrow$  (iii)  $(c) \leftrightarrow (iv),$  $(d) \leftrightarrow (ii)$ **64.** (a)  $\leftrightarrow$  (iii)  $(c) \leftrightarrow (ii)$ (b)  $\leftrightarrow$  (i) 8.3 EXERCISE

1.  ${}^{15}C_{10} \left(\frac{1}{6}\right)^5$  2.  $k = \pm 3$  3. -19 4.  $-3003 (3^{10}) (2^5)$ 

(xi) T

(ix) T

(x) F

**5.** (i) 
$$-252$$
 (ii)  $\frac{189}{8}x^{17}$ ;  $\frac{-21}{16}x^{19}$  **6.**  $-252$  **7.**  $-1365$  **8.**  $252y^{\frac{5}{2}}x^{\frac{5}{3}}$ 

**6.** 
$$-252$$
 **7.**  $-1365$  **8.**  $252y^{\frac{5}{2}}x^{\frac{5}{2}}$ 

9. 
$$r = 6$$

**9.** 
$$r = 6$$
 **11.** 990 **12.**  $p = \pm 2$  **14.**  $n = 9$ 

**14.** 
$$n = 9$$

17. 
$$\frac{17}{54}$$
 18. (C) 19. (A) 20. (C)

**25.** 
$${}^{30}C_{15}$$
 **26.**  $\frac{(n+1)(n+2)}{2}$  **27.**  ${}^{16}C_8$  **28.**  $n=12$ 

27. 
$$^{16}C_8$$

**28.** 
$$n = 12$$

**29.** 
$$\frac{1120}{27} a^{-6} a^4$$
 **30.**  $^{28}$  C<sub>14</sub>  $a^{56} b^{14}$  **31.** 1 **32.** Third term

30. 
$$^{28}$$
 C<sub>14</sub>  $a^{56}$   $b^{14}$ 

7. 
$$\frac{15}{8}$$
 cm 8. 2480 m 9. Rs 725

**11.** (i) 
$$4n^3 + 9n^2 + 6n$$
 (ii) 4960

12. 
$$T_r = 6r - 1$$
 17. D  
20. B 21. C

27. 
$$\frac{a}{z}$$
 or  $\frac{b}{z}$ 

27. 
$$\frac{a}{b}or\frac{b}{c}$$
 28. First term + last term

**35.** (a) 
$$\leftrightarrow$$
 (iii) (b)  $\leftrightarrow$  (i) (c)  $\leftrightarrow$  (ii)

**36.** (a) 
$$\leftrightarrow$$
 (iii) (b)  $\leftrightarrow$  (i) (c)  $\leftrightarrow$  (ii)(d)  $\leftrightarrow$  (iv)

1. 
$$x + y + 1 = 0$$

**1.** 
$$x + y + 1 = 0$$
 **2.**  $x - 4y + 3 = 0$  **3.**  $60^{\circ}$  or  $120^{\circ}$ 

4. 
$$x + y = 7 \text{ or } \frac{x}{6} + \frac{y}{8} = 1$$

7. 
$$y - \sqrt{3}x - 2 + \sqrt{3} = 0$$

8. 
$$3x + 4y + 3 = 0$$

9. 
$$a = \frac{-8}{3}, b = 4$$

**10.** 
$$8x - 5y + 60 = 0$$

11. 
$$\sqrt{3}x + y = 8$$

**12.** 
$$x - 7y - 12 = 0$$

13. 
$$\sqrt{\frac{2}{3}}$$

17. 
$$9x - 20y + 96 = 0$$

**18.** 
$$3x - 4y + 6 = 0$$
 and  $4x - 3y + 1 = 0$ 

**20.** 
$$(0, 2 + \frac{5\sqrt{3}}{2})$$

**42.** 
$$(1, -2)$$

$$\frac{12}{2}$$
  $x + y + 1 = 0$ 

**44.** 
$$3x - y - 7 = 0, x + 3y - 9 = 0$$

**43.** 
$$x + y + 1 = 0$$

**45.** opposite sides **46.** 13 
$$(x^2 + y^2) - 83 x + 64 y + 182 = 0$$

**47.** 4 
$$x^2$$
  $y^2 = p^2 (x^2 + y^2)$ 

$$57. (a) \leftrightarrow (iii)$$

(b) 
$$\leftrightarrow$$
 (i) and

$$(c) \leftrightarrow (ii)$$

$$58. (a) \leftrightarrow (iv)$$

(b) 
$$\leftrightarrow$$
 (iii)

(c) 
$$\leftrightarrow$$
 (i),

$$(d) \leftrightarrow (ii)$$

**59.** (a) 
$$\leftrightarrow$$
 (iii)

(b) 
$$\leftrightarrow$$
 (i)

(c) 
$$\leftrightarrow$$
 (iv),

$$(d) \leftrightarrow (ii)$$

1. 
$$x^2 + y^2 - 2ax - 2ay + a^2 = 0$$

3. 
$$\left(\frac{a}{2}, \frac{b}{2}\right)$$

$$4. \quad x^2 + y^2 - 2x - 4y + 1 = 0$$

5. 
$$\frac{3}{4}$$

$$6. \quad x^2 + y^2 + 4x + 4y + 4 = 0$$

8. 
$$x^2 + y^2 - 2x + 4y - 20 = 0$$

**9.** 
$$k \pm 8$$

$$10. \quad x^2 + y^2 - 6x + 12y - 15 = 0$$

11. 
$$\frac{\sqrt{3}}{2}$$

12. ecentricity = 
$$\frac{4}{5}$$
 and foci (4, 0) and (-4, 0)

13. 
$$\frac{39}{4}$$

14. 
$$\frac{4x^2}{81} + \frac{4y^2}{45} = 1$$
 15. 18

17. 
$$\frac{4a\cos\theta}{\sin^2\theta}$$
 18.  $x^2 + 8y = 32$  19.  $m = 1$  20.  $x^2 - y^2 = 32$ 

8. 
$$x^2 + 8y = 32$$

**19.** 
$$m = 1$$

**20.** 
$$x^2 - y^2 = 32$$

21. 
$$\frac{\sqrt{13}}{2}$$

22. 
$$\frac{x^2}{4} - \frac{y^2}{5} = \frac{4}{9}$$

21. 
$$\frac{\sqrt{13}}{2}$$
 22.  $\frac{x^2}{4} - \frac{y^2}{5} = \frac{4}{9}$ . 23.  $x^2 + y^2 - 2x + 2y = 47$ 

**24.** 
$$x^2 + y^2 - 4x - 10y + 25 = 0$$

**25.** 
$$(x-3)^2 + (y+1)^2 = 38$$
  
**27.**  $x^2 + y^2 - 8x - 6y + 16 = 0$ 

**26.** 
$$x^2 + y^2 - 18x - 16y + 120 = 0$$

27. 
$$x^2 + y^2 - 8x - 6y + 16 = 0$$

**28.** (a) 
$$y^2 = 12x - 36$$
, (b)  $x^2 = 32 - 8y$ , (c)  $4x^2 + 4xy + y^2 + 4x + 32y + 16 = 0$ 

$$30. 9x^2 + 5y^2 = 180$$

$$29. \quad 3x^2 + 4y^2 - 36x = 0$$

32. (a) 
$$15x^2 - y^2 = 15$$
 (b)  $9x^2 - 7y^2 + 343 = 0$ , (c)  $y^2 - x^2 = 5$ 

**41.** 
$$(x-3)^2 + (y+4)^2 = \left(\frac{45}{13}\right)^2$$

**42.** 
$$x^2 + y^2 - 46x + 22y = 0$$

**43.** 
$$6+2\sqrt{5}$$
,  $2\sqrt{5}$ 

44. 
$$\frac{4x^2}{1} + \frac{4y^2}{5} = 1$$

**45.** 
$$4x^2 + 4xy + y^2 + 4x + 32y + 16 = 0$$
 **46.**  $\frac{y^2}{36} - \frac{x^2}{64} = 1$  and  $(0, \pm 10)$ .

**16.** 
$$\frac{y^2}{36} - \frac{x^2}{64} = 1$$
 and  $(0, \pm 10)$ 

```
51. A 52. B 53. A 54. A 555. D 56. B 57. C 58. A 59. A
```

- 2. (i) 1<sup>st</sup> octant (ii) 4<sup>th</sup> octant (iii) viii<sup>th</sup> octant (iv) v<sup>th</sup> octant (v) 2<sup>nd</sup> octant (vi) 3<sup>rd</sup> octant (vii) viii<sup>th</sup> octant (viii) viih octant
- **3.** (i) (3,0,0), (0,4,0), (0,0,2) (ii) (-5, 0, 0), (0,3,0), (0,0,7) (iii) (4,0,0), (0,-3, 0), (0,0,5)
- **4.** (i) (3,4,0), (0,4,5), (3,0,5) (ii) (-5, 3, 0),(0,3,7), (-5, 0, 7) (iii) (4,-3, 0), (0,-3,-5), (4, 0, -5)
- **5.** 5 **6.** 11 **9.** (2,-4, 16) **11.** (-2, -2, -1) **12.** (1, 1, -2) **13.** (-3, 4, -7), (7, 2, 5) and (-3, 12, 17) **14.** (4, 7, 6)
- **15.** (4, -5, 1), (3, -2, -1) **16.** a = -2, b = -8, c = 2
- 17.  $\left(\frac{7}{2}, \frac{13}{2}, 9\right)$  18. 2:1 externally
- **19.** vertices are (3,4,5), (-1,6,-7), (1,2,3) and centroid is  $(1,4,\frac{1}{3})$
- 20. 1:3 externally
- **21.** (2,0,0), (2,2,0), (0,2,0), (0,2,2) (0,0,2) (2,0,2), (0,0,0), (2,2,2)
- 22. A 23. B 24. A 25. B
- 26. A 27. B 28. B 29. A
- **30.** A **31.** B **32.** A **33.** D
- 34. A 35. Three coordinates planes 36. Three pairs
- **37.** given point **38.** Eight **39.** (0, y, z) **40.** x = 0
- **41.** (0, 0, z) **42.** x = 0, y = 0 **43.** z- coordinates
- **44.** (y, z coordinates) **45.** yz-plane **46.** x-axis **47.**  $\sqrt{333}$
- **48.** a = 5 or -3 **49.** (1, 1, -2)
- **50.** (a)  $\leftrightarrow$  (iii) (b)  $\leftrightarrow$  (i) (c)  $\leftrightarrow$  (ii) (d)  $\leftrightarrow$  (vi) (e)  $\leftrightarrow$  (iv) (f)  $\leftrightarrow$  (v) (g)  $\leftrightarrow$  (viii) (h)  $\leftrightarrow$  (vii) (i)  $\leftrightarrow$  (x) (j)  $\leftrightarrow$  (ix)

3. 
$$\frac{1}{\sqrt[2]{x}}$$

3. 
$$\frac{1}{\sqrt[2]{x}}$$
 4.  $\frac{1}{3}2^{\frac{-2}{3}}$ 

6. 
$$\frac{5}{2}(a+2)^{\frac{3}{2}}$$
 7. 7

9. 
$$\frac{8}{5}$$

11. 0 12. 
$$\frac{1}{15}$$

**13.** 
$$\frac{7}{2}$$
 **14.**  $n = 5$  **15.**  $\frac{3}{7}$  **16.**  $\frac{1}{4}$ 

**14.** 
$$n = 3$$

15. 
$$\frac{3}{7}$$

16. 
$$\frac{1}{2}$$

19. 
$$\frac{m^2}{n^2}$$
 20. 3

21. 
$$\sqrt{2}$$
 22. 2

23. 1 24. 
$$2\sqrt{a}\cos a$$

**25.** 4 **26.** 
$$\frac{1}{4\sqrt{2}}$$
 **27.** 0 **28.**  $k = \frac{3}{8}$ 

**28.** 
$$k = \frac{3}{8}$$

**29.** 
$$3x^2 + 2x + 1 - \frac{1}{x^2}$$

30. 
$$3x^2 - \frac{3}{x^2} - \frac{3}{x^4} + 3$$

31. 
$$3x \sec^2 x + 5\sec^2 x + 3\tan x + 3$$

32. 
$$2\tan x \sec^2 x$$

$$33. \quad \frac{55 - 40x - 15x^2}{\left(5x^2 - 7x + 9\right)^2}$$

34. 
$$\frac{-x^5\cos x + 5\sec^4\sin x + 1}{\sin^2 x}$$

$$35. \quad \frac{x}{\sqrt{2}} \csc x (2 - x \cot x)$$

**36.** 
$$(ax^2 + \cot x)(-q\sin x) + (p+q\cos x)(2ax - \csc^2 x)$$

37. 
$$\frac{bc\cos x + ad\sin x + db}{\left(c + d\cos x\right)^2}$$

38. 
$$2\cos 2x$$

39. 
$$(2x-7)(30x-43)(3x+5)^2$$

**40.** 
$$x^2 \cos x + 2x \sin x - 2 \sin 2x$$

41. 
$$\frac{3}{4}\sin^2 2x\cos 2x$$

$$42. \frac{-(2ax+b)}{\left(ax^2+bx+c\right)^2}$$

43. 
$$-2x\sin(x^2+1)$$

44. 
$$\frac{ad-bc}{(cx+d)^2}$$

45. 
$$\frac{2}{3}x^{-\frac{1}{3}}$$

46. 
$$\cos x - x \sin x$$

47. 
$$\sec x(x\tan x + 1)$$

48. 
$$\frac{2\alpha}{\alpha^2 - \beta^2}$$

**50.** 
$$\frac{1}{\sqrt{2}}$$

**52.** 
$$k = 6$$

**53.** 
$$c = 1$$

**78.** 
$$m = \frac{2\sqrt{3}}{3}$$

- 1. (i) to (v) and (viii) to (x) are statements.
- 2. (i) p: Number 7 is prime q: Number 7 is odd
  - (iii) p:100 is divisble by 3
    - q:100 is divisible by 11 r:100 is divisible by 5
- (ii) p: Chennai is in India
  - q: Chennai is capital of Tamil Nadu
- (iv) p: Chandigarh is capital of Haryana
  - q: Chandigarh is the capital of U.P

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- (v)  $p:\sqrt{7}$  is a rational number (vi) p:0 is less than every positive integer
  - $q: \sqrt{7}$  is an irrational number q: 0 is less than every negative integer
- (vii) p: plants use sunlight for photosynthesis
  - q: plants use water for photosynthesis
  - r: plants use carbondioxide for photosynthesis
- (viii) p: two lines in a plane intersect at one point
  - q: two lines in a plane are parallel
- (ix) p: a rectangle is a quadrilateral
  - q: a rectangle is a 5- sided polygons.
- 3. (i) Compound statement is true and its component statements are :
  - p:57 is divisible by 2 and q:57 is divisble by 3
  - (ii) component statement is true and its component statements are :
    - p: 24 is multiple of 4 and q: 24 is multiple of 6
  - (iii) component statement is false and is component statements are
    - p: All living things have two eyes
    - q: All living things have two legs
  - (iv) component statement is true and its component statements are :
    - p: 2 is an number; q: 2 is a prime number
- 4. (i) The number 17 is not prime (ii)  $2 + 7 \neq 6$  (iii) Violet are not blue
  - (iv)  $\sqrt{5}$  is not a rational number (v) 2 is a prime number
  - (vi) There exists a real number which is not an irrational number
  - (vii) Cow has not four legs (viii) A leap year has not 366 days
  - (ix) There exist similar triangles which are not congruent
  - (x) Area of a circle is not same as the perimeter of the circle
- 5. (i)  $p \wedge q$  where p: Rahul passed in Hndi; q: Rahul passed in English
  - (ii)  $p \wedge q$  where p: x is even integer; q: y is even integer
  - (iii)  $p \land q \land r$  where p:2 is factor of 12; q:3 is factor of 12; r:6 is factor of 12
  - (iv)  $p \lor q$  where p : x is an odd integer; q : x + 1 is an odd integer
  - (v)  $p \lor q$  where p : a number is divisible by 2, q : it is divisible by 3
  - (vi)  $p \lor q$  where p : x = 2 is a root of  $3x^2 x 10 = 0$ , q : x = 3 is a root of  $3x^2 x 10 = 0$

- (vii)  $p \lor q$  where p: student can take Hindi as an optional paper and q: student can take English as an optional paper.
- **6.** (i) It is false that all rational numbers are real and complex
  - (ii) It is false that all real numbers are rational or irrational
  - (iii) x = 2 is not a root of the quadratic equation  $x^2 5x + 6 = 0$  or x = 3 is not a root of the quadratic equation  $x^2 5x + 6 = 0$
  - (iv) A triangle has neither 3-sides nor 4-sides
  - (v) 35 is not a prime number and it is not a complex number
  - (vi) It is false that all prime integers are either even or odd
  - (vii) |x| is not equal to x and it not equal to -x
  - (viii) 6 is not divisible by 2 or it is not divisible by 3.
- 7. (i) If the number is odd number then its square is odd number
  - (ii) If you take the dinner then you will get sweet dish
  - (iii) If you will not study then you will fail
  - (iv) If an integer is divisible by 5 then its unit digits are 0 or 5
  - (v) If the number is prime then its square is not prime
  - (vi) If a,b and c are in A.P then 2b = a + c.
- **8.** (i) The unit digit of an integer is zero if and only if it is divisible by 5.
  - (ii) A natural number n is odd if and only if it is not divisible by 2.
  - (iii) A triangle is an equilateral triangle if and only if all three sides of triangle are equal.
- 9. (i) If  $x \neq 3$  then  $x \neq y$  or  $y \neq 3$ 
  - (ii) If n is not an integer then it is not a natural number.
  - (iii) If the triangle is not equilateral then all three sides of the triangle are not equal
  - (iv) If xy is not positive integer then either x or y is not negative integer.
  - (v) If natural number *n* is not divisible by 2 and 3 then *n* is not divisible by 6.
  - (vi) The weather will not be cold if it does not snow.
- **10.** (i) If the rectangle R is rhombus then it is square.
  - (ii) If tomorrow is Tuesday then today is Monday.
  - (iii) If you must visit Taj Mahal you go to Agra.

- (iv) If the triangle is right angle then sum of squares of two sides of a triangle is equal to the square of third side.
- (v) If the triangle is equilateral then all three anlges of triangle are equal.
- (vi) If 2x = 3y then x:y = 3:2
- (vii) If the opposite angles of a quadrilaterals are supplementary then S is
- (viii) If x is neither positive nor negative than x is 0.
- (ix) If the ratio of corresponding sides of two triangles are equal then trianges are similar.
- (i) There exists (ii) For all (iii) There exists (iv) For every (v) For all (vi) There exists (vii) For all (viii) There exists (ix) There exists (x) There exists
- 17... C
- 18. D
- **19.** B
- **20.** D

- **21.** C
- **22.** B
- 23. A
- **24.** B

- 25. C
- **26.** A
- 27. C
- **28.** B

- **29.** A
- **30.** C
- **31.** B
- **32.** A

- **33.** C
- **34.** A
- 35. C
- **36.** D
- 37. (i), (ii) and (iv) are statement; (iii) and (v) are not statements.

- 0.32
- **2.** 1.25

- **6.** 3.87
- 7.  $\sqrt{\frac{n_1(s_1)^2 + n_2(s_2)^2}{n_1 + n_2} + \frac{n_1 n_2 (\overline{x}_1 \overline{x}_2)^2}{(n_1 + n_2)^2}}$

- 5.59
- **9.** 7
- **10.** 1.38
- 11. Mean = 2.8, SD = 1.12
- **12.** 8.9

**13.** 5000, 251600

- 15. Mean = 5.5, Var. = 4.26
- **14.** Mean = 5.17, SD = 1.53
- **16.** 0.99

**17.** 7.08

18. Mean =  $\frac{239}{40}$ , SD = 2.85

**20.** Mean = 
$$a + \frac{d(n-1)}{2}$$
,

$$S.D = d \sqrt{\frac{n^2 - 1}{12}}$$

21. Hashina is more intelligent and consistent

**23.** Mean = 
$$42.3$$
, Var.  $43.81$ 

- 1.  $\frac{1}{72}$  2.  $\frac{2}{3}$
- **3.** 0.556
- 4. (a)  $5^{k-1}$  elements (b)  $\frac{5^k-1}{4}$  5.  $\frac{4}{9}$  6. 0.93

- (a) 0.65 (b) 0.55 (c) 0.8 (d) 0 (e) 0.35 (f) 0.2

- (a) 0.35 (b) 0.77 (c) 0.51 (d) 0.57 **9.** (a)  $\frac{2}{9}$  (b)  $\frac{5}{9}$
- 10. (a)p(John promoted) =  $\frac{1}{8}$ , p(Rita promoted) =  $\frac{1}{4}$ , p(Aslam promoted) =  $\frac{1}{2}$ ,  $p(Gurpreet promoted) = \frac{1}{8}$  (b)  $P(A) = \frac{1}{4}$
- **11.** (a) 0.20 (b) 0.17 (c) 0.45 (d) 0.13 (e) 0.15 (f) 0.51

- **12.** (a)  $S = \{B_1B_2, B_1W, B_2B_1, B_2W, WB_1, WB_2BW_1, BW_2, W_1B, W_1W_2, W_2B, W_2W_1\}$ 
  - (b)  $\frac{1}{6}$  (c)  $\frac{2}{3}$

**13.** (a) 
$$\frac{5}{143}$$
 (b)  $\frac{28}{143}$  (c)  $\frac{40}{143}$ 

**13.** (a) 
$$\frac{5}{143}$$
 (b)  $\frac{28}{143}$  (c)  $\frac{40}{143}$  **14.** (a)  $\frac{2}{143}$  (b)  $\frac{2}{143}$  (c)  $\frac{25}{26}$  (d)  $\frac{15}{26}$ 

15. 
$$\frac{7}{13}$$

**16.** (a) 
$$p(A) = .25$$
,  $p(B) = .32$ ,  $p(A \cap B) = .17$  (b)  $p(A \cup B) = .40$  (c) .40 (d) .68

17. (a) 
$$\frac{1}{2}$$
 (b)  $\frac{3}{4}$  (c)  $\frac{3}{26}$  (d)  $\frac{5}{36}$ 

**18.** A **19.** B

**22.** D 23. A

**26.** B **27.** C

30. False **31.** False

**34.** True 35. False

**38.** 0.3

**39.** 
$$\overline{E} = \{2,4,6\}$$

**41.** 0.2

**42.** (a) 
$$\leftrightarrow$$
 (iv) (b)  $\leftrightarrow$  (v) (c)  $\leftrightarrow$  (i) (d)  $\leftrightarrow$  (iii) (e)  $\leftrightarrow$  (ii)

**43.** (a) 
$$\leftrightarrow$$
 (iv) (b)  $\leftrightarrow$  (iii) (c)  $\leftrightarrow$  (ii) (d)  $\leftrightarrow$  (i)