

Title to find ...

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Abstract

Simulating large pairwise interactions is a very important issue for Scientific research. It plays an important role in Astrophysics to know the dynamics of galaxies, in plasma physics or in our case in biophysics. This kind of simulations is typically with a complexity of $\mathcal{O}(N^2)$ which scales badly with the size of the system.

Some other techniques, such as the PME (Particle Mesh Ewald) and the FMM (Fast Multipole Method) are able to obtain a complexity of respectively $\mathcal{O}(N \log(N))$ and $\mathcal{O}(N)$.

La simulation de larges systemes de particules en interaction est tres importante pour le calcul scientifique. Elles jouent un role important en Astrophysique pour connaitre la dynamique des galaxies, en physique des plasmas ainsi que, dans notre cas, en Biophysique.

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Presentation of the Lab

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Context of the Internship

The Context of this Internship is driven by the "SPPEXA (Software for exascale computing) / GromEx" project funded by the DFG (Deutsche Forschungsgemeinschaft). The Idea of this project is to create a flexible and fast solver for computing forces and potentials, which is a preliminary for molecular simulations.

A poster¹ of the project can be found below :

¹from <http://www.mpibpc.mpg.de/grubmueller/sppexa>

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Figure 1: Poster for the SPEXXA project

Currently the method used for computing electrostatic forces is called the PME (Particle Mesh Ewald). It works nicely but one of its problems is that the algorithms cannot be efficiently parallelised tasks as there is a lot of communication between the CPU and GPU cores. The idea would be to replace this method with a new method called the Fast-Multipole Method which is based on a tree Structure and may allow an greater parallelization of the system as wanted.

So the Idea of the Internship is first to know if the both method method have the same accuracy and for which parameters.

Chapter 1

Methods for computing electrostatic forces

1.1 $\mathcal{O}(N^2)$ method

In this section, we will explain the most basic method to compute pairwise interactions and explain why the method leads to long computation times and sometimes artifacts.

1.1.1 Naive Method

The coulombic interaction between two charged particles can be written the following way:

$$\vec{F}_{A \rightarrow B} = \frac{q_A q_B \hat{r}_{AB}}{4\pi\epsilon_0 |R_{AB}|^2} \quad (1.1)$$

where q_A and q_B are respectively the charges of A and B, and R_{AB} is the distance between A and B.

In the thesis we will simplify the units of (1.1) for computational reasons by just writing :

$$\vec{F}_{A \rightarrow B} = \frac{q_A q_B \hat{r}_{AB}}{|R_{AB}|^2} \quad (1.2)$$

The Corresponding potential for a charged particle, with a charge q is :

$$V = \frac{1}{r} \quad (1.3)$$

1.1. $\mathcal{O}(N^2)$ method

The first, naive way to compute electrostatic forces is the following : in order to compute the force acting on one particle, it is needed to obtain the coulombic interaction for each pair of particles.

So if we consider a set of N charged particles, $N - 1$ interactions are needed to compute the force acting on one specific particle. So in order to know the forces of the set of particles, $N \cdot (N - 1)$ operations are needed, hence an algorithmic complexity of $\mathcal{O}(N^2)$.

This gives the following algorithm:

```
input : A set of  $N$  charged Particles
output: A List of the forces for each particle

For each particle  $i$ ;
for  $i \leftarrow 1$  to  $N - 1$  do
    | add interaction between particle  $i$  and particle  $j$  ;
    | for  $j \leftarrow i + 1$  to  $N$  do
    | | force  $[i] \leftarrow$  force  $[i] + \text{computeForce}(i, j)$  ;
    | end
end
```

Algorithm 1: Naive method

The complexity of such a computation limits its use to rather small systems and is not really usable for bigger systems such as proteins or astrophysical systems.

1.1.2 Possible improvements

A possible improvement is to limit the interaction to a certain radius : if the distance between two particles is greater than R_0 , then the force is set to 0.

So we have the following system :

$$\vec{F}_{A \rightarrow B} = \begin{cases} \frac{q_A q_B \hat{r}_{AB}}{|R_{AB}|^2} & \text{if } R_{AB} < R_0 \\ \vec{0} & \text{otherwise} \end{cases} \quad (1.4)$$

This technique is for example used for Lennard-Jones potentials ($V_{LJ} = 4\epsilon[(\frac{\sigma}{r})^{12} - (\frac{\sigma}{r})^6]$), where the Intensity of the force is quickly decreasing. It allows to limit the number of interactions to only the close neighbours.

However, one of the problems of this optimisation, especially for long-range interactions such as coulombic interactions is that using a cut-off can lead to artefacts : A particle feels the force, then crosses the cut-off radius. Suddenly, the particle doesn't feel any force anymore, thus the artefacts as it is showed figure 1.1 .

1.2. Fourier Transform-Based methods

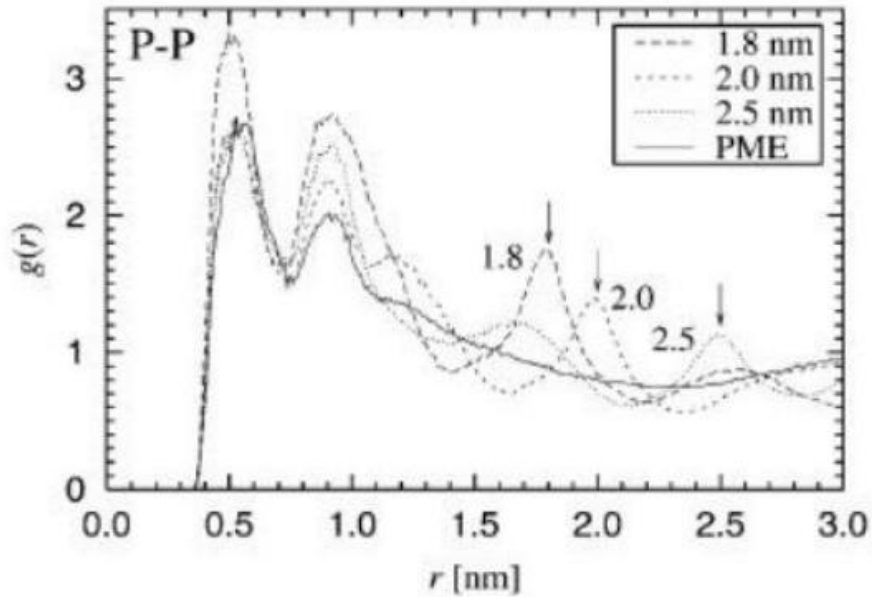


Figure 1.1: Radial distribution function (RDF) $g(r)$ between the two central atoms in the headgroup of a molecule: Cutoff distances are indicated by arrows. from [ADD REFERENCE]

As we can see in figure 1.1, the radial distribution of the distance between two atom shows a peak, corresponding to the cutoff of the system. This shows that by using a cut-off technique we might see some artefacts.

So the two reasons we don't use a $\mathcal{O}(N^2)$ method is first because of its complexity, and using some optimization techniques can also lead to artifacts.

1.2 Fourier Transform-Based methods

In this section, we will explain techniques using periodic boundary conditions and Fourier transformation in order to compute the potentials and the forces of the particles.

1.2.1 Ewald Summation

This subset of techniques comes from a theoretical physics technique called the Ewald summation.

Using periodic boundary conditions, the potential V of one particle of the system is:

1.2. Fourier Transform-Based methods

$$V = \sum_{n_x, n_y, n_z} \sum_i^N \sum_j^N \frac{q_i q_j}{r_{ij}} \quad (1.5)$$

where n_x, n_y, n_z are the box index vector.

The equation 1.5 is conditionally convergent and slow to converge. One technique discovered by Ewald is to split the potential in two absolutely convergent terms and one constant term:

If the system is neutral, ie. $\sum_{i=1}^N q_i = 0$, The idea is to split the potential the following way :

$$V = \frac{1}{r} = \frac{f(x)}{r} + \frac{1-f(x)}{r} \quad (1.6)$$

$$V = V_{\text{direct}} + V_{\text{reciprocal}} \quad (1.7)$$

We want to choose f , so that $\frac{f(x)}{r}$ is quickly decaying and $\frac{1-f(x)}{r}$ is as smooth as possible. In this decomposition $\frac{f(x)}{r}$ is as small as possible, even 0 above a certain cut-off. Then, $\frac{1-f(x)}{r}$ is smooth enough so we can compute its Fourier transform with just a few \vec{k} vectors. This gives a quick computation of the reciprocal space.

a good choice is often $f(x) = \text{erfc}(\alpha x)$, where α is called the splitting parameter, and $\text{erfc}(x) = \frac{2}{\sqrt{\pi}} \int_x^{+\infty} e^{-t^2} dt$

so we obtain the following potentials :

For the direct space :

$$V_{\text{direct}} = \frac{1}{2} \sum_{n_x, n_y, n_z} \sum_{i,j}^N q_i q_j \frac{\text{erfc}(\alpha r)}{r} \quad (1.8)$$

and for the reciprocal space :

$$V_{\text{reciprocal}} = \frac{1}{2\pi V} \sum_{i,j}^N q_i q_j \sum_{n_x^*, n_y^*, n_z^*} \frac{\exp -(\pi \vec{m}/\alpha)^2 + 2\pi i \vec{m} \cdot (r_i - r_j)}{m^2} \quad (1.9)$$

where n_x^*, n_y^*, n_z^* are the vectors in the reciprocal space.

1.2. Fourier Transform-Based methods

Once the electrostatic potentials are obtained, it is possible to differentiate the potentials to obtain the force on each particle.

let $p = (x, y, z)$ a coordinate of the system, then :

$$\vec{F}_p^{\text{direct}} = \vec{\nabla}_p V_{\text{direct}} \quad (1.10)$$

so we have:

$$\vec{F}_p^{\text{direct}} = q_i \sum_{i=1, i \neq j}^N \sum_{\mathbf{n}} q_j \frac{(r_{ij,n})_p}{r_{ij,n}^3} \left\{ \text{erfc}(\alpha r_{ij,n}) + \frac{2\alpha}{\sqrt{\pi}} r_{ij,n} \exp(-(\alpha r_{ij,n})^2) \right\} \quad (1.11)$$

$$\vec{F}_p^{\text{reciprocal}} = \frac{2q_i}{L} \sum_{i=1, i \neq j}^N \sum_{\mathbf{n}^* \neq 0} \frac{n_p^*}{n^{*2}} \exp\left(-\left(\frac{\pi m}{\alpha L}\right)^2\right) \sin \frac{2\pi}{L} m \cdot r_{ij} \quad (1.12)$$

Equations 1.11 and 1.12 can then be used to compute the force on each particle by adding the direct space and the reciprocal space contribution.

1.2.2 PME

One way to improve this method is to compute the fourier sum using the FFT (Fast Fourier Transform). This allows the algorithm to get a complexity of $\mathcal{O}(N \log N)$. There is different methods that are based on the Ewald summation, namely the **P3M** (Particle-Particle Particle-Mesh Method) or the **FFP** (Fast fourier poisson method).

In our case, we will focus on the **PME** as it is the method currently used in GROMACS.

We remind that the potential for the reciprocal space $V_{\text{reciprocal}}$ is written in equation (1.9):

$$V_{\text{reciprocal}} = \frac{1}{2\pi V} \sum_{i,j} q_i q_j \sum_{\mathbf{n}^*} \frac{\exp\left[-(\pi \vec{m}/\alpha)^2 + 2\pi i \vec{m} \cdot (r_i - r_j)\right]}{m^2}$$

This equation can be rewritten as :

1.3. Fast Summation methods

$$V_{\text{reciprocal}} = \frac{1}{2\pi V} \sum_{\mathbf{n}^* \neq 0}^N \frac{\exp -(\pi \vec{m}/\alpha)^2}{m^2} S(-\mathbf{n}^*) S(\mathbf{n}^*)$$

where $S(\mathbf{n}^*)$ is defined as the Structure factor:

$$S(\mathbf{n}^*) = \sum_{k=1}^N q_k \exp(2\pi i \mathbf{n}^* \cdot \mathbf{r}) \quad (1.13)$$

The idea of the method is the following : In order to apply a FFT to the system, it is needed to "map" the positions of the charges on a grid of size $p \times p$. We will define the size of the Grid as the *Fourier Spacing*. Let also define $\mathcal{F}(Q)$ the 3D FFT of Q . The charges q_i are mapped to the grid using interpolation. Originally, lagrange interpolation was used, but now a b-spline interpolation is used. The order of interpolation is called the *PME Order*

then the Structure factor can be approximated as its FFT :

$$S(\mathbf{m}) \approx \tilde{S}(\mathbf{m}) = \mathcal{F}(Q)(\mathbf{m}) \quad (1.14)$$

so the reciprocal energy can also be approximated by:

$$V_{\text{reciprocal}} \approx \tilde{V}_{\text{reciprocal}} = \frac{1}{2\pi V} \sum_{\mathbf{n}^* \neq 0}^N \frac{\exp -(\pi \vec{m}/\alpha)^2}{m^2} \mathcal{F}(Q)(\mathbf{m}) \mathcal{F}(Q)(-\mathbf{m}) \quad (1.15)$$

It can be shown that the complexity of such a system is $\mathcal{O}(N \log(N))$ which is a much bigger improvement compared to the $\mathcal{O}(N^2)$ complexity of the direct algorithm. However, one of its disadvantages is that it relies on a periodic sum, which is theoretically infinite.

1.3 Fast Summation methods

In the previous section we showed a method which allows to improve the speed of the computation. In this section, another algorithm will be explained, which has a complexity of $\mathcal{O}(N)$.

1.3. Fast Summation methods

1.3.1 Mathematical preliminaries

Let's move back to the potential created by a charged particle as in (1.3),

$$V = \frac{1}{d}$$

Let two particles $A(a, \alpha, \beta)$ and $B(r, \theta, \phi)$, separated by a certain distance d : The distance between the particles is $d = |a - r|$. We would like to achieve is to "factorize the addition", having a product of one function depending only on a and one depending only on r .

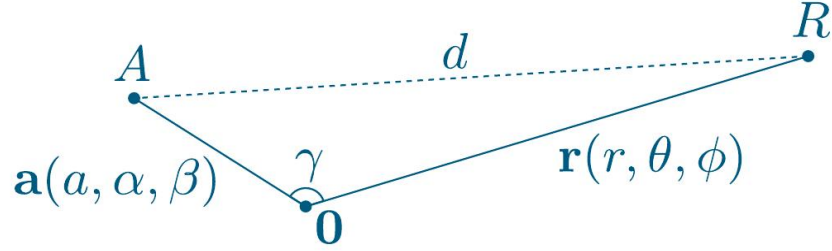


Figure 1.2: Figure representing two particles $A(a, \alpha, \beta)$ and $B(r, \theta, \phi)$, separated by a certain distance d

The inverse distance can be written as :

$$\frac{1}{d} = \frac{1}{|a - r|} = \frac{1}{\sqrt{a^2 + r^2}}$$

This distance can then written as a series :

$$\frac{1}{d} = \frac{1}{\sqrt{a^2 + r^2}} = \sum_{l=0}^{+\infty} P_l(u) \mu^l \quad (1.16)$$

where $\mu = \frac{a}{r}$ and $u = \cos \gamma$. The $P_l(u)$ are the Legendre polynomials of degree l .

with some manipulation as explained [ADD REFERENCE], we obtain :

$$\frac{1}{|r - a|} = \sum_{l=0}^{+\infty} \sum_{m=-l}^{+l} \frac{(l-m)!}{(l+m)!} \frac{a^l}{r^{l+1}} P_{lm} \cos(\alpha) P_{lm} \cos(\theta) e^{-im(\beta-\alpha)} \quad (1.17)$$

in order to approximate the scheme, we can truncate the series to a certain order p , we call this order the **multipole order**

1.3. Fast Summation methods

$$\frac{1}{|r-a|} \simeq \sum_{l=0}^{\textcolor{red}{p}} \sum_{m=-l}^{+l} \frac{(l-m)!}{(l+m)!} \frac{a^l}{r^{l+1}} P_{lm} \cos(\alpha) P_{lm} \cos(\theta) e^{-im(\beta-\alpha)} \quad (1.18)$$

We can now rewrite the summation the following way :

$$\frac{1}{|r-a|} \simeq \sum_{l=0}^p \sum_{m=-l}^{+l} \underbrace{\frac{a^l}{(l+m)!} P_{lm}(\cos(\alpha)) e^{-im\beta}}_{O_{lm}(\mathbf{a})} \underbrace{\frac{(l-m)!}{r^{l+1}} P_{lm}(\cos(\theta)) e^{+im\phi}}_{M_{lm}(\mathbf{r})} \quad (1.19)$$

hence,

$$\frac{1}{|r-a|} \simeq \sum_{l=0}^p \sum_{m=-l}^{+l} O_{lm}(\mathbf{a}) M_{lm}(\mathbf{r}) \quad (1.20)$$

We have shown that it is possible to "factorize" the inverse of the the distance $\frac{1}{d}$ so we can obtain two independent terms for two independent particles $O_{lm}(\mathbf{a})$ and $M_{lm}(\mathbf{r})$

We can then define the multipole moment $\omega_{lm}(q, \mathbf{a}) = q O_{lm}(\mathbf{a})$ and the Taylor-like moment $\mu_{lm}(q, \mathbf{r}) = q M_{lm}(\mathbf{r})$

Then, it is possible to show that it is possible to obtain the following "bipolar expansion" for two particles associated with two different origins :

$$\frac{1}{|\mathbf{a}_1 - \mathbf{a}_2 + \mathbf{R}|} = \sum_{l=0}^{+\infty} \sum_{j=0}^{+\infty} \sum_{m=-l}^{+l} \sum_{k=-j}^{+j} (-1)^j \cdot O_{lm}(\mathbf{a}_1) \cdot M_{l+j, m+k}(\mathbf{R}) \cdot O_{jk}(\mathbf{a}_2) \quad (1.21)$$

1.3. Fast Summation methods

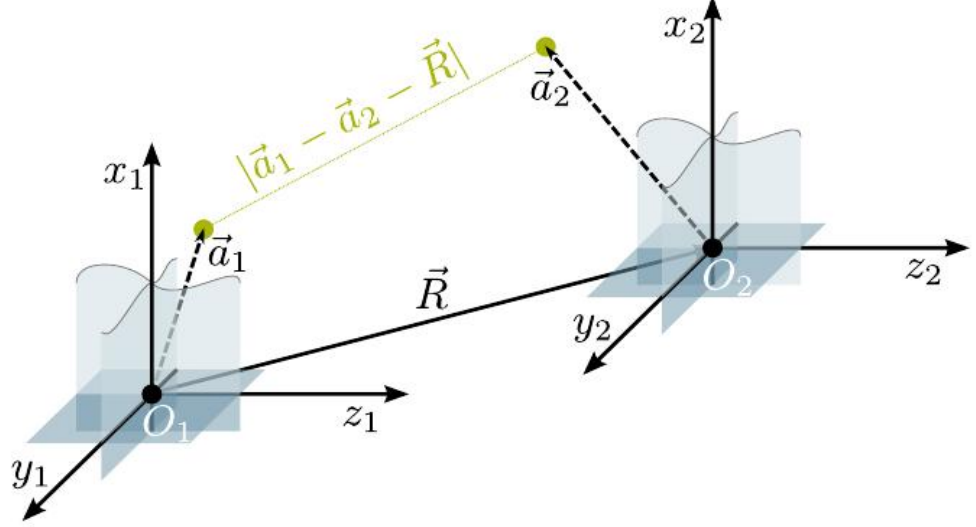


Figure 1.3: Scheme of two particles expanded according to two different origins [from ADD REFERENCE]

1.3.2 Workflow of the algorithm

Once some Mathematical preliminaries are set, it is possible to explain the workflow of the Algorithm.

1.3.2.1 Splitting the Space

The first step of the scheme is to split the space in order to generate different groups. The idea is to recursively split the space in eight octants, created the so-called structure of an *octree*. So the number of boxes is 8^{D-1} , where D is the depth of the oct-tree.

1.3. Fast Summation methods

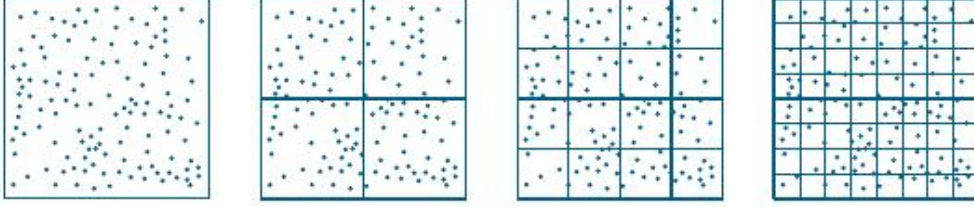


Figure 1.4: Example of a division of the space in boxes. The following example is in 2D so the structure of the space is a *quadtree*.

The number of subdivisions is called the *depth* D . For example, in figure 1.5, we can observe from left to right the depths 0, 1, 2 and 3.

It is then possible to assign each particle of the simulation to the boxes of lowest depth.

1.3.2.2 Defining a Separation Criterion

For the further Computations it is needed to define a separation criterion ws : It is the ws^{th} next neighbours of a given box. Two boxes A and B are called *next neighbors* if they are at the same level and box B is enclosed by a box of size $(2ws + 1)^3$ around the center of A

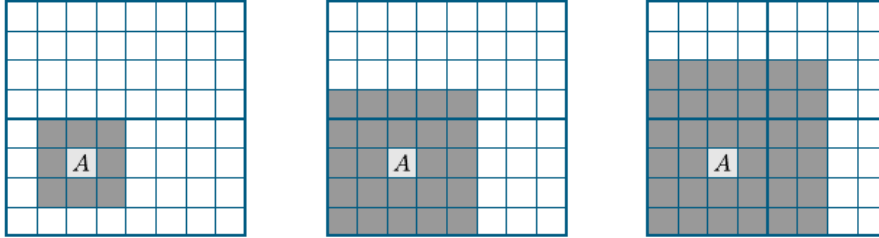


Figure 1.5: Example of the influence of the separation criterion ws for a given box A, from left to right, $ws = 1, 2, 3$.

This separation criterion divides the space into two parts. If two particles are close so they are in the same grey space as defined figure (1.8), then, they will interact via a direct $\mathcal{O}(N^2)$ coulombic interaction ; else they will interact via using the FMM Method.

It is most of the time not possible to set the separation criterion ws to 0, as the multipole expansion might overlap. Using a bigger ws means that the order of the multipole expansions need to be less important for the same

1.3. Fast Summation methods

precision, however this will increase the number of direct $\mathcal{O}(N^2)$ operation, which are more computationally expensive.

1.3.2.3 PASS 1 : Computing the Multipole moments

Once every particle is assigned to its box, we will compute the multipole moment ω_{lm}^j of each box.

$$\omega_{lm}^j(q, \mathbf{a}) = q^j a_j^l \tilde{P}_{lm}(\cos(\alpha_j)) e^{-im\beta_j} \quad (1.22)$$

Then each multipole order can be moved to the Center of the box using the so-called *M2M* (Multipole to Multipole) operator:

$$\omega(\mathbf{a} + \mathbf{b}) = \sum_{j=0}^k \sum_{k=-j}^j \omega_{jk}(\mathbf{a}) O_{l-j, m-k}(\mathbf{b}) \quad (1.23)$$

$O_{l-j, m-k}(\mathbf{b})$ is called the *M2M* operator

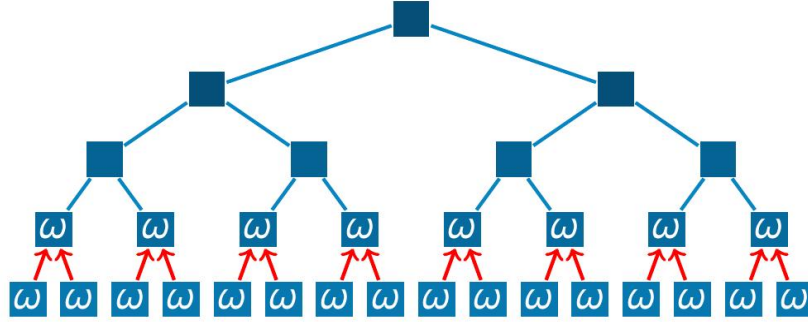


Figure 1.6: Example in 1-D showing the shifting of the multipole moments using the M2M operator.

1.3.2.4 PASS 2 : Transforming distant expansions into multipoles

Now it is possible to transform distant expansions (above the separation criterion) ω_{lm} into a Taylor-like moment μ_{lm} . This transformation is done over at most 189 boxes. This transformation is applied for each depth of the tree.

1.3. Fast Summation methods

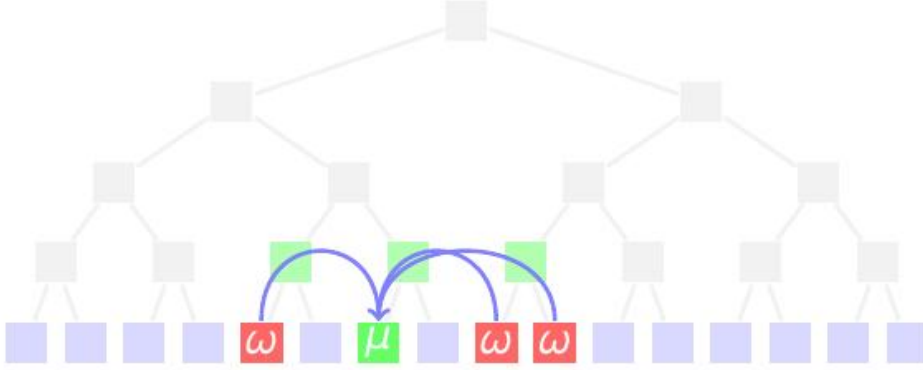
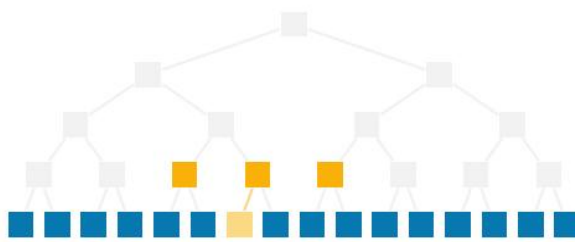


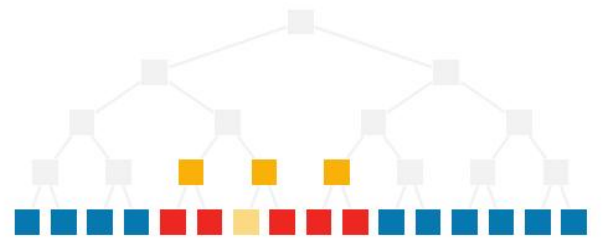
Figure 1.7: Example in 1-D showing the transformation of distant expansions into multipoles

In order to compute this transformation, two different rules have to be applied:

- The first rule is to take the non-separated parent boxes, as showed sub-figure (a) below.
- Then the children of the parent box are selected, taking into account the separation criterion for the child boxes.



(a) First, the parents of the box are chosen



(b) Then, then children of the parents are chosen. Then the separation criterion can apply

Figure 1.8: Iteration Rules for the transformation of the multipole expansions

Mathematically speaking, the transformation from multipole expansions to multipole moments is given using the M2L (Multipole to Local) Operator

1.3. Fast Summation methods

$$\mu_{lm}(\mathbf{b} - \mathbf{a}) = \sum_{j=0}^{+\infty} \sum_{k=-j}^j M_{j+l,k+m}(\mathbf{b}) \cdot \omega_{jk}(\mathbf{a}) \quad (1.24)$$

where $M_{j+l,k+m}(\mathbf{b})$ is the M2L operator : It allows to exchange, as figure (??) shows, information between boxes of the same level.

1.3.2.5 PASS 3 : Shift Taylor-Like expansions down the tree

Once the local μ_{lm} expansions are computed, the expansion have to shifted to the lowest level of the tree using the L2L (Local to Local) operator.

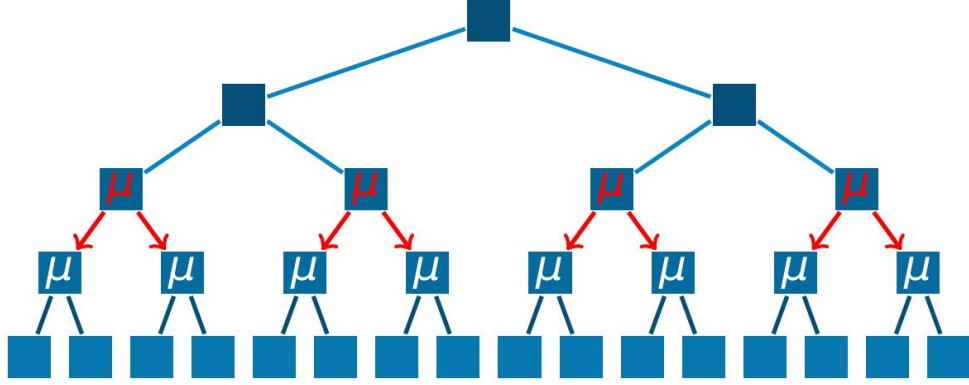


Figure 1.9: Example in 1-D showing the shifting of the local moments using the L2L operator.

This shift operation is done by the following formula :

$$\mu_{lm}(\mathbf{r} - \mathbf{b}) = \sum_{j=l}^p \sum_{k=-j}^j O_{j-l,k-m}(\mathbf{b}) \cdot \mu_{jk}(\mathbf{a}) \quad (1.25)$$

where $O_{j-l,k-m}(\mathbf{b})$ is the L2L operator : It allows to exchange, as figure (??) shows, information between levels downwards.

1.3.2.6 PASS 4 : Computing forces and Energies

After PASS 3, we have at the lowest level both the multipole expansion as well as the local expansion.

1.3. Fast Summation methods

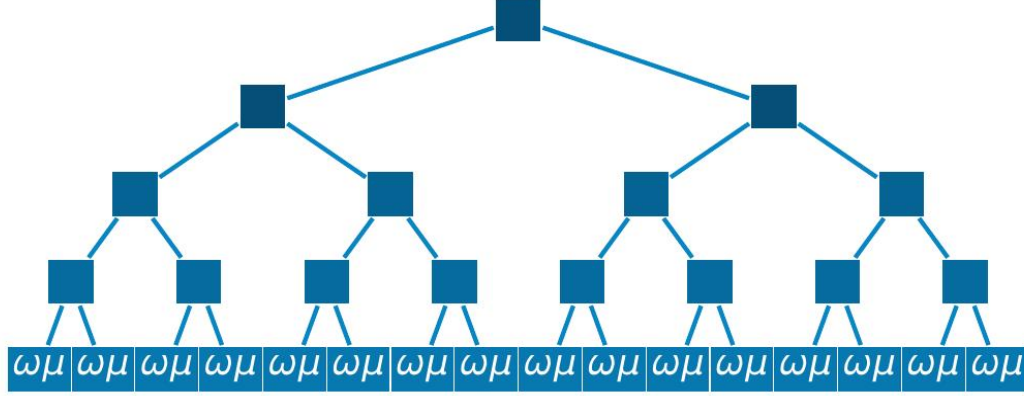


Figure 1.10: Situation after PASS 3

Then we have everything to compute the far-field contribution for the forces or the portentials of the system.

So we have for the Electric Field :

$$E_{FF} = \sum_{l=0}^p \sum_{m=-l}^{+l} \mu_{lm}(\mathbf{r}) \omega_{lm}(\mathbf{a}) \quad (1.26)$$

For the Potential :

$$\Phi_{FF} = - \sum_{l=0}^p \sum_{m=-l}^{+l} \mu_{lm}(\mathbf{r}) \nabla_{\mathbf{a}_i} [a_i^l \tilde{P}_{lm}(\cos \alpha_i) e^{-im\beta_i}] \quad (1.27)$$

and for the Force :

$$\mathbf{F}_{FF} = - \sum_{l=0}^p \sum_{m=-l}^{+l} \mu_{lm}(\mathbf{r}) \nabla_{\mathbf{a}_i} [a_i^l \tilde{P}_{lm}(\cos \alpha_i) e^{-im\beta_i}] \quad (1.28)$$

Then the near-field contribution can be easiliy computed :

Chapter 2

Comparing FMM and PME accuracy

In this chapter I will more precisely explain my work done in the Lab, which consisted in comparing the PME methods, which is for example used by gromacs, and the FMM method, used by a solver made between the Jülich Forschungszentrum and the Max Planck Institute for Biophysics in Göttingen.

I will first explain for Gromacs work and then

2.1 Presentation of GROMACS

GROMACS (GRoningen MACHine for Chemical Simulations) is a simulation software used for Molecular dynamics. It was originally developed in the Biophysical Chemistry department of University of Groningen but it is now developed around the world. GROMACS is made to be as fast as possible using all possible techniques to improve its performance (MPI, GPU computing)

2.1.1 Structure of a File

The program is used by modifying text files that giving information on the structure of the system that has to be simulated and the parameters of the simulation. The files are the following

- The *.pdb file are the *Protein DataBank* file : In this file is denoted the position and the type of the particles of the system. It also gives the size of the simulation box

2.1. Presentation of GROMACS

- The *.top files (namelt *topology* files) are the file where the properities of the atoms are defined. These properties are for example the charge, the Van-der-Waals parameters or the binding forces of the system. This configuration is often done with force field files such as AMBER or CHARMM
- The *.mdp files are defining the physical and computational parameters of the simulation. It is defining the methods used for the simulation. In our case we are mostly interested in the electrostatics part of the computation ; it is then possible to select the method (PME or Cut-Off methods) and the parameters for the PME

2.1.2 PME parameters

In this paragraph I will explain the parameters it is possible to play with:

CutOff The first parameter is the CutOff : It allows to set the Cut-Off radius for the Cut-Off method, but it also sets the difference between the direct part and the reciprocal part in the PME method

Fourier Spacing The other important parameter is the fourier spacing. I remind that in the PME method a 3D FFT is done in order to compute the energies and the forces of the system. The FFT is so computed on a grid : The dimension of the grid is given by the *Fourier Spacing* parameter.

PME Order The PME order gives the order of the interpolation. For instance, PMEorder= 4 corresponds to a cubic interpolation.

2.1.3 Command to launch a GROMACS simulation

The workflow to launch a GROMACS Simulation is the following :

First generate a .tpr binary file conaining all the information about the simulation. The file is processed using the *grompp* (Gromacs Preprocessor). The command is :

```
grompp -f mdpfile
      -p topFile.top
      -c pdbFile.pdb
      -o tprFile.tpr
```

where the input files are the *.mdp , *.top and *.pdb (Respectively properties of the Simulation, of the atom, and the oposition of the At and contains arroundoms). The *.tpr file ris the output file.

2.2. Presentation of fmsolvr

It is then possible to run the simulation using the program `mdrun`, which as its name stands, runs the md simulation. A possible example is :

```
mdrun -s tprfile.tpr
      -ntomp = 4
      -ntmpi = 4
      -nsteps= 0
```

Where the `.tpr` File is now the input file, containing everything about the simulation, `-nsteps` is the number of time steps needed (In the case of this Internship, no time intergration is needed as just the forces are required). It is also possible to choose the number of CPU cores needed for the simulation (Using MPI and OpenMP).

2.2 Presentation of fmsolvr

The software used to compute the electrostatic forces with the FMM is not `gromacs` (at least not for the moment). It is developed by both the Max-Planck Institut for Biophysical Chemistry and the Jülich Forschungszentrum . In the following chapters, we will call this code *fmsolvr*.

The codebase is mostly written in C++. There exists several git branches for the program, allowing different versions of the system. The First version is a sequential version, which is the "basic" version of the FMM code . There also exists a version which allows periodic boundary conditions : We will use this version a lot as we need to compare it to the PME, which, by construction, uses periodic boundary conditions.

The input file, is a `*.hpp` file containing 4 arrays of size N , where N is the number of atoms in the simulation : one charge array q , and three array x, y, z for the positions of the atoms.

2.2.1 FMM Parameters

The simulation can be launched using the following command :

```
DEPTH=$DEPTH MULTIPOLEORDER=$MULTIPOLEORDER WS=$WS
OPENBOUNDARY=0 UNITBOX=$UNITBOX CENTER=c
./fmmtest $inputFile.qxyz $outputFile.dat
```

The environment variables are the following :

DEPTH The maximal subdivision of the space : if `DEPTH=n` the space will be divided in 8^n boxes.

2.3. Making GROMACS and fmsolvr comparable

MULTIPOLEORDER The Order of truncation in a the series, for instance :

$$\frac{1}{|r - a|} \simeq \sum_{l=0}^{\textcolor{red}{p}} \sum_{m=-l}^{+l} \frac{(l-m)!}{(l+m)!} \frac{a^l}{r^{l+1}} P_{lm} \cos(\alpha) P_{lm} \cos(\theta) e^{-im(\beta-\alpha)}$$

where the multipole order is the red **p** in the first summation.

WS This gives the separation criterion $ws \geq 1$, which separates the far-field computation from the near space.

OPENBOUDARY if OPENBOUNDARY = 0, periodic boundary conditions will be used, if OPENBOUNDARY=1, then openboundaries will be used.

UNITBOX Gives the size of the simulation box (in nm).

2.3 Making GROMACS and fmsolvr comparable

The first part, if we want to make the PME and the FMM comparable, is to use the same simulation for both programs, hence requiring coding some tools transforming a GROMACS-compatible file to fmsolvr-compatible one. Then, we saw that the results we obtained weren't good enough as one system was using some dipole correction, so we needed to implements the dipole correction to the FMM system.

2.3.1 File manipulation

2.3.1.1 Making GROMACS only compute electrostatics forces

2.3.1.2 Assure compatibility between *.qxyz and *.pdb files

2.3.2 Adding Dipole correction to fmsolvr

2.4 Discussion

Conclusion

Appendices

Appendix A

Glossary

Appendix B

Structure of Gromacs files

The contents...