# CBSE Class-12 Physics Quick Revision Notes Chapter-03: Current Electricity

# • Electrical Conductivity:

It is the inverse of specific resistance for a conductor whereas the specific resistance is the resistance of unit cube of the material of the conductor.

$$\sigma = \frac{1}{\rho} = \frac{ne^2\tau}{m}$$

Where  $\sigma$  is the conductivity and  $\rho$  is resistivity.

### • SI Unit of Conductivity:

The SI unit of conductivity is mhom-1.

### • Current through a given area of a conductor:

It is the net charge passing per unit time through the area.

## • Current Density Vector:

The current density vector  $\vec{J}$  gives current per unit area flowing through area  $\Delta A$  when it is held normal to the direction of charge flow. Note that the direction of  $\vec{J}$  is in the direction of current flow.

### Current Density:

Current density j gives the amount of charge flowing per second per unit area normal to the flow.

$$J = nqV_d$$

where n is the number density (number per unit volume) of charge carriers each of charge q and vd is the drift velocity of the charge carriers. For electrons q = -e. If j is normal to a cross – sectional area A and is constant over the area, the magnitude of the current I through the area is  $neV_dA$ .

#### • Mobility:

Mobility <sup>H</sup> is defined to be the magnitude of drift velocity per unit electric field.

$$\mu = \left(\frac{V_d}{E}\right)$$

Now, 
$$V_d = \frac{q\tau E}{m_q}$$

where q is the electric charge of the current carrier and mq is its mass.

$$\therefore \mu = \left(\frac{q_{\tau}}{m_q}\right)$$

Thus, mobility is a measure of response of a charge carrier to a given external electric field.

## • Resistivity:

Resistivity  $\rho$  is defined to be reciprocal of conductivity.

$$\rho = \frac{1}{\sigma}$$

It is measured in ohm-metre (Qm).

# • Resistivity as a function of temperature:

It is given as,

$$\rho_T = \rho_0 [1 + \alpha (T - T_0)]$$

Where  $\alpha$  is the temperature coefficient of resistivity and  $\rho_{\scriptscriptstyle T}$  is the resistivity of the material at temperature T.

## • Ranges of Resistivity:

- a) Metals have low resistivity: Range of  $\rho$  varies from  $10^{-8} \Omega$  m to  $10^{-6} \Omega$  m.
- b) Insulators like glass and rubber have high resistivity: Range of  $\rho$  varies from  $10^{22}$  to  $10^{24}$  times greater than that of metals.
- c) Semiconductors like Si and Ge lie roughly in the middle range of resistivity on a logarithmic scale.

### • Total resistance in Series and in Parallel

- (a) Total resistance R of n resistors connected in series is given by R = R1 + R2 + ... + Rn
- (b) Total resistance R of n resistors connected in parallel is given by

$$\frac{1}{R} = \frac{1}{R_1} + \frac{1}{R_2} + \dots + \frac{1}{R_n}$$

• If the mass of a charge carrier is large, then for a given field  $\overrightarrow{E}$ , its acceleration will be small and will contribute very little to the electric current.

# • Electrical Conductivity:

When a conducting substance is brought under the influence of an electric field  $\overrightarrow{E}$ , free charges (e.g. free electrons in metals) move under the influence of this field in such a manner, that the current density  $\overrightarrow{J}$  due to their motion is proportional to the applied electric field.

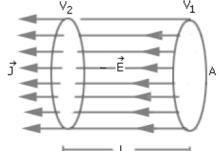
$$\vec{J} = \sigma \vec{E}$$

where  $\sigma$  is a constant of proportionality called electrical conductivity. This statement is one possible form of Ohm's law.

• Consider a cylindrical material with cross sectional area A and length L through which a current is passing along the length and normal to the area A, then, since  $\overrightarrow{J}$  and  $\overrightarrow{E}$  are in the same direction,

$$J = \sigma E$$
$$JAL = \sigma ELA$$

Where A is cross sectional area and L is length of



the material through which a current is passing along the length, normal to the area A. But, JA = I, the current through the area A and  $EL = V_1 - V_2$ , the potential difference across the ends of the cylinder denoting  $V_1$ - $V_2$  as V,

$$V = \frac{IL}{\sigma A} = RI$$

Where  $R = \frac{L}{\sigma A}$  is called resistance of the material. In this form, Ohm's law can be stated as a linear relationship between the potential drop across a substance and the current passing through it.

## Measuring resistance:

R is measured in ohm (( $\Omega$ )), where  $1\Omega = \frac{1V}{A}$ 

#### EMF:

Emf (Electromotive force) is the name given to a non-electrostatic agency. Typically, it is a battery, in which a chemical process achieves this task of doing work in driving the positive charge from a low potential to a high potential. The effect of such a source is measured in terms of work done per unit charge in moving a charge once around the circuit. This is denoted by  $\in$ .

### Significance of Ohm's Law:

Ohm's law is obeyed by many substances, but it is not a fundamental law of nature. It fails if

- a) V depends on I non-linearly. Example is when  $\rho$  increases with I (even if temperature is kept fixed).
- b) The relation between V and I depends on the sign of V for the same absolute value of V.
- c) The relation between V and I is non-unique. For e.g., GaAs An example of (a) & (b) is of a rectifier
- When a source of emf (( $\varepsilon$ )) is connected to an external resistance R, the voltage  $V_{ext}$  across R is given by

$$V_{ext} = IR = \frac{\mathcal{E}}{R+r}R$$

Where r is the internal resistance of the source.

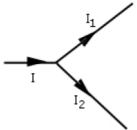
## • Kirchhoff's First Rule:

At any junction of several circuit elements, the sum of currents entering the junction must equal the sum of currents leaving it.

In the above junction, current I enters it and currents  $I_1$  and  $I_2$  leave it. Then,

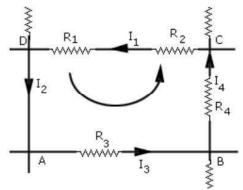
$$I = I_1 + I_2$$

This is a consequence of charge conservation and assumption that currents are steady, that is no charge piles up at the junction.



### Kirchhoff's Second Rule:

The algebraic sum of changes in potential around any closed resistor loop must be zero. This is based on the principle that electrostatic forces alone cannot do any work in a closed loop, since this work is equal to potential difference, which is zero, if we start at one point of the loop and come back to it.



This gives:  $(R_1 + R_2) I_1 + R_3 I_3 + R_4 I_4 = 0$ 

# • In case of current loops:

- i) Choose any closed loop in the network and designate a direction (in this example counter clockwise) to traverse the loop.
- ii) Go around the loop in the designated direction, adding emf's and potential differences. An emf is counted as positive when it is traversed (-) to (+) and negative in the opposite case i.e., from (+) to (-). An IR term is counted negative if the resistor is traversed in the same direction of the assumed current, and positive if in the opposite direction.
- iii) Equate the total sum to zero.

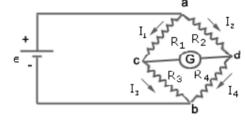
# • Wheatstone Bridge:

Wheatstone bridge is an arrangement of four resistances  $R_1$ ,  $R_2$ ,  $R_3$ ,  $R_4$ . The null point condition is given by,

$$\therefore \frac{R_1}{R_2} = \frac{R_3}{R_4}$$

This is also known as the balanced condition. If  $R_1$ ,  $R_2$ ,  $R_3$  are known,  $R_4$  can be determined.

$$R_4 = \left(\frac{R_2}{R_1}\right) R_3$$



• In a balanced condition of the meter bridge,

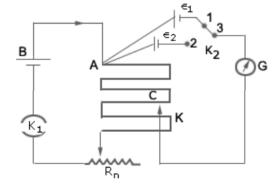
$$\frac{R}{S} = \frac{P}{Q} = \frac{\sigma l_1}{100 - l_1}$$

$$\therefore R = \frac{Sl_1}{(100 - l_1)}$$

Where  $\sigma$  is the resistance per unit length of wire and  $l_1$  is the length of wire from one end where null point is obtained.

# Potentiometer:

The potentiometer is a device to compare potential differences. Since the method involves a condition of no current flow, the device can be used to measure potential differences; internal resistance of a cell and compare emf's of two sources.



## • Potential Gradient:

The potential gradient of the wire in a potentiometer depends on the current in the wire.

• If an emf  $\in$ <sub>1</sub> is balanced against length  $l_1$ , then  $\in$ <sub>1</sub>=  $\rho l_1$ Similarly, if  $\in$ <sub>2</sub> is balanced against  $l_2$ , then  $\in$ <sub>2</sub>=  $\rho l_2$ 

The comparison of emf's of the two cells is given by,

$$\therefore \frac{\epsilon_1}{\epsilon_2} = \frac{l_1}{l_2}$$