

1. Introduction

This assignment have been completed into the following enviroment and the system specification

1. GCC Compiler,
2. HP – 2000,
3. RAM – 2GB
4. Processor - Intel® Core™ i3-3110M CPU @ 2.40GHz × 4
5. Operating System (OS) – Ubuntu 16.04 (64 bit)

2. Hashing using Chaining Technique

Ans:

Hash Function

$h(key) = key \% M$; M – prime number (should NOT be close to EVEN Number)

Hash Function used for experiment:

- a) $h(key) = key \% 1000003$
- b) $h(key) = key \% 1000033$

Dataset	Hash Function 1 ($M = 1000003$)		Hash Function 2 ($M = 1000033$)		$\text{Alpha} = \frac{N}{M}$	
	Elapsed Time in Seach Operation		Elapsed Time in Seach Operation			
	Succefull	Unsuccessful	Successful	Unsuccessful		
100000	2	1	3	2	0.1	
500000	3	1	2	1	0.5	
800000	2	1	2	1	0.8	
990003	2	1	3	1	0.99	

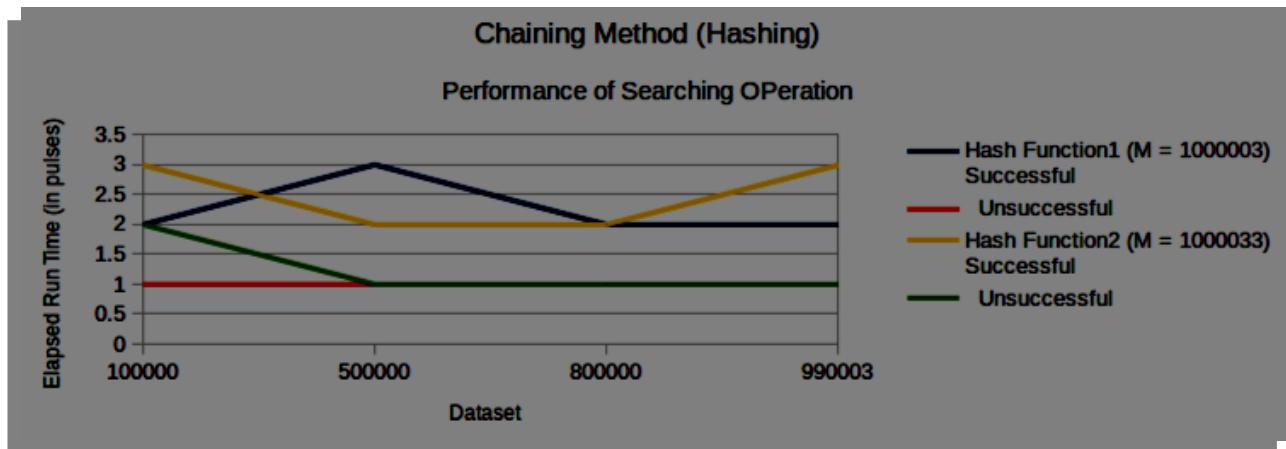


Figure:1. Performance of Search Operation in Chaining Method of Hashing

Observation:

1. From the experimet – it is clear that the seach operation takes a constant amount of time
2. From the theoretical point of view which is:
 $T(N) = \text{Hash function calculation time} + \text{Alpha}$
- unsuccessful Search: $T(N) = 1 + (\text{Alpha}) = 1 + (N/M)$
- Successful Search : $T(N) = 1 + (\text{Alpha}) = 1 + (N/2*M) - (N/2*M*N) = 1 + \text{Alpha}$

Hence, it akes the constant searching time that is ' $T(N) = 1 + \text{ALPHA}$ ' irrespective of the unsuccessful or successful seach.

3. Quadratic Method

Ans:

Hash Function

$h(key) = key \% M$; M – prime number (should NOT be close to EVEN Number)

Hash Function used for experiment:

Frist Hash Funciton

a) $h1(key) = key \% 1000003$, and $h1(key) = (h1(key) + i*i)\%1000003$

Second Hash Function

b) $h1(key) = key \% 1000033$, and $h1(key) = (h1(key) + i*i)\%1000033$

Quadratic Hashing

Dataset	Hash Function 1 ($M = 1000003$)		Hash Function 2 ($M = 1000033$)		Alpha = N/M	
	Elapsed Time in Seach Operation		Elapsed Time in Seach Operation			
	Successfull	Unsuccessful	Successful	Unsuccessful		
100000	3	1	3	1	0.1	
500000	1	1	2	2	0.5	
800000	2	1	2	1	0.8	
990003	2	1	2	1	0.99	

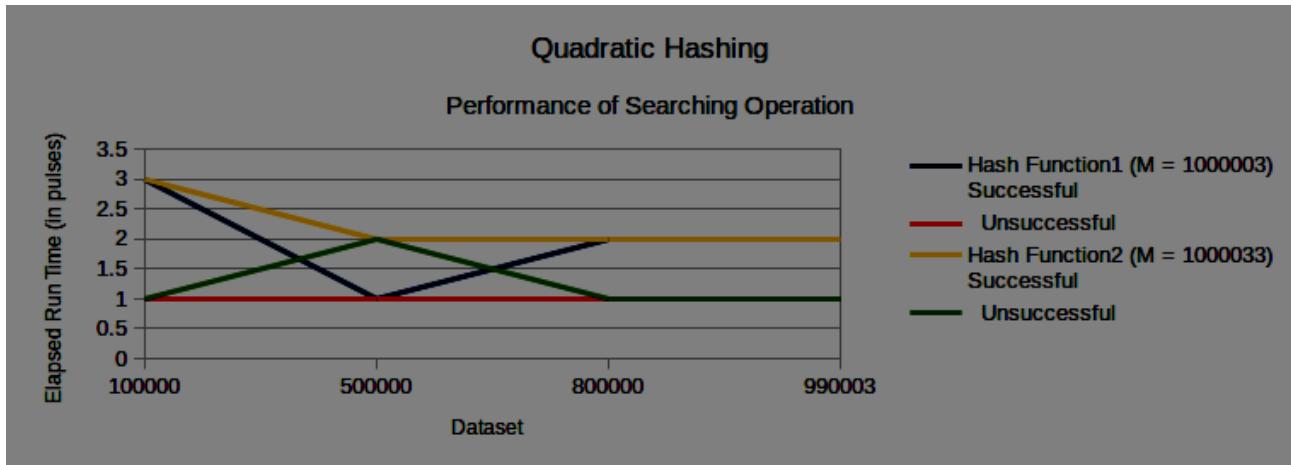


Figure:2. Performance of Search Operation in Quadratic Hashing

Observation:

1. From the experimet – it is clear that the seach operation takes a constant amount of time
2. From the theoretical point of view which is:
 $T(N) = \text{Hash function calculation time} + \text{Alpha}$
 - unsuccessful Search: $T(N) = 1 + (\text{Alpha}) = 1 + (N/M)$
 - Successful Search : $T(N) = 1 + (\text{Alpha}) = 1 + (N/2*M) - (N/2*M*N) = 1 + \text{Alpha}$
 Hence, it akes the constant searching time that is ' $T(N) = 1 + \text{ALPHA}$ ' irrespective of the unsuccessful or successful seach.

4. Double Hashing Technique

Ans: Hash Function

$h(key) = key \% M$; M – prime number (should NOT be close to EVEN Number)

Hash Function used for experiment:

a) $h1(key) = key \% 1000003$, $h2(key) = h1(key) = key \% 1000001$
for each iteration

$$h1(key) = (h1(key) + i * h2(key)) \% 1000003$$

b) $h1(key) = key \% 1000033$, $h2(key) = h1(key) = key \% 1000031$
for each iteration

$$h1(key) = (h1(key) + i * h2(key)) \% 1000033$$

Dataset	Hash Function 1 ($M = 1000003$)		Hash Function 2 ($M = 1000033$)		$\text{Alpha} = N/M$
	Elapsed Time in Search Operation	Succefull	Elapsed Time in Search Operation	Successful	
100000	5	1	4	1	0.1
500000	5	1	4	1	0.5
800000	6	1	4	1	0.8
990003	6	1	4	1	0.99

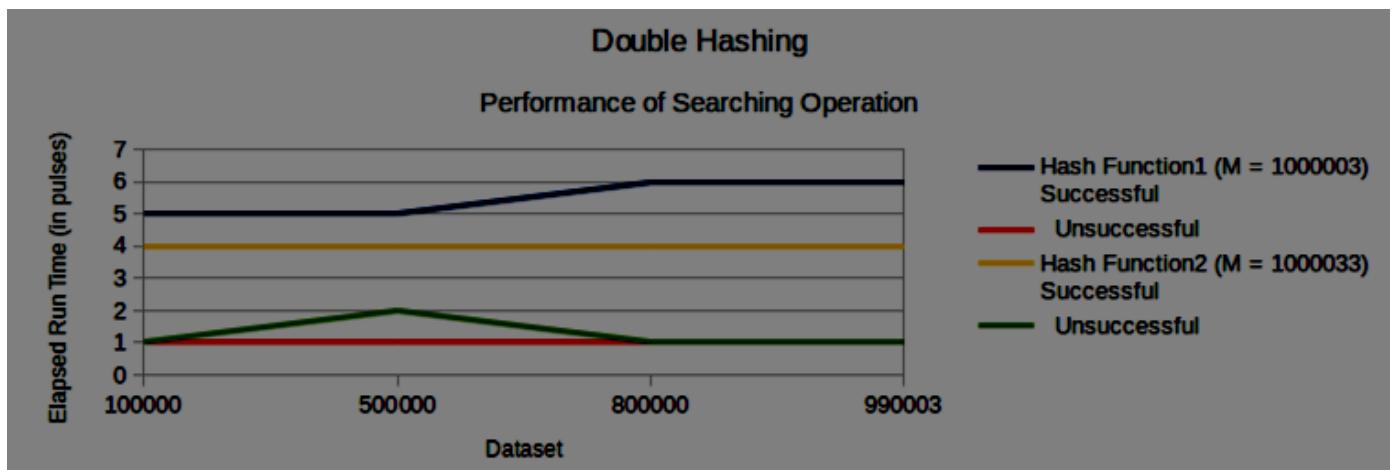


Figure:2. Performance of Search Operation in Double Hashing

Observation:

1. From the experiment – it is clear that the search operation takes a constant amount of time
2. From the theoretical point of view which is:
 $T(N) = \text{Hash function calculation time} + \text{Alpha}$
 - unsuccessful Search: $T(N) = 1 + (\text{Alpha}) = 1 + (N/M)$
 - Successful Search : $T(N) = 1 + (\text{Alpha}) = 1 + (N/2*M) - (N/2*M*N) = 1 + \text{Alpha}$

Hence, it takes the constant searching time that is ' $T(N) = 1 + \text{ALPHA}$ ' irrespective of the unsuccessful or successful search.

References:

1. Cormen, Thomas H., et al. *Introduction to algorithms*, (30, 37). MIT press, 2010.
2. Horowitz, Ellis. "Sartaj Sahni.., Fundamentals of Computer Algorithms, (145, 154)." (1998).
3. https://en.wikipedia.org/wiki/chaining_sort
4. https://en.wikipedia.org/wiki/double_sort
5. https://en.wikipedia.org/wiki/double_sort