- 1. A mathematical sequence is an ordered list of numbers. This question involves a sequence called a hailstone sequence. If n is the value of a term in the sequence, then the following rules are used to find the next term, if one exists.
  - If *n* is 1, the sequence terminates.
  - If *n* is even, then the next term is  $\frac{n}{2}$ .
  - If n is odd, then the next term is 3n + 1.

For this question, assume that when the rules are applied, the sequence will eventually terminate with the term n=1.

The following are examples of hailstone sequences.

## Example 1: 5, 16, 8, 4, 2, 1

- The first term is 5, so the second term is 5\*3+1=16.
- The second term is 16, so the third term is  $\frac{16}{2} = 8$ .
- The third term is 8, so the fourth term is  $\frac{8}{2} = 4$ .
- The fourth term is 4, so the fifth term is  $\frac{4}{2} = 2$ .
- The fifth term is 2, so the sixth term is  $\frac{2}{2} = 1$ .
- Since the sixth term is 1, the sequence terminates.

## Example 2: 8, 4, 2, 1

- The first term is 8, so the second term is  $\frac{8}{2} = 4$ .
- The second term is 4, so the third term is  $\frac{4}{2} = 2$ .
- The third term is 2, so the fourth term is  $\frac{2}{2} = 1$ .
- Since the fourth term is 1, the sequence terminates.

The Hailstone class, shown below, is used to represent a hailstone sequence. You will write three methods in the Hailstone class.

```
public class Hailstone
{
    /** Returns the length of a hailstone sequence that starts with n,
     * as described in part (a).
     * Precondition: n > 0
     */
   public static int hailstoneLength(int n)
    { /* to be implemented in part (a) */ }
    /** Returns true if the hailstone sequence that starts with n is considered long
     * and false otherwise, as described in part (b).
     * Precondition: n > 0
   public static boolean isLongSeq(int n)
    { /* to be implemented in part (b) */ }
    /** Returns the proportion of the first n hailstone sequences that are considered long,
     * as described in part (c).
     * Precondition: n > 0
     */
    public static double propLong(int n)
    { /* to be implemented in part (c) */ }
    // There may be instance variables, constructors, and methods not shown.
}
```

(a) The length of a hailstone sequence is the number of terms it contains. For example, the hailstone sequence in example 1 (5, 16, 8, 4, 2, 1) has a length of 6 and the hailstone sequence in example 2 (8, 4, 2, 1) has a length of 4.

Write the method hailstoneLength(int n), which returns the length of the hailstone sequence that starts with n.

```
/** Returns the length of a hailstone sequence that starts with n, as described in part (a).
 * Precondition: n > 0
 */
public static int hailstoneLength(int n)
```

Begin your response at the top of a new page in the Free Response booklet and fill in the appropriate circle indicating the question number. If there are multiple parts to this question, write the part letter with your response.

```
Class information for this question
public class Hailstone
public static int hailstoneLength(int n)
public static boolean isLongSeq(int n)
public static double propLong(int n)
```

(b) A hailstone sequence is considered long if its length is greater than its starting value. For example, the hailstone sequence in example 1 (5, 16, 8, 4, 2, 1) is considered long because its length (6) is greater than its starting value (5). The hailstone sequence in example 2 (8, 4, 2, 1) is not considered long because its length (4) is less than or equal to its starting value (8).

Write the method isLongSeq(int n), which returns true if the hailstone sequence starting with n is considered long and returns false otherwise. Assume that hailstoneLength works as intended, regardless of what you wrote in part (a). You must use hailstoneLength appropriately to receive full credit.

```
/** Returns true if the hailstone sequence that starts with n is considered long
* and false otherwise, as described in part (b).
* Precondition: n > 0
*/
public static boolean isLongSeq(int n)
```

Begin your response at the top of a new page in the Free Response booklet and fill in the appropriate circle indicating the question number.

If there are multiple parts to this question, write the part letter with your response.

(c) The method propLong (int n) returns the proportion of long hailstone sequences with starting values between 1 and n, inclusive.

Consider the following table, which provides data about the hailstone sequences with starting values between 1 and 10, inclusive.

Starting Value	Terms in the Sequence	Length of the Sequence	Long?
1	1	1	No
2	2, 1	2	No
3	3, 10, 5, 16, 8, 4, 2, 1	8	Yes
4	4, 2, 1	3	No
5	5, 16, 8, 4, 2, 1	6	Yes
6	6, 3, 10, 5, 16, 8, 4, 2, 1	9	Yes
7	7, 22, 11, 34, 17, 52, 26, 13, 40, 20, 10, 5, 16, 8, 4, 2, 1	17	Yes
8	8, 4, 2, 1	4	No
9	9, 28, 14, 7, 22, 11, 34, 17, 52, 26, 13, 40, 20, 10, 5, 16, 8, 4, 2, 1	20	Yes
10	10, 5, 16, 8, 4, 2, 1	7	No

The method call Hailstone.propLong(10) returns 0.5, since 5 of the 10 hailstone sequences shown in the table are considered long.

Write the propLong method. Assume that hailstoneLength and isLongSeq work as intended, regardless of what you wrote in parts (a) and (b). You must use isLongSeq appropriately to receive full credit.

- /\*\* Returns the proportion of the first n hailstone sequences that are considered long,
- as described in part (c).
- **Precondition:** n > 0

public static double propLong(int n)

Begin your response at the top of a new page in the Free Response booklet and fill in the appropriate circle indicating the question number. If there are multiple parts to this question, write the part letter with your response.

```
Class information for this question
public class Hailstone
public static int hailstoneLength(int n)
public static boolean isLongSeq(int n)
public static double propLong(int n)
```

3. A student plans to analyze product reviews found on a Web site by looking for keywords in posted reviews. The ProductReview class, shown below, is used to represent a single review. A product review consists of a product name and a review of that product.

```
public class ProductReview
       private String name;
       private String review;
       /** Constructs a ProductReview object and initializes the instance variables. */
       public ProductReview(String pName, String pReview)
          name = pName;
          review = pReview;
       }
       /** Returns the name of the product. */
       public String getName()
       { return name; }
       /** Returns the review of the product. */
       public String getReview()
       { return review; }
The ReviewCollector class, shown below, is used to represent a collection of reviews to be analyzed.
   public class ReviewCollector
       private ArrayList<ProductReview> reviewList;
       private ArrayList<String> productList;
       /** Constructs a ReviewCollector object and initializes the instance variables. */
       public ReviewCollector()
           reviewList = new ArrayList<ProductReview>();
           productList = new ArrayList<String>();
       }
       /** Adds a new review to the collection of reviews, as described in part (a). */
       public void addReview(ProductReview prodReview)
       { /* to be implemented in part (a) */ }
       /** Returns the number of good reviews for a given product name, as described in part (b). */
       public int getNumGoodReviews(String prodName)
       { /* to be implemented in part (b) */ }
       // There may be instance variables, constructors, and methods not shown.
   }
```

- (a) Write the addReview method, which adds a single product review, represented by a ProductReview object, to the ReviewCollector object. The addReview method does the following when it adds a product review.
  - The ProductReview object is added to the reviewList instance variable.
  - The product name from the ProductReview object is added to the productList instance variable if the product name is not already found in productList.

Elements may be added to reviewList and productList in any order.

Complete method addReview.

/\*\* Adds a new review to the collection of reviews, as described in part (a). \*/
public void addReview(ProductReview prodReview)

Begin your response at the top of a new page in the Free Response booklet and fill in the appropriate circle indicating the question number. If there are multiple parts to this question, write the part letter with your response.

(b) Write the getNumGoodReviews method, which returns the number of good reviews for a given product name. A review is considered good if it contains the string "best" (all lowercase). If there are no reviews with a matching product name, the method returns 0. Note that a review that contains "BEST" or "Best" is not considered a good review (since not all the letters of "best" are lowercase), but a review that contains "asbestos" is considered a good review (since all the letters of "best" are lowercase).

Complete method getNumGoodReviews.

/\*\* Returns the number of good reviews for a given product name, as described in part (b). \*/ public int getNumGoodReviews(String prodName)

Begin your response at the top of a new page in the Free Response booklet and fill in the appropriate circle indicating the question number. If there are multiple parts to this question, write the part letter with your response.

```
Class information for this question
public class ProductReview
private String name
private String review
public ProductReview(String pName, String pReview)
public String getName()
public String getReview()
public class ReviewCollector
private ArrayList<ProductReview> reviewList
private ArrayList<String> productList
public ReviewCollector()
public void addReview(ProductReview prodReview)
public int getNumGoodReviews(String prodName)
```