

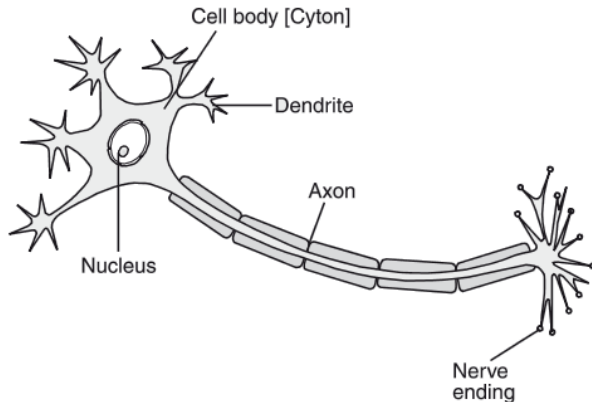
Introduction to Neural Networks

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Introduction

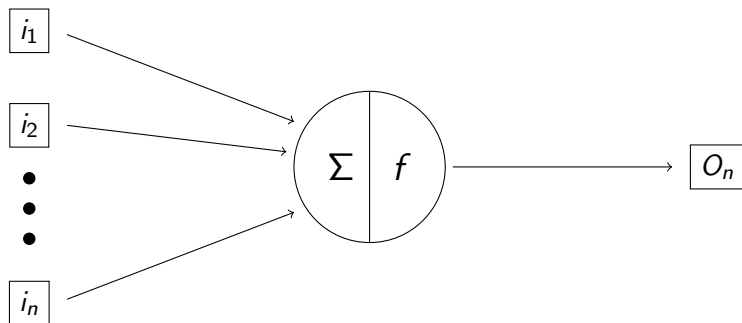


Theory

Let's start with a single neuron from the brain. Dendrites feed information into it, then there is the body of the neuron that performs some 'biology' operation on the inputs then outputs this information with its axons.

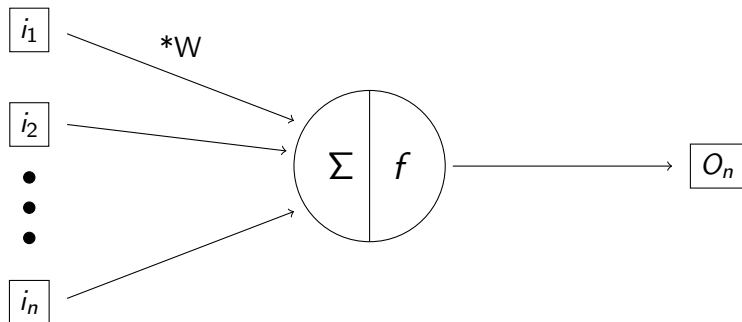
Single Neuron Construction

With this is in mind, let's try to model a single neuron mathematically:

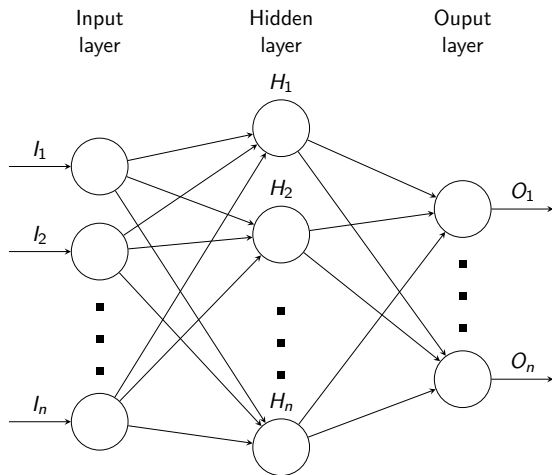


Our input denoted by i_n have our inputs and then flow into the 'nucleus' of the neuron. There, a function is performed on all of the inputs and that information is then passed to another neuron or neurons.

Single Neuron Construction



Full Neural Network



Let X_1, X_2, \dots, X_n be a sequence of independent and identically distributed random variables with $E[X_i] = \mu$ and $\text{Var}[X_i] = \sigma^2 < \infty$, and let

$$S_n = \frac{X_1 + X_2 + \dots + X_n}{n} = \frac{1}{n} \sum_i^n X_i$$

denote their mean. Then as n approaches infinity, the random variables $\sqrt{n}(S_n - \mu)$ converge in distribution to a normal $\mathcal{N}(0, \sigma^2)$.