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HW 9

1)

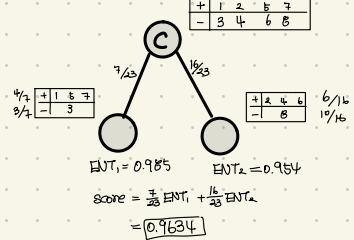
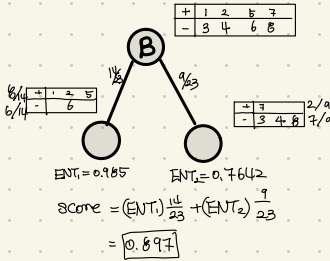
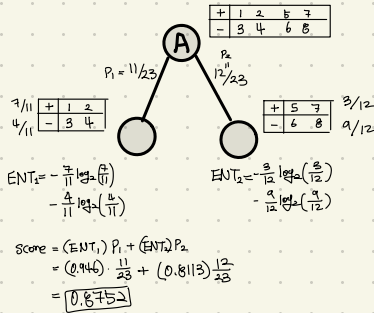
Example	Input Attributes			Class	#
	A	B	C	D	
x ₁	T	T	T	Yes	1
x ₂	T	T	F	Yes	6
x ₃	T	F	T	No	3
x ₄	T	F	F	No	1
x ₅	F	T	T	Yes	1
x ₆	F	T	F	No	6
x ₇	F	F	T	Yes	2
x ₈	F	F	F	No	3

To decide the first node (root), we should compare entropy to have better attribute. in a node.

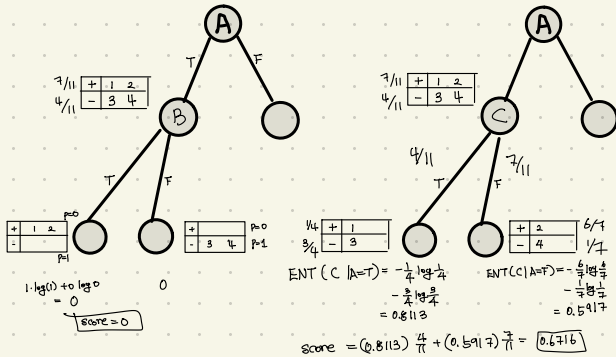
✓ when root is A

✓ when root is B

✓ when root is C



When root is with the attribute (A), its score is the smallest. So it should be (A)

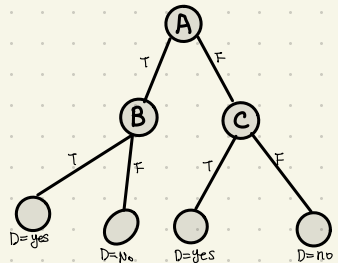
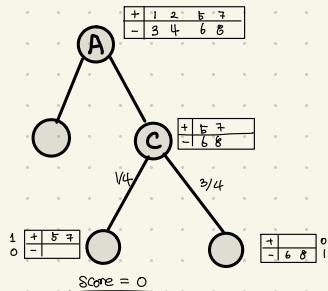
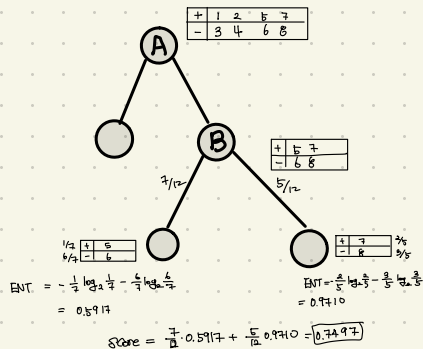


So the left child from (A) is (B)

Since the score is 0

So that the right child node of (A) is (C)

So that the final result is



2)

$$\underbrace{(A \vee \neg B)}_X \oplus \underbrace{(\neg C \vee D)}_Y$$

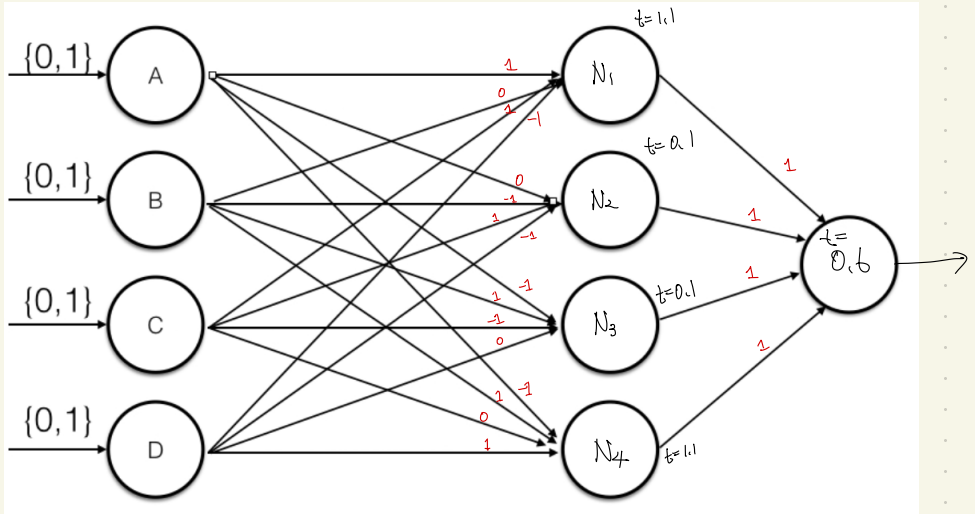
X

Y

$$X \oplus Y = (X \wedge \neg Y) \vee (\neg X \wedge Y)$$

$$= ((A \vee \neg B) \wedge (C \wedge \neg D)) \vee ((\neg A \wedge B) \wedge (\neg C \vee D))$$

$$= (A \wedge C \wedge \neg D) \vee (\neg B \wedge C \wedge \neg D) \vee (\neg A \wedge B \wedge \neg C) \vee (\neg A \wedge B \wedge D)$$

 N_1 N_2 N_3 N_4 

(N₁) if D=0, 1+1+0+0=2
if D=1, 1+1+0+(-1)=1 } So t can be (1.1)

(N₂) if D=0 & B=0, 1
D=1 & B=1, -1
D=1 & B=0, 0
D=0 & B=1, 0 } So t can be (0.1)

(N₃) if A=0 & C=0, 1
A=1 & C=1, -1
A=1 & C=0, 0
A=0 & C=1, 0 } So t can be (0.1)

(N₄) if A=0, 0
if A=1, 1 } So t can be (1.1)

To satisfy output node (t),
$$\frac{1.1 + 1.1 + 0.1 + 0.1}{4} = 0.6$$