

Homework 2

Exercise 1

Fill in the following table. Use \checkmark when the set is **closed** and \times when the set is not closed:

$(-1, 2]$	$(-1, 1)$	$[-1, 1]$	$\mathbb{R} \setminus \{1\}$	$\{1, 2, 3\}$	$\mathbb{R} \setminus (0, 1)$	\mathbb{Z}	\mathbb{Q}	$\mathbb{R} \setminus \mathbb{Q}$	\mathbb{R}

Prove each statement using the theoretical results from the lectures and seminars.

Exercise 2

Specify the type of the following sets (open or closed). Prove your statements.

$$A = \bigcup_{n \in \mathbb{N}} \left(-1 + \frac{1}{n}, 1 - \frac{1}{n} \right), \quad B = \bigcup_{n \in \mathbb{N}} \left[-1 + \frac{1}{n}, 1 - \frac{1}{n} \right]$$

$$C = \bigcap_{n \in \mathbb{N}} \left(-1 + \frac{1}{n}, 1 - \frac{1}{n} \right) \quad D = \bigcap_{n \in \mathbb{N}} \left[-1 + \frac{1}{n}, 1 - \frac{1}{n} \right]$$

$$E = \bigcup_{n \in \mathbb{N}} \left[-1 - \frac{1}{n}, 1 + \frac{1}{n} \right] \quad D = \bigcap_{n \in \mathbb{N}} \left(-1 - \frac{1}{n}, 1 + \frac{1}{n} \right)$$

Exercise 3

Fill in the following table. Use \checkmark when the set is a **neighborhood** of -1 and \times when it is not:

$(-1, 2]$	$(-2, 1)$	$[-1, 1]$	$\mathbb{R} \setminus \{1\}$	\mathbb{Z}	$\mathbb{R} \setminus (-1, 0)$	\mathbb{Q}

Prove each statement using the theoretical results from the lectures and seminars.