ASSIGNMENT - 01

Ans 1 Asymptotic notations are mathematical tools used to describe the limiting behaviour of a function as its input approaches infinity.

They help analyze the efficiency of algorithm by providing a concise way to express their time or space complexity.

1. Big O notation (O): Represents the upper bound of an algorithm's running time in the worst case scenario.
   Example: $O(n^2)$ for a quadratic algorithm.

2. Omega notation (Ω): Represents the lower bound of an algorithm's running time in the best case scenario.
   Example: $\Omega(n)$ for a linear algorithm.

3. Theta notation (Θ): Represents both the upper and lower bounds providing a tight bound on the algorithm's running time.
   Example: $\Theta(n)$ for a linear algorithm.

Ans 2:

Ans 2: The time complexity of the given code is $O(\log n)$. Since the variable "i" doubles in each iteration, the loop executes approximately $\log_2(n)$ times.

... bound by -

Ans 3.

Ans 3. The recurrence relation $T(n) = 3T(n-1)$ represent the exponential growth. Therefore the time complexity is $O(3^n)$

Ans 4: The recurrence relation $T(n) = 2T(n-1) - 1$ represents exponential growth. Therefore the time complexity is $O(2^n)$

Ans 5: The time complexity of the given code is $O(n^{1/2})$. The loop iterates until the sum "s" exceeds "n" which happens approximately when "i" reaches $n^{1/2}$.

Ans 6: The time complexity of the given code is $O(n^{1/2})$. The loop iterates until $i*i$ is greater than n which happens approximately when i reaches $(n^{1/2})$.

Ans 7. The time complexity of the given codes is $O(n \log n)$. The outer loop runs $n/2$ to n times, the middle loop runs $\log n$ times & the inner loop also runs $\log n$ times. Therefore, the total time complexity is $O(n \log n)$

Ans 8. Inner loop runs n times and the outer loop runs n times, making it $O(n^2)$. Additionally, the function recursively calls with $n-3$ so the no. of times it recurses can be represented as $n/3$

$$O(n^2) * O(n/3) = O(n^3)$$

Ans 9. The outer loop runs n times and the inner loop runs n/i times. Therefore Time complexity of second function is $O(n) * O(n/1 + n/2 + n/3 \ldots n/n)$

harmonic series is $\log n$

so Time complexity is $O(n \log n)$

Ans 10.

n^k growth rate increases polynomially with n.

c^n growth rate increases exponentially with n.

c^n grows faster than n^k

if $c > 1$ & $k > 0$ then

$$\lim_{n \to \infty} \frac{c^n}{n^k}$$

therefore for any $c > 1$ & $k > 0$ c^n grows faster than n^k.

Ans 11. Time complexity for extracting minimum element from a heap using extractmin() operation typically has a complexity of $O(\log n)$.

n is number of elements in heap.

this complexity arises because after extracting the minimum element, the heap needs to restructure itself to maintain its properties, which involves heapify operations that take logarithmic time.

Ans 12 After deleting 15