# Additional material for: Network Thermodynamics of Biological Systems: A Bond Graph Approach

# Peter Gawthrop and Michael Pan April 26, 2022

# **Contents**

1	Intr	oduction	3
	1.1	Some useful imports	3
	1.2	Photosynthesis	4
2	Pho	oton Energetics	5
3	Red	lox reactions	6
	3.1	2 port Re version	6
	3.2	1 port Re version	7
	3.3	Redox formulation	8
		3.3.1 Stoichiometry	8
		3.3.2 Pathway analysis	8
4	Che	emical reaction network (CRN) representation	9
	4.1		10
	4.2	Pathway analysis	10
5	Red	lox potentials and equivalent species potentials $\phi$	11
6	Bon	nd graph description of ETC complexes	13
		Complex PII – Photosystem II	13
			13
		6.1.2 Pathway analysis with redox and pathway potentials	14
	6.2	Complex Cyt – Cytochrome bf	15
		J	15
			15
	6.3	$\mathbf{I}$	16
		C 0.1 Ct at all tables at time	1/
		J control of the cont	16
		6.3.2 Pathway analysis with redox and pathway potentials	17
	6.4	6.3.2 Pathway analysis with redox and pathway potentials	17 17
	6.4	6.3.2 Pathway analysis with redox and pathway potentials	17 17 18
	6.4	6.3.2 Pathway analysis with redox and pathway potentials	17 17
7		6.3.2 Pathway analysis with redox and pathway potentials	17 17 18 18
7		6.3.2 Pathway analysis with redox and pathway potentials  Complex Fer – Feredoxin-NADP reductase  6.4.1 Stoichiometry  6.4.2 Pathway analysis with redox and pathway potentials  Electron Transport Chain  Graphical description	17 17 18 18 <b>19</b>
7	The	6.3.2 Pathway analysis with redox and pathway potentials  Complex Fer – Feredoxin-NADP reductase 6.4.1 Stoichiometry 6.4.2 Pathway analysis with redox and pathway potentials  Electron Transport Chain Graphical description 7.1.1 Stoichiometry	17 17 18 18

	7.2	Computational description	
8	Chl	oroplast	22
	8.1	Modular model	22
	8.2	Generate equations	23
	8.3	Pathway analysis	23
		8.3.1 Pathway reaction	23
	8.4	Efficiency from estimated $\phi$	
		Efficiency by direct calculation	

#### 1 Introduction

- This document contains additional material for the paper: *Network Thermodynamics of Biological Systems: A Bond Graph Approach* by Peter Gawthrop and Michael Pan.
- It illustrates how the Python package BondGraphTools can be used to create and analyse chemical reaction networks.
- It provides background to Section 4.2 *Redox Reactions*, Section 6 *Stoichiometry and Bond Graphs* and Section 7 *Example: Photosynthesis*.
- This document is **Chloroplast.pdf** (see also **Reactions.pdf**).
- The document is available as the Jupyter notebook **Chloroplast.ipynb**.

## 1.1 Some useful imports

```
[1]: ## Some useful imports
     import BondGraphTools as bgt
     print('Using BondGraphTools', bgt.version)
     import numpy as np
     import sympy as sp
     import matplotlib.pyplot as plt
     ## Stoichiometric analysis
     import stoich as st
     ## SVG bg representation conversion
     import svgBondGraph as sbg
     ## Stoich to BG
     import stoichBondGraph as stbg
     ## Modular bond graphs
     import modularBondGraph as mbg
     ## Display (eg disp.SVG(), disp.
     import IPython.display as disp
     ## Data
     import phiData
     import redoxData
     ## Copy
     import copy
     import importlib as imp
     quiet = True
     chemformula = True
```

Using BondGraphTools 0.3.7

```
[2]: def mV(E):
    return int(round(1000*E))
```

#### 1.2 Photosynthesis

Photosynthesis within plant chloroplasts is the basis of life on earth Blankenship (2021), Nicholls and Ferguson (2013).

Like the mitochondrion, the chloroplast has a membrane seperating an inner space (lumen) from an outer space (stroma). In the chloroplast, the lumen gains protons and is called the p-space, the stroma looses protons and is called the n-space. Thus geometrically, the lumen corresponds to the mitochondrial matrix and the stroma to the mitochondrial intermembrane space; but electrically the p-space is inside and the n-space outside - the reverse of the mitochondrial situation.

The chloroplast electron transport chain has 4 complexes.

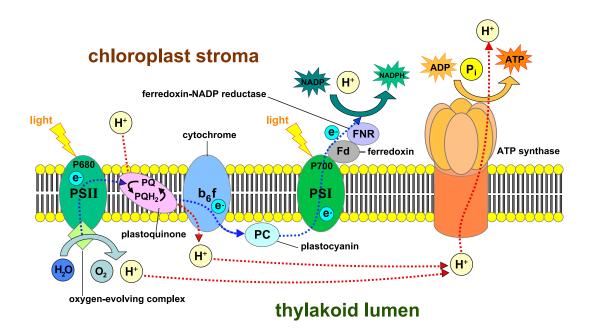
- 1. Photosystem II (PII) which absorbs photons at 680nm and splits water releasing protons into the p-space and passing electrons to the plastoquinone(PQ)/plastoquine(PQH2) couple which absorbs protons from the n-space.
- 2. Cytochrome bf (Cyt) which passes electrons to the plastoquine/plastoquinone couple which releases two protons into the p-space. Electrons are passed to the plastocyanine couple (PcOx/PcRed). Two protons are pumped across the membrane.
- 3. Photosystem I (PI) which absorbs photons at 700nm and transports electrons from the plastocyanine (PcRed/PcOx) couple to the ferredoxin (FdOx/FdRed) couple.
- 4. Ferredoxin-NADP reductase which transfers electrons from the ferredoxin (FdRed/FdOx) couple to convert NADP to NADPH absorbing a proton from the n-space.

The following figure is: https://commons.wikimedia.org/wiki/File:Thylakoid\_membrane\_3.svg

• See section 7 of paper.

```
[3]: # https://commons.wikimedia.org/wiki/File:Thylakoid_membrane_3.svg disp.SVG("Thylakoid_membrane_3.svg")
```

[3]:



# 2 Photon Energetics

• See section 7.2 of paper.

$$\phi_{photon} = \frac{N_{av}hc}{F\lambda} \tag{1}$$

where 
$$N_{av} = \text{Avogadro's number}$$
 (2)

$$h = Planck's constant$$
 (3)

$$c = \text{velocity of light}$$
 (4)

$$F = Faraday's constant$$
 (5)

and 
$$\lambda = \text{wavelength}$$
 (6)

For example:

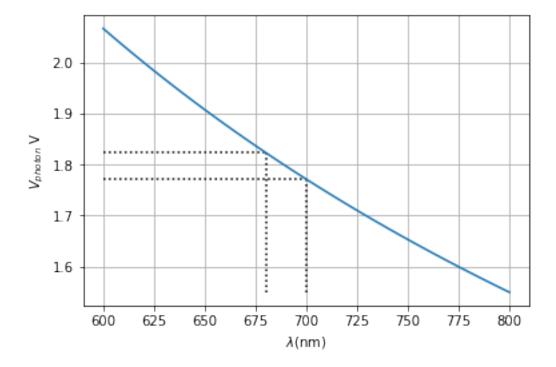
$$\phi_{photon} = \begin{cases} 1.82V & \lambda = 680nm \\ 1.77V & \lambda = 700nm \end{cases}$$
 (7)

```
[4]: ## Plot
    wavelength = np.linspace(600,800,100)
    phi_680 = redoxData.V_photon(680)
    phi_700 = redoxData.V_photon(700)
    print(f'phi_680 = {phi_680:0.2f}')
    print(f'phi_700 = {phi_700:0.2f}')
    phi_wave = [phi_680,phi_700]
    wave = [680,700]
    one = np.ones(2)

PHI = redoxData.V_photon(wavelength)
    plt.plot(wavelength,PHI)
```

```
plt.hlines(phi_wave,min(wavelength)*one,wave,linestyles='dotted')
plt.vlines(wave,min(PHI)*one,phi_wave,linestyles='dotted')
plt.grid()
plt.xlabel('$\lambda$(nm)')
plt.ylabel('$V_{photon}$ V')
plt.savefig('Figs/V_photon.pdf')
```

```
phi_680 = 1.82
phi_700 = 1.77
```



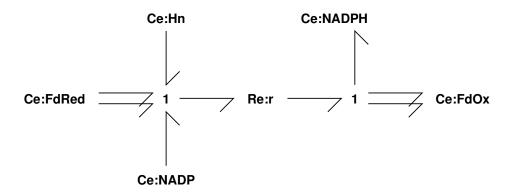
# 3 Redox reactions

# 3.1 2 port Re version

• See section 3.5 of paper.

```
[5]: ## 2 port Re version
disp.SVG('Fer0_abg.svg')
```

[5]:

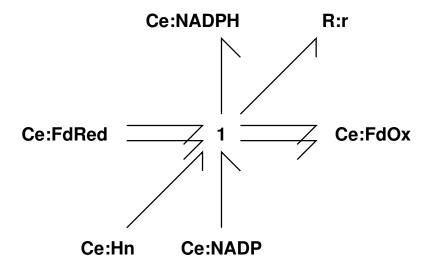


# 3.2 1 port Re version

• See section 3.6 of paper.

```
[6]: ## One-port Re version
disp.SVG('Fer1_abg.svg')
```

[6]:



```
[7]: ## Convert to BGtools
sbg.model('Fer1_abg.svg',convertCe=True,convertR=True,quiet=quiet)
import Fer1_abg

[8]: ## Stoichiometry
sFer1= st.stoich(Fer1_abg.model(),quiet=True)
disp.Latex(st.sprintrl(sFer1,chemformula=chemformula))
```

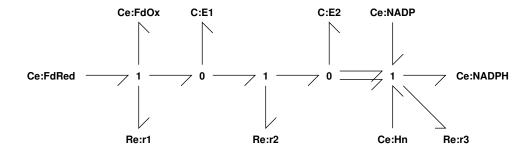
[8]:

$$2 FdRed + Hn + NADP \stackrel{r}{\Longleftrightarrow} 2 FdOx + NADPH$$
 (8)

#### 3.3 Redox formulation

This redox reaction can be written as two half-reactions with the following BG representation:

[9]:



```
[10]: sbg.model('Fer_abg.svg',convertCe=True,convertR=True,quiet=quiet)
import Fer_abg
# imp.reload(Fer_abg)
```

#### 3.3.1 Stoichiometry

[11]:

$$FdRed \stackrel{r_1}{\Longleftrightarrow} E_1 + FdOx$$
 (9)

$$E_1 \stackrel{r_2}{\longleftrightarrow} E_2 \tag{10}$$

$$2E_2 + Hn + NADP \stackrel{r_3}{\Longleftrightarrow} NADPH$$
 (11)

#### 3.3.2 Pathway analysis

[12]:

$$2 \text{FdRed} + \text{Hn} + \text{NADP} \xrightarrow{\text{pr}_1} 2 \text{FdOx} + \text{NADPH}$$
 (12)

# 4 Chemical reaction network (CRN) representation

• See section 6.4 of paper.

[13]: disp.Latex(st.sprintl(sFer, 'species'))

[13]:

$$X = \begin{pmatrix} X_{E1} \\ X_{E2} \\ X_{FdOx} \\ X_{FdRed} \\ X_{Hn} \\ X_{NADP} \\ X_{NADPH} \end{pmatrix}$$

$$(13)$$

[14]: disp.Latex(st.sprintl(sFer,'N'))

[14]:

$$N = \begin{pmatrix} 1 & -1 & 0 \\ 0 & 1 & -2 \\ 1 & 0 & 0 \\ -1 & 0 & 0 \\ 0 & 0 & -1 \\ 0 & 0 & -1 \\ 0 & 0 & 1 \end{pmatrix}$$
 (14)

[15]: disp.Latex(st.sprintl(sFer, 'Z'))

[15]:

$$Z = \begin{pmatrix} 0 & 1 & 0 & 1 & 0 & 0 \\ 0 & 0 & 2 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix}$$

$$(15)$$

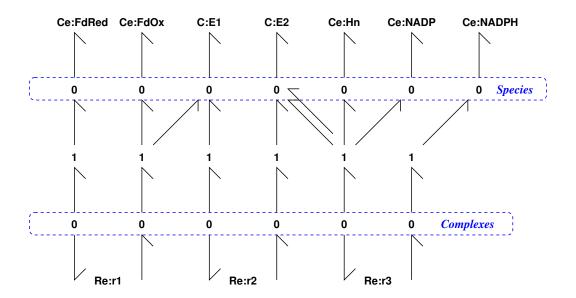
[16]: disp.Latex(st.sprintl(sFer, 'D'))

[16]:

$$D = \begin{pmatrix} -1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & -1 \\ 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix} \tag{16}$$

```
[17]: disp.SVG('FerCRN_abg.svg')
```

[17]:



```
[18]: sbg.model('FerCRN_abg.svg',quiet=quiet)
import FerCRN_abg
# imp.reload(FerCRN_abg)
```

## 4.1 Stoichiometry

```
[19]: ## Stoichiometry
imp.reload(st)
sFerCRN= st.stoich(FerCRN_abg.model(),quiet=quiet)
disp.Latex(st.sprintrl(sFerCRN,chemformula=chemformula))
```

[19]:

$$FdRed \xrightarrow{r_1} E_1 + FdOx$$
 (17)

$$E_1 \stackrel{\mathbf{r}_2}{\longleftarrow} E_2 \tag{18}$$

$$2E_2 + Hn + NADP \xrightarrow{r_3} NADPH$$
 (19)

#### 4.2 Pathway analysis

```
[20]: ## Pathway analysis
    chemostats = ['FdRed','FdOx','NADP','NADPH','Hn']
    scFerCRN = st.stoich(FerCRN_abg.model(),chemostats=chemostats,quiet=True)
    spFerCRN = st.path(sFerCRN,scFerCRN)
    disp.Latex(st.sprintrl(spFerCRN,chemformula=chemformula))
```

[20]:

$$2 \text{FdRed} + \text{Hn} + \text{NADP} \xrightarrow{\text{pr}_1} 2 \text{FdOx} + \text{NADPH}$$
 (20)

## 5 Redox potentials and equivalent species potentials $\phi$

Note that photon energies have been used for  $V_700$  and  $V_680$ ; this value is too large as the energy conversion is not direct. A model of this needs to be built. See, for example: Blankenship and Prince (1985)

According to Blankenship (2021) (sec. 8.3) the *electrical* part of the membrane potential is small in isolated choroplasts.

```
[21]: #disp.Latex(redoxData.table())
[22]: import redoxData
      ## pH from BerTymStr 19.3
      pH_p = 4 \# pH \ of \ p-space
      pH_n = pH_p + 3
      VpH = redoxData.VpH(pH_p - pH_n)
      V680 = redoxData.V_photon(wavelength=680)
      V700 = redoxData.V_photon(wavelength=700)
      print(VpH)
      print('V_pH =',int(1000*VpH),'mV')
      print('V_680 =',int(1000*V680),'mV')
      print('V_700 =',int(1000*V700),'mV')
     0.18462122057715774
     V_pH = 184 mV
     V_{680} = 1823 \text{ mV}
     V_700 = 1771 \text{ mV}
[23]: ## Convert redox potentials to species phi
      phi_redox = redoxData.phi()
      phi_redox['Hn'] = redoxData.VpH(pH_n)
      phi_redox['Hp'] = redoxData.VpH(pH_p)
      ## The electrical membrane potential is close to zero ()
      phi_redox['dV'] = VpH
      ## Put in my computed values for photon potentials
      phi_redox['P680'] = phi_680
      phi_redox['P700'] = phi_700
[24]: ## phi for ATP etc from Phi for hydrolysis
      # Phi_Hyd = 0.424
      Phi_Hyd = 35e3/st.F()
      print(f'Phi_hyd = {Phi_Hyd:0.2f}')
      phi_H20 = phi_redox['H20']
      phi_H = phi_redox['Hn']
      Phi_A = Phi_Hyd - phi_H2O + phi_H
      print(f'Phi_A: {Phi_A:0.2f}')
      phi_ATP = Phi_A/2
      phi_ADP = phi_Pi = -Phi_A/4
```

```
phi_redox['ATP'] = phi_ATP
      phi_redox['ADP'] = phi_ADP
      phi_redox['Pi'] = phi_Pi
      ## Sanity check
      Phi_Hyd_check = phi_ATP + phi_H2O -(phi_ADP + phi_Pi + phi_H)
      print(f'{Phi_Hyd_check-Phi_Hyd:0.2f}')
     Phi_hyd = 0.36
     Phi_A: 1.18
     0.00
[25]: # Print values
      for spec in phi_redox.keys():
          if not (('*' in spec) or ('E' in spec) or ('+' in spec)):
              print(f'phi_{spec} = {phi_redox[spec]:0.2f} V')
     phi_NADP = -0.11 V
     phi_NADPH = 0.11 V
     phi_NAD = -0.10 V
     phi_NADH = 0.10 V
     phi_02 = 2.49 V
     phi_H20 = -1.25 V
     phi_P700 = 1.77 V
     phi_P870 = 0.45 V
     phi_P680 = 1.82 V
     phi_PQ = 0.43 V
     phi_PQH2 = -0.43 V
     phi_PcOx = 0.19 V
     phi_PcRed = -0.19 V
     phi_Fd0x = -0.21 V
     phi_FdRed = 0.21 V
     phi_Hn = -0.43 V
     phi_Hp = -0.25 V
     phi_dV = 0.18 V
     phi\_ATP = 0.59 V
     phi\_ADP = -0.29 V
     phi_Pi = -0.29 V
[26]: | ## Compatibility with Chloroplast model (but makes no difference)
      phi_redox['etc_FdRed'] = phi_redox['FdRed']
      phi_redox['etc_PcRed'] = phi_redox['PcRed']
      phi_redox['etc_PQH2'] = phi_redox['PQH2']
[27]: ## Redox potentials with zero photon contribution
      phi_redox_0 = copy.copy(phi_redox)
      phi_redox_0['P680'] = phi_redox_0['P700'] = 0
```

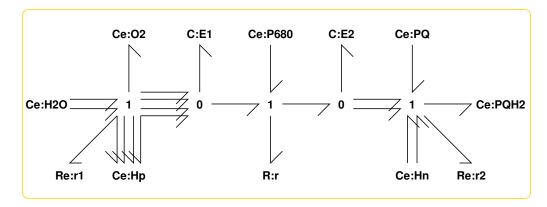
# 6 Bond graph description of ETC complexes

- The four ETC complexes are represented by SVG graphics which are automatically converted into BondGraphTools format.
- The stoichiometric toolbox is then used to generate the pathway-reduced equation for the complex.
- See section 7 of paper.

## 6.1 Complex PII – Photosystem II

[28]: disp.SVG('PII\_abg.svg')

[28]:



```
[29]: imp.reload(sbg)
    sbg.model('PII_abg.svg',convertCe=True,convertR=True,quiet=quiet)
    import PII_abg
    # imp.reload(PII_abg)
```

### 6.1.1 Stoichiometry

```
[30]: ## Stoichiometry
sPII = st.stoich(PII_abg.model(),quiet=quiet)
chemostats = ['H2O','O2','PQ','PQH2','Hn','Hp','P680']
scPII = st.statify(sPII,chemostats=chemostats)
spPII = st.path(sPII,scPII)
## All reactions
disp.Latex(st.sprintrl(sPII,chemformula=chemformula))
```

[30]:

$$E_1 + P_{680} \stackrel{r}{\longleftarrow} E_2 \tag{21}$$

$$2 H_2 0 \stackrel{r_1}{\iff} 4 E_1 + 4 Hp + 0_2$$
 (22)

$$2E_2 + 2Hn + PQ \stackrel{r_2}{\Longleftrightarrow} PQH_2$$
 (23)

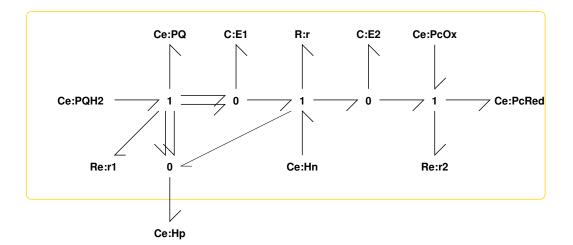
#### 6.1.2 Pathway analysis with redox and pathway potentials

```
[31]: ## Pathway analysis
      disp.Latex(st.sprintrl(spPII,chemformula=chemformula))
[31]:
                        2 H_2 O + 4 Hn + 4 P_{680} + 2 PQ \stackrel{pr_1}{\Longleftrightarrow} 4 Hp + O_2 + 2 PQH_2
                                                                                       (24)
[32]: ## Compute net redox potential
      RP_PII = (
                   - redoxData.EpH('02/2H20',pH=pH_p)
                   + redoxData.EpH('PQ/PQH2',pH=pH_n)
                )
      print(redoxData.EpH('02/2H20',pH=pH_p))
      print(redoxData.E('P680+/P680*'))
      print(redoxData.E7('PQ/PQH2'))
      print(redoxData.EpH('PQ/PQH2',pH=pH_n))
      #print(RP_PII)
      print('RP_PII =',int(1000*RP_PII), 'mV')
     1.0006212205771576
     0.8
     0
     0.0
     RP_PII = 822 mV
[33]: ## Compute the reaction potential Phi
      phi = phiData.phi_species(phi_redox,spPII['species'])
      Phi_PII_ = -spPII['N'].T@phi
      Phi_PII = Phi_PII_[0][0]
      print(f'Phi_PII = {int(1000*Phi_PII)} mV')
      print(f'Ratio = {(Phi_PII/RP_PII):.2f}')
     Phi_PII = 3290 mV
     Ratio = 4.00
[34]: ## Photon contribution
      n_{phot}=4
      print(f"Photon contribution = {mV(n_phot*redoxData.E('P680+/P680*'))} mV")
     Photon contribution = 3200 mV
[35]: ## Potential per proton
      n_prot = 4
      print(f'Potential per proton = {mV(Phi_PII/n_prot)}')
     Potential per proton = 823
```

## 6.2 Complex Cyt – Cytochrome bf

```
[36]: disp.SVG('Cyt_abg.svg')
```

[36]:



```
[37]: sbg.model('Cyt_abg.svg',convertR=True,convertCe=True,quiet=quiet)
import Cyt_abg
# imp.reload(Cyt_abg)
```

#### 6.2.1 Stoichiometry

```
[38]: ## Stoichiometry
sCyt = st.stoich(Cyt_abg.model(),quiet=True)
chemostats = ['PQ','PQH2','PcOx','PcRed','Hp','Hn']
scCyt = st.statify(sCyt,chemostats=chemostats)
spCyt = st.path(sCyt,scCyt)
disp.Latex(st.sprintrl(sCyt,chemformula=chemformula))
```

[38]:

$$E_1 + Hn \stackrel{r}{\Longleftrightarrow} E_2 + Hp$$
 (25)

$$PQH_2 \stackrel{r_1}{\rightleftharpoons} 2E_1 + 2Hp + PQ$$
 (26)

$$E_2 + PcOx \stackrel{r_2}{\Longleftrightarrow} PcRed$$
 (27)

#### 6.2.2 Pathway analysis with redox and pathway potentials

[39]: disp.Latex(st.sprintrl(spCyt,chemformula=chemformula))

[39]:

$$2 \operatorname{Hn} + \operatorname{PQH}_2 + 2 \operatorname{PcOx} \stackrel{\operatorname{pr}_1}{\rightleftharpoons} 4 \operatorname{Hp} + \operatorname{PQ} + 2 \operatorname{PcRed}$$
 (28)

```
+ redoxData.E('PcOx/PcRed')
)

#print(RP_Cyt)
print('RP_Cyt =',redoxData.mV(RP_Cyt), 'mV')
```

 $RP_Cyt = 11 mV$ 

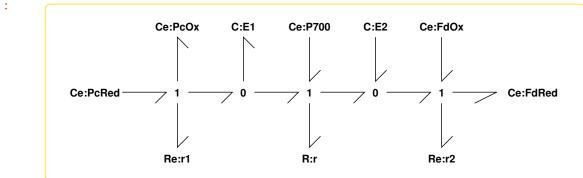
```
[41]: ## Compute the reaction potential Phi
phi = phiData.phi_species(phi_redox,spCyt['species'])
Phi_Cyt_ = -spCyt['N'].T@phi
Phi_Cyt = Phi_Cyt_[0][0]
print('Phi_Cyt =',redoxData.mV(Phi_Cyt), 'mV')
print(f'Ratio = {(Phi_Cyt/RP_Cyt):0.2f}')
```

Phi\_Cyt = 22 mV Ratio = 2.00

## 6.3 Complex PI – Photosystem I

[42]: disp.SVG('PI\_abg.svg')

[42]:



```
[43]: sbg.model('PI_abg.svg',convertR=True,convertCe=True,quiet=True)
import PI_abg
# imp.reload(PI_abg)
```

#### 6.3.1 Stoichiometry

```
[44]: ## Stoichiometry
sPI = st.stoich(PI_abg.model(),quiet=quiet)
chemostats = ['PcOx','PcRed','FdOx','FdRed','P700']
scPI = st.statify(sPI,chemostats=chemostats)
spPI = st.path(sPI,scPI)
disp.Latex(st.sprintrl(sPI,chemformula=chemformula))
```

Γ441 :

$$E_1 + P_{700} \stackrel{r}{\Longleftrightarrow} E_2 \tag{29}$$

$$PcRed \stackrel{r_1}{\Longleftrightarrow} E_1 + PcOx$$
 (30)

$$E_2 + FdOx \stackrel{r_2}{\Longleftrightarrow} FdRed$$
 (31)

#### 6.3.2 Pathway analysis with redox and pathway potentials

[45]: disp.Latex(st.sprintrl(spPI,chemformula=chemformula))

[45]:

$$FdOx + P_{700} + PcRed \stackrel{pr_1}{\rightleftharpoons} FdRed + PcOx$$
 (32)

 $RP_PI = 961 \text{ mV}$ 

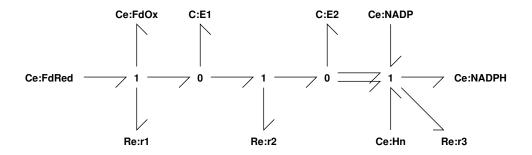
```
[47]: ## Compute the reaction potential Phi
phi = phiData.phi_species(phi_redox,spPI['species'])
Phi_PI_ = -spPI['N'].T@phi
Phi_PI = Phi_PI_[0][0]
print('Phi_PI =',redoxData.mV(Phi_PI), 'mV')
print(f'Ratio = {(Phi_PI/RP_PI):0.2f}')
```

Phi\_PI = 961 mV Ratio = 1.00

## 6.4 Complex Fer – Feredoxin-NADP reductase

[48]: disp.SVG('Fer\_abg.svg')

[48]:



```
[49]: sbg.model('Fer_abg.svg',convertR=True,convertCe=True,quiet=quiet)
import Fer_abg
# imp.reload(Fer_abg)
```

#### 6.4.1 Stoichiometry

```
[50]: ## Stoichiometry
sFer = st.stoich(Fer_abg.model(),quiet=True)
chemostats = ['FdRed','FdOx','NADP','NADPH','Hn']
scFer = st.stoich(Fer_abg.model(),chemostats=chemostats,quiet=True)
spFer = st.path(sFer,scFer)
disp.Latex(st.sprintrl(sFer,chemformula=chemformula))
```

[50]:

$$FdRed \stackrel{r_1}{\iff} E_1 + Fd0x \tag{33}$$

$$E_1 \stackrel{r_2}{\Longleftrightarrow} E_2 \tag{34}$$

$$2E_2 + Hn + NADP \stackrel{r_3}{\Longleftrightarrow} NADPH$$
 (35)

#### 6.4.2 Pathway analysis with redox and pathway potentials

```
[51]: disp.Latex(st.sprintrl(spFer,chemformula=chemformula))
```

[51]:

$$2 \text{FdRed} + \text{Hn} + \text{NADP} \xrightarrow{\text{pr}_1} 2 \text{FdOx} + \text{NADPH}$$
 (36)

 $RP_Fer = 105 mV$ 

```
[53]: ## Compute the reaction potential Phi
phi = phiData.phi_species(phi_redox,spFer['species'])
Phi_Fer_ = -spFer['N'].T@phi
Phi_Fer = Phi_Fer_[0][0]
print('Phi_Fer =',mV(Phi_Fer), 'mV')
print(f'Ratio = {(Phi_Fer/RP_Fer):0.2f}')
```

```
Phi_Fer = 212 mV
Ratio = 2.00
```

# 7 The Electron Transport Chain

• See section 7.1 of paper.

## 7.1 Graphical description

```
[54]: disp.SVG('ETCg_abg.svg')
[54]:
                                                  Ce:Hn
                                   Ce:PQH2
                                                              Ce:PcRed
                                                                           Ce:P700
                                                                                        Ce:FdRed
             Ce:H2O
Ce:P680 |
                                                                                                         Ce:NADPH
                                                                           ed] [P700] [FdRed]
                                                                                                       Fer:fer[NADP]
                                                 Cyt:cyt
                                                                                                         Ce:NADP
                                     Ce:PQ
                                                              Ce:PcOx
                                                                                         Ce:FdOx
                    Ce:O2
                                                  Ce:Hp
```

```
[55]: sbg.model('ETCg_abg.svg',convertR=True,convertCe=True,quiet=quiet)
import ETCg_abg
imp.reload(ETCg_abg)
```

Creating subsystem: Cyt:cyt Creating subsystem: Fer:fer Creating subsystem: PI:pi Creating subsystem: PII:pii

[55]: <module 'ETCg\_abg' from '/home/peterg/WORK/Dissemination/Edmund/SpecialIssue/

⇒Exa

mples/Chloroplast/ETCg\_abg.py'>

#### 7.1.1 Stoichiometry

```
[56]: ## Stoichiometry
sETCg = st.stoich(ETCg_abg.model(),quiet=True)
disp.Latex(st.sprintrl(sETCg,chemformula=chemformula))
```

[56]:

$$Hn + cyt_{E1} \stackrel{cyt_r}{\longleftarrow} Hp + cyt_{E2}$$
 (37)

$$PQH_2 \stackrel{cyt_{r1}}{\rightleftharpoons} 2Hp + PQ + 2cyt_{E1}$$
 (38)

$$PcOx + cyt_{E2} \stackrel{cyt_{r2}}{\longleftarrow} PcRed$$
 (39)

FdRed 
$$\stackrel{\text{fer}_{r1}}{\longleftrightarrow}$$
 FdOx + fer<sub>E1</sub> (40)

$$fer_{E1} \xrightarrow{fer_{r2}} fer_{E2}$$
 (41)

$$Hn + NADP + 2 fer_{E2} \xrightarrow{fer_{r3}} NADPH$$
 (42)

$$P_{700} + pi_{E1} \stackrel{pi_r}{\rightleftharpoons} pi_{E2}$$
 (43)

$$PcRed \stackrel{pi_{r1}}{\longleftarrow} PcOx + pi_{r1}$$
 (44)

$$Fd0x + pi_{E2} \stackrel{pi_{r2}}{\longleftarrow} FdRed$$
 (45)

$$P_{680} + pii_{E1} \stackrel{pii_{r}}{\longleftarrow} pii_{E2}$$
 (46)

$$2 H_2 0 \stackrel{\text{pii}_{r1}}{\rightleftharpoons} 4 Hp + 0_2 + 4 pii_{E1}$$
 (47)

$$2 \operatorname{Hn} + \operatorname{PQ} + 2 \operatorname{pii}_{E2} \stackrel{\operatorname{pii}_{r2}}{\rightleftharpoons} \operatorname{PQH}_{2}$$
 (48)

#### 7.1.2 Pathway analysis with redox and pathway potentials

```
[57]: chemostats = ['P680','P700','H20','02','Hn','Hp','NADP','NADPH']
scETCg = st.stoich(ETCg_abg.model(),chemostats=chemostats,quiet=True)
spETCg = st.path(sETCg,scETCg)
disp.Latex(st.sprintrl(spETCg,chemformula=chemformula,all=True))
```

[57]:

$$2 H_2 O + 10 Hn + 2 NADP + 4 P_{680} + 4 P_{700} \xrightarrow{pr_1} 12 Hp + 2 NADPH + O_2$$
 (49)

```
[58]: ## Compute the reaction potential Phi
species = spETCg['species']
print(species)
phi = phiData.phi_species(phi_redox,species)
Phi_ = -spETCg['N'].T@phi
Phi= Phi_[0][0]
print('Phi =',mV(Phi), 'mV')
```

```
['FdRed', 'H2O', 'Hn', 'Hp', 'NADP', 'NADPH', 'O2', 'P680', 'P700', 'PQH2', 'PcRed']
Phi = 7603 mV
```

```
[59]: ## Flatten
stbg.model(sETCg,filename='ETCg_abg')
import ETCg_abg
imp.reload(ETCg_abg)
```

```
[59]: <module 'ETCg_abg' from '/home/peterg/WORK/Dissemination/Edmund/SpecialIssue/
→Exa
mples/Chloroplast/ETCg_abg.py'>
```

#### 7.2 Computational description

The overall model is described a bond graph tools file:

```
[60]: ## File ETC_abg.py
      ## Import the modules
      import PII_abg
      import Cyt_abg
      import PI_abg
      import Fer_abg
      ## Create the model using BondGraphTools
      def model():
          n n n
          Model of chloroplast electron transport chain
          ETC = bgt.new(name='ETC') # Create system
          PII = PII_abg.model()
          Cyt = Cyt_abg.model()
          PI = PI_abg.model()
          Fer = Fer_abg.model()
          bgt.add(ETC,PII,Cyt,PI,Fer)
          return ETC
```

## 7.2.1 Unify species in model using mbg.unify()

```
[61]: # import ETC_abg
ETC = model()
common = ['PQ','PQH2','PcOx','PcRed','FdOx', 'FdRed','Hn','Hp']
mbg.unify(ETC,common,quiet=quiet)
ss = st.stoich(ETC,quiet=quiet)
disp.Latex(st.sprintrl(ss,chemformula=chemformula))
```

[61]:

$$E_1 + P_{680} \stackrel{\mathbf{r}}{\Longleftrightarrow} E_2 \tag{50}$$

$$2 H_2 0 \stackrel{r_1}{\iff} 4 E_1 + 0_2 + 4 Hp$$
 (51)

$$2E_2 + PQ + 2Hn \stackrel{r_2}{\rightleftharpoons} PQH_2$$
 (52)

$$E_1 + Hn \stackrel{r}{\Longleftrightarrow} E_2 + Hp \tag{53}$$

$$PQH_2 \stackrel{r_1}{\rightleftharpoons} 2E_1 + PQ + 2Hp$$
 (54)

$$E_2 + PcOx \stackrel{r_2}{\rightleftharpoons} PcRed$$
 (55)

$$E_1 + P_{700} \stackrel{r}{\rightleftharpoons} E_2 \tag{56}$$

$$PcRed \stackrel{r_1}{\Longleftrightarrow} E_1 + PcOx$$
 (57)

$$E_2 + FdOx \stackrel{r_2}{\rightleftharpoons} FdRed$$
 (58)

$$FdRed \stackrel{r_1}{\longleftarrow} E_1 + FdOx$$
 (59)

$$E_1 \stackrel{r_2}{\longleftarrow} E_2 \tag{60}$$

$$2E_2 + NADP + Hn \stackrel{r_3}{\Longleftrightarrow} NADPH$$
 (61)

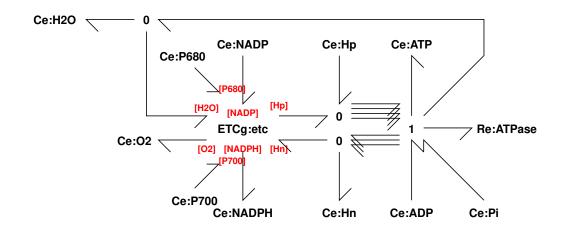
# 8 Chloroplast

• See section 7.1 of paper.

#### 8.1 Modular model

[62]: disp.SVG('Chloroplast\_abg.svg')

[62]:



Creating subsystem: ETCg:etc

[63]: <module 'Chloroplast\_abg' from '/home/peterg/WORK/Dissemination/Edmund/
→SpecialIs
sue/Examples/Chloroplast/Chloroplast\_abg.py'>

#### 8.2 Generate equations

[64]:

$$Hn + etc_cyt_{E1} \stackrel{etc_cyt_r}{\Longleftrightarrow} Hp + etc_cyt_{E2}$$
 (62)

$$etc_pQH_2 \xrightarrow{etc_cyt_{r1}} 2Hp + etc_pQ + 2etc_cyt_{E1}$$
 (63)

$$etc_pcOx + etc_cyt_{E2} \xrightarrow{etc_cyt_{r2}} etc_pcRed$$
 (64)

$$etc_{F}dRed \xrightarrow{etc_{f}er_{r1}} etc_{F}d0x + etc_{f}er_{E1}$$
 (65)

$$etc_fer_{E1} \xrightarrow{etc_fer_{r2}} etc_fer_{E2}$$
 (66)

$$Hn + NADP + 2 etc_f er_{E2} \xrightarrow{etc_f er_{r3}} NADPH$$
(67)

$$P_{700} + etc_pi_{E1} \xrightarrow{etc_pi_r} etc_pi_{E2}$$
 (68)

$$etc_{p}cRed \xrightarrow{etc_{p}i_{r1}} etc_{p}cOx + etc_{p}i_{E1}$$
(69)

$$etc_{F}d0x + etc_{p}i_{E2} \xrightarrow{etc_{p}i_{r2}} etc_{F}dRed$$
 (70)

$$P_{680} + etc_{p}ii_{E1} \xrightarrow{etc_{p}ii_{r}} etc_{p}ii_{E2}$$
 (71)

$$2 H_2 0 \stackrel{\text{etc}_p \text{ii}_{r1}}{\rightleftharpoons} 4 Hp + O_2 + 4 \text{etc}_p \text{ii}_{E1}$$
 (72)

$$2 \operatorname{Hn} + \operatorname{etc_pQ} + 2 \operatorname{etc_pii_{r2}} \stackrel{\operatorname{etc_pii_{r2}}}{\longleftarrow} \operatorname{etc_pQH_2}$$
 (73)

$$ADP + 4Hp + Pi \stackrel{ATPase}{\longleftarrow} ATP + H_2O + 3Hn$$
 (74)

## 8.3 Pathway analysis

#### 8.3.1 Pathway reaction

[66]: disp.Latex(st.sprintrl(spChloroplast,chemformula=chemformula,all=True))

[66]:

$$3 \text{ ADP} + \text{Hn} + 2 \text{ NADP} + 4 P_{680} + 4 P_{700} + 3 Pi \xrightarrow{pr_1} 3 \text{ ATP} + H_2 O + 2 \text{ NADPH} + O_2$$
 (75)

## 8.4 Efficiency from estimated $\phi$

```
[67]: ## Compute the reaction potential Phi
      species = spChloroplast['species']
      # species = chemostats
      # print(species)
      phi = phiData.phi_species(phi_redox,species)
      Phi_ = -spChloroplast['N'].T@phi
      Phi= Phi_[0][0]
      print(f'Phi = {Phi:0.2f} V')
      ## Photo input
      # print(phi_redox['P680'] , phi_redox['P700'])
      Phi_phot = 4*(phi_redox['P680'] + phi_redox['P700'])
      print(f'Phi_phot = {Phi_phot:0.2f} V')
      ##Outputs
      Phi_out = Phi_phot - Phi
      print(f'Phi_out = {Phi_out:0.2f} V')
      ## Efficiency
      efficiency = Phi_out/Phi_phot
      print(f'Efficiency = {(efficiency*100):.1f} %')
     Phi = 8.73 V
     Phi_phot = 14.38 V
     Phi_out = 5.65 V
     Efficiency = 39.3 %
[68]: | ## Compute the reaction potential Phi but with no photons
      phi = phiData.phi_species(phi_redox_0,species)
      Phi_ = -spChloroplast['N'].T@phi
      Phi_out = -Phi_[0][0]
      print(f'Phi_out = {Phi_out:0.2f} V')
      ## Photo input
      # print(phi_redox['P680'] , phi_redox['P700'])
      Phi_phot = 4*(phi_redox['P680'] + phi_redox['P700'])
      print(f'Phi_phot = {Phi_phot:0.2f} V')
      ## Efficiency
      efficiency = Phi_out/Phi_phot
      print(f'Efficiency = {(efficiency*100):.1f} %')
     Phi_out = 5.65 V
     Phi_phot = 14.38 V
     Efficiency = 39.3 %
```

#### 8.5 Efficiency by direct calculation

• See section 7.2 of paper.

```
[69]: def getPhi(name):
          redox_data = redoxData.data()
          n = redox_data[name]['electrons']
          E = redox_data[name]['E7']
          Phi = n*E
          print(f'\{name\}: \ E = \{E\} \ V; \ n = \{n\}; \ Phi = \{Phi\} \ V')
          return Phi
[70]:  ## Photons
      Phi_phot = 4*(phi_redox['P680'] + phi_redox['P700'])
      print(f'Phi_phot = {Phi_phot:0.2f} V')
      ## NADPH
      Phi_1 = getPhi('NADP/NADPH')
      ## 02
      Phi_2 = getPhi('02/2H20')
      ## ATP Hydrolysis
      print(f'Hydrolysis:\t Phi = {Phi_Hyd:0.3f}')
     Phi_phot = 14.38 V
     NADP/NADPH:
                      E = -0.324 \text{ V};
                                       n = 2; Phi = -0.648 V
     02/2H20:
                       E = 0.816 V;
                                       n = 4; Phi = 3.264 V
     Hydrolysis:
                      Phi = 0.363
[71]: ## All
      Phi\_chem = -2*Phi\_1 + Phi\_2 + 3*Phi\_Hyd
      print(f'Phi_chem = {Phi_chem:0.2f}')
     Phi_chem = 5.65
[72]: | ## Efficiency
      efficiency = Phi_chem/Phi_phot
      print(f'Efficiency = {(efficiency*100):.1f} %')
     Efficiency = 39.3 %
 []:
```

#### References

Robert E. Blankenship. Molecular mechanisms of photosynthesis. Wiley, Chichester, UK, 3rd edition, 2021.

Robert E. Blankenship and Roger C. Prince. Excited-state redox potentials and the z scheme of photosynthesis. Trends in Biochemical Sciences, 10(10):382 - 383, 1985. ISSN 0968-0004. doi: 10.1016/0968-0004(85)90059-3.

David G Nicholls and Stuart Ferguson. Bioenergetics 4. Academic Press, Amsterdam, 2013.