Electrochemical Modelling and Ion Channels

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Note: This example is discussed in detail by (Gawthrop and Pan, 2020) available here.

Note: this is the ElectroChemical.ipynb notebook. The PDF version "Electrochemical Modelling and Ion Channels" is available here.

1 Introduction

1.1 Faraday equivalent potential

The bond graph approach uses the notion of energy covariables: a pair of variables whose product is power. Thus, for example, electrical systems have voltage (with units V) and current (with units A) as covariables and the product has units of power (W or J s⁻¹). Chemical system covariables are chemical potential μ (with units J C⁻¹) and molar flow f (with units mol s⁻¹)(Oster et al., 1971, 1973; Gawthrop and Crampin, 2014); again the product has units of power (W or J s⁻¹).

The commonality of power over different physical domains makes the bond graph approach particularly appropriate to model multi-domain systems, in particular chemoelectrical systems (Gawthrop et al., 2017). Noting that the conversion factor relating the electrical and chemical domains is *Faraday's constant* $F \approx 96\,485\,\mathrm{C}\,\mathrm{mol}^{-1}$. As discussed by Karnopp (1990) and Gawthrop et al. (2017), this conversion can be represented by the bond graph transformer (**TF**) component. An alternative approach introduced by Gawthrop (2017) is to divide the covariables μ and f by F to give the pair of covariables ϕ and f where:

Faraday-equivalent chemical potential
$$\phi = \frac{\mu}{F} V$$
 (1)

Faraday-equivalent flow
$$f = FvA$$
 (2)

1.2 Chemical properties

The **Ce** components representing chemical species generate Faraday-equivalent potential (FEP) ϕ (measured in Volts) in terms of the amount of species x as:

$$\phi = \phi^{\ominus} + \phi_N \ln \frac{x}{x^{\ominus}} \tag{3}$$

$$= \phi_N \ln Kx \tag{4}$$

where
$$K = \frac{K^{\ominus}}{x^{\ominus}}$$
 (5)

$$V_N = \frac{RT}{F} \approx 26mV \tag{6}$$

and
$$K^{\ominus} = \ln \frac{\phi^{\ominus}}{\phi_N}$$
 (7)

 ϕ^{\ominus} in the standard potential at the standard amount x^{\ominus} . R is the universal gas constant and F Faraday's constant.

The amount of species *x* is the integral of the species flow *f*:

$$x = \int_{-\tau}^{t} f(\tau)d\tau \tag{8}$$

The formula can also be expressed in terms of concentration c as:

$$\phi = \phi_N \ln K_C' c \tag{9}$$

where
$$K_c' = \frac{K^{\ominus}}{C^{\ominus}}$$
 (10)

(11)

 c^{\ominus} is the concentration at standard conditions. ## Electrical properties The **C** components representing electrical capacitance generate electrical potential ϕ (measured in Volts) in terms of the amount of positively charges x and electrical capacitance C as:

$$\phi = \frac{x}{C} \tag{12}$$

$$=\phi_N K_E x_E \tag{13}$$

where
$$K_E = \frac{1}{x_N}$$
 (14)

and
$$x_N = C\phi_N$$
 (15)

The amount of charge x_E is the integral of the charge flow (current) f_E :

$$x_E = \int_0^t f_E(\tau) d\tau \tag{16}$$

```
In [1]: ## Some useful imports
    import BondGraphTools as bgt
    import numpy as np
    import sympy as sp
    import matplotlib.pyplot as plt

## Stoichiometric analysis
    import stoich as st

## SVG
    import svgBondGraph as sbg

## Display (eg disp.SVG(), disp.
    import IPython.display as disp

quiet = True

## Fix the concentrations via chemostats
Fix_conc = False
```

In /home/peterg/.local/lib/python3.6/site-packages/matplotlib/mpl-data/stylelib/_classic_test.mp
The text.latex.unicode rcparam was deprecated in Matplotlib 3.0 and will be removed in 3.2.
In /home/peterg/.local/lib/python3.6/site-packages/matplotlib/mpl-data/stylelib/_classic_test.mp
The savefig frameon reparam was deprecated in Matplotlib 3.1 and will be removed in 3.3

The savefig.frameon rcparam was deprecated in Matplotlib 3.1 and will be removed in 3.3. In /home/peterg/.local/lib/python3.6/site-packages/matplotlib/mpl-data/stylelib/_classic_test.mp

The pgf.debug rcparam was deprecated in Matplotlib 3.0 and will be removed in 3.2. In /home/peterg/.local/lib/python3.6/site-packages/matplotlib/mpl-data/stylelib/_classic_test.mp

The verbose.level rcparam was deprecated in Matplotlib 3.1 and will be removed in 3.3.

In /home/peterg/.local/lib/python3.6/site-packages/matplotlib/mpl-data/stylelib/_classic_test.mp The verbose.fileo rcparam was deprecated in Matplotlib 3.1 and will be removed in 3.3.

```
In [2]: ## Concentrations in nM for Na and K in Giant Squid Axon
    ## From Keener & Sneyd Table 2.1
    conc_e = {'Na':437, 'K':20}
    conc_i = {'Na':50, 'K':397}
```

2 Electrodiffusion

Cellular membranes have pores though which chemical species can diffuse. If the species are charged, the diffusion both depends on and creates an electrical potential. This section looks at a single ionic species with generic name I⁺; this can be thought of as Na⁺ or K⁺.

The bond graph representation of a charged ion has three components: a **Ce** component to represent the *chemical* properties of the ion, a **C** component to repesent the *electrical* properties of the ion and a **1** junction to make the flow into the two components identical.

The resultant potential is then the sum of the chemical and electrical components:

$$\phi = \phi_C + \phi_E \tag{17}$$

where
$$\phi_C = \phi_N \ln Kx$$
 (18)

and
$$\phi_E = \phi_N K_E x_E$$
 (19)

If the ion has *two* charges (I^{++}) the bold bonds in the diagram would each be replaced by *two* bonds; alternatively, if the ion had a *negative* charge (Γ) the bold bonds in the diagram would each be replaced by a bond with *reversed* direction.

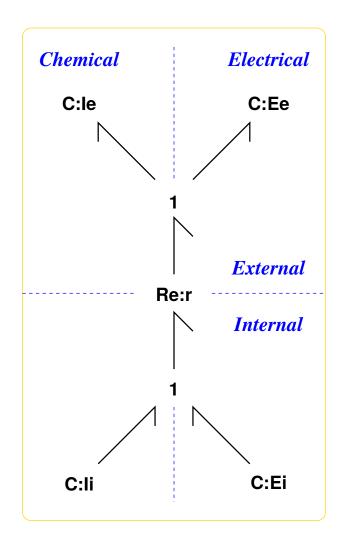
The bond graph of the pore itself has two pools of charged ions: internal and external connected by a reaction (**Re**) component. As the ion in each pool is the same, the property K' is the same for each pool. Thus the reaction potential Φ is the difference of the potentials of the internal and external ion pools:

$$\Phi = \phi_N \left(\ln K' c_i - \ln K' c_e \right) + (\phi_{Ei} - \phi_{Ee})$$
(20)

Defining $\Delta E = \phi_{Ei} - \phi_{Ee}$ and noting that at equilibrium $\Phi = 0$:

$$\Delta E = \phi_N \ln \frac{c_e}{c_i} \tag{21}$$

This is the expresion for the *Nernst potential* for a species with a single positive charge.



```
In [4]: ## Stoichiometry: linear Re
    s = st.stoich(Electrodiffusion_abg.model(),linear=['Ei','Ee','r'],quiet=quiet)

if Fix_conc:
    chemostats = ['Ii','Ie']
    else:
        chemostats = []

sc = st.statify(s,chemostats=chemostats)
    #print(s['species'])

In [5]: ## Stoichiometric matrix
    disp.Latex(st.sprintl(s,'N'))
    #print(st.sprintl(s,'species'))
Out[5]:
```

$$N = \begin{pmatrix} 1 \\ -1 \\ 1 \\ -1 \end{pmatrix} \tag{22}$$

In [6]: ## Reactions
diam Later(at april

disp.Latex(st.sprintrl(s,chemformula=True,all=True))

Out[6]:

$$Ei + Ii \stackrel{r}{\Longleftrightarrow} Ee + Ie$$
 (23)

In [7]: ## Flows

disp.Latex(st.sprintvl(s))

Out[7]:

$$v_r = \kappa_r \left(-K_{Ee} \chi_{Ee} + K_{Ei} \chi_{Ei} - V_N \left(\log \left(K_{Ie} \chi_{Ie} \right) - \log \left(K_{Ii} \chi_{Ii} \right) \right) \right) \tag{24}$$

In [8]: ## Stoichiometry: nonlinear Re

s = st.stoich(Electrodiffusion_abg.model(),linear=['Ei', 'Ee'],quiet=quiet)

if Fix_conc:

chemostats = ['Ii', 'Ie']

else:

chemostats = []

sc = st.statify(s,chemostats=chemostats)

#print(s['species'])

In [9]: ## Reactions

disp.Latex(st.sprintrl(s,chemformula=True,all=True))

Out [9]:

$$Ei + Ii \stackrel{r}{\Longleftrightarrow} Ee + Ie$$
 (25)

In [10]: ## Flows

print(st.sprintvl(s))
disp.Latex(st.sprintvl(s))

\begin{align}

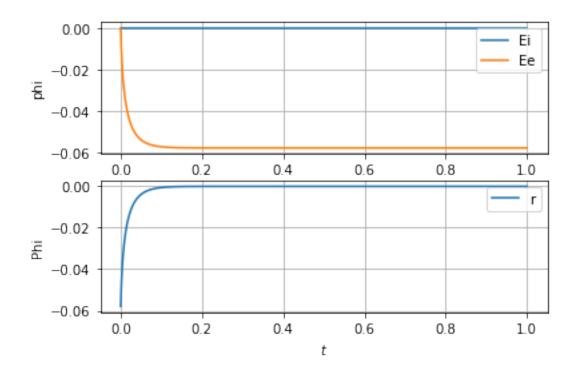
 $v_{r} &= \kappa_{r} \left(K_{Ie} x_{Ie} e^{\frac{K_{Ee} x_{Ee}}{V_{N}}} + K_{Ii} x_{Ii} e^{\frac{1}{r}} \right) \\ &= \kappa_{r} x_{Ie} e^{\frac{1}{r}} e^$

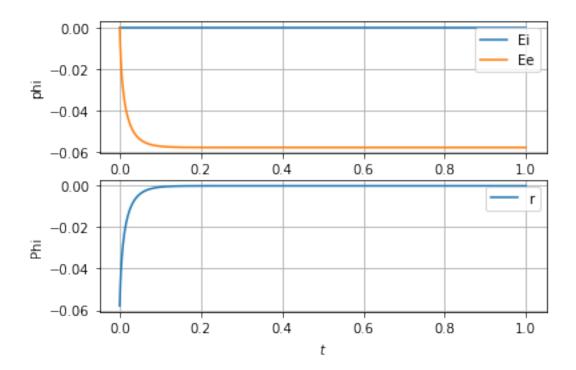
Out[10]:

```
v_r = \kappa_r \left( -K_{Ie} x_{Ie} e^{\frac{K_{Ee} x_{Ee}}{V_N}} + K_{Ii} x_{Ii} e^{\frac{K_{Ei} x_{Ei}}{V_N}} \right)
In [11]: #disp.Latex(st.sprintl(s,'species'))
In [12]: #disp.Latex(st.sprintl(s,'N'))
In [13]: ## Set non-unit parameters
          K_{Ii} = 1e-3
          K_Ie = 1e-3
          C = 1
          def setPar(s,C=1,conc_i=1,conc_e=1,prefix=['']):
               \#V_N = st.V_N()
              K_E = 1/C
               #print(K_E)
               ## Parameters
               parameter = {}
              parameter['K_Ei'] = 0
              parameter['K_Ee'] = K_E
               ## Initial state
               sp = s['species']
              re = s['reaction']
              X0 = np.ones(s['n_X'])
              X0[sp.index('Ei')] = 0
              X0[sp.index('Ee')] = 0
              for p in prefix:
                   ## Parameters
                   KK = 'K_' + p
                   kk = 'kappa_'+p
                   parameter[KK+'Ii'] = K_Ii
                   parameter[KK+'Ie'] = K_Ie
                   ## States and kappa
                   if len(p) is 0:
                        Ion = 'Na'
                   else:
                        Ion = p[0:len(p)-1]
                        #X0[sp.index('Ee')] = 0.077/K_E
                   print(Ion)
                   X0[sp.index(p+'Ii')] = conc_i[Ion]/K_Ii
```

(26)

```
X0[sp.index(p+'Ie')] = conc_e[Ion]/K_Ie
                 parameter[kk+'r'] = 1/conc_i[Ion]
             return parameter, XO
In [14]: def CheckTheory(dat):
             if 'Ii' in s['species']:
                 ## Check Nernst potential
                 t = dat['t']
                 phi_Ei = dat['phi'][:,s['species'].index('Ei')]
                 phi_Ee = dat['phi'][:,s['species'].index('Ee')]
                 x_Ii = dat['X'][:,s['species'].index('Ii')]
                 x_Ie = dat['X'][:,s['species'].index('Ie')]
                  v = dat['V'][:,s['reaction'].index('r')]
                 V_N = st.V_N()
                  v_ss = v[-1]
                 dV = (phi_Ei[-1]-phi_Ee[-1])
                 dV\_theory = V\_N*np.log(x\_Ie[-1]/x\_Ii[-1])
                   print(f'Steady-state flow is {v_ss:0.2}')
                 print(f'dV = {dV*1000:4.1f}mV')
                 print(f'dV_Theory = {dV_theory*1000:4.1f}mV')
In [15]: def Simulate(s,sc,T=1,X_chemo=None,prefix=['']):
             ## Time
             t = np.linspace(0,T,500)
             ## Parameters and initial state
             parameter,X0 = setPar(s,C=C,conc_i=conc_i,conc_e=conc_e,prefix=prefix)
             ## Simulate
             dat = st.sim(s,sc=sc,t=t,parameter=parameter,X0=X0,X_chemo=X_chemo,quiet=True)
             CheckTheory(dat)
             return dat
In [16]: dat = Simulate(s,sc)
         #st.plot(s,dat)
         st.plot(s,dat,plotPhi=True,species=['Ei','Ee'])
         st.plot(s,dat,plotPhi=True,species=['Ei','Ee'],filename='Figs/electrodiffusion.pdf')
Na
dV = 57.9mV
dV_Theory = 57.9mV
```

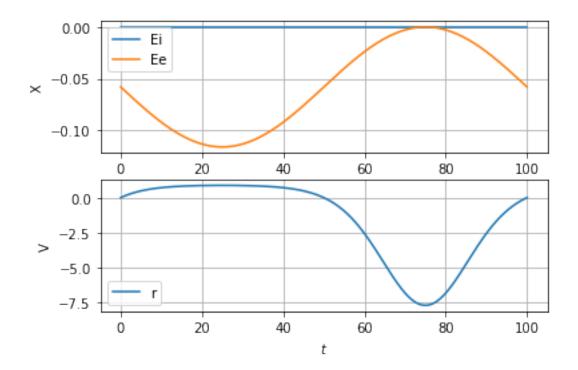




2.1 Voltage clamp

The voltage agross the membrane is clamped by setting C:Ei and C_Ee as chemostats. This allows the voltage-current relationship to be plotted. It is compared with the Hodgkin-Huxley (linear) model and the Goldman-Huxley-Katz model. The bond graph model can be modified to reflect the other two models (Gawthrop et al., 2017).

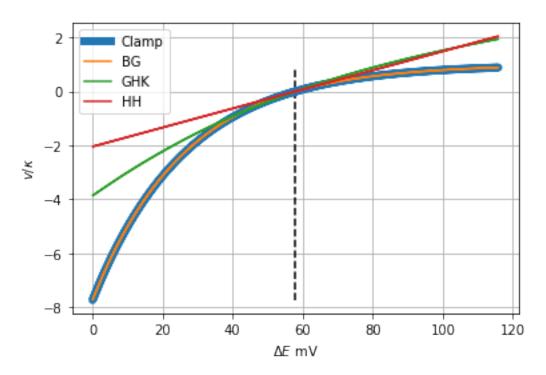
```
In [17]: ## Stoichiometry
         ##chemostats = ['Ii', 'Ie', 'Ei', 'Ee']
         chemostats = chemostats + ['Ei', 'Ee']
         scc = st.statify(s,chemostats=chemostats)
          #print(s['species'])
In [18]: X_{chemo} = \{\}
         V_Nernst = st.V_N()*np.log(conc_e['Na']/conc_i['Na'])
          #print(f'V_Nernst = {1000*V_Nernst:4.1f} mV')
         T = 100
         CV = C*V_Nernst
         \# x\_chemo = f'\{CV\}*(np.sin(\{2*np.pi/T\}*t))'
         \# \#X_{chemo}['Ee'] = f'\{-CV/2\}-'+x_{chemo}
         \# X_chemo['E'] = x_chemo
         x_{chemo} = f' - \{CV\}*(1+1.0*np.sin(\{2*np.pi/T\}*t))'
         X_{\text{chemo}}['Ee'] = x_{\text{chemo}}
         #print(X_chemo)
         dat = Simulate(s,scc,T=T,X_chemo=X_chemo)
          #st.plot(s,dat)
         st.plot(s,dat,species=['Ei','Ee'])
Na
dV = 57.9mV
dV_Theory = 57.8mV
```



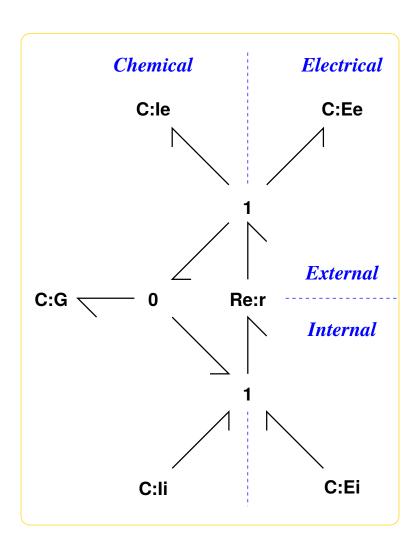
```
In [19]: def PlotClamp():
             t = dat['t']
             phi_Ei = dat['phi'][:,s['species'].index('Ei')]
             phi_Ee = dat['phi'][:,s['species'].index('Ee')]
             x_Ii = dat['X'][:,s['species'].index('Ii')]
             x_Ie = dat['X'][:,s['species'].index('Ie')]
             v = dat['V'][:,s['reaction'].index('r')]
             V_N = st.V_N()
             dV = phi_Ei-phi_Ee
             ## BG
             v_BG = (1/x_Ii)*(x_Ii - x_Ie*np.exp(-dV/V_N))
             ## GHK
             v_GHK = 0.5*v_BG*(dV/V_N)/(1-np.exp(-dV/V_N))
             ## HH
             v_HH = (np.exp(-V_Nernst))*(dV - V_Nernst)/V_N
             plt.plot(dV*1000,v,label='Clamp',lw = 6)
             plt.plot(dV*1000,v_BG,label='BG')
             plt.plot(dV*1000,v_GHK,label='GHK')
             plt.plot(dV*1000,v_HH,label='HH')
             plt.vlines(1000*V_Nernst,min(v),max(v),linestyle='dashed')
```

```
plt.grid()
plt.legend()
plt.xlabel('$\Delta E$ mV')
plt.ylabel('$v/\kappa$')
plt.savefig('Figs/clamp.pdf')
```

PlotClamp()



3 Gated ion channel



```
In [21]: ## Stoichiometry
    s = st.stoich(IonChannel_abg.model(),linear=['Ei','Ee'],quiet=quiet)
    if Fix_conc:
        chemostats = ['Ii','Ie','G']
    else:
        chemostats = ['G']
    sc = st.statify(s,chemostats=chemostats)
        print(s['species'])

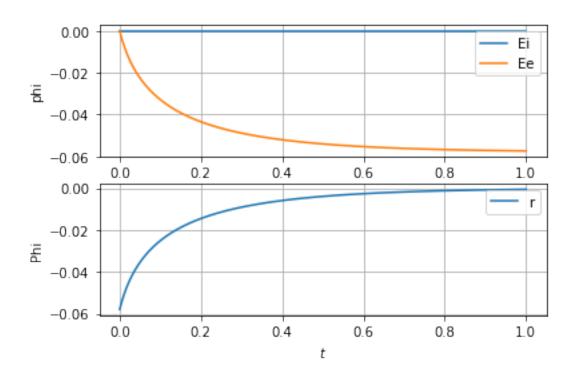
['Ee', 'Ei', 'G', 'Ie', 'Ii']

In [22]: ## Reactions
        disp.Latex(st.sprintrl(s,chemformula=True,all=True))
Out[22]:
```

 $Ei + G + Ii \stackrel{r}{\rightleftharpoons} Ee + G + Ie$

(27)

$$v_r = K_G \kappa_r x_G \left(-K_{Ie} x_{Ie} e^{\frac{K_{Ee} x_{Ee}}{V_N}} + K_{Ii} x_{Ii} e^{\frac{K_{Ei} x_{Ei}}{V_N}} \right)$$
 (28)



4 Interacting ion channels

Two instances of the ion channel module are combined; one corresponds to Na^+ and one to K^+ . The species concentations are encapsulated in the individual modules, but the electrical capaciter are shared. This is a simplified version of the Hodgkin-Huxley model of the squid giant axon and the corresponding Na^+ and K^+ concentrations are used.

The simulations use piecewise constant gating variables G_{Na} and G_K :

$$G_K = \begin{cases} 10^{-6} & \text{for } 0.3 < t < 0.35\\ 1 & \text{otherwise} \end{cases}$$
 (29)

$$G_K = \begin{cases} 10^{-6} & \text{for } 0.3 < t < 0.35\\ 1 & \text{otherwise} \end{cases}$$

$$G_{Na} = \begin{cases} 1 & \text{for } 0.3 < t < 0.35\\ 4.3 \times 10^{-3} & \text{otherwise} \end{cases}$$
(29)

The time course of the membrane potential ΔE can be explained as follows.

 $t < 0.3 \Delta E$ moves from the initial condition of zero to a *resting potential* of about -65mV.

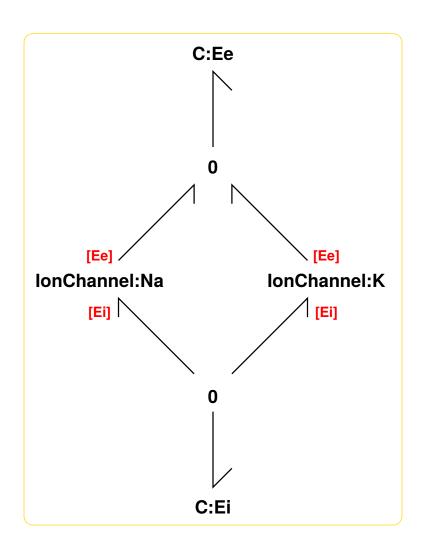
This corresponds to the value in Table 2.1 of Keener & Sneyd; the resting potential depends not only on Nernst potentials of chNa+ and K⁺ (which in turn depends on the concentrations) but also on the values of the gating potential.

0.3 < t < 0.35 ΔE undergoes a typical action potential as the Na⁺ gate opens and moves toward the Nernst potential for Na⁺ until the gate closes.

 $t > 0.35 \Delta E$ returns to the resting potential.

In this simple example the gating variables G_{Na} and G_K are independent variables, in reality, and in the HH model, the gating variables are modulated by the membrane potential ΔE . This is discussed in a bond graph context by Gawthrop et al. (2017).

```
In [25]: ## Ion Channels
         sbg.model('IonChannels_abg.svg')
         import IonChannels_abg
         disp.SVG('IonChannels_abg.svg')
Creating subsystem: IonChannel:K
Creating subsystem: IonChannel:Na
Out [25]:
```



```
In [26]: ## Stoichiometry
    s = st.stoich(IonChannels_abg.model(),linear=['Ei','Ee'],quiet=quiet)
    if Fix_conc:
        chemostats = ['Na_Ii','Na_Ie','Na_G', 'K_Ii','K_Ie','K_G']
    else:
        chemostats = ['Na_G','K_G']
    sc = st.statify(s,chemostats=chemostats)
    print(s['species'])

['Ee', 'Ei', 'K_G', 'K_Ie', 'K_Ii', 'Na_G', 'Na_Ie', 'Na_Ii']

In [27]: ## Reactions
    disp.Latex(st.sprintrl(s,chemformula=True,all=True))

Out[27]:
```

$$Ei + K_G + K_I i \stackrel{K_r}{\rightleftharpoons} Ee + K_G + K_I e$$
 (31)

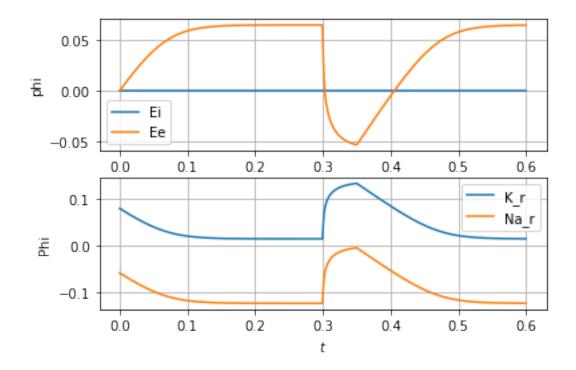
$$Ei + Na_G + Na_Ii \xrightarrow{Na_r} Ee + Na_G + Na_Ie$$
 (32)

Out [28]:

$$v_{Kr} = K_{KG} \kappa_{Kr} x_{KG} \left(-K_{KIe} x_{KIe} e^{\frac{K_{Ee} x_{Ee}}{V_N}} + K_{KIi} x_{KIi} e^{\frac{K_{Ei} x_{Ei}}{V_N}} \right)$$
(33)

$$v_{Nar} = K_{NaG} \kappa_{Nar} x_{NaG} \left(-K_{NaIe} x_{NaIe} e^{\frac{K_{Ee} x_{Ee}}{V_N}} + K_{NaIi} x_{NaIi} e^{\frac{K_{Ei} x_{Ei}}{V_N}} \right)$$
(34)

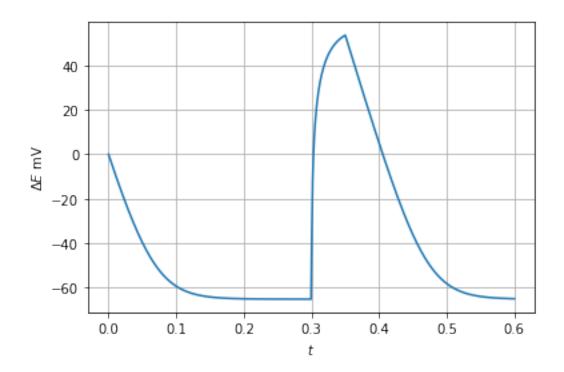
Na K

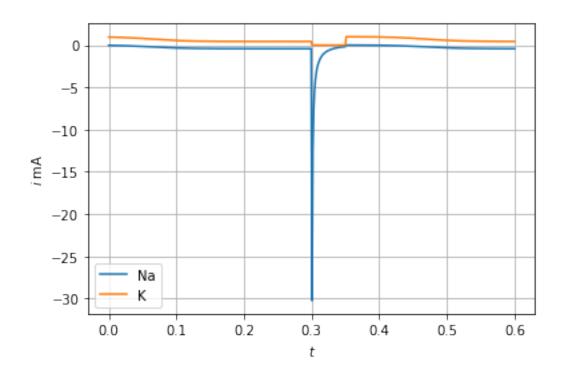


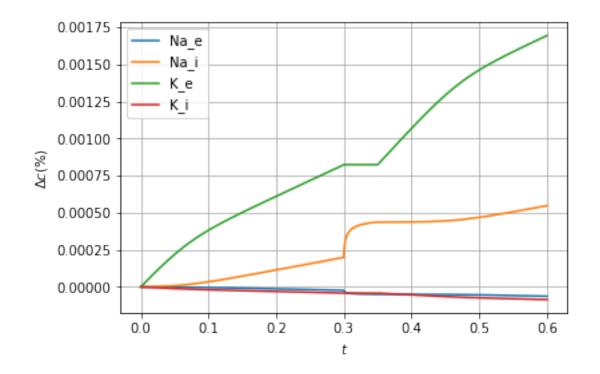
```
In [30]: def PlotAction():
             t = dat['t']
             phi_Ei = dat['phi'][:,s['species'].index('Ei')]
             phi_Ee = dat['phi'][:,s['species'].index('Ee')]
             dE = phi_Ei-phi_Ee
             print(f'Resting potential = {1000*dE[-1]:.2f} mV')
             X_G_K = dat['X'][:,s['species'].index('K_G')]
             X_G_Na = dat['X'][:,s['species'].index('Na_G')]
             v_Na = dat['V'][:,s['reaction'].index('Na_r')]
             v_K = dat['V'][:,s['reaction'].index('K_r')]
             conc_Na_e = K_Ie*dat['X'][:,s['species'].index('Na_Ie')]
             conc_Na_i = K_Ii*dat['X'][:,s['species'].index('Na_Ii')]
             conc_Na_e_0 = conc_Na_e[0]
             conc_Na_i_0 = conc_Na_i[0]
             conc_K_e = K_Ie*dat['X'][:,s['species'].index('K_Ie')]
             conc_K_i = K_Ii*dat['X'][:,s['species'].index('K_Ii')]
             conc_K_e_0 = conc_K_e[0]
             conc_K_i_0 = conc_K_i_0
```

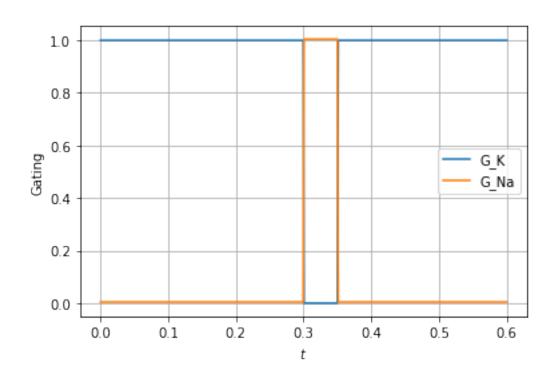
```
plt.plot(t,1000*dE)
    plt.grid()
    plt.ylabel('$\Delta E$ mV')
    plt.xlabel('$t$')
    plt.savefig('Figs/action.pdf')
    plt.show()
    plt.plot(t,v_Na,label='Na')
    plt.plot(t,v_K,label='K')
    plt.grid()
    plt.legend()
    plt.ylabel('$i$ mA')
    plt.xlabel('$t$')
    plt.savefig('Figs/action_current.pdf')
    plt.show()
    plt.plot(t,100*(conc_Na_e-conc_Na_e_0)/conc_Na_e_0,label='Na_e')
    plt.plot(t,100*(conc_Na_i-conc_Na_i_0)/conc_Na_i_0,label='Na_i')
    plt.plot(t,100*(conc_K_e-conc_K_e_0)/conc_K_e_0,label='K_e')
    plt.plot(t,100*(conc_K_i-conc_K_i_0)/conc_K_i_0,label='K_i')
    plt.legend()
    plt.grid()
    plt.ylabel(r'$\Delta c (\%)$')
    plt.xlabel('$t$')
    plt.savefig('Figs/action_conc.pdf')
    plt.show()
    plt.plot(t,X_G_K,label='G_K')
    plt.plot(t,X_G_Na,label='G_Na')
    plt.legend()
    plt.grid()
    plt.ylabel('Gating')
    plt.xlabel('$t$')
    plt.savefig('Figs/action_gating.pdf')
    plt.show()
PlotAction()
```

Resting potential = -64.90 mV









References

- Peter J. Gawthrop and Michael Pan. Network thermodynamical modelling of bioelectrical systems: A bond graph approach. Available at arXiv:2009.02217, 2020.
- George Oster, Alan Perelson, and Aharon Katchalsky. Network thermodynamics. *Nature*, 234: 393–399, December 1971. doi:10.1038/234393a0.
- George F. Oster, Alan S. Perelson, and Aharon Katchalsky. Network thermodynamics: dynamic modelling of biophysical systems. *Quarterly Reviews of Biophysics*, 6(01):1–134, 1973. doi:10.1017/S0033583500000081.
- Peter J. Gawthrop and Edmund J. Crampin. Energy-based analysis of biochemical cycles using bond graphs. *Proceedings of the Royal Society A: Mathematical, Physical and Engineering Science*, 470(2171):1–25, 2014. doi:10.1098/rspa.2014.0459. Available at arXiv:1406.2447.
- P. J. Gawthrop, I. Siekmann, T. Kameneva, S. Saha, M. R. Ibbotson, and E. J. Crampin. Bond graph modelling of chemoelectrical energy transduction. *IET Systems Biology*, 11(5):127–138, 2017. ISSN 1751-8849. doi:10.1049/iet-syb.2017.0006. Available at arXiv:1512.00956.
- Dean Karnopp. Bond graph models for electrochemical energy storage: electrical, chemical and thermal effects. *Journal of the Franklin Institute*, 327(6):983 992, 1990. ISSN 0016-0032. doi:10.1016/0016-0032(90)90073-R.
- P. J. Gawthrop. Bond graph modeling of chemiosmotic biomolecular energy transduction. *IEEE Transactions on NanoBioscience*, 16(3):177–188, April 2017. ISSN 1536-1241. doi:10.1109/TNB.2017.2674683. Available at arXiv:1611.04264.