

Sri Lanka Institute of Information Technology

Year 02 – Semester II – 2022

Probability and Statistics – IT2110

Tutorial 05

1) An officer is always late to the office and arrives within the grace period of ten minutes after the start. Let *X* be the time that elapses between the start and the time the officer signs in with a probability density function

$$\mathbf{f}(\mathbf{x}) = \begin{cases} k\mathbf{x}^2 & 0 \le \mathbf{x} \le 10 \\ 0 & \text{otherwise} \end{cases}$$

where k > 0 is a constant.

- a) Compute the value of k.
- b) Find the cumulative distribution function of X.
- c) Find the probability that the he arrives less than 3 minutes after the start of the office.
- d) Calculate the mean and variance of X.
- 2) The time taken to assemble a car in a certain plant is a random variable having a normal distribution of 20 hours and a standard deviation of 2 hours. What is the probability that a car can be assembled at this plant in a period of time,
 - a) Less than 19.5 hours?
 - b) Between 20 and 22 hours?
- 3) A large group of students took a test in Physics and the final grades have a mean of 70 and a standard deviation of 10. If we can approximate the distribution of these grades by a normal distribution, what percent of the students,
 - a) Scored higher than 80?
 - b) Should pass the test (grades≥60)?
 - c) Should fail the test (grades<60)?

- 4) A radar unit is used to measure speeds of cars on a motorway. The speeds are normally distributed with a mean of 90 *km/hr* and a standard deviation of 10 *km/hr*. What is the probability that a car picked at random is travelling at more than 100 *km/hr*?
- 5) Suppose we know that the birth weights of babies are normally distributed with mean 3500g and standard deviation 500g. What is the probability that a baby is born that weighs less than 3100g?
- 6) Suppose that we are told that the heights of adult males in a particular region of the world are normally distributed with a mean of 70 inches and standard deviation of 2 inches.
 - a) Approximately what proportion of adult males are taller than 73 inches?
 - b) What proportion of adult males are between 72 and 73 inches?
 - c) What height corresponds to the point where 20% of all adult males are greater than this height?
 - d) What height corresponds to the point where 20% of all adult males are less than this height?
- 7) Assume the speed of vehicles along a stretch of a highway has an approximately normal distribution with a mean of 71 mph and a standard deviation of 8 mph.
 - a) The current speed limit is 65 mph. What is the proportion of vehicles less than or equal to this speed limit?
 - b) What proportion of the vehicles would be going less than 50 mph?
 - c) A new speed limit will be initiated such that approximately 10% of vehicles will be over the speed limit. What is the new speed limit based on this criterion?
- 8) The bottom 30% of students failed an end semester examination. The mean for the test was 120 and the standard deviation was 17. What was the passing score?
- 9) Suppose that customers arrive at Banks ATM at the rate 20 per hour. If customer has just arrived, what is the probability that the next customer arrives within 6 minutes?
- 10) The time required to repair a machine is an exponential random variable with rate λ = 0.5 downs/hour. What is the probability that a repair time exceeds 2 hours?