```
fun append (xs,ys) =
    if xs=[]
    then ys
    else (hd xs)::append(tl xs,ys)

fun map (f,xs) =
    case xs of
      [] => []
      | x::xs' => (f x)::(map(f,xs'))

val a = map (increment, [4,8,12,16])
val b = map (hd, [[8,6],[7,5],[3,0,9]])
```

Programming Languages Dan Grossman

Polymorphic Types and Equality Types

An example

"Write a function that appends two string lists"

```
fun append (xs,ys) =
    case xs of
    [] => ys
    | x::xs' => x :: append(xs',ys)
```

- You expect string list * string list -> string list
- Implementation says 'a list * 'a list -> 'a list
- This is okay [such as on your homework]: why?

More general

The type

'a list * 'a list -> 'a list
is more general than the type
 string list * string list -> string list

- It "can be used" as any less general type, such as
 int list * int list -> int list
- But it is not more general than the type
 int list * string list -> int list

The "more general" rule

Easy rule you (and the type-checker) can apply without thinking:

A type *t1* is more general than the type *t2* if you can take *t1*, replace its type variables consistently, and get *t2*

- Example: Replace each 'a with int * int
- Example: Replace each 'a with bool and each 'b with bool
- Example: Replace each 'a with bool and each 'b with int
- Example: Replace each 'b with 'a and each 'a with 'a

Other rules

- Can combine the "more general" rule with rules for equivalence
 - Use of type synonyms does not matter
 - Order of field names does not matter.

Equality types

- You might also see type variables with a second "quote"
 - Example: ''a list * ''a -> bool
- These are "equality types" that arise from using the = operator
 - The = operator works on lots of types: int, string, tuples containing all equality types, ...
 - But not all types: function types, real, ...
- The rules for more general are exactly the same except you have to replace an equality-type variable with a type that can be used with =
 - A "strange" feature of ML because = is special

Example

```
(* ''a * ''a -> string *)
fun same_thing(x, y) =
   if x=y then "yes" else "no"

(* int -> string *)
fun is_three x =
   if x=3 then "yes" else "no"
```

(You can ignore the warning about "calling polyEqual")