Constrained Ordination

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Introduction

Introduction

Constrained Ordination

Canonical Correspondence Analysis

CCA is the constrained form of CA; fitted using cca().

Two interfaces for specifying models

- basic; cca1 <- cca(X = varespec, Y = varechem)</pre>
- formula; cca1 <- cca(varespec ~ ., data = varechem)</pre>

Formula interface is the more powerful — recommended

Canonical Correspondence Analysis

```
cca1 <- cca(varespec ~ .. data = varechem)
cca1
Call: cca(formula = varespec ~ N + P + K + Ca + Mg + S + Al + Fe +
Mn + Zn + Mo + Baresoil + Humdepth + pH, data = varechem)
             Inertia Proportion Rank
Total
              2.0832
                       1.0000
Constrained
             1 4415
                      0.6920 14
Unconstrained 0.6417
                      0.3080 9
Inertia is mean squared contingency coefficient
Eigenvalues for constrained axes:
 CCA1 CCA2 CCA3 CCA4 CCA5 CCA6 CCA7 CCA8 CCA9 CCA10
0.4389 0.2918 0.1628 0.1421 0.1180 0.0890 0.0703 0.0584 0.0311 0.0133
CCA11 CCA12 CCA13 CCA14
0.0084 0.0065 0.0062 0.0047
Eigenvalues for unconstrained axes:
    CA1
           CA2
                  CA3
                          CA4
                                  CA5
                                         CA6
                                                 CA7
                                                                CA9
0.19776 0.14193 0.10117 0.07079 0.05330 0.03330 0.01887 0.01510 0.00949
```

Redundancy Analysis

Eigenvalues for unconstrained axes: PC2 PC3

PC4 PC5 PC6

186.19 88.46 38.19 18.40 12.84 10.55 5.52 4.52 1.09

```
RDA is the constrained form of PCA: fitted using rda()
rda1 <- rda(varespec ~ ., data = varechem)
rda1
Call: rda(formula = varespec ~ N + P + K + Ca + Mg + S + Al + Fe +
Mn + Zn + Mo + Baresoil + Humdepth + pH, data = varechem)
              Inertia Proportion Rank
Total
            1825.6594
                         1.0000
Constrained 1459.8891
                         0.7997 14
                         0.2003 9
Unconstrained 365,7704
Inertia is variance
Eigenvalues for constrained axes:
 RDA1 RDA2 RDA3 RDA4 RDA5 RDA6 RDA7 RDA8 RDA9 RDA10 RDA11 RDA12
820.1 399.3 102.6 47.6 26.8 24.0 19.1 10.2 4.4 2.3 1.5 0.9
RDA13 RDA14
 0.7 0.3
```

PC7

The cca.object

- Objects of class "cca" are complex with many components
- Entire class described in ?cca.object
- · Depending on what analysis performed some components may be NULL
- \cdot Used for (C)CA, PCA, RDA, and CAP (capscale())

The cca.object

cca1 has a large number of components

- **\$call** how the function was called
- \$grand.total in (C)CA sum of 'rowsum}
- **\$rowsum** the row sums
- **\$colsum** the column sums
- **\$tot.chi** total inertia, sum of Eigenvalues
- **\$pCCA** Conditioned (partial-ed out) components
- **\$CCA** Constrained components
- **\$CA** Unconstrained components
- · \$method Ordination method used
- **\$inertia** Description of what inertia is

The cca.object

Depending on how one called cca() etc some of these components will be NULL

\$pCCA is only filled in if a *partial* constrained ordination fitted

rda() returns objects with classes "rda" and "cca", but in most cases those objects work like those of class "cca"

The Eigenvalues and axis scores are now spread about the \$CA and \$CCA components (also \$pCCA if a partial CCA)

Thankfully we can use extractor functions to get at such things

Eigenvalues

lise eigenvals() to extract Figenvalues from a fitted ordination object eigenvals(ccal)

```
CCA1
              CCA2
                        CCA3
                                  CCA4
                                                      CCA6
                                                                CCA7
                                            CCA5
0.4388704 0.2917753 0.1628465 0.1421302 0.1179519 0.0890291 0.0702945
    CCA8
              CCA9
                       CCA10
                                 CCA11
                                           CCA12
                                                     CCA13
                                                               CCA14
0.0583592 0.0311408 0.0132944 0.0083644 0.0065385 0.0061563 0.0047332
     CA1
               CA2
                         CA3
                                   CA4
                                             CA5
                                                       CA6
                                                                CA7
0.1977645 0.1419256 0.1011741 0.0707868 0.0533034 0.0332994 0.0188676
      CA8
               CA9
0.0151044 0.0094876
```

Your turn

- Fit a CCA model to the lichen pasture data. The model should include, N, P, and K only.
- · Save the model in object mycca1
- · How much variance is explained by this model?
- Extract the eigenvalues, how many constrained axes are there?

library("vegan")
data(varechem, varespec)
...your code here...

Extracting axis scores

To extract a range of scores from a fitted ordination use scores()

- · takes an ordination object as the first argument
- · choices which axes? Defaults to c(1,2)
- display which type(s) of scores to return
 - · "sites" or "wa": scores for samples in response matrix
 - "species": scores for variables/columns in response
 - · "lc": linear combination site scores
 - "bp": biplot scores (coords of arrow tip)
 - "cn": centroid scores (coords of factor centroids)

Extracting axis scores

Scalings...

When we draw the results of many ordinations we display 2 or more sets of data Can't display all of these and maintain relationships between the scores Solution scale one set of scores relative to the other via the scaling argument

- \cdot scaling = 1 Focus on sites, scale site scores by λ_i
- \cdot scaling = 2 Focus on species, scale species scores by λ_i
- · scaling = 3 Symmetric scaling, scale both scores by $\sqrt{\lambda_i}$
- · scaling = -1 As above, but
- · scaling = -2 For cca() multiply results by $\sqrt{(1/(1-\lambda_i))}$
- scaling = -3 this is Hill's scaling
- \cdot scaling < 0 For rda() divide species scores by species' σ
- scaling = 0 raw scores

scores(cca1, choices = 1:2, display = "species", scaling = 3)

Scalings...

Thankfully we can use alternative descrpitors to extract scores:

- · "none"
- · "sites"
- \cdot "species"
- · "symmetric"

Two modifiers select negative scores depending on whether the model is CCA or RDA:

- · hill = TRUE
- · correlation = TRUE

Your turn

 $\boldsymbol{\cdot}$ Using the CCA model you fitted, extract the site scores for axes 2 and 3 with Hill's scaling

Partial constrained ordinations

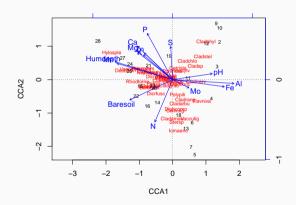
Partial constrained ordinations remove the effect of one or more variables then fit model of interest

Argument Z is used for a data frame of variables to partial out

Or with the formula interface use the Condition() function

Triplots

Triplots will generally produce a mess; we can really only display a couple of bits approximately anyway Trving to cram three things in is a recine for a mess—but we can do it plot(cca1)



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Your turn

- Using mycca, draw a triplot of axes 2 and 3 with sites scaling
- \cdot Use the help file ?plot.cca to help you work out how to do this

Building constrained ordination models

If we don't want to think it's easy to fit a poor model with many constraints

That's what I did with cca1 and rda1

Remember, CCA and RDA are just regression methods — everything you know about regression applies here

A better approach is to think about the important variables and include only those

The formula interface allows you to create interaction or quadratic terms easily (though be careful with latter)

It also handles factor or class constraints automatically unlike the basic interface

Building constrained ordination models

```
vare.cca <- cca(varespec ~ Al + P*(K + Baresoil), data = varechem)
vare.cca
Call: cca(formula = varespec ~ Al + P * (K + Baresoil), data =
varechem)
             Inertia Proportion Rank
Total
               2.083
                          1.000
Constrained
               1 846
                          0.502
                          0.498 17
Unconstrained 1.038
Inertia is mean squared contingency coefficient
Eigenvalues for constrained axes:
 CCA1 CCA2 CCA3 CCA4 CCA5 CCA6
0.3756 0.2342 0.1407 0.1323 0.1068 0.0561
Eigenvalues for unconstrained axes:
   CA1
           CA2
                                          CA6
                                                  CA7
0.27577 0.15411 0.13536 0.11803 0.08887 0.05511 0.04919 0.03781
(Showed only 8 of all 17 unconstrained eigenvalues)
```

Building constrained ordination models

For CCA we have little choice but to do

- 1. Fit well-chosen set of candidate models & compare, or
- 2. Fit a full model of well-chosen variables & then do stepwise selection

But automatic approaches to model building should be used cautiously!

The standard step() function can be used as vegan provides two helper methods, deviance() and extractAIC(), used by step()

Vegan also provides methods for class "cca" for add1() and drop1()

Variance inflation factors

Linear dependencies between constraints can be investigated via the variance inflation factor or VIF VIF is a measure of how much the variance of $\hat{\beta}_j$ is inflated by presence of other covariates Lots of rules of thumb

- VIF >= 20 indicates strong collinearity in constraints
- \cdot VIF >= 10 potentially of concern & should be looked at

Computed via vif.cca()

step() uses AIC which is a fudge for RDA/CCA. Alternatively use function ordistep()

- 1. Define an upper and lower model scope, say the full model and the null model
- 2. To step from the lower scope or null model we use

```
upr <- cca(varespec ~ ., data = varechem)
lwr <- cca(varespec ~ 1, data = varechem)
set.seed(1)
mods <- ordistep(lwr, scope = formula(upr), trace = 0)</pre>
```

trace = 0 is used her to turn off printing of progress

Permutation tests are used (more on these later); the theory for an AIC for ordination is somewhat loose

The object returned by step() is a standard "cca" object with an extra component \$anova

The \$anova component contains a summary of the steps involved in automatic model huilding mods

```
Call: cca(formula = varespec ~ Al + P + K, data = varechem)
             Inertia Proportion Rank
Total
              2.0832
                         1.0000
                         0.3092
Constrained
               0.6441
Unconstrained 1.4391
                         0.6908 20
Inertia is mean squared contingency coefficient
Eigenvalues for constrained axes:
 CCA1 CCA2 CCA3
0.3616 0.1700 0.1126
Eigenvalues for unconstrained axes:
   CA1
         CA2
                CA3
                       CA4
                              CA5
                                     CA6
                                            CA7
0.3500 0.2201 0.1851 0.1551 0.1351 0.1003 0.0773 0.0537
(Showed only 8 of all 20 unconstrained eigenvalues)
```

The **\$anova** component contains a summary of the steps involved in automatic model huilding mods\$anova

Step-wise model selection is fairly fragile; if we start from the full model we won't end up with the same

```
final modal
mods2 <- step(upr, scope = list(lower = formula(lwr), upper = formula(upr)), trace = 0,</pre>
             test = "perm")
mods2
Call: cca(formula = varespec ~ P + K + Mg + S + Mn + Mo + Baresoil
+ Humdenth, data = varechem)
             Inertia Proportion Rank
Total
              2.0832
                         1.0000
Constrained
              1 1165
                       0.5360
Unconstrained 0.9667
                        0.4640 15
Inertia is mean squared contingency coefficient
Eigenvalues for constrained axes:
 CCA1 CCA2 CCA3 CCA4 CCA5 CCA6 CCA7 CCA8
0.4007 0.2488 0.1488 0.1266 0.0875 0.0661 0.0250 0.0130
Eigenvalues for unconstrained axes:
            C<sub>A</sub>2
                    CA3
                                           CA6
                                                   CA7
0.25821 0.18813 0.11927 0.10204 0.08791 0.06085 0.04461 0.02782 0.02691
   CA10
           CA11
                   CA12
                          CA13
                                  CA14
                                          CA15
0.01646 0.01364 0.00823 0.00655 0.00365 0.00238
```

Adjusted R^2 for linear models

As with ordinary R^2 , that of an RDA is biased for the same reasons as for a linear regression

- adding a variable to constraints will increase R^2
- the larger the number of constraints in the model the larger R^2 is due to random correlations

Can attempt to account for this bias via an adjusted R² measure

$$R_{adj}^2 = 1 - \frac{n-1}{n-m-1} (1 - R^2)$$

- *n* is number of samples *m* is number of constraints (model degrees of freedom)
- Can be used up to $\sim M > n/2$ before becomes too conservative
- · Can be negative
- Compute using RsquareAdj()

Stepwise selection via adjusted R^2

The problems with stepwise selection in regression models are myriad. Affects RDA, CCA, etc as well Blanchet, Legendre, and Borcard (2008) proposed a two-step solution for models where R_{adi}^2 makes sense

- · Global test of all constraints
 - · Proceed only if this test is significant
 - · Helps prevent inflation of overall type I error
- Proceed with forward selection, but with two stopping rules
 - \cdot Usual significance threshold lpha
 - The global R_{adi}^2
 - · Stop if next candidate model is non-significant or if R^2_{adj} exceeds the global R^2_{adj}

Available in ordiR2step()

Permutation tests

Permutation tests in vegan

RDA has lots of theory behind it, CCA not as much. However, ecological/environmental data invariably violate what little theory we have

Instead we use permutation tests to assess the *importance* of fitted models — the data are shuffled in some way and the model refitted to derive a Null distribution under some hypothesis of *no effect*

Permutation tests in vegan

What is shuffled and how is of paramount importance for the test to be valid

- · No conditioning (partial) variables then rows of the species data are permuted
- · With conditioning variables, two options are available, both of which permute residuals from model fits
 - The full model uses residuals from model $Y = X + Z + \varepsilon$
 - The reduced model uses residuals from model $Y = X + Z + \varepsilon$
- In vegan which is used can be set via argument model with "direct", "full", and "reduced" respectively
- In current vegan option method = "full" is disabled

Permutation tests in vegan

A test statistic is required, computed for observed model & each permuted model ${\bf vegan}$ uses a pseudo- ${\it F}$ statistic

$$F = \frac{\chi_{model}^2/df_{model}}{\chi_{resid}^2/df_{resid}}$$

Evaluate whether F is unusually large relative to the null (permutation) distribution of F

Permutation tests in vegan: anova()

- The main user function is the anova() method
- It is an interface to the lower-level function permutest.cca()
- · At its most simplest, the anova() method tests whether the "model" as a whole is significant

$$F = \frac{1.4415/14}{0.6417/9} = 1.4441$$

Permutation tests in vegan: anova()

· anova.cca() has a number of arguments

```
args(anova.cca)
function (object, ..., permutations = how(nperm = 999), by = NULL,
    model = c("reduced", "direct", "full"), parallel = getOption("mc.cores"),
    strata = NULL, cutoff = 1, $cope = NULL).
    NULL * Object is the fitted Ordination
```

- permutations controls what is permuted and how
- by determines what is tested; the default is to test the model

Types of permutation test in vegan

A number of types of test can be envisaged

- Testing the overall significance of the model
- Testing constrained (canonical) axes
- · Testing individual model terms sequentially
- · The marginal effect of a single variable

The first is the default in anova()

The other three can be selected via the argument $\ensuremath{\mathbf{b}}\ensuremath{\mathbf{y}}$

Permutation tests | testing canonical axes

- The constrained (canonical) axes can be individually tests by specifying by = "axis"
- The first axis is tested in terms of variance explained compared to residual variance
- · The second axis is tested after partialling out the first axis... and so on

```
set.seed(1)
anova(mods, by = "axis")
Permutation test for cca under reduced model
Marginal tests for axes
Permutation: free
Number of permutations: 999
Model: cca(formula = varespec ~ Al + P + K, data = varechem)
         Df ChiSquare
                          F Pr(>F)
CCA1
         1 0 36156 5 0249 0 001 +++
CCA2
         1 0.16996 2.3621 0.011 *
CCA3
         1 0.11262 1.5651 0.124
Residual 20 1.43906
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

Permutation tests | testing terms sequentially

- The individual terms in the model can be tested using by = "terms"
- · The terms are assessed in the order they were specified in the model, sequentially from first to last
- Test is of the additional variance explained by adding the kth variable to the model
- · Ordering of the terms will affect the results

Permutation tests | testing terms marginal effects

- The marginal effect of a model term can be assessed using by = "margin"
- The marginal *effect* is the effect of a particular term when all other model terms are included in the

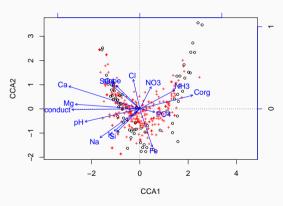
Your turn - Spring meadows

Example & data taken from Leps & Smilauer, Case Study 2

Spring fen meadow vegetation in westernmost Carnathian mountains

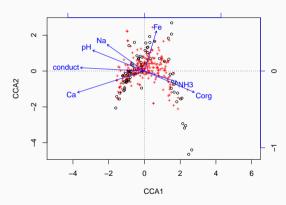
```
## load vegan
library("vegan")
## load the data
spp <- read.csv("../00-data-sets/meadow-spp.csv", header = TRUE, row.names = 1)
env <- read.csv("../00-data-sets/meadow-env.csv", header = TRUE, row.names = 1)</pre>
```

plot(m1)



```
set.seed(67)
lwr <- cca(spp ~ 1, data = env)
m2 <- ordistep(lwr, scope = formula(m1), trace = FALSE)</pre>
m2
Call: cca(formula = spp ~ Ca + conduct + Corg + Na + NH3 + Fe +
pH, data = env)
             Inertia Proportion Rank
Total
              5 3107
                         1.0000
Constrained
               0.9899
                         0.1864
                         0.8136 62
Unconstrained 4.3208
Inertia is mean squared contingency coefficient
Eigenvalues for constrained axes:
 CCA1 CCA2 CCA3 CCA4 CCA5 CCA6 CCA7
0.4268 0.1447 0.1116 0.0936 0.0760 0.0719 0.0652
Eigenvalues for unconstrained axes:
            CAR
                    CV3
                            CA4
                                   CAS
                                           CAG
                                                   CA7
                                                           CAR
0.27251 0.19518 0.16703 0.14993 0.14606 0.14168 0.13292 0.12154
(Showed only 8 of all 62 unconstrained eigenvalues)
```

plot(m2)

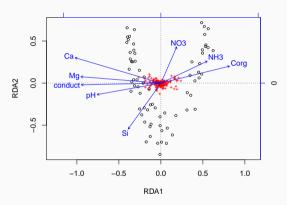


m2\$anova AIC F Pr(>F) + Ca 1 453.14 4.7893 0.005 ** + conduct 1 453.29 1.7915 0.005 ** + Corg 1 453.61 1.6011 0.005 ** 1 453.93 1.5827 0.005 ** + Na + NH3 1 454.36 1.4507 0.020 * 1 454.89 1.3386 0.015 * + Fe 1 455.46 1.2756 0.015 * + pH Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Alternative is RDA with a transformation

```
spph <- decostand(spp, method = "hellinger")
m3 <- rda(spph ~ ., data = env)
lwr <- rda(spph ~ 1, data = env)
m4 <- ordistep(lwr, scope = formula(m3), trace = FALSE)</pre>
```

plot(m4)



```
Stepwise using R_{adi}^2
```

```
m5 <- ordiR2step(lwr. scope = formula(m3), trace = FALSE)
m5$anova
               R2.adi Df
                             AIC
                                       F Pr(>F)
               0.12588 1 -41.779 10.9370 0.002 **
+ Ca
+ NH3
               0.14628 1 -42.468 2.6242 0.002 **
+ conduct
               0.16322 1 -42.925 2.3570 0.002 **
               0.17711 1 -43.164 2.1136 0.002 **
+ Si
               0.18518 1 -42.940 1.6442 0.006 **
+ Corg
               0.19257 1 -42.680 1.5853 0.018 *
+ NO3
+ pH
               0.19966 1 -42.417 1.5583 0.010 **
<All variables> 0.20332
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

Restricted permutation tests

Restricted permutation tests

What is shuffled and how is of paramount importance for the test to be valid

Complete randomisation (default in **vegan**) assumes a null hypothesis where all observations are *independent*

Ecological / environmental data often aren't independent

- · Temporal or spatial correlation
- · Clustering, repeated measures
- Nested sampling designs (Split-plots designs)
- Blocks
- ...

Permutation *must* give null distribution of the test statistic whilst preserving the *dependence* between observations

Trick is to shuffle the data whilst preserving that dependence

Restricted permutations

Canoco has had restricted permutations for a *long* time. **vegan** has only recently caught up & we're not (quite) there yet

vegan used to only know how to completely randomise data or completely randomise within blocks (via strata in vegan)

The newish package **permute** grew out of initial code in the **vegan** repository to generate the sorts of restricted permutations available in Canoco

We have now fully integrated **permute** into **vegan**...

vegan depends on **permute** so it will already be installed & loaded when using **vegan**

Restricted permutations with permute

permute follows Canoco closely — at the chiding of Cajo ter Braak when it didn't do what he wanted! Samples can be thought of as belonging to three levels of a hierarchy

- the sample level; how are individual samples permuted
- the *plot* level; how are samples grouped at an intermediate level
- the *block* level; how are samples grouped at the outermost level

Blocks define groups of plots, each of which can contain groups of samples

Restricted permutations with permute

Blocks are *never* permuted; if defined, only plots or samples *within* the blocks get shuffled & samples are never swapped between blocks

Plots or samples within plots, or both can be permuted following one of four simple permutation types

- 1. Free permutation (randomisation)
- 2. Time series or linear transect, equal spacing
- 3. Spatial grid designs, equal regular spacing
- 4. Permutation of plots (groups of samples)
- 5. Fixed (no permutation)

Multiple plots per block, multiple samples per plot; plots could be arranged in a spatial grid and samples within each of the plots form a time series

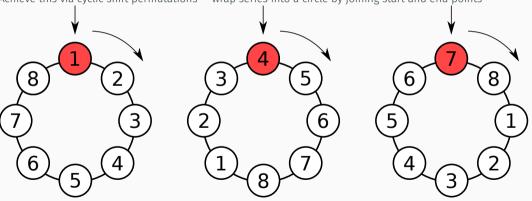
Restricted permutations with permute | blocks

Blocks are a random factor that does not interact with factors that vary within blocks
Blocks form groups of samples that are never permuted between blocks, only within blocks
Using blocks you can achieve what the strata argument used to in vegan; needs to be a factor variable
The variation between blocks should be excluded from the test; permute doesn't do this for you!
Use + Condition(blocks) in the model formula where blocks is a factor containing the block
membership for each observation

Restricted permutations with permute | time series & linear transects

Can link *randomly* starting point of one series to any time point of another series if series are stationary under null hypothesis that the series are unrelated

Achieve this via cyclic shift permutations — wrap series into a circle by joining start and end points



Restricted permutations with permute | time series & linear transects

Works OK if there are no trends or cyclic pattern — autocorrelation structure only broken at the end points *if* series are stationary

Can detrend to make series stationary but not if you want to test significance of a trend shuffle(10, control = how(within = Within(type = "series")))

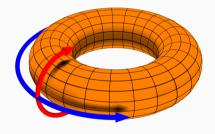
```
[1] 9 10 1 2 3 4 5 6 7 8
```

Restricted permutations with permute | spatial grids

The trick of cyclic shifts can be extended to two dimensions for a regular spatial grid arrangement of points

Now shifts are *toroidal* as we join the end point in the x direction together and in the y direction together matrix(perm, ncol = 3)

```
[,1] [,2] [,3]
[1,] 6 9 3
[2,] 4 7 1
[3,] 5 8 2
```



Source: Dave Burke, Wikimedia 🞯 🕦

Restricted permutations with permute | whole-plots & split-plots I

Split-plot designs are hierarchical with two levels of units

- 1. whole-plots, which contain
- 2. **split-plots** (the samples)

Can permute one or both of these but whole-plots must be of equal size

Essentially allows more than one error stratum to be analyzed

Test effect of constraints that vary *between* whole plots by permuting the whole-plots whilst retaining order of split-splots (samples) within the whole-plots

Test effect of constraints that vary within whole-plots by permuting the split-plots within whole-plots without permuting the whole-plots

Restricted permutations with permute | whole-plots & split-plots II

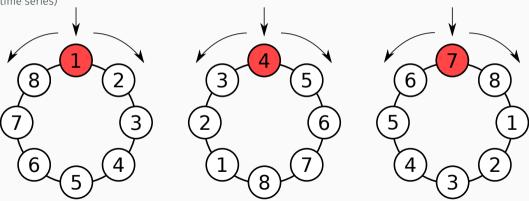
Whole-plots or split-plots can be time series, linear transects or rectangular grids in which case the appropriate restricted permutation is used

If the split-plots are parallel time series & time is an autocorrelated error component affecting all series then the same cyclic shift can be applied to each time series (within each whole-plot) (constant = TRUE)

Restricted permutations with permute | mirroring

Mirroring in restricted permutations allows for isotropy in dependencies by reflecting the ordering of samples in time or spatial dimensions

For a linear transect, technically the autocorrelation at lag h is equal to that at lag -h (also in a trend-free time series)



Restricted permutations with permute | mirroring

Hence the series (1, 2, 3, 4) and (4, 3, 2, 1) are equivalent fom this point of view & we can draw permutations from either version

Similar argument can be made for spatial grids

Using mirror = TRUE then can double (time series, linear transects) or quadruple (spatial grids) the size of the set of permutations

Restricted permutations with permute | the set of permutations

Using restricted permutations can severely reduce the size of the set of allowed permutations. As the minimum p value obtainable is 1/np where np is number of allowed permutations (including the observed) this can impact the ability to detect signal/pattern. If we don't want mirroring

- in a time series of 20 samples the minimum p is 1/20 (0.05)
- in a time series of 100 samples the minimum p is 1/100 (0.01)
- in a data set with 10 time series each of 20 observations (200 total), if we assume an autocorrelated error component over all series (constant = TRUE) then there are only 20 permutations of the data and minimum p is 0.05

When the set of permutations is small it is better to switch to an exact test & evaluate all permutations in the set rather than randomly sample from the set

In **permute**, we set up a permutation scheme with **how()**We sample from the permutation scheme with

- · shuffle(), which gives a single draw from scheme, or
- shuffleSet(), which returns a set of n draws from the scheme

allPerms() can generated the entire set of permutations — note this was designed for small sets of permutations & is slow if you request it for a scheme with many thousands of permutations!

how() has three main arguments

- within takes input from helper Within()
- 2. plots takes input from helper Plots()
- 3. blocks takes a factor variable as input

```
plt <- gl(3, 10)
h <- how(within = Within(type = "series"), plots = Plots(strata = plt))</pre>
```

Helner functions make it easy to change one or a few aspects of permutation scheme rest left at defaults args(Within)

```
function (type = c("free", "series", "grid", "none"), constant = FALSE,
    mirror = FALSE, ncol = NULL, nrow = NULL)

MILI
args(Plots)

function (strata = NULL, type = c("none", "free", "series", "grid"),
    mirror = FALSE, ncol = NULL, nrow = NULL)
NULL
```

how() has additional arguments, many of which control the heuristics that kick in to stop you shooting yourself in the foot and demanding 9999 permutations when there are only 10

- · complete should we enumerate the entire set of permutations?
- minperm lower bound on the size of the set of permutations at & below which we turn on complete enumeration

Restricted permutations with permute | time series example I

Restricted permutations with permute | time series example II

Ohraz Case Study

Restricted permutations with permute | worked example with vegan

Now we've seen how to drive **permute**, we can use the same **how()** commands to set up permutation designs within **vegan** functions

Analyse the Ohraz data Case study 5 of Leps & Smilauer

Repeated observations of composition from an experiment

- · Factorial design (3 replicates)
- · Treatments: fertilisation, mowing, Molinia removal

Test 1 of the hypotheses

There are no directional changes in species composition in time that are common to all treatments or specific treatments

Analyse the Ohraz data Case study 5 of Lens & Smilauer ## load yegan library("yegan") ## load the data spp <- read.csv("../00-data-sets/ohraz-spp.csv", header = TRUE, row.names = 1) env <- read.csv("../00-data-sets/ohraz-env.csv", header = TRUE, row.names = 1) molinia <- spp[, 1] ## Year as numeric env <- transform(env, year = as.numeric(as.character(year)))

```
c1 <- rda(spp ~ year + year:mowing + year:fertilizer + year:removal + Condition(plotid), data = env)</pre>
(h <- how(within = Within(type = "none"), plots = Plots(strata = env$plotid, type = "free")))</pre>
Permutation Design:
Blocks:
 Defined by: none
Plots:
  Plots: env$plotid
  Permutation type: free
  Mirrored?: No
Within Plots:
  Permutation type: none
Permutation details:
 Number of permutations: 199
 Max. number of permutations allowed: 9999
  Evaluate all permutations?: No. Activation limit: 5040
```

```
set.seed(24)
anova(c1, permutations = h, model = "reduced", by = "axis")
Permutation test for rda under reduced model
Marginal tests for axes
Plots: env$plotid, plot permutation: free
Permutation: none
Number of permutations: 199
Model: rda(formula = spp ~ year + year:mowing + year:fertilizer + year:removal + Condition(plotid), data = env)
        Df Variance
                         F Pr(>F)
RDA1
         1 89.12 14.4173 0.005 **
RDA2
         1 34.28 5.5458 0.005 **
             26.52 4.2900 0.010 **
RDA3
RDA4
       1 8.94 1.4458 0.650
Residual 90 556.30
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

Hierarchical analysis of crayfish

Hierarchical analysis of crayfish

Variation in communities may exist at various scales, sometimes hierarchically

A firt step in understanding this variation is to test for its exisistence

In this example from Leps & Smilauer (2014) uses crayfish data from Spring River, Arkansas/Missouri, USA, collected by Dr.~Camille Flinders.

567 records of 5 species (each sub-divided into Large & Small individuals

Hierarchical analysis of crayfish

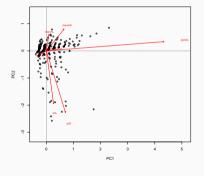
Hierarchical analysis of crayfish — Unconstrained

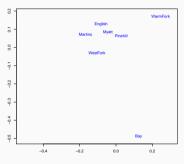
```
Number of samples have 0 cravfish which excludes unimodal methods m.pca <- rda(crayfish) summary(eigenvals(m.pca))
```

```
Importance of components:
                         PC1
                                PC2
                                      PC3
                                              PC4
                                                                      PC7
Eigenvalue
                     3.5728 1.8007 1.1974 0.9012 0.79337 0.38886 0.28132
Proportion Explained 0.3818 0.1924 0.1280 0.0963 0.08478 0.04155 0.03006
Cumulative Proportion 0.3818 0.5742 0.7022 0.7985 0.88325 0.92480 0.95486
                          PC8
                                  PC9
                                         PC10
Eigenvalue
                     0.21225 0.20528 0.004881
Proportion Explained 0.02268 0.02194 0.000520
Cumulative Proportion 0.97754 0.99948 1.000000
```

Hierarchical analysis of crayfish — Unconstrained

```
layout(matrix(1:2, ncol = 2))
biplot(m.pca, type = c("text", "points"), scaling = "species")
set.seed(23)
ev.pca <- envfit(m.pca ~ Watershed, data = design, scaling = "species")
plot(ev.pca, labels = levels(design$Watershed), add = FALSE)
layout(1)</pre>
```





Hierarchical analysis of crayfish — Watershed scale

```
m.ws <- rda(cravfish ~ Watershed, data = design)
m.ws
Call: rda(formula = crayfish ~ Watershed, data = design)
             Inertia Proportion Rank
              9.3580
                        1.0000
Total
Constrained
              1.7669
                        0.1888
Unconstrained 7.5911
                        0.8112 10
Inertia is variance
Eigenvalues for constrained axes:
  RDA1 RDA2
               RDA3 RDA4
                           RDA5
                                   DD46
0.7011 0.5540 0.3660 0.1064 0.0381 0.0013
Eigenvalues for unconstrained axes:
              PC3
                       PC4
                              PC5
                                    PC6
                                           PC7
                                                  PC8
                                                              PC10
3.0957 1.2109 0.9717 0.7219 0.5333 0.3838 0.2772 0.2040 0.1879 0.0048
```

Hierarchical analysis of crayfish — Watershed scale

```
summary(eigenvals(m.ws. constrained = TRUE))
Importance of components:
                              RDA2 RDA3
                                            RDA4
                                                    RDA5
                                                             RDA6
Figenvalue
                     0.7011 0.5540 0.3660 0.1064 0.03814 0.001279
Proportion Explained 0.3968 0.3135 0.2072 0.0602 0.02159 0.000720
set.seed(1)
ctrl <- how(nperm = 499, within = Within(type = "none"),
            plots = with(design, Plots(strata = Stream, type = "free")))
(sig.ws <- anova(m.ws. permutations = ctrl))
Permutation test for rda under reduced model
Plots: Stream, plot permutation: free
Permutation: none
Number of permutations: 499
Model: rda(formula = crayfish ~ Watershed, data = design)
         Df Variance
                          F Pr(>F)
          6 1.7669 21.724 0.002 **
Model
Residual 560 7.5911
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

Hierarchical analysis of crayfish — Stream scale

```
m.str <- rda(crayfish ~ Stream + Condition(Watershed), data = design)
m.str
Call: rda(formula = cravfish ~ Stream + Condition(Watershed), data
= design)
             Inertia Proportion Rank
Total
              9.3580
                        1.0000
              1.7669
                        0.1888
Conditional
Constrained
             1.1478
                       0.1227 10
Unconstrained 6,4433
                        0.6885 10
Inertia is variance
Some constraints were aliased because they were collinear (redundant)
Eigenvalues for constrained axes:
               RDA3 RDA4 RDA5
                                   RDA6
                                          RDA7
0.4928 0.2990 0.2058 0.0782 0.0372 0.0224 0.0063 0.0030 0.0029 0.0002
Eigenvalues for unconstrained axes:
              PC3
                       PC4
                              PC5
                                     PC6
                                           PC7
2.7853 0.8528 0.7737 0.6317 0.5144 0.2808 0.2517 0.1923 0.1559 0.0046
```

Hierarchical analysis of crayfish — Stream scale

```
summarv(eigenvals(m.str. constrained = TRUE))
Importance of components:
                              RDA2 RDA3
                                             RDA4
                                                             RDA6
Eigenvalue
                     0.4928 0.2990 0.2058 0.07824 0.03719 0.02235
Proportion Explained 0.4293 0.2605 0.1793 0.06816 0.03240 0.01947
Cumulative Proportion 0.4293 0.6898 0.8691 0.93731 0.96971 0.98918
                          RDA7
                                  RDA8
                                           RDA9
                                                    RDA10
Eigenvalue
                     0.006326 0.003042 0.002894 0.0001546
Proportion Explained 0.005510 0.002650 0.002520 0.0001300
set.seed(1)
ctrl <- how(nperm = 499, within = Within(type = "none").
            plots = with(design, Plots(strata = Reach, type = "free")).
            blocks = with(design, Watershed))
(sig.str <- anova(m.str, permutations = ctrl))
Permutation test for rda under reduced model
Blocks: with(design, Watershed)
Plots: Reach, plot permutation: free
Permutation: none
Number of permutations: 499
Model: rda(formula = cravfish ~ Stream + Condition(Watershed), data = design)
          Df Variance
                           F Pr(>F)
Labow
          14 1.1478 6.9477 0.004 **
Residual 546 6.4433
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

Hierarchical analysis of crayfish — Reach scale

```
(m.re <- rda(crayfish ~ Reach + Condition(Stream), data = design))
Call: rda(formula = crayfish ~ Reach + Condition(Stream), data =
design)
             Inertia Proportion Rank
Total
              9.3580
                        1.0000
Conditional
              2.9148
                        0.3115 20
                        0.1585 10
Constrained
              1.4829
Unconstrained 4.9603
                        0.5301 10
Inertia is variance
Some constraints were aliased because they were collinear (redundant)
Eigenvalues for constrained axes:
  RDA1 RDA2
               RDA3 RDA4
                           RDA5
                                   RDA6
                                          RDA7
                                                 DDV8
                                                        DDAG DDA10
0.6292 0.2706 0.2146 0.1414 0.1123 0.0467 0.0344 0.0270 0.0064 0.0003
Eigenvalues for unconstrained axes:
         PC2 PC3
                       PC4
                              PC5
                                           PC7
                                    PC6
                                                  PC8
                                                              PC10
2.1635 0.6080 0.5605 0.5166 0.3749 0.2212 0.2052 0.1588 0.1477 0.0040
```

Hierarchical analysis of crayfish — Reach scale

```
set.seed(1)
ctrl <- how(nperm = 499, within = Within(type = "none"),
            plots = with(design, Plots(strata = Run, type = "free")),
            blocks = with(design, Stream))
(sig.re <- anova(m.re, permutations = ctrl))</pre>
Permutation test for rda under reduced model
Blocks: with(design, Stream)
Plots: Run, plot permutation: free
Permutation: none
Number of permutations: 499
Model: rda(formula = crayfish ~ Reach + Condition(Stream), data = design)
          Df Variance
                          F Pr(>F)
Model
         42 1.4829 3.5875 0.002 **
Residual 504 4.9603
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

Hierarchical analysis of crayfish — Run scale

```
(m.run <- rda(cravfish ~ Run + Condition(Reach), data = design))
Call: rda(formula = crayfish ~ Run + Condition(Reach), data =
design)
             Inertia Proportion Rank
Total
              9.3580
                        1.0000
Conditional
              4.3977
                        0.4699 62
Constrained
              1.8225
                        0.1948 10
Unconstrained 3.1378
                        0.3353 10
Inertia is variance
Some constraints were aliased because they were collinear (redundant)
Eigenvalues for constrained axes:
  RDA1 RDA2
               RDA3 RDA4
                           RDA5
                                   RDA6
                                          RDA7
                                                 DDV8
                                                        DDAG DDA10
0.8541 0.3141 0.1679 0.1393 0.1328 0.0835 0.0474 0.0429 0.0390 0.0016
Eigenvalues for unconstrained axes:
         PC2 PC3
                       PC4
                              PC5
                                    PC6
                                           PC7
                                                  PC8
                                                              PC10
1.3137 0.4165 0.3832 0.2759 0.2378 0.1725 0.1215 0.1130 0.1016 0.0021
```

Hierarchical analysis of crayfish — Run scale

Other stuff

Diagnostics for constrained ordinations

 \boldsymbol{vegan} provides a series of diagnostics to help assess the model fit

- · goodness()
- · inertcomp()
- · spenvcor()
- · intersetcor()
- · vif.caa()

Diagnostics for constrained ordinations | goodness of fit

goodness() computes two goodness of fit statistics for species or sites
Which goodness of fit measure is returned is controlled by argument statistic

- statistic = "explained (default) gives the cumulative proportion of variance explained by each axis
- statistic = "distance" gives the residual distance between the "fitted" location in constrained ordination space and the location in the full dimensional space

Diagnostics for constrained ordinations | goodness of fit

0.8254657 0.1953245 0.1824153 0.2406730 0.2110550 0.0060096

```
head(goodness(mods))

CCA1 CCA2 CCA3

Callvulg 0.0062471656 0.318907619 0.8254657

Empenigr 0.1164701677 0.137604904 0.1953245

Rhodtome 0.0999089739 0.169697909 0.1824153

Vaccmyrt 0.2361482843 0.240516323 0.2406730

Vaccviti 0.1523704591 0.15562301 0.2116550

Dimurul 0.00007λλ27 0.00λ0007λ727 0.00λ00006

head(goodness(mods, summarize = TNUE))

Callvulg Empenigr Rhodtome Vaccmyrt Vaccviti Pinusyly
```

Diagnostics for constrained ordinations | inertia decomposition

inertcomp() decomposes the variance in samples or species in partial, constrained, and unconstrained components

Same two types of measure available by argument statistic

- statistic = "explained (default) gives the decomposition in terms of variance
- statistic = "distance" gives decomposition in terms of the the residual distance
- · Can output as proportions of total via proportion = TRUE

```
head(inertcomp(mods, proportional = TRUE))

CCA CA
Callvulg 0.8254657 0.1745343
Empenigr 0.1953245 0.8046755
Rhodtome 0.1824153 0.8175847
Vaccwyrt 0.2406730 0.7593270
Vaccviti 0.2110550 0.7889450
Pinusylv 0.0060006 0.9939904
```

Diagnostics for constrained ordinations | species-environment correlations

spenvcor() returns the species-environment correlation

The (weighted) correlation between the weighted average-based and the linear combination-based sets of site scores

A poor measure of goodness of fit. Sensitive to

- outliers (like all correlations)
- overfitting (using too many constraints)

Retter models can have noorer species-environment correlations spenvcor(mods)

```
CCA1 CCA2 CCA3
0.8554808 0.8132873 0.8792797
```

Diagnostics for constrained ordinations | interset correlations

intersetcor() returns the interset correlations; the (weighted) correlation between the weighted average-based site scores and each constraint variable Another poor diagnostic

- · correlation based
- · focuses on a single constraint-axis combination at a time

 $\label{lem:vector} Vector \ \text{fitting} \ (\textbf{envfit()}) \ \text{or hinlot scores} \ (\textbf{scores} \ (\textbf{model}\ .\ \textbf{display}\ =\ \textbf{"hn"})) \ \text{are hetter alternatives} \ intersetcor(\textbf{mods})$

```
CCA1 CCA2 CCA3
Al 0.7356445 -0.1304293 0.4260453
P -0.3588931 -0.6109601 0.4478786
K -0.3767902 -0.1339051 0.7759566
```

Links

I have several **vegan**-related posts on my blog. For a list of posts see http://www.fromthebottomoftheheap.net/blog/

Re-use

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International License.



References

Blanchet, F Guillaume, Pierre Legendre, and Daniel Borcard. 2008. "Forward Selection of Explanatory Variables." *Ecology* 89 (9). Eco Soc America: 2623–32.