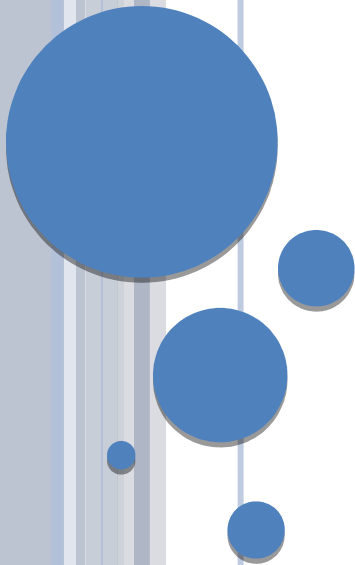


# MASTERING TIC TAC TOE USING SELF PLAY AND REINFORCEMENT LEARNING

## CONSIDERING 3X3 MAZE



# MOTIVATION

- In March 2016, Deepmind's AlphaGo beat world champion Go player Lee Sedol 4–1
- 18th October 2017, AlphaGo Zero, that had defeated AlphaGo 100–0
- 5th December 2017, DeepMind released another paper showing how AlphaGo Zero could be adapted to beat the world-champion programs StockFish and Elmo at chess and shogi
- An algorithm for getting good at something without any prior knowledge of human expert strategy was born



# OVERVIEW

- Generate training data using the current best player through self play to train the second best and then evaluate it's performance against the best and if it wins 55% of time then replace it with the best for the next iteration



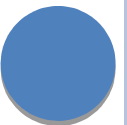
# GOAL

- The goal here is to predict two things
- At each point, which move to take which is actually learning the policy
- At each point, what is the immediate reward which is actually learning the value function



# METHODOLOGY

- Self Play
- Network Weights Optimization
- Network Evaluation

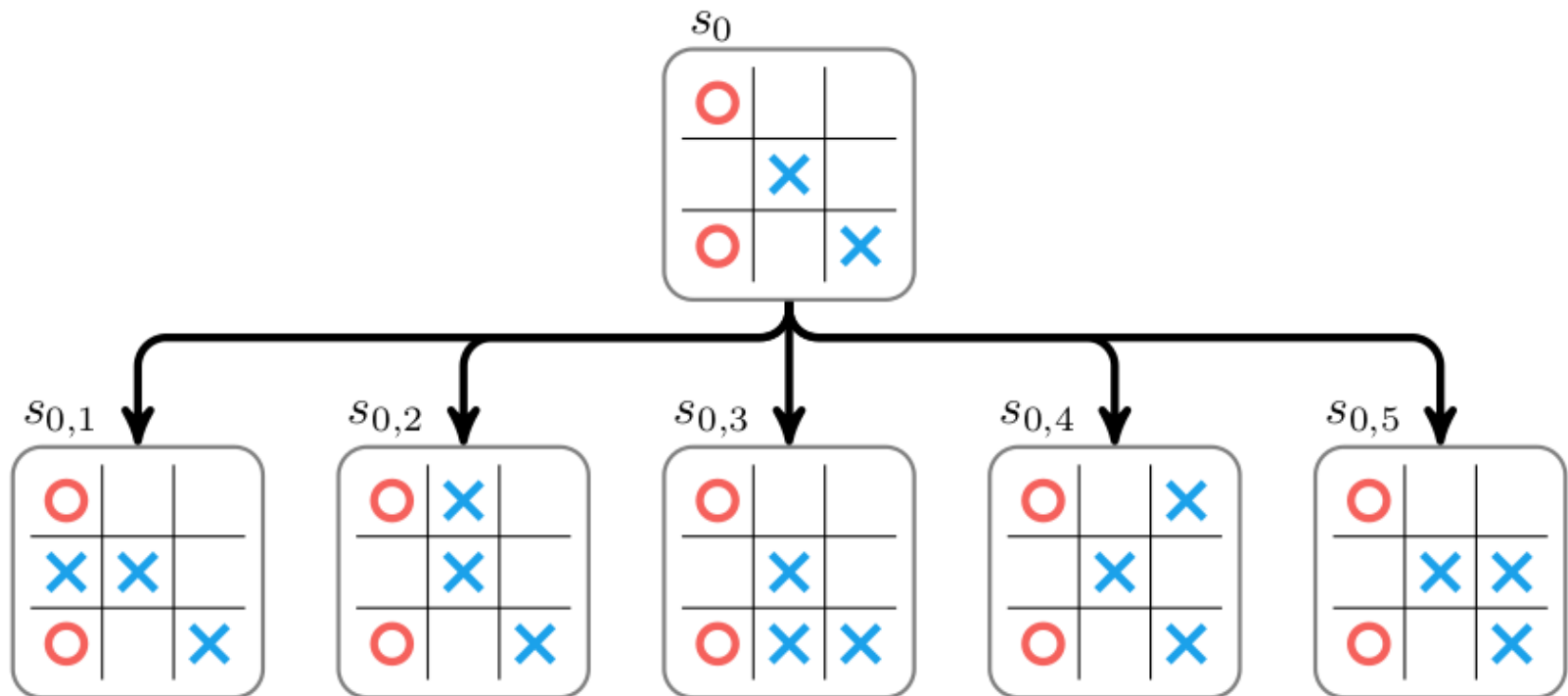


# SELF PLAY

- Move Selection through Monte Carlo Tree Search
- At each move, the following information is stored
  - The game state
  - The search probabilities
  - The winner



# A STATE AND ITS CHILDREN



# REPRESENTATION

- 0 represents no move has been played at that position
- 1 represents player 1
- 2 represents player 2





# STATE

- At any instance, the condition of the game is a state depending on the representation
- Here, it is the complete maze  
0000000001  
0000000002
- Along with a turn indicator
- Above shown is the initial state of the game under consideration



# CHILDREN

- Possible moves from a state are considered as its children
- Children of initial state of the game are

1 0 0	0 1 0	0 0 1	0 0 0	0 0 0	0 0 0
0 0 0	0 0 0	0 0 0	1 0 0	0 1 0	0 0 1
0 0 0	0 0 0	0 0 0	0 0 0	0 0 0	0 0 0

0 0 0	0 0 0	0 0 0
0 0 0	0 0 0	0 0 0
1 0 0	0 1 0	0 0 1



# CHILDREN

- A child stores five values
- $N \rightarrow$  number of times the action has been taken
- $W \rightarrow$  total value of the state
- $Q \rightarrow$  mean value of the state
- $P \rightarrow$  policy function prediction
- $V \rightarrow$  value function prediction



# MONTE CARLO TREE SEARCH

- Given a state, explore the tree until a leaf node is reached by selecting the best child
- At leaf node, predict probabilities of each of its children
- Back propagate from the leaf to the root which in this case is the input and update the values of  $N$ ,  $W$  and  $Q$
- Repeat this cycle for a certain time period
- Select the best action among the lot



# CHILD SELECTION

- A child is selected based on the equation
- $Q+U$
- $Q \rightarrow$  The mean value of the state
- $U \rightarrow$  A function of  $P$  and  $N$  that increases if an action hasn't been explored much, relative to the other actions, or if the prior probability of the action is high



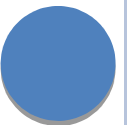
# CHILD SELECTION

- U in this case is  $P/N$
- So the equation becomes  $(P/N)+Q$
- Because early on in the simulation, U should dominate (more exploration), but later Q is more important (exploitation)
- So a slight modification is needed which is
- $(\epsilon*(P/N))+Q$



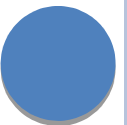
# VALUE UPDATE

- During back propagation, the values are updated as follows
- $N = N+1$
- $W = W+V$
- $Q = W/N$



# EPIISODE

- A game played from start to finish is an episode





# DATA GENERATION

- Once an episode has ended, all the steps which were performed will be given labels
- All the steps taken by the winning player will be assigned +1 and to all other steps -1 will be assigned.
- Similarly every move will be assigned a probability provided by the CNN



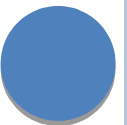
# DEEP NEURAL NETWORK

- It's a network with 1 convolution layer and 40 residual layers with a double headed output, a value head and a policy head
- Value head giving a single prediction in the range  $[-1,1]$ , actually trying to predict the outcome of the game
- Policy head giving 9 probabilities, actually trying to predict the probability distribution among the children
- For faster convergence, I divided the model in to one each for the different heads



# DEEP NEURAL NETWORK

- The loss function in case of value head is mean square error while in case of policy head, it is softmax crossentropy



# NETWORK WEIGHTS OPTIMIZATION

- Once data has been generated using the current best player through self play, now it's time to retrain the second best using the data generated by the best
- Sample a mini batch from the data
- Retrain the current network on these positions



# NETWORK EVALUATION

- After training, it's time to evaluate the performance of the retrained network against the best so far and if the retrained network wins 55% of the games, it will become the new best and for the next iteration, roles will be changed as the new best will generate data for training of the previous best



# SOME HYPER PARAMETERS

- Number of training epochs : 1
- Number of training iterations : 20
- Number of games during self play : 100
- Number of games during evaluation : 40
- Batch Size : 256
- Sample Size : 512
- Monte Carlo Simulations : 100
- Regularization Constant : 0.0001
- Learning Rate : 0.01
- Momentum : 0.9
- Optimizer : SGD



# RESULTS

- After 100 games, defeated untrained algorithm with 40-0
- After 200 games, defeated first best with 40-0

