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*Lab 8 report*

## *Head of dataset*

|   | Id | SepalLengthCm | SepalWidthCm | PetalLengthCm | PetalWidthCm | Species     |
|---|----|---------------|--------------|---------------|--------------|-------------|
| 0 | 1  | 5.1           | 3.5          | 1.4           | 0.2          | Iris-setosa |
| 1 | 2  | 4.9           | 3.0          | 1.4           | 0.2          | Iris-setosa |
| 2 | 3  | 4.7           | 3.2          | 1.3           | 0.2          | Iris-setosa |
| 3 | 4  | 4.6           | 3.1          | 1.5           | 0.2          | Iris-setosa |
| 4 | 5  | 5.0           | 3.6          | 1.4           | 0.2          | Iris-setosa |

## *Dataset after applying standard scaler*

```
array([[ -0.90068117,  1.03205722, -1.3412724 , -1.31297673],  
       [ -1.14301691, -0.1249576 , -1.3412724 , -1.31297673],  
       [ -1.38535265,  0.33784833, -1.39813811, -1.31297673],  
       [ -1.50652052,  0.10644536, -1.2844067 , -1.31297673],  
       [ -1.02184904,  1.26346019, -1.3412724 , -1.31297673]])
```

# ANALYSIS

## *PCA feature reduction by 90%*

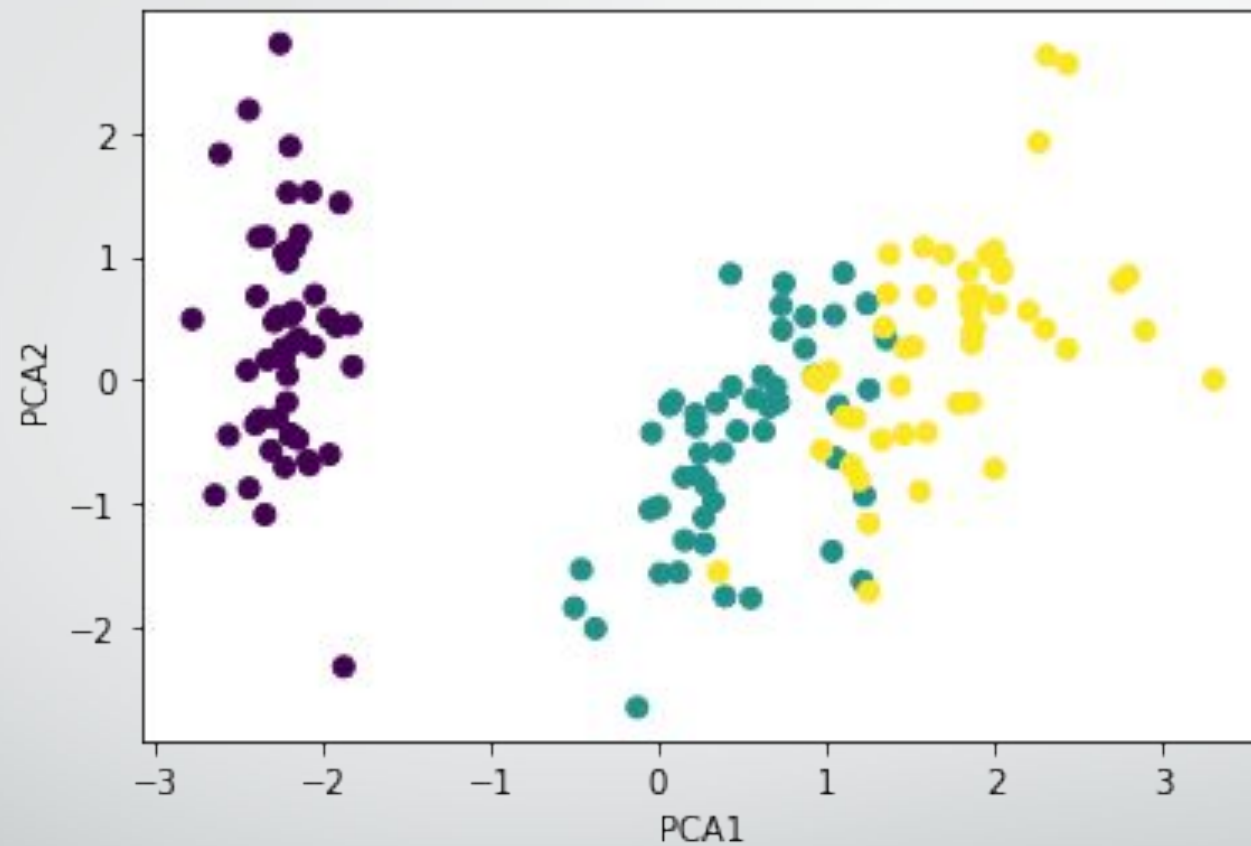
```
array([[ -2.26454173,  0.5057039 ],
       [ -2.0864255 , -0.65540473],
       [ -2.36795045, -0.31847731],
       [ -2.30419716, -0.57536771],
       [ -2.38877749,  0.6747674 ]])
```

- **Model :** `PCA(copy=True, iterated_power='auto', n_components=0.9, random_state=None, svd_solver='auto', tol=0.0, whiten=False)`
- **Ratio of variance in each column :** `array([0.72770452, 0.23030523])`
- **Contribution of each feature in PCA1 and PCA2 respectively:** `array([ [ 0.52237162, -0.26335492, 0.58125401, 0.56561105], [ 0.37231836, 0.92555649, 0.02109478, 0.06541577]])`
- **Variance of both columns:** `array([2.93035378, 0.92740362])`

# ANALYSIS

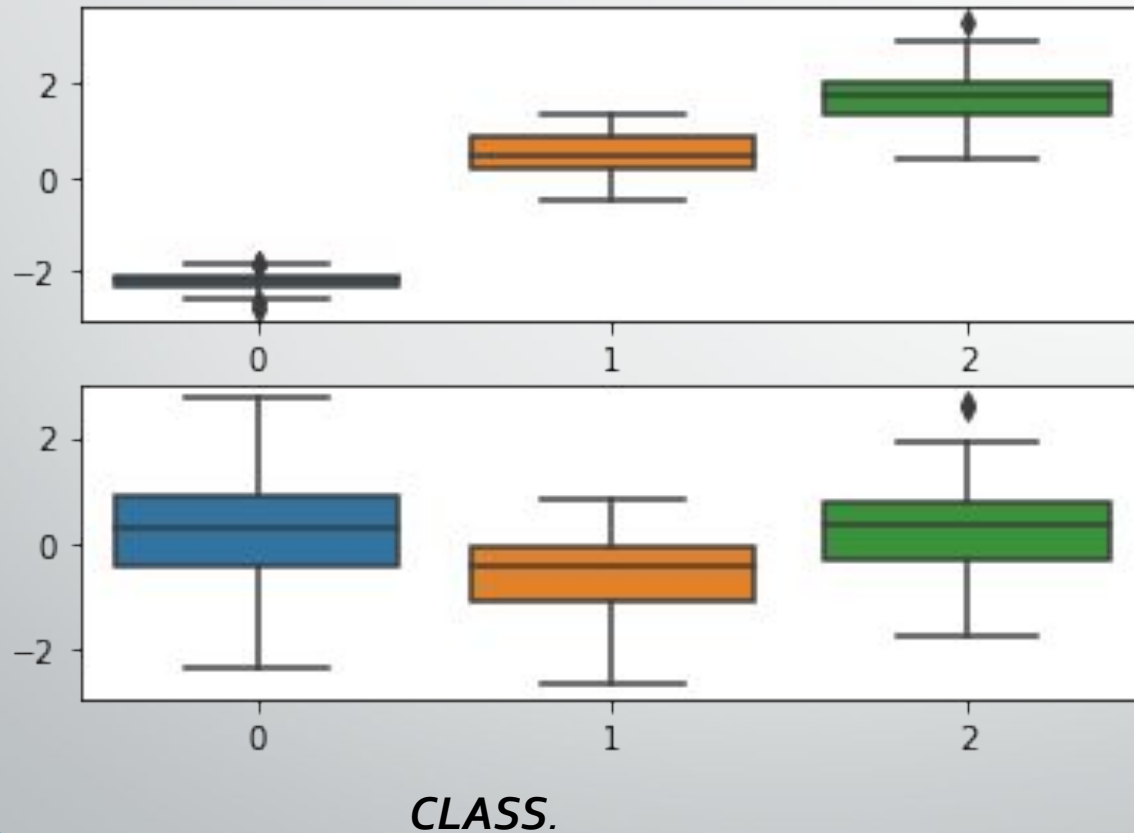
- **Eigen vector of each principal components PC1 and PC2:** `array([  
[ 0.52237162, -0.26335492, 0.58125401, 0.56561105],  
[ 0.37231836, 0.92555649, 0.02109478, 0.06541577]])`
- **So we can see that feature 1,3 and 4 have higher values of eigenvalues for PC1 and the eigenvalues are positive. Feature 2 has low negative eigenvalue.**
- **For second principal component, feature2 has very high contribution.**
- **We can also see that both PC1 and PC2 are orthogonal to each other.**

# *CLUSTERING BY PCA*



|        | PC1          | PC2           | target    |
|--------|--------------|---------------|-----------|
| PC1    | 1.000000e+00 | 5.988877e-17  | 0.944763  |
| PC2    | 5.988877e-17 | 1.000000e+00  | -0.014869 |
| target | 9.447635e-01 | -1.486929e-02 | 1.000000  |

# *Analysis of principal components of PCA*

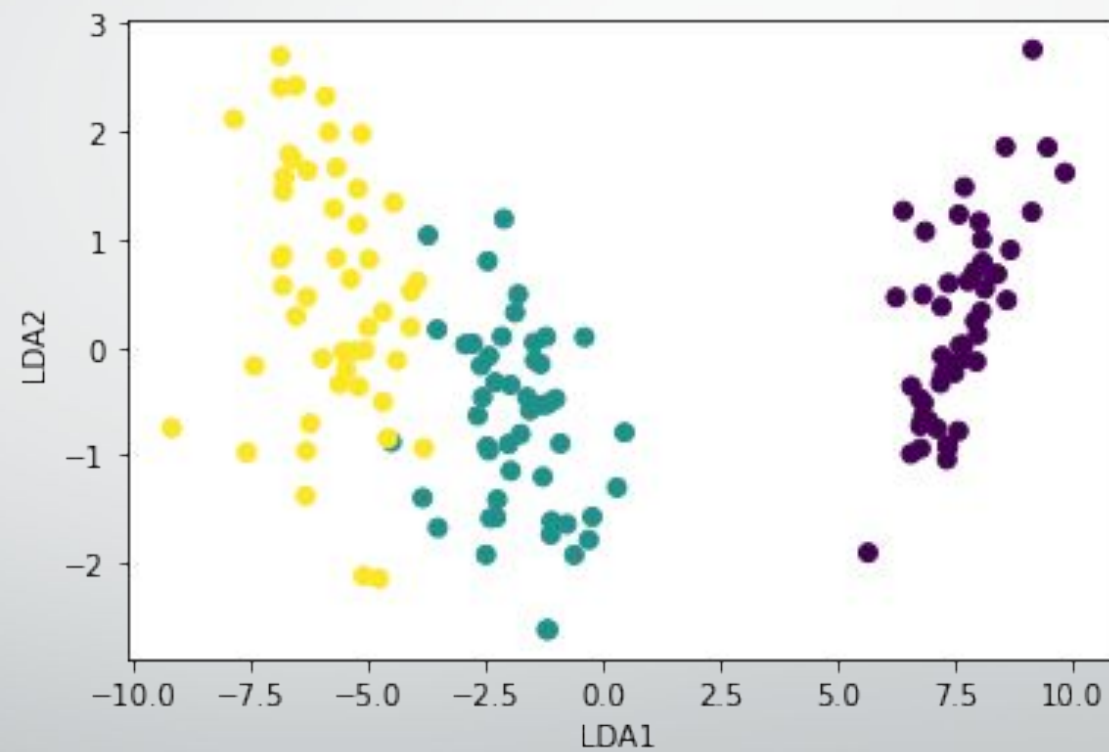


*We can see the variation corresponding to each class in the second component of resultant PCA is higher than the first component.*

*As class is increasing from 0 to 2, the average value of PCA1 is also increasing (high correlation).*

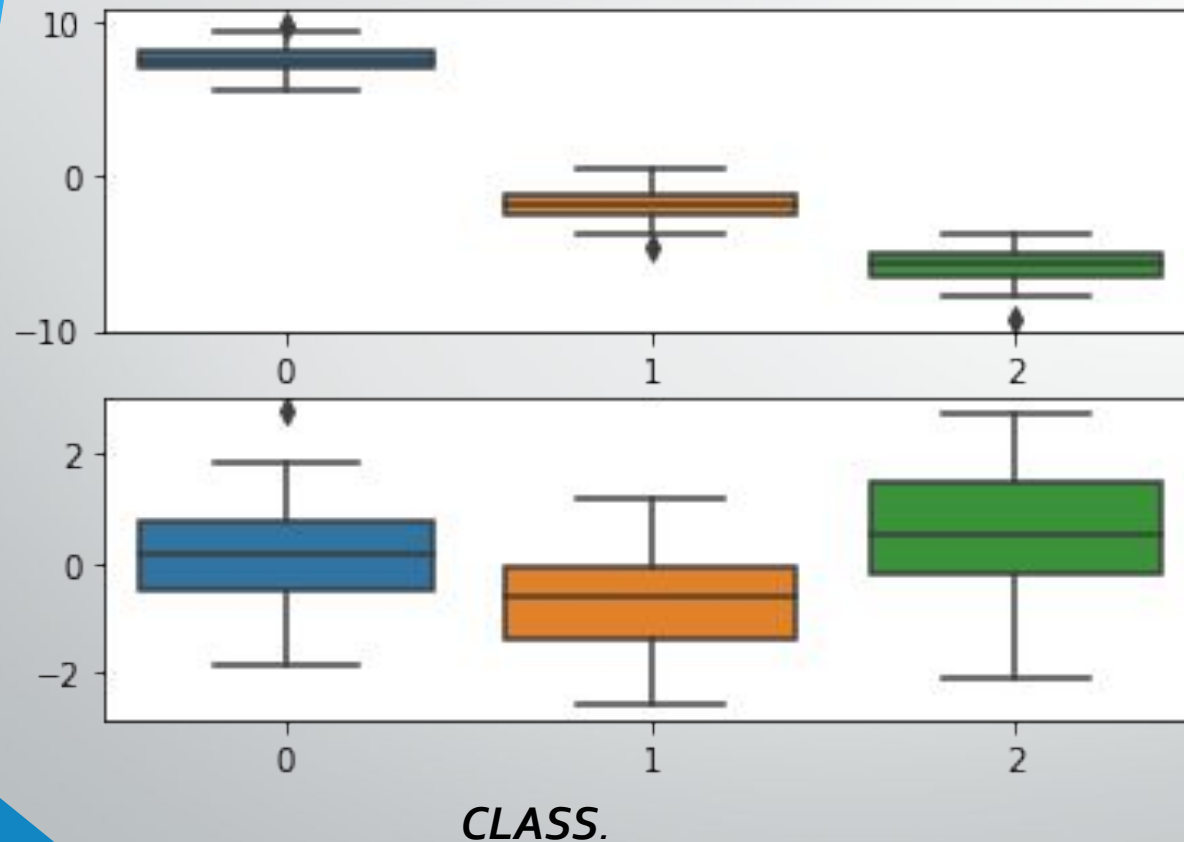
*PCA2 is neither increasing nor decreasing with increase in class value. Hence, we can say that PCA1 is the most important principal component for clustering the dataset.*

# *CLUSTERING BY LDA*





# *Analysis of principal components of LDA*

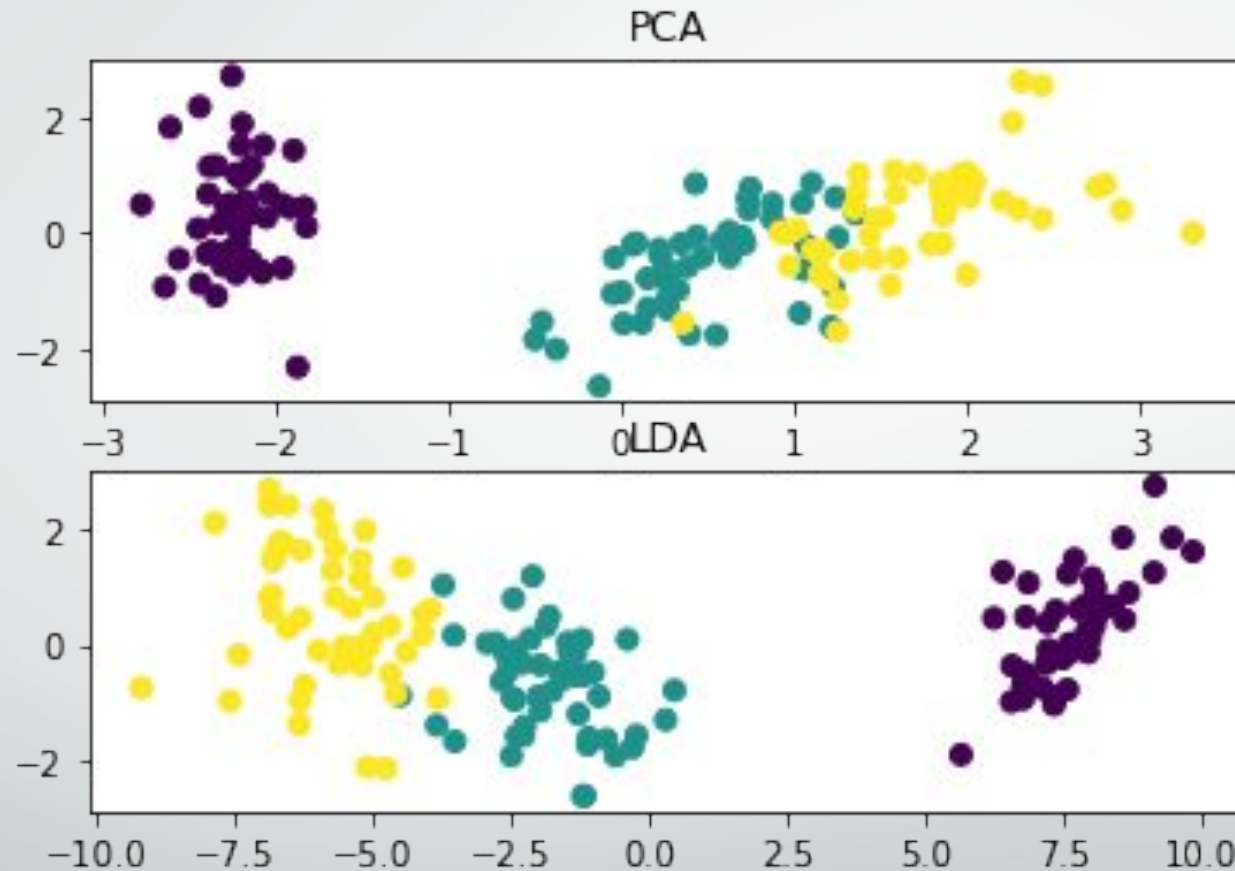


*We can see the variation in the second component of resultant LDA is lower than the first component.*

*As class is increasing from 0 to 2, the average value of LDA1 is decreasing.*

*LDA2 is neither increasing nor decreasing with increase in class value. Hence, we can say that LDA1 is the most important component for clustering the dataset.*

# *PCA vs LDA*



*Accuracy of PCA = 0.8*

*Accuracy of LDA = 0.9*

# Analysis

- *The LDA model performed better than PCA model.*
- *LDA takes the output into account while PCA perform feature reduction only based on input variables.*
- *In PCA 90% data conservation came through 2 eigen vectors.*
- *In nutshell we can say that PCA is concerned with differences in x-values while LDA is concerned with differences in x-values with respect to y.*
- *Both the models are used for feature reduction.*

# *Feature Selection*

- *Method 1: RFE (Recursive Feature Elimination)*

- *Parameters:*

```
RFE(estimator=LinearDiscriminantAnalysis(n_components=2,  
priors=None, shrinkage=None, solver='svd',  
store_covariance=False, tol=0.0001), n_features_to_select=2,  
step=1, verbose=0)
```

- *Selected Features: ['SepalWidthCm', 'PetalWidthCm']*

## *Feature Selection Method 2*

- *Model 2: Select k-best, score function: Chi Squared*
- *Parameters*: `SelectKBest(k=2, score_func=<function chi2>)`
- *Score of each feature*: `array([ 10.81782088, 3.59449902, 116.16984746, 67.24482759])`
- *Selected Features*: `['PetalLengthCm', 'PetalWidthCm']`

# *Classification report of feature selection by RFE model*

|              | precision | recall | f1-score | support |
|--------------|-----------|--------|----------|---------|
| 0            | 1.00      | 1.00   | 1.00     | 11      |
| 1            | 0.91      | 0.71   | 0.80     | 14      |
| 2            | 0.75      | 0.92   | 0.83     | 13      |
| accuracy     |           |        | 0.87     | 38      |
| macro avg    | 0.89      | 0.88   | 0.88     | 38      |
| weighted avg | 0.88      | 0.87   | 0.87     | 38      |

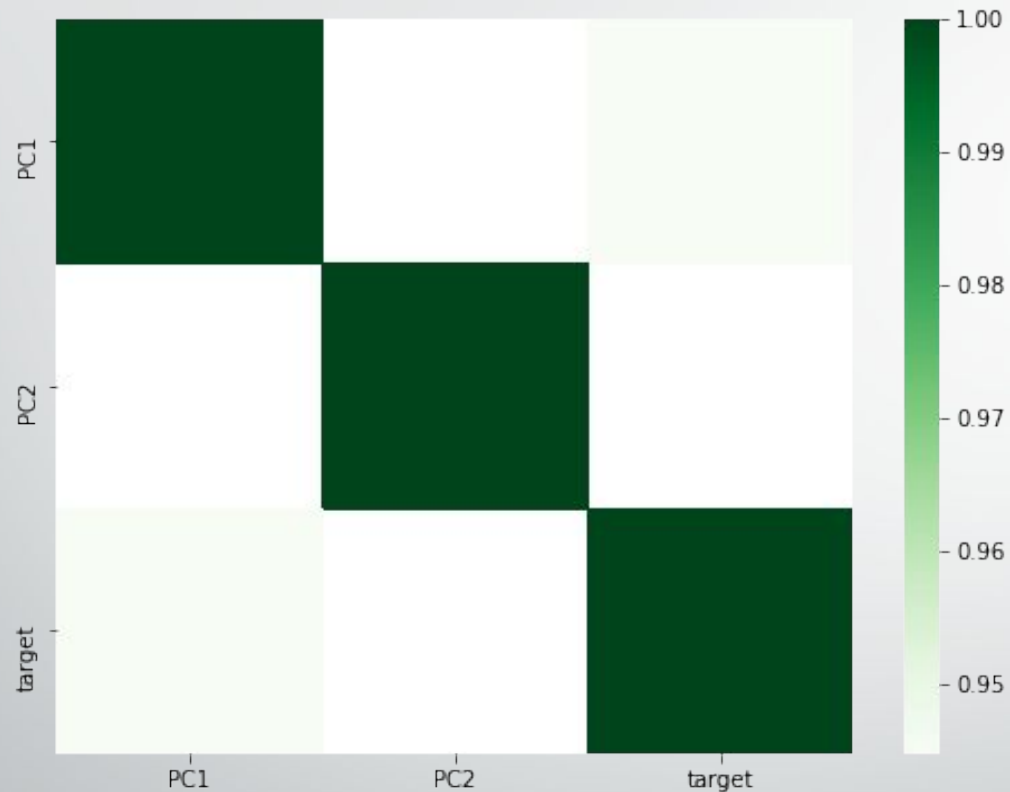
**Accuracy** : 0.9210526315789473, **f1-score**: 0.87

## *Classification report of feature selection by Select-KBest model*

|              | precision | recall | f1-score | support |
|--------------|-----------|--------|----------|---------|
| 0            | 1.00      | 1.00   | 1.00     | 9       |
| 1            | 0.93      | 0.93   | 0.93     | 15      |
| 2            | 0.93      | 0.93   | 0.93     | 14      |
| accuracy     |           |        | 0.95     | 38      |
| macro avg    | 0.95      | 0.95   | 0.95     | 38      |
| weighted avg | 0.95      | 0.95   | 0.95     | 38      |

**Accuracy** : 0.9736842105263158, **f1-score**: 0.95

*For PCA model correlation greater than 0.7*



|        | PC1          | PC2           | target    |
|--------|--------------|---------------|-----------|
| PC1    | 1.000000e+00 | 5.988877e-17  | 0.944763  |
| PC2    | 5.988877e-17 | 1.000000e+00  | -0.014869 |
| target | 9.447635e-01 | -1.486929e-02 | 1.000000  |

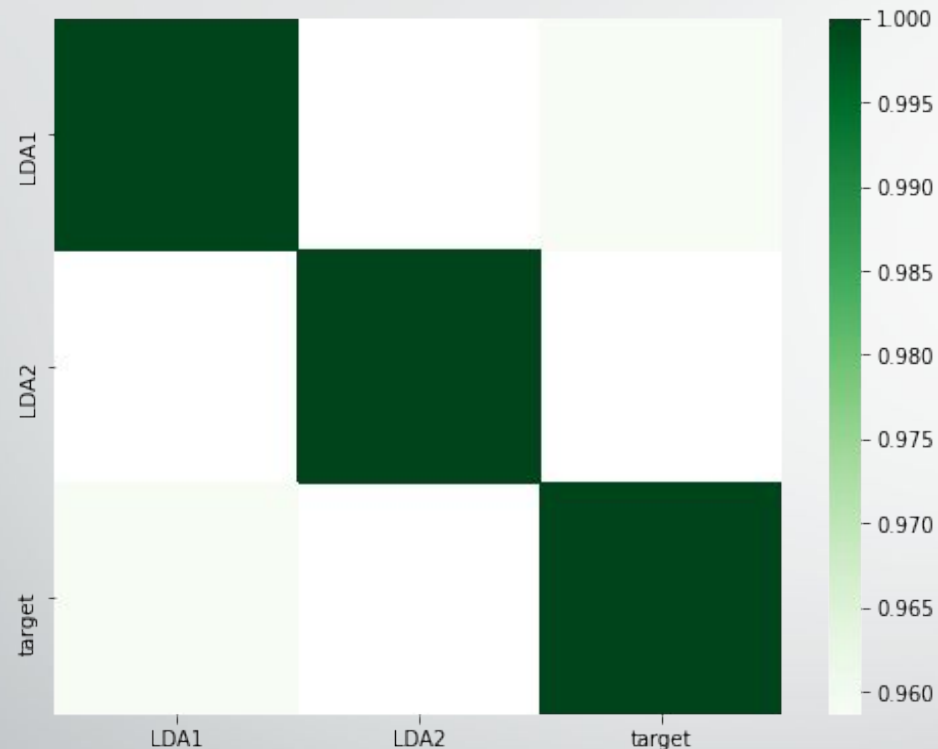


*Applying 70% filter*

|        | PC1      | PC2 | target   |
|--------|----------|-----|----------|
| PC1    | 1.000000 | NaN | 0.944763 |
| PC2    | NaN      | 1.0 | NaN      |
| target | 0.944763 | NaN | 1.000000 |



*For LDA model correlation greater than 0.7*

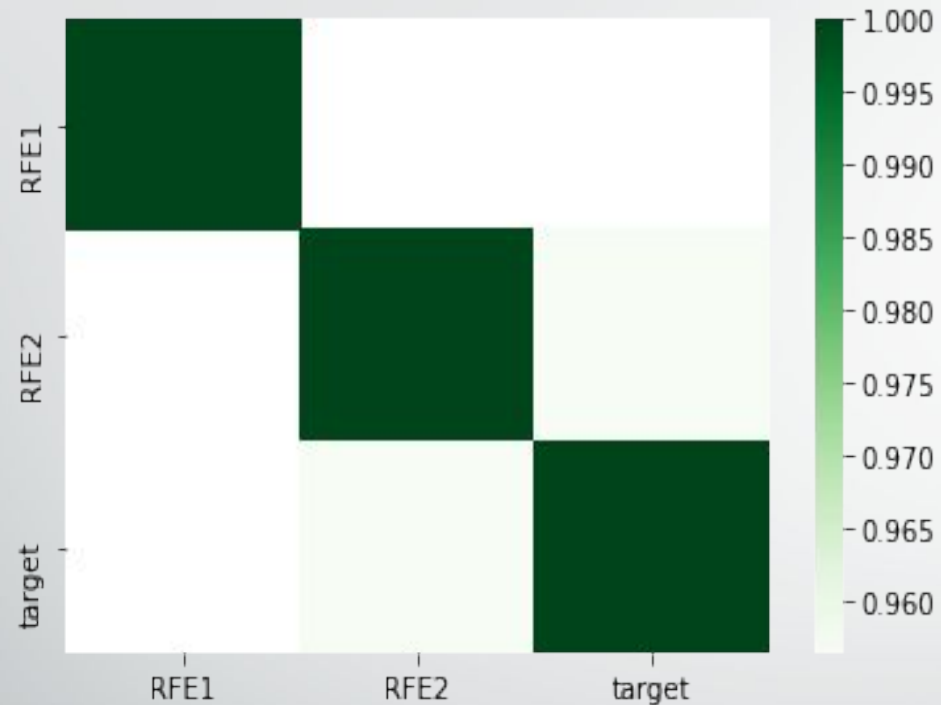


|        | LDA1          | LDA2          | target    |
|--------|---------------|---------------|-----------|
| LDA1   | 1.000000e+00  | -1.811288e-15 | -0.958652 |
| LDA2   | -1.811288e-15 | 1.000000e+00  | 0.106809  |
| target | -9.586523e-01 | 1.068088e-01  | 1.000000  |

*Applying 70% filter*

|        | LDA1     | LDA2 | target   |
|--------|----------|------|----------|
| LDA1   | 1.000000 | NaN  | 0.958652 |
| LDA2   | NaN      | 1.0  | NaN      |
| target | 0.958652 | NaN  | 1.000000 |

*For RFE model correlation greater than 0.7*

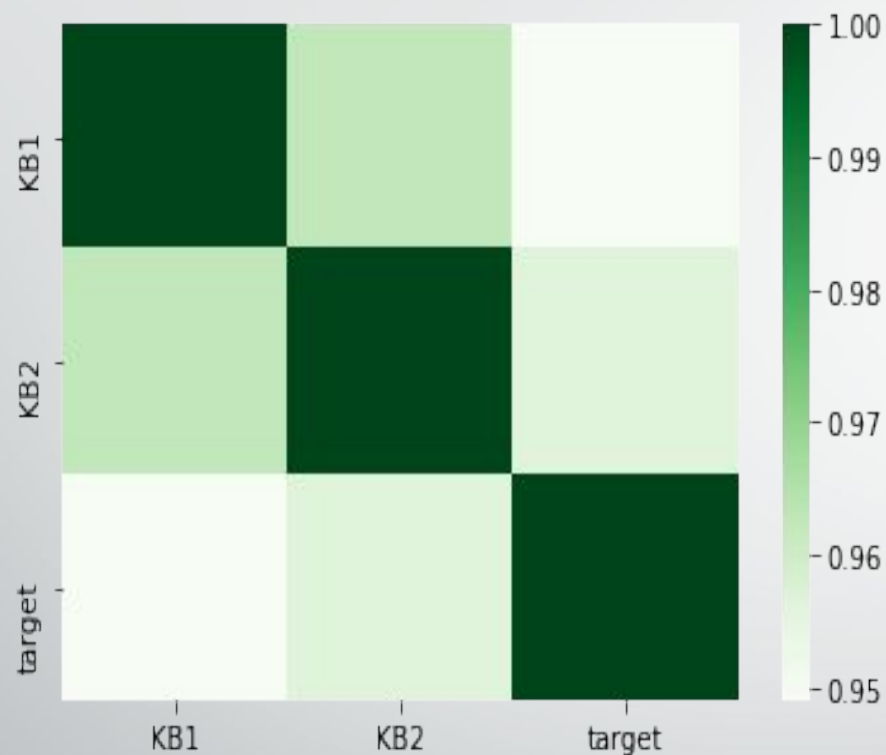


|        | RFE1      | RFE2      | target    |
|--------|-----------|-----------|-----------|
| RFE1   | 1.000000  | -0.356544 | -0.419446 |
| RFE2   | -0.356544 | 1.000000  | 0.956464  |
| target | -0.419446 | 0.956464  | 1.000000  |

*Applying 70% filter*

|        | RFE1 | RFE2     | target   |
|--------|------|----------|----------|
| RFE1   | 1.0  | NaN      | NaN      |
| RFE2   | NaN  | 1.000000 | 0.956464 |
| target | NaN  | 0.956464 | 1.000000 |

*For kbest model correlation greater than 0.7*



|        | KB1      | KB2      | target   |
|--------|----------|----------|----------|
| KB1    | 1.000000 | 0.962757 | 0.949043 |
| KB2    | 0.962757 | 1.000000 | 0.956464 |
| target | 0.949043 | 0.956464 | 1.000000 |



*Applying 70% filter*

|        | KB1      | KB2      | target   |
|--------|----------|----------|----------|
| KB1    | 1.000000 | 0.962757 | 0.949043 |
| KB2    | 0.962757 | 1.000000 | 0.956464 |
| target | 0.949043 | 0.956464 | 1.000000 |

*Unchanged*

# ANALYSIS

- *In PCA model,  $PC_1$  is more correlated to target than  $PC_2$ . Hence, we can say that most important component of a PCA model is the first set of eigen vectors.*
- *Similarly, in LDA model, first axis is more correlated to target than second. Hence, the priority decreases with increasing column number.*
- *In RFE second attribute had higher correlation but this cannot be generalised for such models.*
- *In k-best model, both the selected features had higher correlation than 70%.*
- *K-best model performed better than RFE in terms of both parameters, accuracy as well as  $f_1$ -score.*

# CONCLUSION

- *We learnt about dimension reduction.*
- *We analyzed PCA (Principal Component Analysis) model.*
- *We compared PCA with LDA model and found their differences and similarities.*
- *We learnt about feature selection.*
- *We analysed and compared RFE model and k-best model.*
- *Lastly, we analysed the correlation matrix of all the models and their principal components.*