The Chloroplast Electron Transport Chain

Peter Gawthrop (peter.gawthrop@unimelb.edu au)

November 6, 2019

Contents

1	Introduction	2
2	Photon Energetics	3
3	Redox reactions 3.1 Redox potentials	4 5
4	Bond graph description 4.1 Complex PII Photosystem II	7 9
5	The Electron Transport Chain 5.1 Unify species in model using mbg.unify()	12 13

Note: this is the Chloroplast.ipynb notebook. The PDF version "The Chloroplast Electron Transport Chain" is available here.

This is a work in progress and needs more explanatory notes.

```
In [1]: ## Some useful imports
        import BondGraphTools as bgt
        import numpy as np
        import sympy as sp
        import matplotlib.pyplot as plt
        ## Stoichiometric analysis
        import stoich as st
        ## SVG bg representation conversion
        import svgBondGraph as sbg
        ## Modular bond graphs
        import modularBondGraph as mbg
        ## Display (eg disp.SVG(), disp.
        import IPython.display as disp
        ## Data
        import phiData
        import redoxData
```

1 Introduction

Photosynthesis within plant chloroplasts is the basis of life on earth (Blankenship, 2015), (Nicholls and Ferguson, 2013).

Like the mitochondrion, the chloroplast has a membrane seperating an inner space (lumen) from an outer space (stroma). In the chloroplast, the lumen gains protons and is called the p-space, the stroma looses protons and is called the n-space. Thus geometrically, the lumen corresponds to the mitochondrial matrix and the stroma to the mitochondrial intermembrane space; but electrically the p-space is inside and the n-space outside - the reverse of the mitochondrial situation.

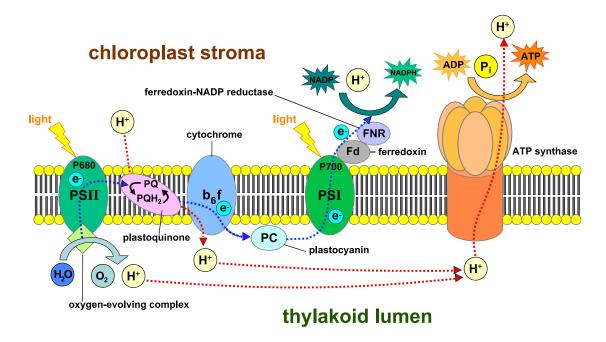
The chloroplast electron transport chain has 4 complexes.

- 1. Photosystem II (PII) which absorbs photons at 680nm and splits water releasing protons into the p-space and passing electrons to the plastoquinone(PQ)/plastoquine(PQH2) couple which absorbs protons from the n-space.
- 2. Cytochrome bf (Cyt) which passes electrons to the plastoquine/plastoquinone couple which releases two protons into the p-space. Electrons are passed to the plastocyanine couple (PcOx/PcRed). Two protons are pumped across the membrane.
- 3. Photosystem I (PI) which absorbs photons at 700nm and transports electrons from the plastocyanine (PcRed/PcOx) couple to the ferredoxin (FdOx/FdRed) couple.

4. Feredoxin-NADP reductase which transfers electrons from the ferredoxin (FdRed/FdOx) couple to convert NADP to NADPH absorbing a proton from the n-space.

The following figure is: https://commons.wikimedia.org/wiki/File:Thylakoid_membrane_3.svg

Out[2]:



2 Photon Energetics

$$\phi_{photon} = \frac{N_{av}hc}{F\lambda} \tag{1}$$

where
$$N_{av} = \text{Avogadro's number}$$
 (2)

$$h = \text{Planck's constant}$$
 (3)

$$c = \text{velocity of light}$$
 (4)

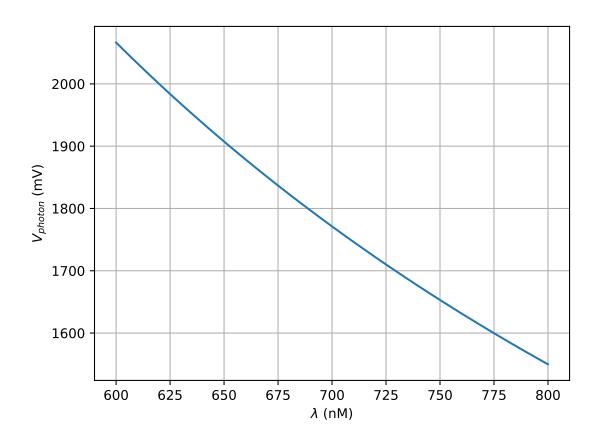
$$F = Faraday's constant$$
 (5)

and
$$\lambda$$
 = wavelength (6)

For example:

$$\phi_{photon} = \begin{cases} 1.82V & \lambda = 680nm \\ 1.77V & \lambda = 700nm \end{cases}$$
 (7)

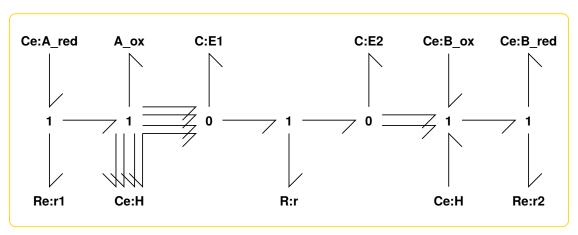
In [3]: disp.SVG('V_photon.svg')
Out[3]:



3 Redox reactions

In [4]: disp.SVG('Redox_abg.svg')

Out[4]:



Redox reactions can be written as two half-reactions:

$$A_{\text{red}} \stackrel{r_1}{\iff} n_1 e_1^- + m_1 H_1^+ + A_{\text{ox}}$$
 (8)

$$B_{ox} + n_2 e_2^- + m_2 H_2^+ \stackrel{r_2}{\Longleftrightarrow} B_{red}$$
 (9)

3.1 Redox potentials

Note that photon energies have been used for V_700 and V_680; this value is too large as the energy conversion is not direct. A model of this needs to be built. See, for example: (Blankenship and Prince, 1985)

```
In [5]: import redoxData
        ## pH from BerTymStr 19.3
        pH_p = 4 \# pH \ of \ p-space
        pH_n = pH_p + 3
        VpH = redoxData.VpH(pH_p - pH_n)
        V680 = redoxData.V_photon(wavelength=680)
        V700 = redoxData.V_photon(wavelength=700)
        print(VpH)
        print('V_pH =',int(1000*VpH),'mV')
        print('V_680 =',int(1000*V680),'mV')
        print('V_700 =',int(1000*V700),'mV')
0.18462115653058278
V_pH = 184 mV
V_{680} = 1823 \text{ mV}
V_700 = 1771 \text{ mV}
In [6]: ## Convert redox potentials to species phi
        phi_redox = redoxData.phi()
        phi_redox['Hn'] = redoxData.VpH(pH_n)
        phi_redox['Hp'] = redoxData.VpH(pH_p)
        ## The correct photon potentials need sorting out
        ## The raw valyes used here are an overestimate. See BlaPri85
        phi_redox['P680'] = V680
        phi_redox['P700'] = V700
        #phi_redox['P680'] = phi_redox['P680+']
        #phi_redox['P700'] = phi_redox['P700+']
        ## The membrane potential is said by some to be zero. (check this)
        phi_redox['dV'] = VpH
```

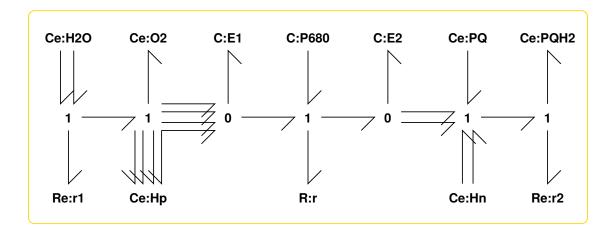
4 Bond graph description

The four complexes are represented by svg graphics which are automatically converted into Bond-GraphTools format.

The stoichiometric toolbox is then used to generate the pathway-reduced equation for the complex.

4.1 Complex PII -- Photosystem II

In [7]: disp.SVG('PII_abg.svg')
Out[7]:



```
In [8]: sbg.model('PII_abg.svg',convertR=True,convertCe=True,quiet=True)
    import PII_abg

In [9]: ## Stoichiometry
    sPII = st.stoich(PII_abg.model(),quiet=True)
    chemostats = ['H2O','O2','PQ','PQH2','Hn','Hp','P680']
    scPII = st.statify(sPII,chemostats=chemostats)
    spPII = st.path(sPII,scPII)
    ## All reactions
    disp.Latex(st.sprintrl(sPII,chemformula=True))
```

Out[9]:

$$E_1 + P_{680} \stackrel{\mathbf{r}}{\Longleftrightarrow} E_2 \tag{10}$$

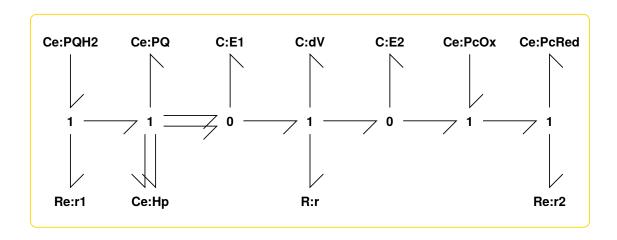
$$2 H_2 O \stackrel{r_1}{\iff} 4 E_1 + 4 Hp + O_2$$
 (11)

$$2E_2 + 2Hn + PQ \stackrel{r_2}{\rightleftharpoons} PQH_2$$
 (12)

```
4P_{680} + 2H_2O + 4Hn + 2PQ \xrightarrow{pr_1} 4Hp + O_2 + 2PQH_2
                                                                                   (13)
In [11]: ## Compute net redox potential
         RP_PII = (
                      - redoxData.EpH('02/2H20',pH=pH_p)
                     + redoxData.EpH('PQ/PQH2',pH=pH_n)
                  )
         print(redoxData.EpH('02/2H20',pH=pH_p))
         print(redoxData.E('P680+/P680*'))
         print(redoxData.E7('PQ/PQH2'))
         print(redoxData.EpH('PQ/PQH2',pH=pH_n))
         #print(RP_PII)
         print('RP_PII =',int(1000*RP_PII), 'mV')
1.0006211565305827
0.8
0
0.0
RP_PII = 822 mV
In [12]: ## Compute the reaction potential Phi
         phi = phiData.phi_species(phi_redox,spPII['species'])
         Phi_PII_ = -spPII['N'].T@phi
         Phi_PII = Phi_PII_[0][0]
         print('Phi_PII =',int(1000*Phi_PII), 'mV')
         print('Ratio =',(Phi_PII/RP_PII))
Phi_PII = 3290 \text{ mV}
Ratio = 4.0
4.2 Complex Cyt -- Cytochrome bf
In [13]: disp.SVG('Cyt_abg.svg')
```

Out[10]:

Out[13]:



Out[15]:

$$E_1 \stackrel{r}{\longleftarrow} E_2 + dV \tag{14}$$

$$PQH_2 \stackrel{r_1}{\Longleftrightarrow} 2E_1 + 2Hp + PQ \tag{15}$$

$$E_2 + PcOx \stackrel{r_2}{\Longleftrightarrow} PcRed$$
 (16)

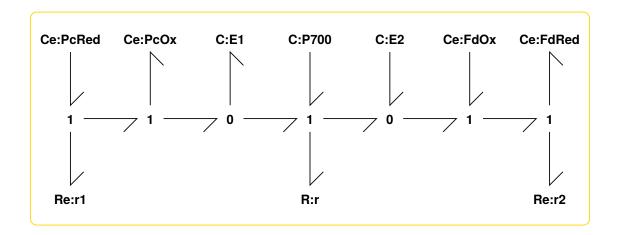
In [16]: disp.Latex(st.sprintrl(spCyt,chemformula=True))

Out[16]:

$$PQH_2 + 2 PcOx \stackrel{pr_1}{\rightleftharpoons} 2 dV + 2 Hp + PQ + 2 PcRed$$
 (17)

4.3 Complex PI -- Photosystem I

```
In [19]: disp.SVG('PI_abg.svg')
Out[19]:
```



$$E_1 + P_{700} \stackrel{r}{\Longleftrightarrow} E_2 \tag{18}$$

$$PcRed \stackrel{r_1}{\Longleftrightarrow} E_1 + PcOx \tag{19}$$

$$E_2 + FdOx \stackrel{r_2}{\longleftrightarrow} FdRed$$
 (20)

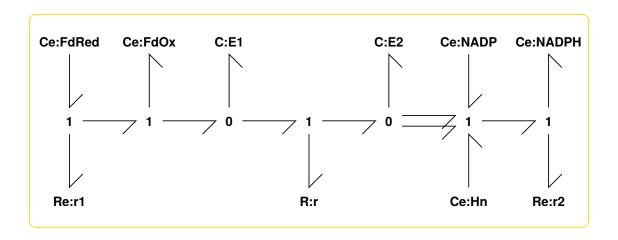
In [22]: disp.Latex(st.sprintrl(spPI,chemformula=True))
Out[22]:

$$P_{700} + FdOx + PcRed \xrightarrow{pr_1} FdRed + PcOx$$
 (21)

```
In [23]: ## Compute net redox potential
         RP_PI = (
                 - redoxData.E('PcOx/PcRed')
                 + V700
                 + redoxData.E('FdOx/FdRed')
         #print(RP_PI)
         print('RP_PI =',redoxData.mV(RP_PI), 'mV')
RP_PI = 961 \text{ mV}
In [24]: ## Compute the reaction potential Phi
         phi = phiData.phi_species(phi_redox,spPI['species'])
         Phi_PI_ = -spPI['N'].T@phi
         Phi_PI = Phi_PI_[0][0]
         print('Phi_PI =',redoxData.mV(Phi_PI), 'mV')
         print('Ratio =', int(round(Phi_PI/RP_PI)))
Phi_PI = 961 mV
Ratio = 1
```

4.4 Complex Fer -- Feredoxin-NADP reductase

```
In [25]: disp.SVG('Fer_abg.svg')
Out[25]:
```



```
In [26]: sbg.model('Fer_abg.svg',convertR=True,convertCe=True,quiet=True)
    import Fer_abg

In [27]: ## Stoichiometry
    sFer = st.stoich(Fer_abg.model())
        chemostats = ['FdRed','FdOx','NADP','NADPH','Hn']
        scFer = st.stoich(Fer_abg.model(),chemostats=chemostats)
        spFer = st.path(sFer,scFer)
        disp.Latex(st.sprintrl(sFer,chemformula=True))

Swapping Re:r for two Sf in Fer
Swapping Re:r2 for two Sf in Fer
Swapping Re:r1 for two Sf in Fer
Swapping Re:r1 for two Sf in Fer
Swapping Re:r2 for two Sf in Fer
Swapping Re:r2 for two Sf in Fer
```

Out[27]:

$$E_1 \stackrel{\mathbf{r}}{\Longleftrightarrow} E_2 \tag{22}$$

$$FdRed \stackrel{r_1}{\Longleftrightarrow} E_1 + FdOx \tag{23}$$

$$2E_2 + Hn + NADP \stackrel{r_2}{\longleftrightarrow} NADPH$$
 (24)

In [28]: disp.Latex(st.sprintrl(spFer,chemformula=True))

Out[28]:

$$2 FdRed + Hn + NADP \xrightarrow{pr_1} 2 FdOx + NADPH$$
 (25)

```
In [29]: ## Compute net redox potential
         RP_Fer = (
                 - redoxData.E('Fd0x/FdRed')
                 + redoxData.EpH('NADP/NADPH',pH_n)
                 )
         #print(RP_Fer)
         print('RP_Fer =',int(1000*RP_Fer), 'mV')
RP_Fer = 105 \text{ mV}
In [30]: ## Compute the reaction potential Phi
         phi = phiData.phi_species(phi_redox,spFer['species'])
         Phi_Fer_ = -spFer['N'].T@phi
         Phi_Fer = Phi_Fer_[0][0]
         print('Phi_Fer =',int(1000*Phi_Fer), 'mV')
         print('Ratio =', int(Phi_Fer/RP_Fer))
Phi_Fer = 212 mV
Ratio = 2
```

5 The Electron Transport Chain

The overall model is described a bond graph tools file:

```
In [31]: ## File ETC_abg.py
         import BondGraphTools as bgt
         import PII_abg
         import Cyt_abg
         import PI_abg
         import Fer_abg
         def model():
             Model of chloroplast electron transport chain
             .....
             ETC = bgt.new(name='ETC') # Create system
             PII = PII_abg.model()
             Cyt = Cyt_abg.model()
             PI = PI_abg.model()
             Fer = Fer_abg.model()
             bgt.add(ETC,PII,Cyt,PI,Fer)
             return ETC
```

5.1 Unify species in model using mbg.unify()

```
In [32]: import ETC_abg
         model = ETC_abg.model()
         common = ['PQ','PQH2','PcOx','PcRed','FdOx', 'FdRed','Hn','Hp']
         mbg.unify(model,common,quiet=True)
         s = st.stoich(model,quiet=True)
In [33]: chemostats = ['H2O','O2','NADP','NADPH','Hp','Hn','P68O','P70O','dV']
         sc = st.statify(s,chemostats=chemostats)
         sp = st.path(s,sc)
         disp.Latex(st.sprintrl(sp,chemformula=True))
   Out [33]:
       4P_{680} + 2H_2O + 4P_{700} + 2NADP + 6Hn \xrightarrow{pr_1} O_2 + 4dV + 2NADPH + 8Hp
                                                                                   (26)
In [34]: ## Compute the reaction potential Phi
         phi = phiData.phi_species(phi_redox,sp['species'])
         Phi_ = -sp['N'].T@phi
         Phi= Phi_[0][0]
         print('Phi =',redoxData.mV(Phi), 'mV')
Phi = 7603 mV
```

References

Robert E. Blankenship. Molecular mechanisms of photosynthesis. Wiley Blackwell, Oxford, 2015.

Robert E. Blankenship and Roger C. Prince. Excited-state redox potentials and the z scheme of photosynthesis. *Trends in Biochemical Sciences*, 10(10):382 – 383, 1985. ISSN 0968-0004. doi:10.1016/0968-0004(85)90059-3.

David G Nicholls and Stuart Ferguson. Bioenergetics 4. Academic Press, Amsterdam, 2013.