

Estimating rates and magnitudes of temporal change

Using generalized additive models with stratigraphic records

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Funding



**NSERC
CRSNG**

Palaeo data *are* time series

Interest in changes in the data over time — implies the estimation of trends in data

Commonly, trend detection involves eye-balling the data

Fundamentally irreproducible — poor science

Conflates **signal** and **noise**

 Victor Freitas

Spurious correlation

Don't correlate time series

Known for almost a century this is bad

Non-parametric doesn't mean no assumptions — still needs i.i.d. data

Only testing for restricted range of trend shapes

- linear (Pearson correlation)
- monotonic (rank correlation)

Vol. LXXXIX.]

[Part I.

JOURNAL
OF THE ROYAL STATISTICAL SOCIETY.

JANUARY, 1926.

WHY DO WE SOMETIMES GET NONSENSE-CORRELATIONS BETWEEN
TIME-SERIES?—A STUDY IN SAMPLING AND THE NATURE OF
TIME-SERIES.

THE PRESIDENTIAL ADDRESS OF MR. G. UDNY YULE, C.B.E., M.A., F.R.S.,
FOR THE SESSION 1925-26. DELIVERED TO THE ROYAL STATISTICAL
SOCIETY, NOVEMBER 17, 1925.

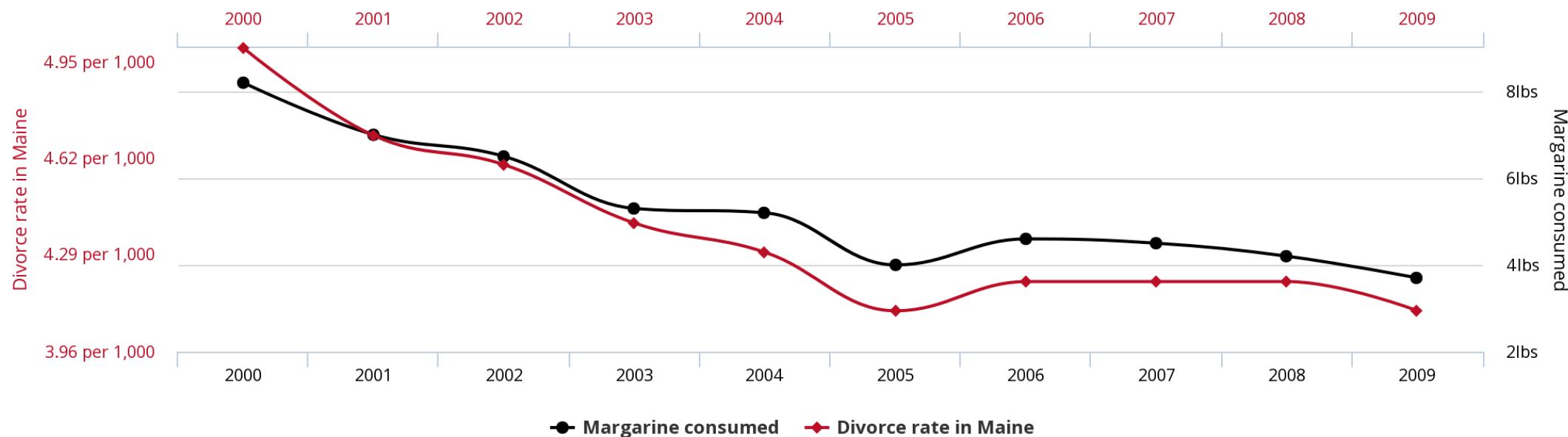
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The problem which I have chosen as the subject of my Address is one that puzzled me for many years. The lines of solution only occurred to me two or three years ago, and I thought that I could not do better than endeavour to work them out during the Session 1924-25—time and opportunity having hitherto been lacking—and utilize them for the present purpose. As often happens, the country

VOL. LXXXIX PART I.

B

Divorce rate in Maine correlates with Per capita consumption of margarine



tylervigen.com

Source: Tyler Viglen <http://www.tylervigen.com/spurious-correlations>

Loess must die

Loess is a simple scatterplot smoother
— fit is controlled by the *span*

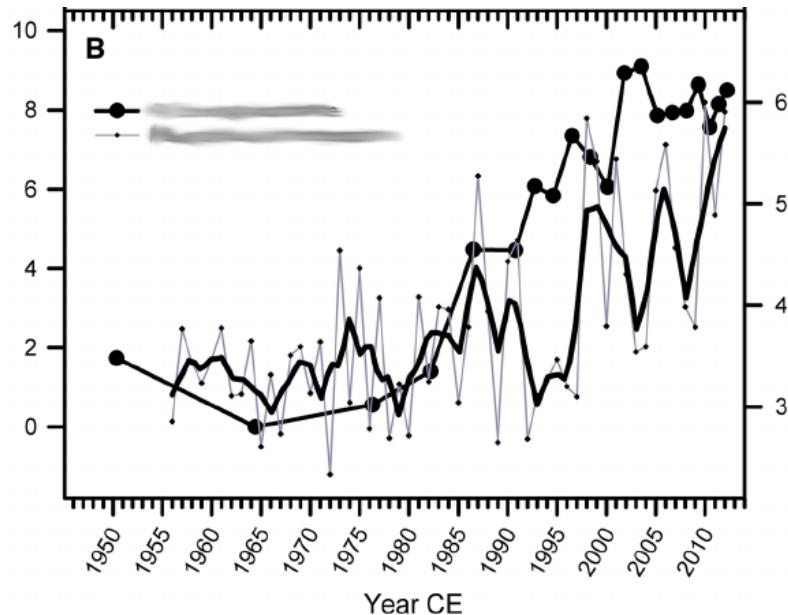
Must choose *span* appropriately

Difficult (impossible?) to do properly...

As a result often chosen subjectively!

Plain wrong — don't do it!

Don't use Loess for inference ...
exploratory data analysis only



Source: [doi: 10/f8gqjj](https://doi.org/10/f8gqjj)

What are we to do...?



© Ross Findon

Model your data

$$\frac{dS}{dt} = q_{\text{fact}} - \gamma_0(N - N_0)(1 - \varepsilon S)S + \frac{\nu e}{T_n} - \frac{\nu}{T_p}$$

$$\frac{dS}{dt} = P_b q_{\text{pe}}(N - N_0)(1 - \varepsilon S)S + \frac{P_f N}{T_n} - \frac{S}{T_p}$$

$$\frac{S}{P_f} = \frac{T_p \times 0}{T_n + \eta n_e}$$

$$TS \leq 1/\varepsilon$$

$$\left. \begin{array}{l} N = 1 \\ P_f = m \end{array} \right\}$$

© Roman Mager

Model your data

Many models available for time series but palaeo data are often unhelpful

1. uneven spacing of observations in time (typically)
2. compaction, variable accumulation rates → non-constant variance

Can't use typical statistical time series models

But we can use generalized additive models



WIGGLY
-THINGS-

GAMs

Linear trend model

$$\mathbb{E}(y_i) = \beta_0 + \beta_1 x_i$$

Generalized Additive Models

$$\mathbb{E}(y_i) = \beta_0 + f(x_i)$$

We assume trend is **smooth**

Splines

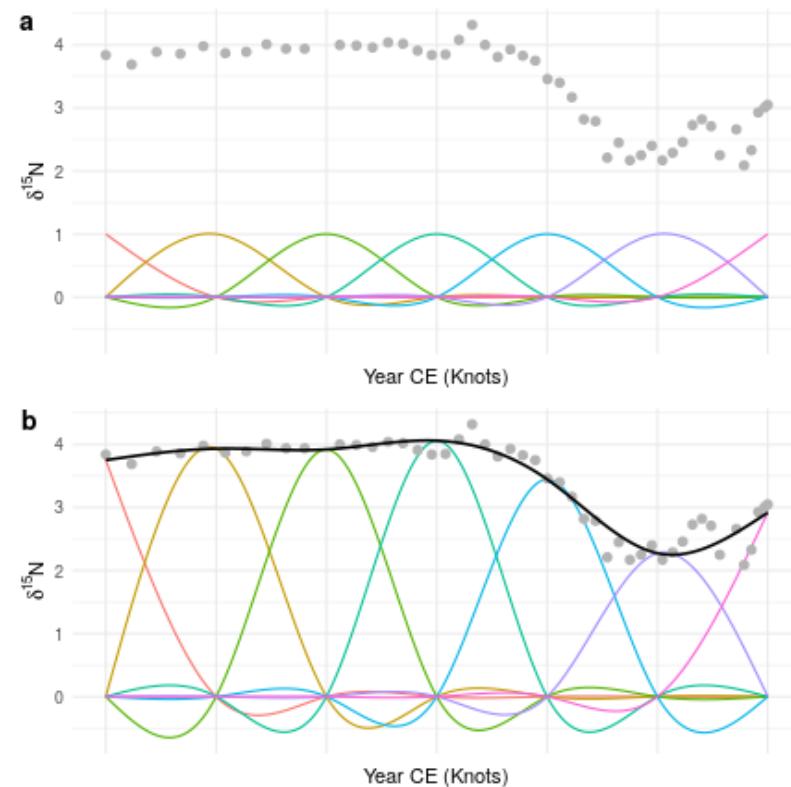
Splines are smooth functions

Made of little basis functions

Estimate β_k for each basis function

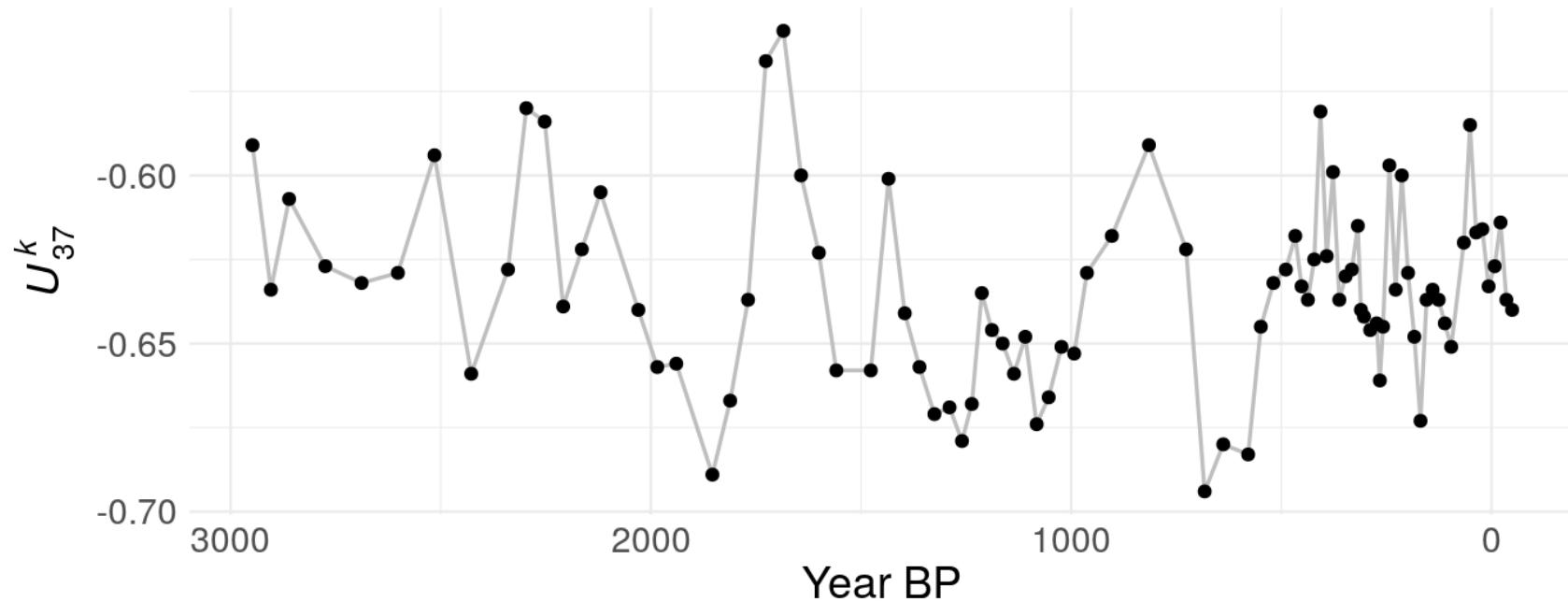
Sum the weighted basis functions at each time point

Use a penalty on **wigginess** to avoid over-fitting



Braya-Sø

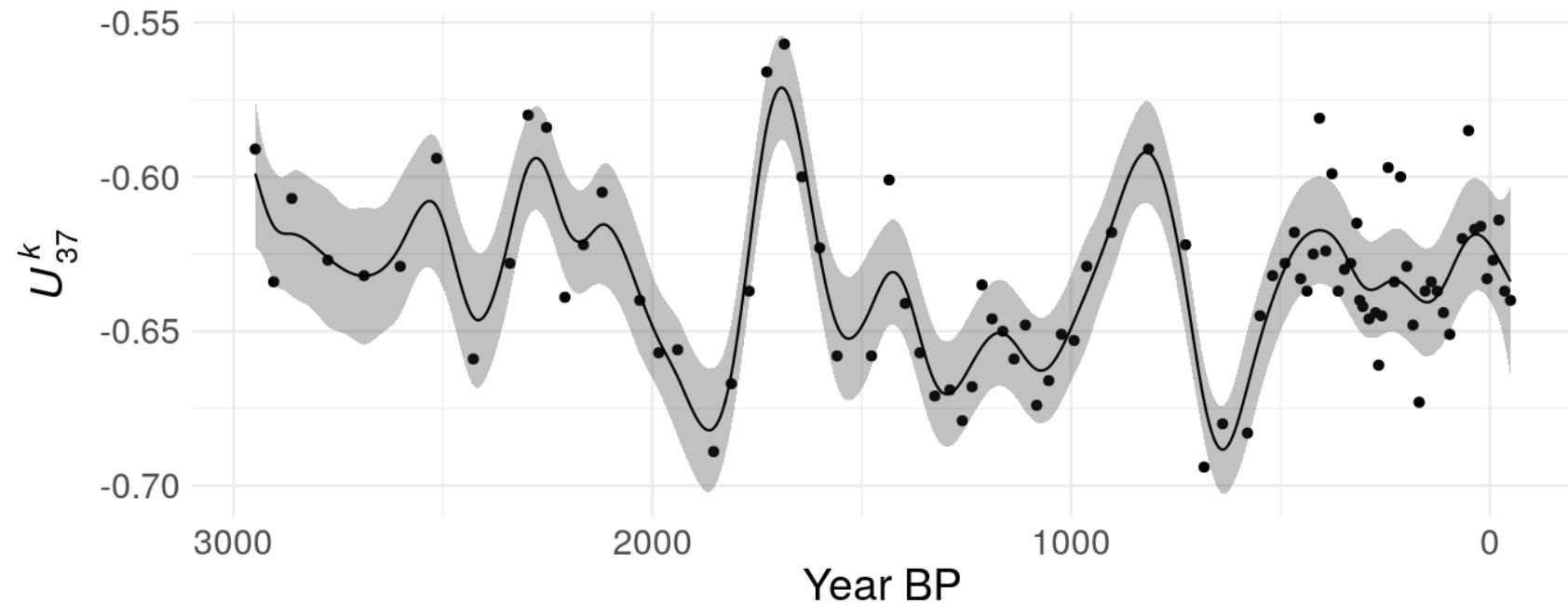
Alkenone unsaturation index — temperature interpretation



D'Andrea, *et al* (2011). PNAS 108: 9765–9769. doi: 10/bnm2n

Braya-Sø — estimated trend

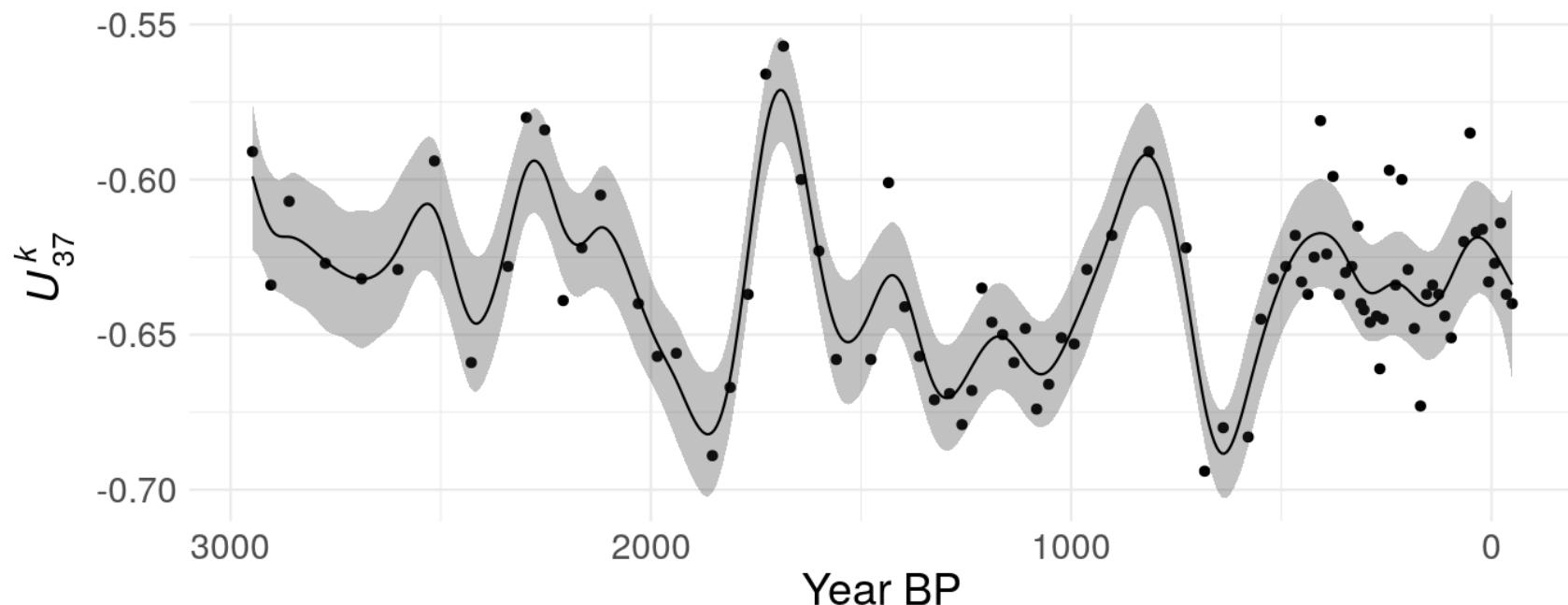
We get some wiggles — but which are real?



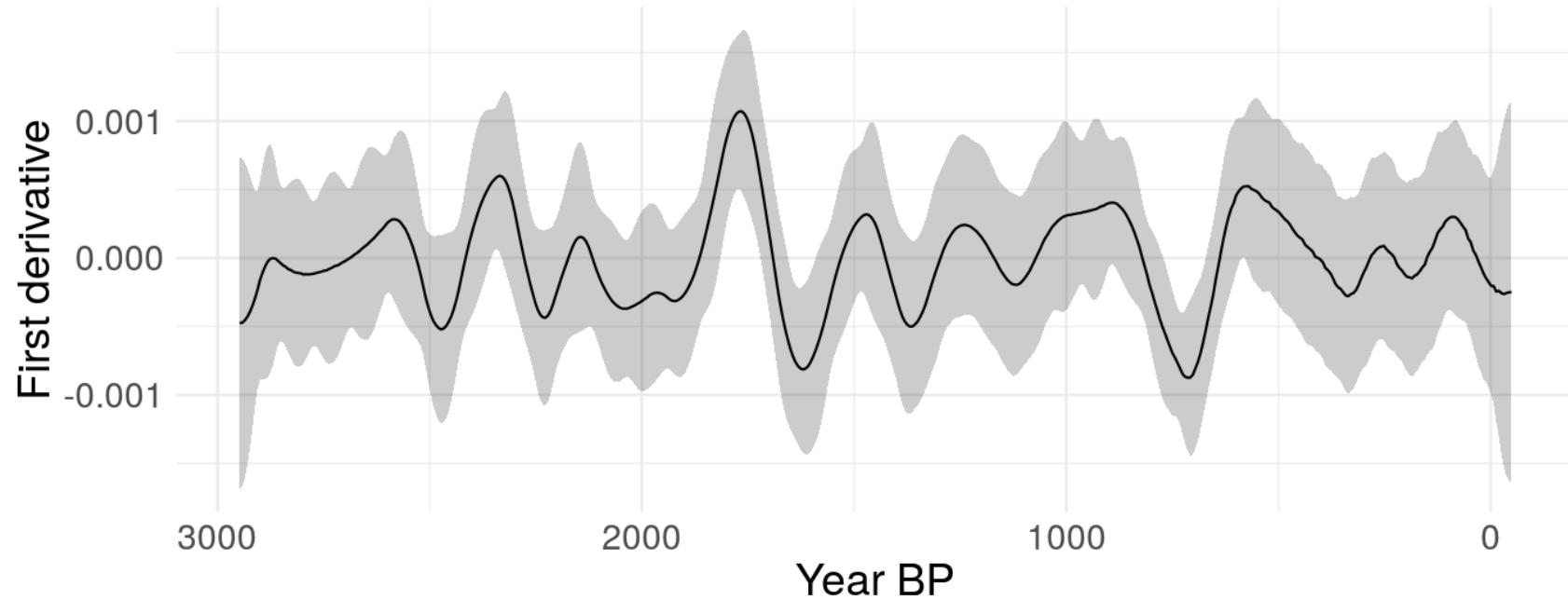
Calculus FTW!

Compute the first derivative of the spline and it's uncertainty

- Where confidence band *includes* **0** we fail to reject the H_0 of *no change*
- Where *doesn't* include **0** we reject $H_0 \rightarrow$ conclude there's change



Braya-Sø rates of change



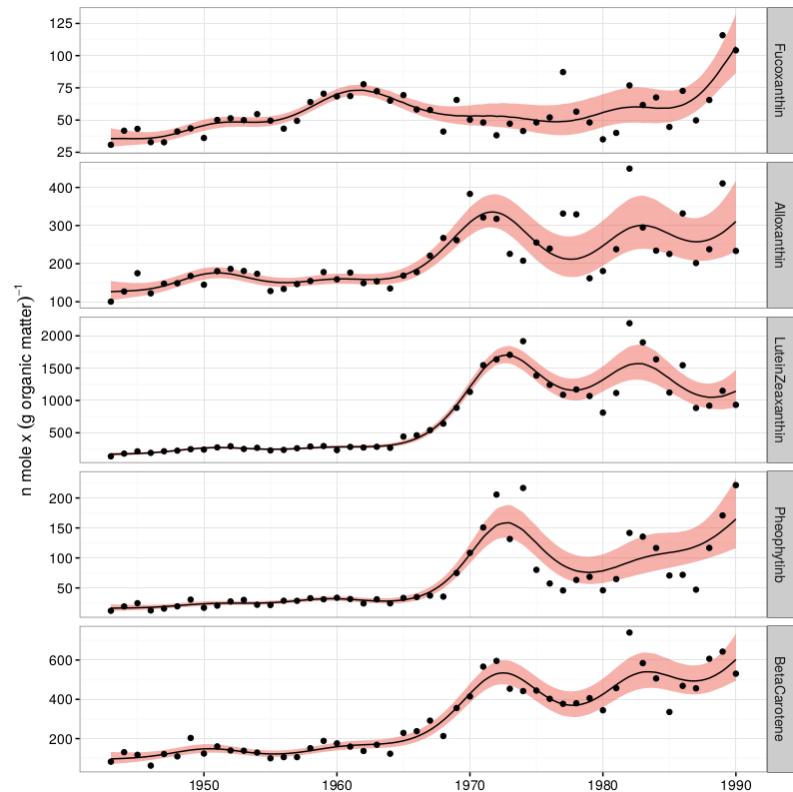
What else...?

Once you start to think in terms of models you can address problems out of reach previously:

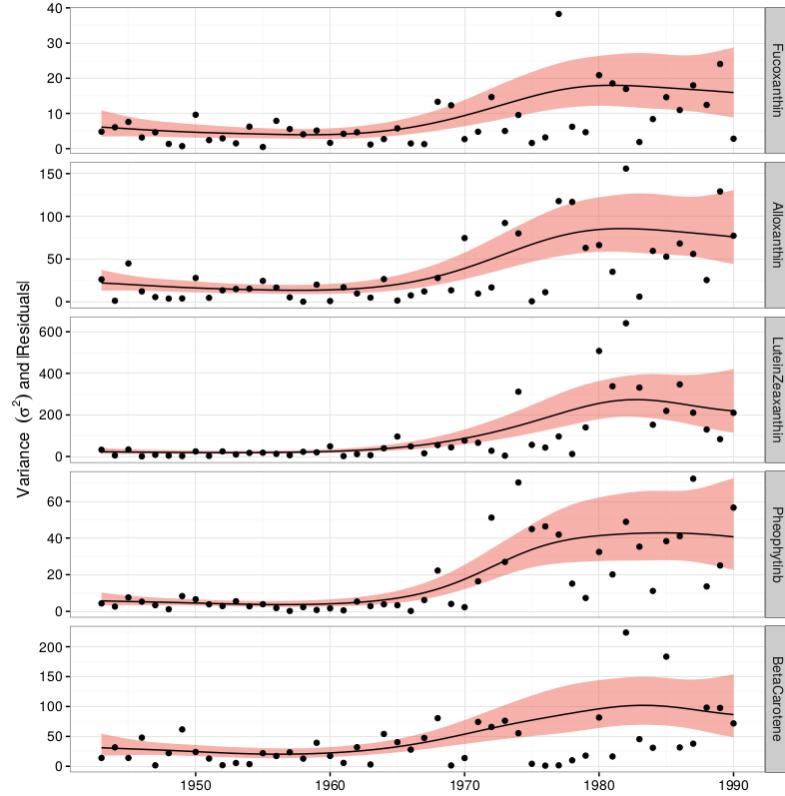
- *models for mean and variance*—resilience & tipping points (?)
- *account for age-model uncertainty*
- *compare trends across multiple sites*
- ...

Lake 227: eutrophication → increased variance

Trend in mean



Trend in variance



Conclusions

Most palaeolimnological data are time series & we're interested in estimating trends in those data

But, we rarely try to estimate those trends statistically

When we do, we often do it inappropriately

We should be modelling our data using statistical models

GAMs are a (relatively) simple model that we could use to model palaeo time series

Want to know more...?

Preprint — doi: [10/cq5k](https://doi.org/10/cq5k)

Blog —
www.fromthebottomoftheheap.net

Slides — bit.ly/ipagams

Modelling palaeoecological time series using
generalized additive models

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⁸ **Keywords**— time series; generalized additive model; simultaneous interval; spline; environmental change

Abstract

In the absence of annual laminations, time series generated from lake sediments or other similar stratigraphic sequences are irregularly spaced in time, which complicates formal analysis using classical statistical time series models. In lieu, statistical analyses of trends in palaeoenvironmental time series, if done at all, have typically used simpler linear regressions or (non-) parametric correlations with little regard for the violation of assumptions that almost surely occurs due to temporal dependencies in the data or that correlations do not provide estimates of the magnitude of change, just whether or not there is a linear or monotonic trend. Alternative approaches have used Loess-estimated trends to justify data interpretations or test hypotheses as to the causal factors without considering the inherent subjectivity of the choice of parameters used to achieve the Loess fit (e.g. span width, degree of polynomial). Generalized additive models (GAMs) are statistical models that can be used to estimate trends as smooth functions of time. Unlike Loess, GAMs use automatic smoothness selection methods to objectively determine the complexity of the fitted trend, and as formal statistical models, GAMs, allow for potentially complex, non-linear trends, a proper accounting of model uncertainty, and the identification of periods of significant temporal change. Here, I present a consistent and modern approach to the estimation of trends in palaeoenvironmental time series using GAMs, illustrating features of the methodology with two example time series of contrasting complexity: a 150-year bulk organic matter $\delta^{15}\text{N}$ time series from Small Water, UK, and a 3000-year alkenone record from Braya-Sø, Greenland. I discuss the underlying mechanics of GAMs that allow them to learn the shape of the trend from the data themselves and how simultaneous confidence intervals and the first derivatives of the trend are used to properly account for