# graphtools Documentation

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# INTRODUCTION

## 1.1 Hierarchy on Twitter

Who are the power players on Twitter (or in a Twitter community)? A good indicator of power is the number of followers a user has. But an identification of the powerful users based solely on the number of followers would miss the users with few but powerful followers. We describe a measure of a user's power which incorporates the power of the user's followers.

Consider the directed graph with vertices the users in a Twitter community and an arrow from user A to user B if and only if A follows B. In this graph, the powerful users will have many in neighbors (followers), and many of their out neighbors (friends) will be powerful themselves. On the other hand, the average user will have many out nieghbors but few in neighbors. Thus the Twitter graph may exhibit high hierarchy as defined below.

Let G = (V, E) be a directed graph. Write n = |V|, m = |E|. All of the following definitions are (directly or adapted) from [FHSN].

**Definition** A ranking of G is a map  $V \to \mathbb{N}$  where  $\mathbb{N}$  is the natural numbers, and the value of a vertex under the map is called the rank of the vertex. Denote the set of rankings of G by R(G).

**Definition** The **agony** of a ranking  $r \in R(G)$  is

$$A(r) := \sum_{(u,v) \in E} \max\{r(u) - r(v) + 1, 0\}.$$

The **hierarchy** of r is

$$h(r) := 1 - (1/m)A(r).$$

The agony of a ranking counts the arrows in the graph which don't go up in rank (counted with one more than the difference in ranks). The naive ranking by the zero map has agony m, so any ranking at least as good as the naive one has hierarchy between 0 and 1.

If a ranking of the graph of a Twitter community has high hierarchy, then the graph exhibits hierarchal structure and rank is a good indicator of power. In the next section, we describe an algorithm to find a ranking of a graph with high hierarchy. In the next chapter, we document an implementation of that algorithm.

# 1.2 The descent algorithm

Let G = (V, E) be a directed graph and let r be a ranking of G. Pick a vertex  $v \in V$ . Will updating r by increasing or decreasing the rank of v by 1 decrease the agony of r? The change in agony if the rank of v is increased by 1 is

$$i(v) := \big| \{ w \in V \mid v \to w \in E \& r(w) \le r(v) + 1 \} \big| - \big| \{ w \in V \mid w \to v \in E \& r(w) \ge r(v) \} \big|$$

while the change in agony if the rank of v is decreased by 1 is

$$i(v) := \big| \big\{ w \in V \mid w \to v \in E \ \& \ r(w) \ge r(v) - 1 \big\} \big| - \big| \big\{ w \in V \mid v \to w \in E \ \& \ r(w) \le r(v) \big\} \big|.$$

If  $i(v) \le -1$ , then increasing the rank of the vertex by 1 will decrease the agony of the ranking, as will decreasing the rank by 1 if  $d(v) \le -1$ 

Our algorithm, which we call the descent algorithm, starts with the naive ranking (all ranks are 0) and iteratively picks a vertex at random and changes its rank by 1 if doing so will decrease the agony of the ranking.

# AN IMPLEMENTATION OF THE ALGORITHM

## 2.1 graphtools Package

This package includes graphtools.gengraph.GenGraph, a superclass implementing the descent algorithm, and subclasses of GenGraph which accommodate various graph data structures. Namely

- graphtools.dbgraph.DBGraph reads graph data stored in a sqlalchemy-supported database,
- graphtools.sagegraph.SageGraph wraps a sage.graphs.digraph.DiGraph object, and
- graphtools.listgraph.ListGraph reads graph data stored as a list of arrows.

Multiple types for the vertices are supported. The type *vertex* refers to the instance-specific type of the vertices.

# 2.2 gengraph Module

class graphtools.gengraph.GenGraph

A graph superclass implementing the descent algorithm. Subclasses should overwrite

```
•get_num_arrows(),
•get_vert_list(),
•get_rank(),
•set_rank() and
•count_neighbors()
```

The method descent () runs the algorithm, updating the ranks of the vertices.

**count\_neighbors** (*vert*, *out=True*, *cond=False*, *less=True*, *cutoff=0*)

Count the number of neighbors of a vertex.

#### **Parameters**

- vert (vertex) the vertex to count the neighbors of
- out (bool) if True, count out neighbors, else in
- cond (bool) if True, count the neighbors satisfying a condition on rank
- less (bool) if True, count the neighbors with rank less than or equal to cutoff, else more

• **cutoff** (*int*) – the cutoff rank for the conditional

**Returns** the number of (in or out) neighbors of *vert* (perhaps satisfying a condition on the rank)

Return type int

```
descend (vert, debug=False)
```

Run one iteration of the descent algorithm.

#### **Parameters**

- **vert** (*vertex*) the vertex whose rank may change
- **debug** (*bool*) if True, output debug code

```
descent (num=1, debug=False)
```

Run descend() a number of times on random vertices.

#### **Parameters**

- **num** (int) the number of times to run descend()
- **debug** (*bool*) if True, output debug code

```
get_hierarchy_list()
```

Return the list of hierarchy scores.

**Returns** the list of hierarchy scores

Return type list

```
get_num_arrows()
```

Return the number of arrows.

**Returns** the number of arrows in the graph

Return type int

```
get_rank (vert)
```

Return the rank of vertex vert.

**Parameters vert** (*vertex*) – the vertex to get the rank of

Returns the rank of vert

Return type int

#### get\_vert\_list()

Return a list of the vertices of the graph.

**Returns** a list of vertices of the graph

Return type list

set\_rank (vert, newrank)

Set the rank of vertex *vert* to int *newrank*.

#### **Parameters**

- vert (vertex) the vertex to set the rank of
- newrank (int) the new rank of vert

# 2.3 dbgraph Module

```
class graphtools.dbgraph.DBGraph (users, arrows, conn, group=None)
    Bases: graphtools.gengraph.GenGraph
```

A subclass of GenGraph for graphs stored in databases.

The vertices are stored in a table called **users** with columns

```
•user_id (any type) and
•rank (int)
```

(the name comes from the original motivation which was Twitter user subgraphs). The table may also have a column *group* (any type) specifying the particular graph that the user belongs to if the database contains multiple graphs. If the table has no *group* column, *user\_id* should be a unique identifier; if there is a *group* column, *user\_id* and *group* together should be unique.

The arrows are stored in a table called **arrows** with columns

```
•follow_id and
•lead id
```

both referring to **users**.user\_id. If **users** has a group column then **arrows** should have a corresponding group column.

#### **Parameters**

- users (sqlalchemy.schema.Table) the table of vertices, described above
- arrows (sqlalchemy.schema.Table) the table of arrows, described above
- **conn** (*sqlalchemy.engine.base.Connection*) a connection to the database
- group (any) an optional identifier, described above

The initializer sets all entries in **user**.rank to 0.

```
reset_ranks()
Set all ranks to zero.
```

# 2.4 listgraph Module

```
{\bf class} \; {\tt graphtools.listgraph.ListGraph} \; ({\it arrows\_list}) \\ {\bf Bases:} \; {\tt graphtools.gengraph.GenGraph} \\
```

A subclass of GenGraph for graphs given as a list of arrows.

**Parameters arrows\_list** (*list*) – a list of the arrows in the graph; each arrow is an ordered list of 2 vertices (any type) where the first vertex is the tail of the arrow and the second is the head.

Graphs with isolated vertices (vertices with no neighbors) are not supported. Isolated vertices don't affect the hierarchy of the graph.

```
neighbors in(vert)
```

Return the list of in neighbors of vertex vert.

**Parameters vert** (*vertex*) – the vertex to count the neighbors of

Returns the number of in neighbors of vert

Return type int

```
neighbors_out(vert)
```

Return the list of out neighbors of vertex vert.

**Parameters vert** (*vertex*) – the vertex to count the neighbors of

**Returns** the number of out neighbors of *vert* 

Return type int

# 2.5 sagegraph Module

 ${f class}$  graphtools.sagegraph.SageGraph (dg)

Bases: graphtools.gengraph.GenGraph

A subclass of GenGraph which wraps a Sage DiGraph object.

Parameters dg (sage.graphs.digraph.DiGraph) - the Sage DiGraph to run descent on

# **BIBLIOGRAPHY**

[FHSN]	M. Gupte, P. Shankar, J	J. Li, S. Muthukrishnan	, L. Iftode, Finding l	hierarchy in directed	l online social network	īs.

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