Assignment 2

CS 230 /CS 561: Probability and Statistics for CS

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INSTRUCTIONS: Solve all problems. Please submit your solutions for assignment in google classroom.

I Conditional Probability

- 1. For the monty hall problem analyse if there are 4 doors instead of 3 doors. (Please see the link shared earlier before you attempt this)
- 2. Repeat the above exercise with python and report the distribution obtained over several runs.
- 3. Show with an appropriate counter example that pairwise independence for several events is not sufficient to claim full independence
- 4. Show with an appropriate counter example the condition

$$P(E_1, \ldots, E_n] = \prod_{i=1}^n P(E_i)$$

is not enough to claim pairwise independence.

- 5. Suppose A and B are independent, show that following events are independent
 - (a) A and B^c
 - (b) A^c and B
 - (c) A^c and B^c
- 6. Prove that conditional probability obeys all the axioms of probability
- 7. Show with an appropriate counter example that unconditional independence doesn't necessarily imply conditional independence
- 8. Show with an appropriate counter example that conditional independence doesn't necessarily imply unconditional independence

II Discrete Random Variables

- 1. Prove that $\lim_{n\to\infty} \lim_{m\to\infty} (2^{m-n}) \neq \lim_{m\to\infty} \lim_{n\to\infty} (2^{m-n})$
- 2. Write a python code to implement monte carlo integration of $\int_0^1 \sqrt{\sin(x)} dx$. Note: please report a distribution and not a single value.

- 3. Compute the expectation and variance for the following discrete random variables
 - (a) Bernoulli
 - (b) Binomial
 - (c) Geometric
 - (d) Poisson
- 4. In python, plot the probability mass function and cumulative distribution function of the following random variables
 - (a) Binomial, n = 30, p = 0.2
 - (b) Geometric, k = 1..., 20, p = 0.2
- 5. Sheldon Ross edition 10, Chapter 2, Exercise 6
- 6. Sheldon Ross edition 10, Chapter 2, Exercise 8
- 7. Sheldon Ross edition 10, Chapter 2, Exercise 9
- 8. Sheldon Ross edition 10, Chapter 2, Exercise 13
- 9. Sheldon Ross edition 10, Chapter 2, Exercise 17
- 10. In the previous question, let X_i , denote the number of times that ith type outcome occurs, i = 1, 2, ..., r. For $0 \le j \le n$, use the definition of conditional probability to find $P(X_i = x_i, i = 1, 2, ..., r 1 | X_r = j)$
- 11. Sheldon Ross edition 10, Chapter 2, Exercise 23
- 12. Sheldon Ross edition 10, Chapter 2, Exercise 24