Date: Y.

1 Working plan for Gautham July-September

Overall research question: How we can use the representation of quantum computations as a MBQC pattern for optimization & compilation tasks? Every work that fits into this question is useful. The research question splits into two main sub topics:

- 1. Which graph rewrites are useful on a MBQC pattern?
- 2. How can we translate MBQC patterns to hardware-adapted instructions?

MBQC patterns can be represented as graph-like diagrams in ZX-calculus.

1.1 Useful graph rewrites

There is no complete rule set for rewriting MBQC patterns so far. Yet, many rules of the complete rule set of standard ZX-diagrams have a similar representation for graph-like diagrams. The bialgebra rule seems to be covered by pivot (resp. local complementation), the copy rule by Z-insertion/Z-deletion, the fusion with again with pivot/ identity removal or neighbor unfusion in the other way.

⇒ Find a complete rule set for graph-like ZX-diagrams.

The most interesting rule for MBQC patterns seems to be local complementation: We can use it to change measurement labels and reduce the number of graph edges in a non trivial way. Optimizing the number of edges with local complementation in general is NP-hard even in the case that all local complementations commute. Yet, if would be interesting to know whether there are restricted graph types for which we can find a sequence of local complementations minimizing the number of edges in polynomial time. One example are graphs locally equivalent to trees. In such cases we can find a sequence of local complementations transforming the graph into a tree which then of course has the minimum number of edges possible. It would be interesting to see whether we can extend the algorithm somehow. Also we could use Pivot instead of local complementation for the same task (although it is restricted in its possibilities)

⇒ Study edge minimization with local complementation.

For an MBQC pattern with Pauli flow, each vertex can be extracted as a Pauli exponential on a quantum circuit, where the underlying graph of the pattern determines the exponential and the Pauli flow determines the order in which we can extract the vertices. We can represent this in a Pauli-dependency DAG. The goal here would be to examine how graph rewrites or changing measurement labels in the Pauli flow affect the exponentials. Yet, determining how the exponentials change is not easy, one can imagine that every operation pushes one or more Pauli strings through the PDDAG updating all Pauli exponentials where the strings anticommute and leaving others unchanged. Still these updates need to be formalized and understood more in order to find algorithms

minimizing Pauli exponentials (reducing non-identities in the strings) or getting other desired forms like all Z-terms which are better realizable on neutral atom hardware.

 \Rightarrow Study graph and Pauli flow rewrites on PDDAG structure.

1. ZX Introduction

2. Measurements

2.1. Pauli Group.

Definition 1. Pauli strings.

$$P_n = \{ \bigotimes_{i=1}^n A_i | A_i \in P \}$$
 (1)

where, P is the Pauli group,

$$P := \alpha \{ I, X, Y, Z \}, \alpha \in \{ \pm 1, \pm i \}$$

$$\tag{2}$$

and I, X, Y, Z have matrix representation,

$$I = \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}, X = \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}, Y = \begin{pmatrix} 0 & -i \\ i & 0 \end{pmatrix}, Z = \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$$
 (3)

Note that this is an *irreducible representation*. We can check that X and Z do not share any eigenvectors (and so any invariant 1dim subspaces).

 \mathbb{Q}_8 is a subgroup of P. P is the smallest subgroup (of U(2)) generated by $\langle X, Y, Z \rangle$.

Quotienting P by the center yields the Klein four-group (TODO with other properties and lie algebra lie group).

Note that,

$$SU(2) \cap P_1 = \pm 1\{I\} \cup \pm i\{X, Y, Z\} \le P_1$$
 (4)

This subgroup is isomorphic to $\mathbb{Q}_8 = \{\pm 1, \pm i, \pm j, \pm k\}$ via the identification.

$$i \to iX, j \to iY, k \to iZ$$
 (5)

2.2. Properties.

2.3. **Measurements.** In an MBQC we need to specify measurement operations for each non-output. We do this by assigning *measurement planes* for each qubit,

Any general measurement for a single qubit is specified by an axis on the Bloch sphere. Convention is to restrict these axes to a plane of the Bloch sphere – XY, YZ, or XZ. The axes selects two states – $|\eta\rangle$ and $|\eta'\rangle$ which are diametrically opposite on the sphere, then we form,

$$\Pi = |\eta\rangle\langle\eta| + |\eta'\rangle\langle\eta'| \tag{6}$$

and make a projective measurement.

We can write these states and axes explicitly. The Bloch sphere is parametrised as (θ, φ) – azimuthal and polar. We choose our axes by fixing one of the angles,

$$\theta = \pi/2 \ (XY), \varphi = 0 \ (YZ) \text{ or } \varphi = \pi/2 \ (XZ)$$
(7)

$$|+_{XY}\rangle = \frac{1}{\sqrt{2}}(|0\rangle + e^{i\alpha}|1\rangle) \qquad \qquad |-_{XY}\rangle = \frac{1}{\sqrt{2}}(|0\rangle - e^{i\alpha}|1\rangle)$$

$$|+_{XZ}\rangle = \cos\frac{\alpha}{2}|0\rangle + \sin\frac{\alpha}{2}|1\rangle \qquad \qquad |-_{XZ}\rangle = \sin\frac{\alpha}{2}|0\rangle - \cos\frac{\alpha}{2}|1\rangle$$

$$|+_{YZ}\rangle = \cos\frac{\alpha}{2}|0\rangle + i\sin\frac{\alpha}{2}|1\rangle \qquad \qquad |-_{YZ}\rangle = \sin\frac{\alpha}{2}|0\rangle - i\cos\frac{\alpha}{2}|1\rangle$$

Note that any point (pure state) on the boundary of the Bloch sphere can be written as,

$$(\theta, \varphi) \mapsto \cos \frac{\varphi}{2} |0\rangle + e^{i\theta} \sin \frac{\varphi}{2} |1\rangle$$
 (8)

The measurement axis coincide with X, Y or Z corresponds to $\alpha = a\pi$ with $a \in \{0, 1\}^{-1}$

¹more exactly $\alpha = \frac{2a}{\pi} \mod 4, a \in \{0, 1, 2, 3\}$ to pick out both axes in each plane.

After picking an axis, we construct our measurement as a projector,

$$\Pi_{\bullet \circ, \alpha} = |+_{\bullet \circ}(\alpha)\rangle\langle+_{\bullet \circ}(\alpha)| - |-_{\bullet \circ}(\alpha)\rangle\langle-_{\bullet \circ}(\alpha)| \tag{9}$$

It is useful to construct the measured Hermitian operators (with eigenbasis $|+\rangle, |-\rangle$) corresponding to each planar measurement.

$$XY \mapsto \cos \alpha X + \sin \alpha Y =: M_{XY,\alpha}$$

 $XZ \mapsto \sin \alpha X + \cos \alpha Z =: M_{XZ,\alpha}$
 $YZ \mapsto \sin \alpha Y + \cos \alpha Z =: M_{YZ,\alpha}$

Typically in MBQC, our "desired outcome" is the +1 eigenvalue collapse to the $|+\rangle$. This is usually denoted as outcome 0, and the undesired $|-\rangle$ collapse as outcome 1.

Depending on the plane of measurement, we can apply a pauli X, Y or Z to correct it. Z changes the relative phase, X swaps 0 and 1 and ZX = Y does both.

$$Z|-_{XY}\rangle = |+_{XY}\rangle, \ Y|-_{XZ}\rangle = |+_{XZ}\rangle \text{ and } X|-_{YZ}\rangle = |+_{YZ}\rangle$$
 (10)

3. Stabilisers

The idea is to specify a state (uniquely) via the generators of its stabiliser subgroup. "Errors" become changes to generators.

3.1. Clifford group.

Definition 2. The Clifford group is the normaliser of the Pauli group P_n in $U(2^n)$,

$$C_n := \{ g \in SU(2^n) | gP_n g^{-1} = P_n \}$$
(11)

A Clifford gate is an element of C_n .

fact: the Clifford group on n-qubits is generated by Hadamard, Phase (i) and CNOT gates.

Theorem 3. (Gottesmann-Knill). Any circuit involving only initial state $|0\rangle^{\otimes n}$, Clifford gates and Pauli measurements is (polynomial time) easily simulatable.

So, we want to try to minimize the number of non-Clifford gates in our circuit.

fact: C_n is not a universal gate-set. The T gate cannot be finitely generated.

$$T = \begin{pmatrix} 1 & 0 \\ 0 & e^{i\pi/4} \end{pmatrix} \tag{12}$$

Note that the Clifford group is not finite because if g normalises P_n then so does $e^{i\phi}g$. We can disregard global phases and just consider $C_n/U(1)$.

3.2. Stabilisers and States.

Definition 4. The subspace stabilised by a subgroup $H \leq P_n$ is,

$$V_H := \{ |\psi\rangle \in (\mathbb{C}^2)^{\otimes n} |h|\psi\rangle = |\psi\rangle \forall h \in H \}$$
(13)

Proposition 5. For all $g \in U(2^n)$ and $H \leq P_n$, $V_{gHg^{-1}} = gV_H$.

Note that if $-\mathbb{1} \in H$, then $-\mathbb{1}|\psi\rangle = |\psi\rangle \implies |\psi\rangle = 0$. This must be excluded for the stabiliser space to be non-trivial.

Proposition 6. If $H \leq P_n$ and $\dim(V_H) > 0$, then H is abelian and $-1 \notin H$.

Proof. $g_1, g_2 \in P_n$ either commute or anticommute. If they anticommute then $g_1g_2|\psi\rangle = -g_2g_1|\psi\rangle \implies |\psi\rangle = 0$

Definition 7. A set $S \leq H$ is independent if for all $g \in S$,

$$\langle S \setminus \{g\} \rangle \neq \langle S \rangle \tag{14}$$

And finally, the theorem below allows us to specify a unique state by specifying n commuting Pauli strings. Let us denote V_S to be the subspace stabilised by a generating set $\langle S \rangle$.

Theorem 8. If $S = \{g_1, \ldots, g_l\}$ is indepdent, pairwise commutative such that $-1 \notin S$, then $\dim(V_S) = 2^{n-l}$

There is a surjective group homomorphism, $r: P_n \to \mathbb{F}_2^{2n}$ with $\ker(r) = \{\pm 1, \pm i\mathbb{1}\}$ via the map,

$$r(X_i) = e_i \text{ and } r(Z_i) = e_{i+n}$$
(15)

we can keep track of X_i, Y_i via this map as a $2 \times 2n$ matrix called the check matrix.

For example, the bell state $(|00\rangle + |11\rangle)$ is the stabiliser state of,

$$\langle X_1 X_2, Z_1 Z_2 \rangle \tag{16}$$

with associated check matrix,

$$\begin{pmatrix} 1 & 1 & 0 & 0 \\ 0 & 0 & 1 & 1 \end{pmatrix} \tag{17}$$

The stabiliser tableaux is an extension of the check matrix of the state.

Since we can specify states via its stabiliser (group), we can also track measurements. First, note that for any $g \in P_n$, the projectors P_+, P_- can be written as,

$$P_{+} = \frac{1}{2}(I+g) \text{ and } P_{-} = \frac{1}{2}(I-g)$$
 (18)

with probabiltiies,

$$p(+) = \frac{1}{2} (1 + \langle \psi | \tilde{g} | \psi \rangle) \text{ and } p(-) = \frac{1}{2} (1 - \langle \psi | \tilde{g} | \psi \rangle)$$
(19)

We want to measure some observable $\tilde{g} \in P_n$.

It is easy to check that any $g \in P_n$ either commutes or anticommutes with \tilde{g} . Consider a stabiliser V_S generated by $S = \langle g_1, \dots, g_n \rangle$. There are two cases,

(i) \tilde{q} commutes with all stabilisers.

Then, for any g, $g(\tilde{g}|\psi) = \tilde{g}|\psi\rangle$. So, $\tilde{g}|\psi\rangle$ is a common +1 eigenvector of all stabilisers. Since V_S is one-dimensional, $\tilde{g}|\psi\rangle \propto |\psi\rangle$, but because it has eigenvalues ± 1 , $\tilde{g}|\psi\rangle = \pm |\psi\rangle$. So, one of $\pm \tilde{g}$ is a stabiliser

The outcome is deterministic + or - if $+\tilde{g} \in S$ or $-\tilde{g} \in S$. We do not need to update the stabilisers,

$$S = \langle g_1, \dots, g_n \rangle \tag{20}$$

(ii) \tilde{g} anticommutes with some stabilisers.

wlog, we can assume that \tilde{g} anticommutes with g_1 and commutes with all other g_i by picking g_1 such that $\{\tilde{g},g_1\}=0$ and for other $i,g_i\mapsto g_1g_i=:g_i'$,

$$gg_i' = g(g_1g_i) = -g_1(gg_i) = -g_1(-g_ig) = g_i'g$$
(21)

note that this is just a change of choice of generators and does not change S.

In this case, the measurement is *not* deterministic because,

$$p(+) = \frac{1}{2}(1 + \langle \psi | \tilde{g} | \psi \rangle) = \frac{1}{2}(1 + \langle \psi | \tilde{g}g_1 | \psi \rangle) = \frac{1}{2}(1 - \langle \psi | \tilde{g} | \psi \rangle) = p(-) = \frac{1}{2}$$
 (22)

In this case, depending on the measurement outcome we update the stabiliser (after measurement) to,

$$S = \langle \pm \tilde{g}, g_2, \dots, g_n \rangle \tag{23}$$

The GHZ state for example cannot be described by a stabiliser because $p(Z_1 = +) = \frac{1}{3}$.

Note that all of this assumes that we are making a pauli measurement. In an MBQC, before we make the X_u local measurement, we must update the tableaux to the above form – anticommuting with one (neighbour) vertex and commuting with all others as in 21.

This update for a X-measurement is the exact same as local complementation on the measured vertex (prove later).

4. MBQC

MBQC leverages entanglement (teleportation) instead of unitary gates to create a one-way model of quantum computation.

Definition 9. A measurement pattern consists of an n-qubit register V with distinguished sets $I, O \subseteq V$ of inputs and outputs. Additionally there is a sequence of the following operations:

- i. Preparations intialising all qubits $i \notin I$ in the $|+\rangle$ state.
- ii. Entangling applying a CZ_{ij} to qubit i as control and qubit j as target for (chosen) pairs $(i, j) \in V \times V$.
- iii. Destructive measurements which project qubits $i \notin O$ onto orthonormal basis $\{|+_{\lambda,\alpha},|-_{\lambda},\alpha\rangle\rangle\}$ as described in 2.3.
- iv. Corrections conditionally applying X or Z gates onto qubits $i \in V$.

The graph (state) for a measurement pattern is determined by the set of tuples $(i, j) \in V \times V$ such that we apply CZ_{ij} . Along with specifying measurement axes and angles for non-outputs $\bar{O} := V \implies$, we get a labelled open graph.

Definition 10. A labelled open graph is a tuple $\Gamma = (G, I, O, \lambda)$ where G = (V, E) is a graph, $I, O \subseteq V$ are (input and output) subsets of V and $\lambda : \overline{O} \to \{XY, YZ, XZ\} \times [0, 2\pi)$.

Every measurjement yields an outcome 0 or 1. In total there are $2^{|\bar{O}|}$ possible outcomes – these are called *branches* of the measurement pattern.

After corrections we can sometimes ensure that every branch yields the same output. When this is possible, the measurement pattern is called **deterministic**. This is formalised via *flow*.

The linear map associated with a deterministic MBQC then looks like,

$$\underbrace{\left(\prod_{i\in\bar{O}}\langle+_{\lambda(i),\alpha(i)}|\right)}_{\text{(det) measurement}}\underbrace{\left(\prod_{i\sim j}CZ_{ij}\right)}_{\text{entangling}}\underbrace{\left(\prod_{i\in\bar{I}}|+\rangle_{i}\right)}_{\text{preperation}} \tag{24}$$

This acts on the input state $\bigotimes_{i\in I} |\psi_i\rangle$. The resource state used is,

$$\left(\prod_{i\sim j} CZ_{ij}\right) \left(\prod_{i\in \bar{I}} |+\rangle_i\right) |\psi\rangle_I \tag{25}$$

4.1. Corrections. Note that we cannot simply apply corrections by applying a Z or X gate on an incorrect outcome (typically a hardware/cost limitation on MBQC). Let us construct the stabiliser of the graph state.

First note that $|+\rangle_u = X_u |+\rangle_u$ and the identity,

$$CZ_{uv}X_u = X_uZ_vCZ_{uv} (26)$$

Then, for any $w \in \bar{I}$,

$$\left(\prod_{u \sim v} CZ_{u,v}\right) \left(\prod_{u \in \bar{I}} |+\rangle_u\right) = \left(\prod_{u \sim v} CZ_{u,v}\right) X_w \left(\prod_{u \in \bar{I}} |+\rangle_u\right) \tag{27}$$

$$= \left(\prod_{v \in N_G(w)} Z_v\right) X_w \left(\prod_{u \sim v} C Z_{u,v}\right) \tag{28}$$

where we use the identity above when CZ involves vertex w, and otherwise it commutes with X_w . Also, the Z string commutes with X_w .

So, we see that,

$$\left[\left(\prod_{v \in N_G(w)} Z_v \right) X_w \right] \left(\prod_{u \sim v} |+\rangle_u \right) = \left(\prod_{u \sim v} |+\rangle_u \right) \tag{29}$$

For each vertex we get a stabiliser string of Z on the neighbours and X on the vertex.

Equivalently, we obtain the following operator equivalence that will allow us to perform corrections,

$$X_w \left(\prod_{u \sim v} |+\rangle_u \right) = \left(\prod_{v \in N_G(w)} Z_v \right) \left(\prod_{u \sim v} |+\rangle_u \right) \tag{30}$$

The above case is easy – to correct by applying a local X on vertex w can be achieved by applying a Z to all neighbours of w.

We can also take the product of stabilisers indexed (defined) by many vertices. To correct by applying a local Z, we can take the stabiliser of vertices in in its neighbourhood.

Generally, we look for a stabiliser of the graph state,

$$S = Q_v \otimes P_{rest} \tag{31}$$

where Q_v is the local correction operator on vertex v. This is dependent (only) on the choice of plane and angle. The string of paulis P_{rest} is called an *extraction string*. Simple algebraic manipulation of a chosen stabiliser is the generator for corrections.

We want P_{rest} to be supported on the future (unmeasured) qubits. This is possible when we have a flow condition on the graph.

4.2. Flow. The simplest case is causal flow, we assume that all vertices are measured in the XY basis.

Definition 11. (causal flow).

Given a labelled open graph $\Gamma = (G, I, O, \lambda)$ such that $\lambda(v) = XY$ for all $v \in \bar{O}$, a causal flow is a tuple (f, \prec) where $f : \bar{O} \to \bar{I}$ and \prec is strict partial order on V satisfying,

i.
$$v \sim f(v)$$

ii.
$$v \prec f(v)$$

iii.
$$\forall u \in N_G(f(v)), u = v \text{ or } v \prec u$$

The partial ordering \prec gives us the order in which to perform measurements.

Here, an error on any $v \in \bar{O}$ can be corrected via applying Z_v . Consider the stabiliser of vertex f(v), rearranging we get,

$$\prod_{w \in N_G(f(v) \setminus \{v\})} Z_w X_{f(v)} = Z_v$$
(32)

Allowing measurements in all three planes and products of vertex stabilisers gives us generalised flow.

The following algebraic relation is very useful, let the stabiliser be specified by a set $g(v) \subseteq \overline{I}$,

$$\prod_{u \in g(v)} \left(\prod_{w \in N_G(u)} Z_w \right) X_u = \left(\prod_{u \in g(v)} \prod_{w \in N_G(u)} Z_w \right) \left(\prod_{u \in g(v)} X_u \right)$$

$$= \left(\prod_{u \in \text{odd}(g(v))} Z_u \right) \left(\prod_{u \in g(v)} X_u \right)$$

$$= \left(\prod_{u \in \text{odd}(g(v)) \setminus g(v)} Z_u \right) \left(\prod_{u \in g(v) \cap \text{odd}(g(v))} Y_u \right) \left(\prod_{u \in g(v) \setminus \text{odd}(g(v))} X_u \right)$$
(34)

where, in the second line we use that $Z_w^2 = I$, and only Z on the odd neighbourhood of g(v) survive.

We then write the expression as a disjoint product – either,

i. $u \in \text{odd}(g(v))$ and $u \notin g(v)$ – apply Z

ii. $u \in g(v)$ and $u \in \text{odd}(g(v))$ – apply Y

iii. $u \in g(v)$ and $u \notin \text{odd}(g(v))$ – apply X

Finally, based on whether we require a X_v, Y_v or Z_v correction, we choose g(v) appropriately such that v belongs to one of the corresponding sets. We search for subsets g(v) and the ordering \prec simultaneously, not separately.

Definition 12. (generalised flow).

Given a labelled open graph $\Gamma = (G, I, O, \lambda)$ such that $\lambda(v) \in \{XY, XZ, YZ\}$ for all $v \in \bar{O}$, a generalised flow or glow for Γ is a tuple (g, \prec) where $g : \bar{O} \to \mathcal{P}(\bar{I})$ and \prec is a strict partial order over V satisfying for all $v \in \bar{O}$,

i. for all $u \in q(v)$, $v \neq u \implies v \prec u$

ii. for all $u \in \text{odd}(q(v)), v \neq u \implies v \prec u$

iii.
$$\lambda(v) = XY \implies v \in \text{odd}(q(v)) \setminus q(v)$$

iv.
$$\lambda(v) = XZ \implies v \in q(v) \cap \operatorname{odd}(q(v))$$

$$v. \ \lambda(v) = YZ \implies v \in g(v) \setminus \operatorname{odd}(g(v))$$

Conditions i, ii ensure that correction sets are in the *future*, and iii - v follow from the stabiliser algebra.

We can generalise this by noting that if some measurements are pauli, $\lambda(u) \in \{X, Y, Z\}$, then u can be in the correcting set of some v in the future $(u \prec v)$ as long as correcting v induces the same pauli $\lambda(u)$ on u. This is described as a *free correction in the past*. Note that the \pm sign must still be tracked, but doesn't require the application of any operator.

Definition 13. (Pauli flow).

Given a labelled open graph $\Gamma = (G, I, O, \lambda)$, a Pauli flow for Γ is a tuple (p, \prec) where $p : \bar{O} \to \mathcal{P}(\bar{I})$ and \prec is a strict partial order over V satisfying for all $v \in \bar{O}$,

$$[\prec .X]$$
 for all $u \in p(v)$, $v \neq u$ and $\lambda(u) \notin \{X,Y\} \implies v \prec u$.

$$[\prec .Z]$$
 for all $u \in \text{odd}(p(v))$, $v \neq u$ and $\lambda(u) \notin \{Y,Z\} \implies v \prec u$.

$$[\prec .Y]$$
 for all $v \not\prec u$, $v \neq u$ and $\lambda(u) = Y \implies u \notin p(v) \triangle \operatorname{odd}(p(v))$

$$[\lambda.XY] \ \lambda(u) = XY \implies v \in \text{odd}(p(v)) \ and \ v \notin p(v)$$

$$[\lambda.XZ] \ \lambda(u) = XZ \implies v \in p(v) \ and \ v \in odd(p(v))$$

$$[\lambda.YZ] \ \lambda(u) = YZ \implies v \in \mathrm{odd}(p(v)) \ and \ v \notin p(v)$$

$$[\lambda.X] \ \lambda(u) = X \implies v \in \text{odd}(p(v))$$

$$[\lambda.Z] \ \lambda(u) = Z \implies v \in p(v)$$

$$[\lambda . Y] \ \lambda(u) = Y \implies v \in p(v) \triangle \operatorname{odd}(p(v))$$

where, \triangle denotes the symmetric difference of sets.

The first three conditions are on the ordering \prec similar to gflow, with the additional exceptional case for planar measurements in the past. The other six conditions are identical to gflow, with the last three explicitly written for the planar case.

We can describe the stabiliser algebra for the correcting set p(v) as,

$$S(p(v)) = \prod_{w \in p(v)} X_w \prod_{w \in \text{odd}(p(v))} Z_w$$
(36)

The local operator at some vertex $u \in p(v)$ is,

$$P_u = X^{1_{u \in p(v)}} Z^{1_{u \in \text{odd}(p(v))}}$$

$$\tag{37}$$

where, $1_{x \in A}$ denotes the characteristics function – 1 if $x \in A$ and 0 if $x \notin A$.

The third axiom $[\prec Y]$ describes the (0,0) corresponding to a local I and (1,1) corresponding to a local Z cases. Note that writing $u \notin p(v) \cap \text{odd}(p(v))$ would not allow the trivial identity case.

5. References

- (1) Pauli and Stabilisers Watrous TQI
- (2) MBQC -
- (3) PDDAG –

- 6. Pauli Flow
 - 7. PDDAG