DATA STRUCTURES AND ALGORITHMS LECTURE 1

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Overview

- Course organization
- 2 Abstract Data Types and Data Structures
- Pseudocode
- 4 Algorithm Analysis

Course Organization I

- Guiding teachers
 - Lecturer PhD. Oneţ-Marian Zsuzsanna
 - Lecturer PhD. Mircea Ioan Gabriel
- Activities
 - Lecture: 2 hours / week
 - **Seminar:** 1 hour / week
 - Course page: www.cs.ubbcluj.ro/~marianzsu/DSA_MI.html
 - Email: marianzsu@cs.ubbcluj.ro
 - Please use your scs.ubbcluj email address for communication (and make sure the email contains your name!).

Course Organization II

- Grading
 - Written exam (W) will be in the last week of the semester
 - Project (P) will be presented in the last week of the semester
 - Seminar grade (S)
 - Partial paper (P) in the 5th seminar
 - Project stage (ST)
 - Seminar grade S = 0.7 * P + 0.3 * ST
 - The final grade is computed as:

$$G = 0.6 * W + 0.2 * P + 0.2 * S$$

To pass the exam W, P and G has to be ≥ 5 (no rounding)!



Rules I

 Attendance is compulsory for the seminar activity. You need at least 5 attendances from the 7 seminars.

- Unless you have the required number of attendances, you cannot participate in the written exam, neither in the regular nor in the retake session!
- The course page contains the link to the Google Sheets document where you can check your attendance situation (codes will be provided to you during the first lecture or seminar).

Rules II

- You have to come to the seminar with your group (we will consider the official student lists for the groups from the faculty's web page).
- If you want to permanently switch from one group to another, you have to find a person in the other group who is willing to switch with you and announce your seminar teacher about the switch in the first two weeks of the semester.
- Seminar attendance can be recovered with another group, within the two weeks allocated for the seminar, with the explicit agreement of the seminar teacher.

Rules III

- There is a project that you will have to realize by the end of the semester. Project topics will be allocated in the 5th seminar, when more information about the requirements of the project and its grading will be given as well.
- The grade for the project has to be ≥ 5 in order to be able to pass the exam (no matter what the value of G is).
- Projects with a grade < 5 have to be redone in the retake session. For these projects the maximum possible grade is 5.

Rules IV

- You will have a partial exam in the 5th seminar. More details about this exam will be given in the 4th seminar (and in Lecture 8).
- In the retake session only the written exam can be repeated, and grade G will be computed in the same way as in the regular session.
- The partial exam and the seminar activity cannot be redone in the retake session. The project cannot be redone in the retake session (unless the grade for the project is < 5, but in this case it has to be redone).

Course Objectives

- The study of the concept of abstract data types and the most frequently used container abstract data types.
- The study of different data structures that can be used to implement these abstract data types and the complexity of their operations.
- What you should learn from this course:
 - to design and implement different applications starting from the use of abstract data types.
 - to process data stored in different data structures.
 - to choose the abstract data type and data structure best suited for a given application.



Bibliography I

- T. CORMEN, C. LEISERSON, R. RIVEST, C. STEIN, Introduction to algorithms, Third Edition, The MIT Press, 2009
- S. SKIENA, The algorithm design manual, Second Edition, Springer, 2008
- N. KARUMANCHI, Data structures and algorithms made easy, CareerMonk Publications, 2016
- M. A WEISS, Data structures and algorithm analysis in Java, Third Edition, Pearson, 2012

Bibliography II

- R. SEDGEWICK, Algorithms, Fourth Editions, Addison-Wesley Publishing Company, 2011
- R. LAFORE, Data Structures & Algorithms in Java, Second Edition, Sams Publishing, 2003
- M. A. WEISS Data structures and problem solving using C++, Second Edition, Pearson, 2003

Abstract Data Types I

- A data type is a set of values and a set of operations on those values. For example:
 - int
 - set of values are integer numbers from a given interval
 - possible operations: add, subtract, multiply, etc.
 - boolean
 - set of values: true, false
 - possible operations: negation, and, or, xor, etc.
 - String
 - "abc", "text", etc.
 - possible operations: get the length, get a character from a position, get a substring, etc.
 - etc.



Abstract Data Types II

- An Abstract Data Type (ADT) is a data type having the following two properties:
 - the objects from the domain of the ADT are specified independently of their representation
 - the operations of the ADT are specified independently of their implementation

Abstract Data Types - Domain

- The domain of an ADT describes what elements belong to this ADT.
- If the domain is finite, we can simply enumerate them.
- If the domain is not finite, we will use a rule that describes the elements belonging to the ADT.

Abstract Data Types - Interface

- After specifying the domain of an ADT, we need to specify its operations.
- The set of all operations for an ADT is called its interface.
- The interface of an ADT contains the signature of the operations, together with their input data, results, preconditions and postconditions (but no detail regarding the implementation of the method).
- When talking about ADT we focus on the WHAT (it is, it does), not on the HOW.



ADT - Example I

- Consider the Date ADT (made of three numbers: year, month and day)
 - Elements belonging to this ADT are all the valid dates (year is positive, maybe less than 3000, month is between 1 and 12, day is between 1 and maximum number of possible days for the month)
 - One possible operation for the Data ADT could be: difference(Date d1, Date d2)
 - Descr: computed the difference in number of days between two dates
 - Pre: d1 and d2 have to be valid Dates, d1 < d2
 - Post: difference ← d, d is a natural number and represents the number of days between d1 and d2.
 - Throws: and exception if d1 is greater than d2



ADT - Example II

 This information specifies everything we need to use the Date ADT, even if we know nothing about how it is represented or how the operation difference is implemented.

Container ADT I

- A container is a collection of data, in which we can add new elements and from which we can remove elements.
- Different containers are defined based on different properties:
 - do the elements need to be unique?
 - do the elements have positions assigned?
 - can any element be accessed or just some specific ones?
 - do we store simple elements or key value pairs?

Container ADT II

- A container should provide at least the following operations (the interface of the container should contain operations for):
 - creating an empty container
 - adding a new element to the container
 - removing an element from the container
 - returning the *number of elements* in the container
 - provide access to the elements from the container (usually using an iterator)

Container vs. Collection

- Python Collections
- C++ Containers from STL
- Java Collections framework and the Apache Collections library
- Net System.Collections framework
- In the following, in this course we will use the term **container**.

Why abstract data types?

- There are several different Container Abstract Data Types, so choosing the most suitable one is an important step during application design.
- When choosing the suitable ADT we are not interested in the implementation details of the ADT (yet).
- Most high-level programming languages usually provide implementations for different Abstract Data Types.
 - In order to be able to use the right ADT for a specific problem, we need to know their domain and interface.

- Why do we need to implement our own Abstract Data Types if they are already implemented in most programming languages?
 - Implementing these ADT will help us understand better how they work (we cannot use them, if we do not know what they are doing)
 - To learn to create, implement and use ADT for situations when:
 - we work in a programming language where they are not readily implemented.
 - we need an ADT which is not part of the standard ones, but might be similar to them.

Advantages of working with ADTs I

- Abstraction is defined as the separation between the specification of an object (its domain and interface) and its implementation.
- Encapsulation abstraction provides a promise that any implementation of an ADT will belong to its domain and will respect its interface. And this is all that is needed to use an ADT.

Advantages of working with ADTs II

- Localization of change any code that uses an ADT is still
 valid if the ADT changes (because no matter how it changes,
 it still has to respect the domain and interface).
- Flexibility an ADT can be implemented in different ways, but all these implementation have the same interface.
 Switching from one implementation to another can be done with minimal changes in the code.

Advantages of working with ADTs III

- Consider again our example with the Date ADT:
 - Assume you used variables of type Date and the difference operation in your code.
 - If the implementation of the Date changes, these changes will not affect your code, because even if the representation changes and even if the implementation of the operations changes, they still have to respect the interface (the signature and behaviour of the difference operation is still the same).
 - If a new implementation for the Date will appear and you want to switch to that implementation, it can be done with minimal modifications in your code

Data Structures I

- The domain of data structures studies how we can store and access data.
- A data structure can be:
 - Static: the size of the data structure is fixed. Such data structures are suitable if it is known that a fixed number of elements need to be stored.
 - Dynamic: the size of the data structure can grow or shrink as needed by the number of elements.

Data Structures II

 For every container ADT we will discuss several possible data structures that can be used for the implementation. For every possibility we will discuss the advantages and disadvantages of using the given data structure. We will see that, in general, we cannot say that there is one single best data structure for a given container.

Pseudocode I

- The aim of this course if to give a general description of data structures, one that does not depend on any programming language - so we will use the *pseudocode* language to describe the algorithms.
- Our algorithms written in pseudocode will consist of two type of instructions:
 - standard instructions (assignment, conditional, repetitive, etc.)
 - non-standard instructions (written in plain English to describe parts of the algorithm that are not developed yet). These non-standard instructions will start with @.

Pseudocode II

- One line comments in the code will be denoted by //
- For reading data we will use the standard instruction read
- For printing data we will us the standard instruction print
- For assignment we will use ←
- For testing the equality of two variables we will use =

Pseudocode III

 Conditional instruction will be written in the following way (the *else* part can be missing):

```
if condition then
    @instructions
else
    @instructions
end-if
```

Pseudocode IV

• The for loop (loop with a known number of steps) will be written in the following way:

```
for i \leftarrow init, final, step execute
   @instructions
```

end-for

- init represents the initial value for variable i
- final represents the final value for variable i
- step is the value added to i at the end of each iteration. step can be missing, in this case it is considered to be 1.

Pseudocode V

• The while loop (loop with an unknown number of steps) will be written in the following way:

while condition execute
@instructions
end-while

Pseudocode VI

 Subalgorithms (subprograms that do not return a value) will be written in the following way:

subalgorithm name(formal parameter list) is:
 @instructions - subalgorithm body
end-subalgorithm

The subalgorithm can be called as:

name (actual parameter list)

Pseudocode VII

 Functions (subprograms that return a value) will be written in the following way:

```
function name (formal parameter list) is:
    @instructions - function body
    name ← v //syntax used to return the value v
end-function
```

• The function can be called as:

```
result ← name (actual parameter list)
```

Pseudocode VIII

- If we want to define a variable i of type Integer, we will write:
 i: Integer
- If we want to define an array a, having elements of type T, we will write: a: T[]
 - If we know the size of the array, we will use: a: T[Nr] indexing is done from 1 to Nr
 - If we do not know the size of the array, we will use: a: T[] indexing is done from 1

Pseudocode IX

A struct (record) will be defined as:

Array:

```
n: Integer elems: T[]
```

- The above struct consists of 2 fields: n of type Integer and an array of elements of type T called elems
- Having a variable var of type Array, we can access the fields using . (dot):
 - var.n
 - var.elems
 - var.elems[i] the i-th element from the array



Pseudocode X

- For denoting pointers (variables whose value is a memory address) we will use ↑:
 - p:
 † Integer p is a variable whose value is the address of a
 memory location where an Integer value is stored.
 - The value from the address denoted by p is accessed using [p]
- Allocation and de-allocation operations will be denoted by:
 - allocate(p)
 - free(p)
- We will use the special value NIL to denote an invalid address

Specifications I

- An operation will be specified in the following way:
 - pre: the preconditions of the operation
 - post: the postconditions of the operation
 - **throws:** exceptions thrown (optional not every operation can throw an exception)
- When using the name of a parameter in the specification we actually mean its value.
- Having a parameter i of type T, we will denote by $i \in T$ the condition that the value of variable i belongs to the domain of type T.

Specifications II

- The value of a parameter can be changed during the execution of a function/subalgorithm. To denote the difference between the value before and after execution, we will use the ' (apostrophe).
- For example, the specification of an operation decrement, that decrements the value of a parameter x (x : Integer) will be:
 - **pre:** $x \in Integer$
 - post: x' = x 1

Generic Data Types I

- We will consider that the elements of a container ADT are of a generic type: TElem
- The interface of the *TElem* contains the following operations:
 - assignment $(e_1 \leftarrow e_2)$
 - pre: $e_1, e_2 \in TElem$
 - post: $e_1' = e_2$
 - equality test $(e_1 = e_2)$
 - pre: $e_1, e_2 \in TElem$
 - post:

$$equal = \begin{cases} True, & \text{if } e_1 \text{ } equals \text{ } e_2 \\ False, & \text{otherwise} \end{cases}$$



Generic Data Types II

- When the values of a data type can be compared or ordered based on a relation, we will use the generic type: TComp.
- Besides the operations from TElem, TComp has an extra operation that compares two elements:
 - compare(e_1 , e_2)
 - pre: $e_1, e_2 \in TComp$
 - post:

$$compare = \begin{cases} true & \text{if } e_1 <= e_2 \\ false & \text{if } e_1 > e_2 \end{cases}$$

• For simplicity, sometimes instead of calling the *compare* function, we will use the notations $e_1 \le e_2$, $e_1 = e_2$, $e_1 \ge e_2$

The RAM model I

- Analyzing an algorithm usually means predicting the resources (time, memory) the algorithm requires. In order to do so, we need a hypothetical computer model, called RAM (random-access machine) model.
- In the RAM model:
 - Each simple operation (+, -, *, /, =, if, function call) takes one time step/unit.
 - We have fixed-size integers and floating point data types.
 - Loops and subprograms are *not* simple operations and we do not have special operations (ex. sorting in one instruction).
 - Every memory access takes one time step and we have an infinite amount of memory.



The RAM model II

- The RAM is a very simplified model of how computers work, but in practice it is a good model to understand how an algorithm will perform on a real computer.
- Under the RAM model we measure the run time of an algorithm by counting the number of steps the algorithm takes on a given input instance. The number of steps is usually a function that depends on the size of the input data.

```
subalgorithm something(n) is:
//n is an Integer number
   rez \leftarrow 0
   for i \leftarrow 1, n execute
     sum \leftarrow 0
      for i \leftarrow 1, n execute
         sum \leftarrow sum + j
      end-for
      rez \leftarrow rez + sum
   end-for
   print rez
end-subalgorithm
```

• How many steps does the above subalgorithm take?

```
subalgorithm something(n) is:
//n is an Integer number
   rez \leftarrow 0
  for i \leftarrow 1, n execute
     sum \leftarrow 0
     for i \leftarrow 1, n execute
        sum \leftarrow sum + j
     end-for
     rez \leftarrow rez + sum
  end-for
  print rez
end-subalgorithm
```

• How many steps does the above subalgorithm take?

•
$$T(n) = 1 + n * (1 + n + 1) + 1 = n^2 + 2n + 2$$

Order of growth

- We are not interested in the exact number of steps for a given algorithm, we are interested in its order of growth (i.e., how does the number of steps change if the value of n increases)
- We will consider only the leading term of the formula (for example n^2), because the other terms are relatively insignificant for large values of n.

O-notation I

O-notation

For a given function g(n) we denote by O(g(n)) the set of functions:

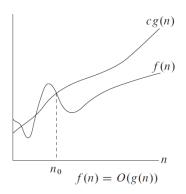
$$O(g(n)) = \{f(n) : \text{there exist positive constants } c \text{ and } n_0 \text{ s. t.}$$

 $0 \le f(n) \le c \cdot g(n) \text{ for all } n \ge n_0\}$

- The O-notation provides an asymptotic upper bound for a function: for all values of n (to the right of n_0) the value of the function f(n) is on or below $c \cdot g(n)$.
- We will use the notation f(n) = O(g(n)) or $f(n) \in O(g(n))$.

O-notation II

• Graphical representation:



O-notation III

Figure taken from Corman et. al: Introduction to algorithms, MIT Press, 2009

Alternative definition

$$f(n) \in O(g(n))$$
 if $\lim_{n \to \infty} \frac{f(n)}{g(n)}$

is either 0 or a constant (but not ∞).

- Consider, for example, $T(n) = n^2 + 2n + 2$:
 - $T(n) = O(n^2)$ because $T(n) \le c * n^2$ for c = 2 and $n \ge 3$
 - $T(n) = O(n^3)$ because

$$\lim_{n\to\infty}\frac{T(n)}{n^3}=0$$

